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PCE, Academic Year 2022-2023



Department of Computer Engineering

Session 2022-2023

Lab Manual

Machine Learning Lab

Year: 3rd Yr. / VI SEM

Lab Code: - 6CS4-22

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Poornima College of Engineering, Jaipur

Department of Computer Engineering

Vision

Evolve as a center of excellence with wider recognition and to adapt the rapid innovation in Computer Engineering.

Mission

To provide a learning-centered environment that will enable students and faculty members to achieve their goals empowering them to compete globally for the most desirable careers in academia and industry.

To contribute significantly to the research and the discovery of new arenas of knowledge and methods in the rapid developing field of Computer Engineering.

To support society through participation and transfer of advanced technology from one sector to another.

Poornima College of Engineering, Jaipur Department of Computer Engineering

Program Educational Objectives (PEOs)

- Graduates will work productively as skillful engineers playing the leading roles inmultifaceted teams.
- Graduates will identify the solutions for challenging issues inspiring the upcoming generations leading them towards innovative, creative, and sophisticated technologies.
- Graduates will implement their pioneering ideas practically to create novel products and thefeasible solutions of research oriented problems



Poornima College of Engineering, Jaipur

Department of Computer Engineering

Program Outcomes (POs)

- a. An ability to apply the knowledge of mathematics, science, engineering fundamentals, algorithmic principles and computing for the solution of complex engineering problems.
- b. An ability to design and conduct experiments, analyze and interpret data finding the computing requirements with appropriate solutions.
- c. An ability to design a computer based system, component, or process to meet the desired needs within realistic constraints such as economic, environmental, social, political, ethical, health, safety, manufacturability and sustainability etc.
- d. An ability to function effectively in multidisciplinary teams,
- e. An ability to identify, formulate, and solve engineering problems by applying the appropriate computing techniques, progressive resources and modern IT tools with an understanding of the limitations.
- f. An understanding of professional, ethical, security, legal, social issues and responsibilities towards these.
- g. An ability to communicate effectively on complex engineering activities with theengineering community and the society.
- h. The widen education necessary to understand and analyze the impact of computing and engineering solutions in a global, economic, environmental and societal context.
- i. Recognition of the need with an engagement in lifelong learning in the context of technological change.
- j. Knowledge of contemporary issues.
- k. An ability to use the techniques, skills, and modern engineering tools necessary for computing and engineering practice.
- l. An ability to contribute in the fruitful working as an efficient member of a team in multidisciplinary environments with a concern of engineering and managementprinciples.
- m. An ability to apply the basic principles and practices of Computer Engineering and itsall arenas to fulfill the requirements of customers in context of business.



Machine Learning LAB Programming (6CS4-22) Lab Objectives & Outcomes

Lab Name	LO	LO Statement	Action Verb	Bloom Level	Level Descriptor	Map to PO
	LO 1	Implement basic python Libraries used in Machine Learning Algorithm	Apply	Apply	III	PO5, PSO1, PSO3
Machine Learning	LO 2	Analyze various Supervised and Unsupervised Machine Learning algorithms for Classification Problems	Solve	Analyze	IV	PO2, PSO1, PSO3
LAB	LO3	Design and Evaluate Machine Learning Algorithms for real world problem	Evaluate	Evaluate	V	PO3, PSO1 , PSO3

LAB Name	Learning Objective	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10	PO11	PO12	PSO1	PSO2	PSO3
Machine	LO-1				3								3		2
Learning LAB	LO-2	3											3		2
	LO-3		3										3		2

LAB PLAN

Total number of experiments 10

Total number of turns required 13

Number of turns required for

Experiment Number	Turns	Scheduled Day
Exp. 1	2	Day 1, 2
Exp. 2	2	Day 3, 4
Exp. 3	1	Day 5
Exp. 4	1	Day 6
Exp. 5	1	Day 7
Exp. 6	1	Day 8
Exp. 7	1	Day 9
Exp. 8	1	Day 10
Exp. 9	1	Day 11
Exp. 10	2	Day 12, 13

Distribution of lab hours

Attendance 05 minutes

Explanation of features of language 15 minutes

Explanation of experiment 15 minutes

Performance of experiment 70 minutes

Viva / Quiz / Queries 15 min

Software required

Python, Anaconda Notebook, Google Colab

LAB RULES

Responsibilities of Users

Users are expected to follow some fairly obvious rules of conduct:



- Enter the lab on time and leave at propertime.
- Wait for the previous class to leave before the next class enters.
- Keep the bag outside in the respective racks.
- Utilize lab hours in the corresponding.
- Turn off the machine before leaving the lab unless a member of lab staff has specifically told you not to do so.
- Leave the labs at least as nice as you found them.
- If you notice a problem with a piece of equipment (e.g. a computer doesn't respond) or the room in general (e.g. cooling, heating, lighting) please report it to lab staff immediately. Do not attempt to fix the problem yourself.



- Don't abuse the equipment.
- Do not adjust the heat or air conditioners. If you feel the temperature is not properly set, inform lab staff; we will attempt to maintain a balance that is healthy for people and machines.
- Do not attempt to reboot a computer. Report problems to lab staff.
- Do not remove or modify any software or file withoutpermission.
- Do not remove printers and machines from the network without being explicitly told to do so by lab staff.
- Don't monopolize equipment. If you're going to be away from your machine for more than 10 or 15 minutes, log out before leaving. This is both for the security of your account, and to ensure that others are able to use the lab resources while you are not.
- Don't use internet, internet chat of any kind in your regular lab schedule.
- Do not download or upload of MP3, JPG or MPEGfiles.
- No games are allowed in the lab sessions.
- No hardware including USB drives can be connected or disconnected in the labs without prior permission of the lab in-charge.
- No food or drink is allowed in the lab or near any of the equipment. Aside from the fact that it leaves a mess and attracts pests, spilling anything on a keyboard or other piece of computer equipment could cause permanent, irreparable, and costly damage. (and in fact *has*) If you need to eat or drink, take a break and do so in the canteen.
- Don't bring any external material in the lab, except your lab record, copy and books.
- Don't bring the mobile phones in the lab. If necessary then keep them in silence mode.
- Please be considerate of those around you, especially in terms of noise level. While labs are a natural place for conversations of all types, kindly keep the volume turneddown.
 - If you are having problems or questions, please go to either the faculty, lab in-charge or the lab supporting staff. They will help you. We need your full support and cooperation for smooth functioning of the lab.

INSTRUCTIONS

Before Entering in the Lab

- All the students are supposed to prepare the theory regarding the next experiment/Program.
- Students are supposed to bring their lab records as per their lab schedule.
- Previous experiment/program should be written in the lab record.
- If applicable trace paper/graph paper must be pasted in lab record with proper labeling.
- All the students must follow the instructions, failing which he/she may not be allowed in the lab.

While Working in the Lab

- Adhere to experimental schedule as instructed by the lab in-charge/faculty.
- Get the previously performed experiment/ program signed by the faculty/ lab incharge.
- Get the output of current experiment/program checked by the faculty/ lab in charge in the lab copy.
- Each student should work on his/her assigned computer at each turn of thelab.

Take responsibility of valuable accessories.

RAJASTHAN TECHNICAL UNIVERSITY, KOTA

Syllabus

III Year-VI Semester: B.Tech. Computer Science and Engineering

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1 1()	Implement the non-parametric Locally Weighted Regression algorithm in order to fit data points. Select appropriate data set for your experiment and draw graphs.	42

Hardware/Software Requirement

There are 25 installed in this Lab. Their configurations are as follows:

Processor : Intel Pentiun (R) Dual Core 3.00 GHz

RAM: 2 GB

Hard Disk : 40 GB

Mouse : Optical Mouse

Network Interface card : Present

Software

➤ All systems are configured in DUAL BOOT mode i.e, Students can boot from Windows XP or Linux as per their lab requirement.

This is very useful for students because they are familiar with different Operating Systems so that they can execute their programs in different programming environments.

- > Systems are provided for students in the 1:1 ratio.
- > Systems are assigned numbers and same system is allotted for students when they do the lab.

Rational behind the lab:

After going through this section, you should be able to:

- mention the features of UNIX;
- recognize, understand and make use of various UNIX commands;
- gain hands on experience of UNIX commands and shell programs;
- feel more confident about writing the shell scripts and shell programs;
- apply the concepts that have been covered in this manual, and
- Know the alternate ways of providing the solutions to the given practical exercises and problems.



Introduction

Machine learning

Machine learning is a subset of artificial intelligence in the field of computer science that often uses statistical techniques to give computers the ability to "learn" (i.e., progressively improve performance on a specific task) with data, without being explicitly programmed. In the past decade, machine learning has given us self-driving cars, practical speech recognition, effective web search, and a vastly improved understanding of the human genome.

Machine learning tasks

Machine learning tasks are typically classified into two broad categories, depending on whether there is a learning "signal" or "feedback" available to a learning system:

- 1. **Supervised learning**: The computer is presented with example inputs and their desired outputs, given by a "teacher", and the goal is to learn a general rule that maps inputs to outputs. As special cases, the input signal can be only partially available, or restricted to special feedback:
- 2. **Semi-supervised learning**: the computer is given only an incomplete training signal: a training set with some (often many) of the target outputs missing.
- 3. **Active learning**: the computer can only obtain training labels for a limited set of instances (based on a budget), and also has to optimize its choice of objects to acquire labels for. When used interactively, these can be presented to the user for labeling.
- 4. **Reinforcement learning**: training data (in form of rewards and punishments) is given only as feedback to the program's actions in a dynamic environment, such as driving a vehicle or playing a game against an opponent.

5. **Unsupervised learning**: No labels are given to the learning algorithm, leaving it on its own to find structure in its input. Unsupervised learning can be a goal in itself (discovering hidden patterns in data) or a means towards an end (feature learning).

Supervised learning	Un Supervised learning	Instance based learning
Find-s algorithm	EM algorithm	
Candidate elimination algorithm		
Decision tree algorithm		
Back propagation Algorithm		Locally weighted
Naïve Bayes Algorithm	K means algorithm	Regression algorithm
K nearest neighbour	(6565))	Solition (PSP)
algorithm(lazy learning		
algorithm)		

Machine Learning Applications

In classification, inputs are divided into two or more classes, and the learner must produce a model that assigns unseen inputs to one or more (multi-label classification) of these classes. This is typically tackled in a supervised manner. Spam filtering is an example of classification, where the inputs are email (or other) messages and the classes are "spam" and "not spam".

In regression, also a supervised problem, the outputs are continuous rather than discrete.

In clustering, a set of inputs is to be divided into groups. Unlike in classification, the groups are not known beforehand, making this typically an unsupervised task.

Density estimation finds the distribution of inputs in some space.

Dimensionality reduction simplifies inputs by mapping them into a lower dimensional space. Topic modeling is a related problem, where a program is given a list of human language documents and is tasked with finding out which documents cover similar topics.

Machine learning Approaches

1. Decision tree learning

Decision tree learning uses a decision tree as a predictive model, which maps observations about an item to conclusions about the item's target value.

2. Association rule learning

Association rule learning is a method for discovering interesting relations between variables in large databases.

3. Artificial neural networks

An artificial neural network (ANN) learning algorithm, usually called "neural network" (NN), is a learning algorithm that is vaguely inspired by biological neural networks. Computations are structured in terms of an interconnected group of artificial neurons, processing information using a connectionist approach to computation. Modern neural networks are non-linear statistical data modeling tools. They are usually used to model complex relationships between inputs and outputs, to find patterns in data, or to capture the statistical structure in an unknown joint probability distribution between observed variables.

4. Deep learning

Falling hardware prices and the development of GPUs for personal use in the last few years have contributed to the development of the concept of deep learning which consists of multiple hidden layers in an artificial neural network. This approach tries to model the way the human brain processes light and sound into vision and hearing. Some successful applications of deep learning are computer vision and speech Recognition.

5. Inductive logic programming

Inductive logic programming (ILP) is an approach to rule learning using logic Programming as a uniform representation for input examples, background knowledge, and hypotheses. Given an encoding of the known background knowledge and a set of examples represented as a logical database of facts, an ILP system will derive a hypothesized logic program that entails all positive and no negative examples. Inductive programming is a related field that considers any kind of programming languages for representing hypotheses (and not only logic programming), such as functional programs.

6. Support vector machines

Support vector machines (SVMs) are a set of related supervised learning methods used for classification and regression. Given a set of training examples, each marked as belonging to one

of two categories, an SVM training algorithm builds a model that predicts whether a new example falls into one category or the other.

7. Clustering

Cluster analysis is the assignment of a set of observations into subsets (called clusters) so that observations within the same cluster are similar according to some pre designated criterion or criteria, while observations drawn from different clusters are dissimilar. Different clustering techniques make different assumptions on the structure of the data, often defined by some similarity metric and evaluated for example by internal compactness (similarity between members of the same cluster) and separation between different clusters. Other methods are based on estimated density and graph connectivity. Clustering is a method of unsupervised learning, and a common technique for statistical data analysis.

8. Bayesian networks

A Bayesian network, belief network or directed acyclic graphical model is a probabilistic graphical model that represents a set of random variables and their conditional independencies via a directed acyclic graph (DAG). For example, a Bayesian network could represent the probabilistic relationships between diseases and symptoms. Given symptoms, the network can be used to compute the probabilities of the presence of various diseases. Efficient algorithms exist that perform inference and learning.

9. Reinforcement learning

Reinforcement learning is concerned with how an agent ought to take actions in an environment so as to maximize some notion of long-term reward. Reinforcement learning algorithms attempt to find a policy that maps states of the world to the actions the agent ought to take in those states. Reinforcement learning differs from the supervised learning problem in that correct input/output pairs are never presented, nor sub-optimal actions explicitly corrected.

10. Similarity and metric learning

In this problem, the learning machine is given pairs of examples that are considered similar and pairs of less similar objects. It then needs to learn a similarity function (or a distance metric function) that can predict if new objects are similar. It is sometimes used in Recommendation systems.

11. Genetic algorithms

A genetic algorithm (GA) is a search heuristic that mimics the process of natural selection, and uses methods such as mutation and crossover to generate new genotype in the hope of finding good solutions to a given problem. In machine learning, genetic algorithms found some uses in the 1980s and 1990s. Conversely, machine learning techniques have been used to improve the performance of genetic and evolutionary algorithms.

12. Rule-based machine learning

Rule-based machine learning is a general term for any machine learning method that identifies, learns, or evolves "rules" to store, manipulate or apply, knowledge. The defining characteristic of a rule- based machine learner is the identification and utilization of a set of relational rules that collectively represent the knowledge captured by the system. This is in contrast to other machine learners that commonly identify a singular model that can be universally applied to any instance in order to make a prediction. Rule-based machine learning approaches include learning classifier systems, association rule learning, and artificial immune systems.

13. Feature selection approach

Feature selection is the process of selecting an optimal subset of relevant features for use in model construction. It is assumed the data contains some features that are either redundant or irrelevant, and can thus be removed to reduce calculation cost without incurring much loss of information. Common optimality criteria include accuracy, similarity and information measures.

1. Implement and demonstrate the FIND-S algorithm for finding the most specific hypothesis based on a given set of training data samples. Read the training data from a .CSV file.

```
Find-s Algorithm:
1. Load Data set
2. Initialize h to the most specific hypothesis in H
3. For each positive training instance x
        • For each attribute constraint ai in h
        If the constraint ai in h is satisfied by x then do nothing
        else replace ai in h by the next more general constraint that is satisfied by x
4. Output hypothesis h
Source Code:
import random
import csv
def read_data(filename):
  with open(filename, 'r') as csvfile:
     datareader = csv.reader(csvfile, delimiter=',')
     traindata = []
     for row in datareader:
        traindata.append(row)
  return (traindata)
h=['phi','phi','phi','phi','phi'
data=read_data('finds.csv')
def isConsistent(h,d):
     if len(h)!=len(d)-1:
        print('Number of attributes are not same in hypothesis.')
     return False
  else:
        matched=0
        for i in range(len(h)):
                if ((h[i]==d[i]) | (h[i]=='any')):
                        matched=matched+1
                if matched==len(h):
                                return True
                else:
                        return False
def makeConsistent(h,d):
       for i in range(len(h)):
                if((h[i] == 'phi')):
                                h[i]=d[i]
                elif(h[i]!=d[i]):
                                h[i]='any'
        return h
```

print('Begin : Hypothesis :',h)

```
print('=======')
for d in data:
    if d[len(d)-1]=='Yes':
         if ( isConsistent(h,d)):
               pass
       else:
                      h=makeConsistent(h,d)
    print ('Training data
                              :',d)
     print ('Updated Hypothesis :',h)
    print()
    print('____')
print('maximally sepcific data set End: Hypothesis:',h)
Output:
Begin: Hypothesis: ['phi', 'phi', 'phi', 'phi', 'phi', 'phi']
                  : ['Cloudy', 'Cold', 'High', 'Strong', 'Warm', 'Change', 'Yes']
Training data
Updated Hypothesis : ['Cloudy', 'Cold', 'High', 'Strong', 'Warm', 'Change']
                  : ['Sunny', 'Warm', 'Normal', 'Strong', 'Warm', 'Same', 'Yes']
Training data
Updated Hypothesis : ['any', 'any', 'any', 'Strong', 'Warm', 'any']
                  : ['Sunny', 'Warm', 'High', 'Strong', 'Warm', 'Same', 'Yes']
Training data
Updated Hypothesis : ['any', 'any', 'any', 'Strong', 'Warm', 'any']
Training data
                  : ['Sunny', 'Warm', 'High', 'Strong', 'Cool', 'Change', 'Yes']
Updated Hypothesis : ['any', 'any', 'any', 'Strong', 'any', 'any']
Training data
                  : ['Overcast', 'Cool', 'Normal', 'Strong', 'Warm', 'Same', 'Yes']
Updated Hypothesis : ['any', 'any', 'any', 'Strong', 'any', 'any']
maximally sepcific data set End: Hypothesis: ['any', 'any', 'any', 'Strong', 'any', 'any']
OR
import csv
def loadCsv(filename):
  lines = csv.reader(open(filename, "r"))
  dataset = list(lines)
  for i in range(len(dataset)):
       dataset[i] = dataset[i]
  return dataset
attributes = ['Sky', 'Temp', 'Humidity', 'Wind', 'Water', 'Forecast']
print('Attributes =',attributes)
num_attributes = len(attributes)
```

```
filename = "finds.csv"
dataset = loadCsv(filename)
print(dataset)
hypothesis=['0'] * num attributes
print("Intial Hypothesis")
print(hypothesis)
print("The Hypothesis are")
for i in range(len(dataset)):
   target = dataset[i][-1]
  if(target == 'Yes'):
     for j in range(num_attributes):
        if(hypothesis[j]=='0'):
          hypothesis[j] = dataset[i][j]
        if(hypothesis[j]!= dataset[i][j]):
          hypothesis[j]='?'
     print(i+1,'=',hypothesis)
print("Final Hypothesis")
print(hypothesis)
Output:
Attributes = ['Sky', 'Temp', 'Humidity', 'Wind', 'Water', 'Forecast']
[['sky', 'Airtemp', 'Humidity', 'Wind', 'Water', 'Forecast', 'WaterSport'],
['Cloudy', 'Cold', 'High', 'Strong', 'Warm', 'Change', 'Yes'],
['Sunny', 'Warm', 'Normal', 'Strong', 'Warm', 'Same', 'Yes'],
['Sunny', 'Warm', 'High', 'Strong', 'Warm', 'Same', 'Yes'],
['Cloudy', 'Cold', 'High', 'Strong', 'Warm', 'Change', 'No'],
['Sunny', 'Warm', 'High', 'Strong', 'Cool', 'Change', 'Yes'],
['Rain', 'Mild', 'High', 'Weak', 'Cool', 'Change', 'No'],
['Rain', 'Cool', 'Normal', 'Weak', 'Cool', 'Same', 'No'],
['Overcast', 'Cool', 'Normal', 'Strong', 'Warm', 'Same', 'Yes']]
Intial Hypothesis
['0', '0', '0', '0', '0', '0']
The Hypothesis are
2 = ['Cloudy', 'Cold', 'High', 'Strong', 'Warm', 'Change']
3 = ['?', '?', '?', 'Strong', 'Warm', '?']
4 = ['?', '?', '?', 'Strong', 'Warm', '?']
6 = ['?', '?', '?', 'Strong', '?', '?']
9 = ['?', '?', '?', 'Strong', '?', '?']
Final Hypothesis
['?', '?', '?', 'Strong', '?', '?']
```

2. For a given set of training data examples stored in a .CSV file, implement and demonstrate the Candidate-Elimination algorithm to output a description of the set of all hypotheses consistent with the training examples.

Candidate-Elimination Algorithm:

- 1. Load data set
- 2. G <-maximally general hypotheses in H
- 3. S <- maximally specific hypotheses in H
- For each training example d=<x,c(x)>

Case 1: If d is a positive example

Remove from G any hypothesis that is inconsistent with d For each hypothesis s in S that is not consistent with d

- Remove s from S.
- Add to S all minimal generalizations h of s such that
 - h consistent with d
 - Some member of G is more general than h
- Remove from S any hypothesis that is more general than another hypothesis in S

```
Case 2: If d is a negative example
```

Remove from S any hypothesis that is inconsistent with d For each hypothesis g in G that is not consistent with d

*Remove g from G.

*Add to G all minimal specializations h of g such that

o h consistent with d

o Some member of S is more specific than h

Remove from G any hypothesis that is less general than another hypothesis in G

Source Code:

```
import numpy as np
import pandas as pd
data = pd.DataFrame(data=pd.read_csv('finds1.csv'))
concepts = np.array(data.iloc[:,0:-1])
target = np.array(data.iloc[:,-1])
def learn(concepts, target):
  specific_h = concepts[0].copy()
  print("initialization of specific_h and general_h")
  print(specific h)
  general_h = [["?" for i in range(len(specific_h))] for i in range(len(specific_h))]
  print(general_h)
  for i, h in enumerate(concepts):
     if target[i] == "Yes":
       for x in range(len(specific_h)):
          if h[x] != specific_h[x]:
            specific_h[x] = '?'
```

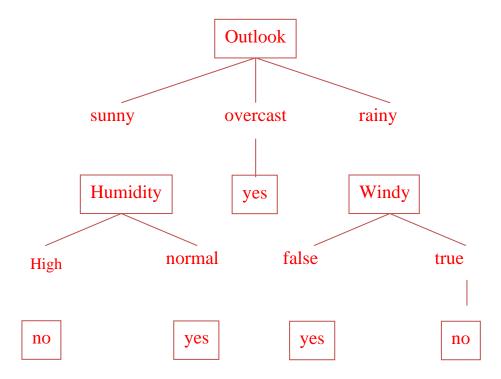
```
general_h[x][x] = '?'
             if target[i] == "No":
                    for x in range(len(specific_h)):
                           if h[x] != specific_h[x]:
                                  general_h[x][x] = specific_h[x]
                           else:
                                 general_h[x][x] = '?'
       print(" steps of Candidate Elimination Algorithm",i+1)
       print("Specific_h ",i+1,"\n ")
       print(specific_h)
       print("general_h ", i+1, "\n ")
       print(general_h)
       indices = [i for i, val in enumerate(general_h) if val == ['?', '?', '?', '?', '?', '?']]
       for i in indices:
                    general_h.remove(['?', '?', '?', '?', '?', '?'])
       return specific_h, general_h
s_final, g_final = learn(concepts, target)
print("Final Specific_h:", s_final, sep="\n")
print("Final General_h:", g_final, sep="\n")
OUTPUT
initialization of specific h and general h
['Cloudy' 'Cold' 'High' 'Strong' 'Warm' 'Change']
[['?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?',\ '?
'?', '?', '?'], ['?', '?', '?', '?', '?', '?']]
 steps of Candidate Elimination Algorithm 8
Specific_h 8
['?' '?' '?' 'Strong' '?' '?']
general_h 8
'?', '?', '?', '?', '?'], ['?', '?', '?', '?', '?', '?']]
Final Specific_h:
['?' '?' '?' 'Strong' '?' '?']
Final General_h:
[['?', '?', '?', 'Strong', '?', '?']]
```

3. Write a program to demonstrate the working of the decision tree based ID3 algorithm. Use an appropriate data set for building the decision tree and apply this knowledge to classify a new sample.

ID3 - Algorithm

ID3(Examples, TargetAttribute, Attributes)

- Create a Root node for the tree
- If all Examples are positive, Return the single-node tree Root, with label = +
- If all Examples are negative, Return the single-node tree Root, with label = -
- If Attributes is empty, Return the single-node tree Root, with label = most common value of TargetAttribute in Examples
- Otherwise Begin
 - $-A \leftarrow$ the attribute from *Attributes* that best classifies *Examples*
 - The decision attribute for Root \leftarrow A
 - For each possible value, vi, of A,
 - Add a new tree branch below *Root*, corresponding to the test A = vi
 - Let Examples vi be the subset of Examples that have value vi for A
 - If $Examples_{vi}$ is empty
 - Then below this new branch add a leaf node with label = most common value of *TargetAttribute* in *Examples*
 - Else below this new branch add the subtree
 ID3(Examples_{vi}, TargetAttribute, Attributes {A})
- End
- Return Root



Source Code:

```
import numpy as np
import math
from data_loader import read_data
class Node:
   def init (self, attribute):
      self.attribute = attribute
      self.children = [] self.answer = ""
   def str (self):
      return self. attribute
def subtables(data, col, delete):
   dict = { }
items = np.unique(data[:, col])
   count = np.zeros((items.shape[0], 1), dtype=np.int32)
   for x in range(items.shape[0]):
     for y in range(data.shape[0]):

if data[y, col] == items[x]:

count[x] += 1
   for x in range(items.shape[0]):
      dict[items[x]] = np.empty((int(count[x]), data.shape[1]), dtype="|S32")
      pos = 0
      for y in range(data.shape[0]):
         if data[y, col] == items[x]:
dict[items[x]][pos] = data[y]
     pos += 1
         dict[items[x]] = np.delete(dict[items[x]], col, 1)
   return items, dict
def entropy(S):
   items = np.unique(S)
  if items.size == 1:
      return 0
   counts = np.zeros((items.shape[0], 1))
   sums = 0
   for x in range(items.shape[0]):
      counts[x] = sum(S == items[x]) / (S.size * 1.0)
   for count in counts:
      sums += -1 * count * math.log(count, 2)
   return sums
def gain ratio(data, col):
   items, dict = subtables(data, col, delete=False)
   total\_size = data.shape[0]
   entropies = np.zeros((items.shape[0], 1))
   intrinsic = np.zeros((items.shape[0], 1))
   for x in range(items.shape[0]):
     ratio = dict[items[x]].shape[0]/(total_size * 1.0)
entropies[x] = ratio * entropy(dict[items[x]][:, -1])
intrinsic[x] = ratio * math.log(ratio, 2)
```

```
total_entropy = entropy(data[:, -1])
iv = -1 * sum(intrinsic)
  for x in range(entropies.shape[0]):
     total_entropy -= entropies[x]
  return total_entropy / iv
def create node(data, metadata):
  #TODO: Co jeśli information gain jest zerowe?
  if (np.unique(data[:, -1])).shape[0] == 1:
  node = Node("")
     node.answer = np.unique(data[:, -1])[0]
     return node
  gains = np.zeros((data.shape[1] - 1, 1))
  for col in range(data.shape[1] - 1):
     gains[col] = gain_ratio(data, col)
  split = np.argmax(gains)
  node = Node(metadata[split])
  metadata = np.delete(metadata, split, 0)
  items, dict = subtables(data, split, delete=True)
  for x in range(items.shape[0]):
     child = create_node(dict[items[x]], metadata)
     node.children.append((items[x], child))
  return node
def empty(size):
  s =
  for x in range(size):
s += " "ge(size):
  return s
def print_tree(node, level):
   if node.answer != "":
     print(empty(level), node.answer)
  print(empty(level), node.attribute)
  for value, n in node children;
     print(empty(level + 1), value)
     print_tree(n, level + 2)
metadata, traindata = read_data("tennis.data")
data = np.array(traindata)
node = create_node(data, metadata)
print_tree(node, 0)
OUTPUT:
outlook
  overcast
    b'yes'
  rain
```

```
wind
b'strong'
b'no'
b'weak'
b'yes'
sunny
humidity
b'high'
b'no'
b'yes'
```

OR

```
import pandas as pd
import numpy as np
dataset= pd.read_csv('playtennis.csv',names=['outlook','temperature','humidity','wind','class',])
def entropy(target_col):
elements,counts = np.unique(target_col,return_counts = True)
  entropy = np.sum([(-counts[i]/np.sum(counts))*np.log2(counts[i]/np.sum(counts)) for i in
range(len(elements))])
  return entropy
def InfoGain(data,split_attribute_name,target_name="class"):
  total_entropy = entropy(data[target_name])
vals,counts= np.unique(data[split_attribute_name],return_counts=True)
Weighted_Entropy
np.sum([(counts[i]/np.sum(counts))*entropy(data.where(data[split_attribute_name]==vals[i]).dr opna()[target_name]) for i in range(len(vals))])
   Information_Gain = total_entropy - Weighted_Entropy
   return Information_Gain
def ID3(data,originaldata,features,target_attribute_name="class",parent_node_class = None):
   if len(np.unique(data[target_attribute_name])) <= 1:
     return np.unique(data[target_attribute_name])[0]
  elif len(data) == 0:
np.unique(originaldata[target_attribute_name])[np.argmax(np.unique(originaldata[target_attribut
e_name],return_counts=True)[1])]
  elif len(features) == 0:
  return parent_node_class else:
parent_node_class = np.unique(data[target_attribute_name])[np.argmax(np.unique(data[target_attribute_name],return
_counts=True)[1])]
item_values = [InfoGain(data,feature,target_attribute_name) for feature in features] #Return the information gain values for the features in the dataset
     best_feature_index = np.argmax(item_values)
     best_feature = features[best_feature_index]
tree = {best_feature:{}}
     features = [i for i in features if i != best_feature]
for value in np.unique(data[best_feature]):
    value = value
        sub_data = data.where(data[best_feature] == value).dropna()
        subtree = ID3(sub_data,dataset,features,target_attribute_name,parent_node_class)
        tree[best_feature][value] = subtree
     return(tree)
tree = ID3(dataset,dataset,dataset.columns[:-1])
print('\nDisplay Tree\n',tree)
OUTPUT:
Display Tree
{'outlook': {'Overcast': 'Yes', 'Rain': {'wind': {'Strong': 'No', 'Weak': 'Yes'}}, 'Sunny':
{'humidity': {'High': 'No', 'Normal': 'Yes'}}}
```

4. Build an Artificial Neural Network by implementing the Back propagation Algorithm and test the same using appropriate data sets.

```
function BackProp (D, \eta, n_{in}, n_{hidden}, n_{out})
  D is the training set consists of m pairs: \{(x_i, y_i)^m\}
- \eta is the learning rate as an example (0.1)

    n<sub>in</sub>, n<sub>hidden</sub> e n<sub>out</sub> are the numbero of imput hidden and output unit of neural network

    Make a feed-forward network with n_{\rm in}, n_{\rm hidden} e n_{\rm out} units
    Initialize all the weight to short randomly number (es. [-0.05 0.05])
    Repeat until termination condition are verifyed:
    For any sample in D:
           Forward propagate the network computing the output o_n of every unit u of the
           network
           Back propagate the errors onto the network:
                                                                           \delta_k = o_k (1 - o_k)(t_k - o_k)
             – For every output unit k, compute the error \delta_k:
             - For every hidden unit h compute the error \delta_h: \delta_h = o_h (1 - o_h) \sum_{k \in outputs} w_{kh} \delta_k
                                                          w_{ji} = w_{ji} + \Delta w_{ji}, \quad where \ \Delta w_{ji} = \eta \delta_j x_{ji}
             - Update the network weight wii:
                                 (x_{ii} \text{ is the input of unit j from coming from unit } i)
```

Back propagation Algorithm:

- 1. Load data set
- 2. Assign all network inputs and output
- 3. Initialize all weights with small random numbers, typically between -1 and 1 repeat

for every pattern in the training set

Present the pattern to the network

// Propagated the input forward through the network:

for each layer in the network

for every node in the layer

- 1. Calculate the weight sum of the inputs to the node
- 2. Add the threshold to the sum
- 3. Calculate the activation for thenode

end

end

// Propagate the errors backward through the network

for every node in the output layer calculate the error signal end

for all hidden layers

for every node in the layer

1. Calculate the node's signal error

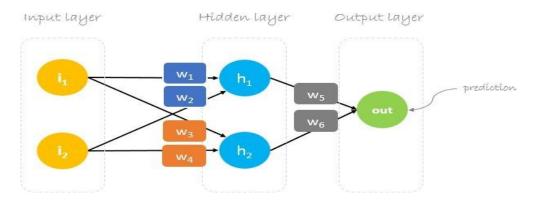
Update each node's weight in the network end

// Calculate Global Error

Calculate the Error Function

end

while ((maximum number of iterations < than specified) AND (Error Function is > than specified))



- Input layer with two inputs neurons
- One hidden layer with two neurons
- Output layer with a single neuron

Source Code:

```
import numpy as np
X = \text{np.array}(([2, 9], [1, 5], [3, 6]), \text{dtype=float})
y = np.array(([92], [86], [89]), dtype=float)
X = X/np.amax(X,axis=0) \# maximum of X array longitudinally <math>y = y/100
#Sigmoid Function
def sigmoid (x):
  return (1/(1 + np.exp(-x)))
#Derivative of Sigmoid Function
def derivatives_sigmoid(x):
  return x * (1 - x)
                                      #Variable initialization
epoch=7000
                                      #Setting training iterations
1r=0.1
                                      #Setting learning rate
                                      #number of features in data set
inputlayer\_neurons = 2
hiddenlayer\_neurons = 3
                                       #number of hidden layers neurons
output\_neurons = 1
                                       #number of neurons at output layer
```

```
#weight and bias initialization
wh=np.random.uniform(size=(inputlayer neurons, hiddenlayer neurons))
bh=np.random.uniform(size=(1,hiddenlayer_neurons))
wout=np.random.uniform(size=(hiddenlayer neurons,output neurons))
bout=np.random.uniform(size=(1,output_neurons))
# draws a random range of numbers uniformly of dim x*y
#Forward Propagation
for i in range(epoch):
  hinp1=np.dot(X,wh)
  hinp=hinp1 + bh
  hlayer act = sigmoid(hinp)
  outinp1=np.dot(hlayer_act,wout)
  outinp= outinp1+ bout
  output = sigmoid(outinp)
#Backpropagation
  EO = y-output
  outgrad = derivatives_sigmoid(output)
  d output = EO* outgrad
  EH = d\_output.dot(wout.T)
  hiddengrad = derivatives_sigmoid(hlayer_act)
#how much hidden layer wts contributed to error
  d_hiddenlayer = EH * hiddengrad
  wout += hlayer_act.T.dot(d_output) *lr
# dotproduct of nextlayererror and currentlayerop
  bout += np.sum(d_output, axis=0,keepdims=True) *lr
  wh += X.T.dot(d hiddenlayer) *lr
#bh += np.sum(d_hiddenlayer, axis=0,keepdims=True) *lr
print("Input: \n" + str(X))
print("Actual Output: \n" + str(y))
print("Predicted Output: \n" ,output)
   Output:
              Input:
              [[ 0.66666667 1.
              [ 0.33333333 0.55555556]
              [ 1.
                       0.66666667]]
              Actual Output:
              [[0.92]]
              [0.86]
              [0.89]
              Predicted Output:
              [[ 0.89559591]
              [ 0.88142069]
              [ 0.8928407 ]]
```

5. Write a program to implement the naïve Bayesian classifier for a sample training data set stored as a .CSV file. Compute the accuracy of the classifier, considering few test data sets.

Problem statement:

- Given features X1,X2,...,Xn
- Predict a label Y

X = (Rainy, Hot, High, False)

y = No

$$P(Y|X_1, \dots, X_n) = \frac{P(X_1, \dots, X_n|Y)P(Y)}{P(X_1, \dots, X_n)}$$

$$P(H | E) = \frac{P(E | H) * P(H)}{P(E)}$$

- P(H) is the probability of hypothesis H being true. This is known as the prior probability.
- P(E) is the probability of the evidence(regardless of the hypothesis).
- P(E|H) is the probability of the evidence given that hypothesis is true.
- P(H|E) is the probability of the hypothesis given that the evidence is there.
- Prior, conditional and joint probability for random variables
 - \triangleright Prior probability: P(x)
 - \triangleright Conditional probability: $P(x_1 | x_2), P(x_2 | x_1)$
 - > Joint probability: $\mathbf{x} = (x_1, x_2), P(\mathbf{x}) = P(x_1, x_2)$
 - Relationship: P(x,x) = P(x | x)P(x) = P(x | x)P(x)

1 2 2 1 1 1 2 2

Independence: $P(x \mid x) = P(x), P(x \mid x) = P(x), P(x,x) = P(x)P(x)$

Example:

- Digit Recognition
- $X_{1},...,X \in \{0,1\}$ (Black vs. White pixels)
- $Y \in \{5,6\}$ (predict whether a digit is a 5 or a 6)



$$P(c|\mathbf{x}) = \frac{P(\mathbf{x}|c)P(c)}{P(\mathbf{x})}$$

Naïve Bayesian classifier Algorthim:

Step 1: Convert the data set into a frequency table

Step 2: Create Likelihood table by finding the probabilities like Overcast probability = 0.29 and probability of playing is 0.64.

Weather	Play
Sunny	No
Overcast	Yes
Rainy	Yes
Sunny	Yes
Sunny	Yes
Overcast	Yes
Rainy	No
Rainy	No
Sunny	Yes
Rainy	Yes
Sunny	No
Overcast	Yes
Overcast	Yes
Rainy	No

Frequency Table						
Weather	No	Yes				
Overcast		4				
Rainy	3	2				
Sunny	2	3				
Grand Total	5	9				

Lik	elihood tab]		
Weather	No	Yes		
Overcast		4	=4/14	0.29
Rainy	3	2	=5/14	0.36
Sunny	2	3	=5/14	0.36
All	5	9		
	=5/14	=9/14		
	0.36	0.64]	

Step 3: Now, use Naive Bayesian equation to calculate the posterior probability for each class. The class with the highest posterior probability is the outcome of prediction.

Problem: Players will play if weather is sunny. Is this statement is correct?

We can solve it using above discussed method of posterior probability.

$$P(Yes | Sunny) = P(Sunny | Yes) * P(Yes) / P(Sunny)$$

Here we have P (Sunny | Yes) =
$$3/9 = 0.33$$
, P(Sunny) = $5/14 = 0.36$, P(Yes)= $9/14 = 0.64$

Now, P (Yes | Sunny) =
$$0.33 * 0.64 / 0.36 = 0.60$$
, which has higher probability.

Naive Bayes uses a similar method to predict the probability of different class based on various attributes. This algorithm is mostly used in text classification and with problems having multiple classes.

$$\mu = \frac{1}{n} \sum_{i=1}^{n} x_{i}$$
 Mean
$$\sigma = \left[\frac{1}{n-1} \sum_{i=1}^{n} \left(x_{i} - \mu \right)^{2} \right]^{0.5}$$
 Standard deviation
$$f(x) = \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{(x-\mu)^{2}}{2\sigma^{2}}}$$
 Normal distribution

Example: Continuous-valued Features

Temperature is naturally of continuous value.

No: 27.3, 30.1, 17.4, 29.5, 15.1

Estimate mean and variance for each class
$$\mu = N \sum_{n=1}^{N} x_n$$
, $\sigma = N \sum_{n=1}^{N} (x_n - \mu)^2$ $\mu_{NO} = 23.88$, $\sigma_{NO} = 7.09$

Learning Phase: output two Gaussian models for P(temp|C)

$$\hat{P}(x|Yes) = \frac{1}{2.35} \frac{\exp\left(-\frac{(x-21.64)^2)\Upsilon_1}{2 \times 2.35^2}\right)} = \frac{\exp\left(-\frac{(x-21.64)^2)}{2 \times 2.35}\right)}{\exp\left(-\frac{(x-21.64)^2)}{2 \times 2.35^2}\right)} = \frac{2.35 \sqrt{2\pi} \exp\left(-\frac{11.09}{(x-23.88)^2}\right)}{\exp\left(-\frac{(x-21.64)^2}{2 \times 2.35^2}\right)} = \frac{\exp\left(-\frac{(x-21.64)^2)}{11.09}\right)}{\exp\left(-\frac{(x-21.64)^2)}{2 \times 7.09^2}\right)} = \frac{\exp\left(-\frac{(x-21.64)^2)}{11.09}\right)}{\exp\left(-\frac{(x-21.64)^2)}{2 \times 7.09^2}\right)}$$

Source Code:

```
import csv
import random
import math
def loadCsv(filename):
       lines = csv.reader(open(filename, "r"))
       dataset = list(lines)
       for i in range(len(dataset)):
               dataset[i] = [float(x) for x in dataset[i]]
       return dataset
def splitDataset(dataset, splitRatio):
       trainSize = int(len(dataset) * splitRatio)
       trainSet = []
       copy = list(dataset)
        while len(trainSet) < trainSize:
               index = random.randrange(len(copy))
               trainSet.append(copy.pop(index))
       return [trainSet, copy]
def separateByClass(dataset):
       separated = \{\}
       for i in range(len(dataset)):
               vector = dataset[i]
               if (vector[-1] not in separated):
```

separated[vector[-1]] = []
separated[vector[-1]].append(vector)
return separated

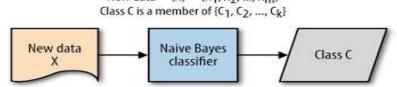
```
def mean(numbers):
       return sum(numbers)/float(len(numbers))
def stdev(numbers):
       avg = mean(numbers)
       variance = sum([pow(x-avg,2) for x in numbers])/float(len(numbers)-1)
       return math.sqrt(variance)
def summarize(dataset):
       summaries = [(mean(attribute), stdev(attribute)) for attribute in zip(*dataset)]
       del summaries[-1]
       return summaries
def summarizeByClass(dataset):
       separated = separateByClass(dataset)
       summaries = \{\}
       for classValue, instances in separated.items():
              summaries[classValue] = summarize(instances)
       return summaries
def calculateProbability(x, mean, stdev):
       exponent = math.exp(-(math.pow(x-mean,2)/(2*math.pow(stdev,2))))
       return (1 / (math.sqrt(2*math.pi) * stdev)) * exponent
def calculateClassProbabilities(summaries, inputVector):
       probabilities = {}
       for classValue, classSummaries in summaries.items():
              probabilities[classValue] = 1
              for i in range(len(classSummaries)):
                      mean, stdev = classSummaries[i]
                      x = inputVector[i]
                      probabilities[classValue] *= calculateProbability(x, mean, stdev)
       return probabilities
def predict(summaries, inputVector):
       probabilities = calculateClassProbabilities(summaries, inputVector)
       bestLabel, bestProb = None, -1
       for class Value, probability in probabilities.items():
              if bestLabel is None or probability > bestProb:
                      bestProb = probability
                      bestLabel = classValue
       return bestLabel
def getPredictions(summaries, testSet):
       predictions = []
       for i in range(len(testSet)):
              result = predict(summaries, testSet[i])
```

```
predictions.append(result)
       return predictions
def getAccuracy(testSet, predictions):
       correct = 0
       for i in range(len(testSet)):
              if testSet[i][-1] == predictions[i]:
                      correct += 1
       return (correct/float(len(testSet))) * 100.0
def main():
       filename = 'data.csv'
       splitRatio = 0.67
       dataset = loadCsv(filename)
       trainingSet, testSet = splitDataset(dataset, splitRatio)
       print('Split {0} rows into train={1} and test={2} rows'.format(len(dataset),
len(trainingSet), len(testSet)))
       # prepare model
       summaries = summarizeByClass(trainingSet)
       # test model
       predictions = getPredictions(summaries, testSet)
       accuracy = getAccuracy(testSet, predictions)
       print('Accuracy: {0}%'.format(accuracy))
main()
OUTPUT:
Split 306 rows into train=205 and test=101 rows
Accuracy: 72.27722772278%
```

6. Assuming a set of documents that need to be classified, use the naïve Bayesian Classifier model to perform this task. Built-in Java classes/API can be used to write the program. Calculate the accuracy, precision, and recall for your data set.

Posterior Probability
$$P(c \mid x) = \frac{P(x \mid c)P(c)}{P(x)}$$
Posterior Probability
$$P(c \mid X) = P(x_1 \mid c) \times P(x_2 \mid c) \times \cdots \times P(x_n \mid c) \times P(c)$$
Classification process

New data = $(X) = (X_1, X_2, ..., X_m)$



The dataset is divided into two parts, namely, feature matrix and the response vector.

- Feature matrix contains all the vectors(rows) of dataset in which each vector consists of the value of dependent features. In above dataset, features are 'Outlook', 'Temperature', 'Humidity' and 'Windy'.
- Response vector contains the value of class variable(prediction or output) for each row of feature matrix. In above dataset, the class variable name is 'Play golf'.

Types of Naive Bayes Algorithm

Gaussian Naive Bayes

When attribute values are continuous, an assumption is made that the values associated with each class are distributed according to Gaussian i.e., Normal Distribution.

If in our data, an attribute say "x" contains continuous data. We first segment the data by the class and then compute mean μ_y & Variance σ_y^2 of each class.

$$P(x_i|y) = \frac{1}{\sqrt{2\pi\sigma_y^2}} exp\left(-\frac{(x_i - \mu_y)^2}{2\sigma_y^2}\right)$$

MultiNomial Naive Bayes

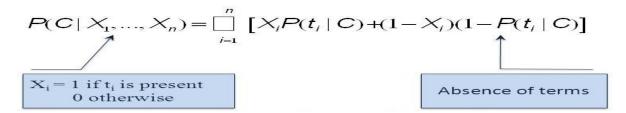
MultiNomial Naive Bayes is preferred to use on data that is multinomially distributed. It is one of the standard classic algorithms. Which is used in text categorization (classification). Each event in text classification represents the occurrence of a word in a document.

$$p(\mathbf{x} \mid C_k) = rac{(\sum_i x_i)!}{\prod_i x_i!} \prod_i p_{ki}{}^{x_i}$$

$$\hat{P}(x_i \mid \omega_j) = rac{\sum t f(x_i, d \in \omega_j) + lpha}{\sum N_{d \in \omega_j} + lpha \cdot V}$$

Bernoulli Naive Bayes

Bernoulli Naive Bayes is used on the data that is distributed according to multivariate Bernoulli distributions.i.e., multiple features can be there, but each one is assumed to be a binary-valued (Bernoulli, boolean) variable. So, it requires features to be binary valued.



Algorithm 1 Pseudocode

- Given training data set D which consists of documents belonging to different class say class A and B.
- Calculate the prior probability of class A=number of objects of class A / total number of objects
 Calculate the prior probability of class B=number of objects of class B / total number of objects
- Find ni, the total number of word frequency of each class.
 na= the total number of word frequency of class A.
 nb= the total number of word frequency of class B.
- Find conditional probability of keyword occurrence given a class.

P(word1 / class A) = wordcount / ni(A)
P(word1 / class B) =wordcount / ni(B)
P(word2 / class A) = wordcount / ni(A)
P(word2 / class B) =wordcount / ni(B)

P(wordn / class B) =wordcount / ni(B)

- Avoid zero frequency problems by applying uniform distribution.
- Classify a new document C based on the probability P(C /W).
 - a) Find P(A / W) = P(A) * P(word1/ class A) * P(word2/ class A) * P(wordn / class A).
 - b) Find P(B / W) = P(B) * P(word1 / class B) * P(word2/class B)* P(wordn / class B).
- Assign document to class that has higher probability.

Source Code:

```
import pandas as pd
msg=pd.read_csv('naivetext1.csv',names=['message','label'])
print('The dimensions of the dataset',msg.shape)
msg['labelnum']=msg.label.map({'pos':1,'neg':0})
X=msg.message
y=msg.labelnum
print(X)
print(y)
from sklearn.model_selection import train_test_split
xtrain,xtest,ytrain,ytest=train_test_split(X,y)
print(xtest.shape)
print(xtrain.shape)
print(ytest.shape)
print(ytrain.shape)
from sklearn.feature_extraction.text import CountVectorizer
count_vect = CountVectorizer()
xtrain_dtm = count_vect.fit_transform(xtrain)
xtest_dtm=count_vect.transform(xtest)
from sklearn.naive_bayes import MultinomialNB
clf = MultinomialNB().fit(xtrain_dtm,ytrain)
predicted = clf.predict(xtest_dtm)
from sklearn import metrics
print('Accuracy metrics')
print('Accuracy of the classifer is',metrics.accuracy_score(ytest,predicted))
print('Confusion matrix')
print(metrics.confusion_matrix(ytest,predicted))
print('Recall and Precison ')
print(metrics.recall_score(ytest,predicted))
print(metrics.precision_score(ytest,predicted))
Output:
The dimensions of the dataset (18, 2)
0
              I love this sandwich
1
            This is an amazing place
2
      I feel very good about these beers
3
               This is my best work
               What an awesome view
4
5
         I do not like this restaurant
6
            I am tired of this stuff
```

```
7
             I can't deal with this
8
              He is my sworn enemy
               My boss is horrible
9
            This is an awesome place
10
    I do not like the taste of this juice
11
12
                  I love to dance
13
       I am sick and tired of this place
               What a great holiday
14
15
         That is a bad locality to stay
16
         We will have good fun tomorrow
       I went to my enemy's house today
17
Name: message, dtype: object
0
    1
    1
1
2
    1
3
    1
4
    1
5
    0
6
    0
7
    0
8
    0
9
    0
10
    1
    0
11
12
    1
13 0
14
    1
15 0
16 1
17 0
Name: labelnum, dtype: int64
(5,)
(13,)
(5,)
(13,)
Accuracy metrics
Accuracy of the classifer is 0.8
Confusion matrix
[[3 1]
[0 1]]
Recall and Precison
1.0
0.5
```

7. Write a program to construct a Bayesian network considering medical data. Use this model to demonstrate the diagnosis of heart patients using standard Heart Disease Data Set. You can use Java/Python ML library classes/API.

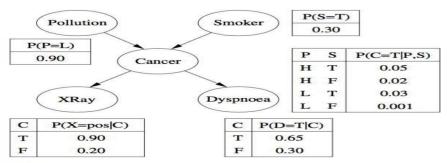


FIGURE 2.1
A BN for the lung cancer problem.

Attribute Information:

- -- Only 14 used
 - -- 1. #3 (age)
 - -- 2. #4 (sex)
 - -- 3. #9 (cp)
 - -- 4. #10 (trestbps)
 - -- 5. #12 (chol)
 - -- 6. #16 (fbs)
 - -- 7. #19 (restecg)
 - -- 8. #32 (thalach)
 - -- 9. #38 (exang)
 - -- 10. #40 (oldpeak)
 - -- 11. #41 (slope)
 - -- 12. #44 (ca)
 - -- 13. #51 (thal)
 - -- 14. #58 (num)

Source Code:

import numpy as np

from urllib.request import urlopen

import urllib

import pandas as pd

from pgmpy.inference import VariableElimination

from pgmpy.models import BayesianModel

from pgmpy.estimators import MaximumLikelihoodEstimator, BayesianEstimator

names = ['age', 'sex', 'cp', 'trestbps', 'chol', 'fbs', 'restecg', 'thalach', 'exang', 'oldpeak', 'slope', 'ca', 'thal', 'heartdisease']

heartDisease = pd.read_csv('heart.csv', names = names)

heartDisease = heartDisease.replace('?', np.nan)

model = BayesianModel([('age', 'trestbps'), ('age', 'fbs'), ('sex', 'trestbps'), ('exang', 'trestbps'), ('trestbps', 'heartdisease'), ('fbs', 'heartdisease', 'restecg'), ('heartdisease', 'thalach'), ('heartdisease', 'chol')])

model.fit(heartDisease, estimator=MaximumLikelihoodEstimator) from pgmpy.inference import VariableElimination HeartDisease_infer = VariableElimination(model)

 $q = HeartDisease_infer.query(variables=['heartdisease'], \ evidence=\{'age': 37, \ 'sex': 0\}) \\ print(q['heartdisease'])$

OUTPUT:

heartdisease	phi(heartdisease)
heartdisease_0	0.5593
heartdisease_1	0.4407

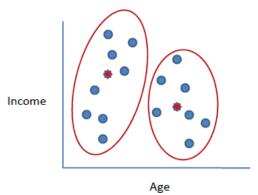
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8. Apply EM algorithm to cluster a set of data stored in a .CSV file. Use the same data set for clustering using k-Means algorithm. Compare the results of these two algorithms and comment on the quality of clustering. You can add Java/Python ML library classes/API in the program.

Distance functions

K-Means Algorithm

- 1. Load data set
- 2. Clusters the data into k groups where k is predefined.
- 3. Select *k* points at random as cluster centers.
- 4. Assign objects to their closest cluster center according to the *Euclidean distance* function.
- 5. Calculate the centroid or mean of all objects in each cluster.
- 6. Repeat steps 3, 4 and 5 until the same points are assigned to each cluster in consecutive rounds.



Example:

Suppose we want to group the visitors to a website using just their age (one-dimensional space) as follows:

$$n = 19$$

15,15,16,19,19,20,20,21,22,28,35,40,41,42,43,44,60,61,65

Initial clusters (random centroid or average):

$$k = 2$$

$$c_1 = 16$$

$$c_2 = 22$$

Iteration 1:

$$c_1 = 15.33$$

 $c_2 = 36.25$

x_i	C1	<i>c</i> ₂	Distance 1	Distance 2	Nearest Cluster	New Centroid
15	16	22	1	7	1	
15	16	22	1	7	1	15.33
16	16	22	0	6	1	
19	16	22	9	3	2	
19	16	22	9	3	2	
20	16	22	16	2	2	
20	16	22	16	2	2	
21	16	22	25	1	2	
22	16	22	36	0	2	
28	16	22	12	6	2	
35	16	22	19	13	2	
40	16	22	24	18	2	36.25
41	16	22	25	19	2	
42	16	22	26	20	2	
43	16	22	27	21	2	
44	16	22	28	22	2	
60	16	22	44	38	2	
61	16	22	45	39	2	
65	16	22	49	43	2	

Iteration 2:

$$c_1 = 18.56$$

 $c_2 = 45.90$

χ_i	C1	<i>c</i> ₂	Distance 1	Distance 2	Nearest Cluster	New Centroid
15	15.33	36.25	0.33	21.25	1	
15	15.33	36.25	0.33	21.25	1	
16	15.33	36.25	0.67	20.25	1	
19	15.33	36.25	3.67	17.25	1	
19	15.33	36.25	3.67	17.25	1	18.56
20	15.33	36.25	4.67	16.25	1	
20	15.33	36.25	4.67	16.25	1	
21	15.33	36.25	5.67	15.25	1	
22	15.33	36.25	6.67	14.25	1	
28	15.33	36.25	12.67	8.25	2	45.0
35	15.33	36.25	19.67	1.25	2	45.9

40	15.33	36.25	24.67	3.75	2	
41	15.33	36.25	25.67	4.75	2	
42	15.33	36.25	26.67	5.75	2	
43	15.33	36.25	27.67	6.75	2	
44	15.33	36.25	28.67	7.75	2	
60	15.33	36.25	44.67	23.75	2	
61	15.33	36.25	45.67	24.75	2	
65	15.33	36.25	49.67	28.75	2	

Iteration 3:

$$c_1 = 19.50$$

 $c_2 = 47.89$

ν.	2.	a.	Distance 1	Distance 2	Nearest	New
x_i	c_1	<i>C</i> ₂	Distance 1	Distance 2	Cluster	Centroid
15	18.56	45.9	3.56	30.9	1	
15	18.56	45.9	3.56	30.9	1	
16	18.56	45.9	2.56	29.9	1	
19	18.56	45.9	0.44	26.9	1	
19	18.56	45.9	0.44	26.9	1	10.50
20	18.56	45.9	1.44	25.9	1	19.50
20	18.56	45.9	1.44	25.9	1	
21	18.56	45.9	2.44	24.9	1	
22	18.56	45.9	3.44	23.9	1	
28	18.56	45.9	9.44	17.9	1	
35	18.56	45.9	16.44	10.9	2	
40	18.56	45.9	21.44	5.9	2	
41	18.56	45.9	22.44	4.9	2	
42	18.56	45.9	23.44	3.9	2	
43	18.56	45.9	24.44	2.9	2	47.89
44	18.56	45.9	25.44	1.9	2	
60	18.56	45.9	41.44	14.1	2	
61	18.56	45.9	42.44	15.1	2	
65	18.56	45.9	46.44	19.1	2	

Iteration 4:

$$c_1 = 19.50$$

 $c_2 = 47.89$

x_i	<i>C</i> ₁	<i>c</i> ₂	Distance 1	Distance 2	Nearest Cluster	New Centroid
15	19.5	47.89	4.50	32.89	1	10.50
15	19.5	47.89	4.50	32.89	1	19.50

	1	31.89	3.50	47.89	19.5	16
	1	28.89	0.50	47.89	19.5	19
	1	28.89	0.50	47.89	19.5	19
	1	27.89	0.50	47.89	19.5	20
	1	27.89	0.50	47.89	19.5	20
	1	26.89	1.50	47.89	19.5	21
	1	25.89	2.50	47.89	19.5	22
	1	19.89	8.50	47.89	19.5	28
	2	12.89	15.50	47.89	19.5	35
	2	7.89	20.50	47.89	19.5	40
	2	6.89	21.50	47.89	19.5	41
	2	5.89	22.50	47.89	19.5	42
47.89	2	4.89	23.50	47.89	19.5	43
	2	3.89	24.50	47.89	19.5	44
	2	12.11	40.50	47.89	19.5	60
	2	13.11	41.50	47.89	19.5	61
	2	17.11	45.50	47.89	19.5	65

No change between iterations 3 and 4 has been noted. By using clustering, 2 groups have been identified 15-28 and 35-65. The initial choice of centroids can affect the output clusters, so the algorithm is often run multiple times with different starting conditions in order to get a fair view of what the clusters should be.

EM algorithm

These are the two basic steps of the EM algorithm, namely E Step or Expectation Step or Estimation Step and M Step or Maximization Step.

• Estimation step:

- initialize $\mu_k, \sum k$ and π_k by some random values, or by K means clustering results or by hierarchical clustering results.
- Then for those given parameter values, estimate the value of the latent variables (i.e γ_k)

• Maximization Step:

- Update the value of the parameters (i.e. $\mu_k, \sum k$ and π_k) calculated using ML method.
- 1. Load data set
- 2. Initialize the mean μ_k , the covariance matrix $\sum k$ and the mixing coefficients
 - 1. π_k by some random values. (or other values)
- 3. Compute the γ_k values for all k.

- 4. Again Estimate all the parameters using the current γ_k values.
- 5. Compute log-likelihood function.
- 6. Put some convergence criterion
- 7. If the log-likelihood value converges to some value (or if all the parameters converge to some values) then **stop**, else return to **Step 3**.

Source Code:

```
import numpy as np
from sklearn.cluster import KMeans
import matplotlib.pyplot as plt
from sklearn.mixture import GaussianMixture
import pandas as pd
X=pd.read_csv("kmeansdata.csv")
x1 = X['Distance\_Feature'].values
x2 = X['Speeding\_Feature'].values
X = \text{np.array}(\text{list}(\text{zip}(x1, x2))).\text{reshape}(\text{len}(x1), 2)
plt.plot()
plt.xlim([0, 100])
plt.ylim([0, 50])
plt.title('Dataset')
plt.scatter(x1, x2)
plt.show()
#code for EM
gmm = GaussianMixture(n_components=3)
gmm.fit(X)
em_predictions = gmm.predict(X)
print("\nEM predictions")
print(em_predictions)
print("mean:\n",gmm.means_)
print('\n')
print("Covariances\n",gmm.covariances_)
print(X)
plt.title('Exceptation Maximum')
plt.scatter(X[:,0], X[:,1],c=em_predictions,s=50)
plt.show()
#code for Kmeans
import matplotlib.pyplot as plt1
kmeans = KMeans(n clusters=3)
```

kmeans.fit(X)

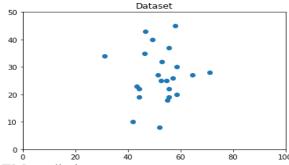
```
print(kmeans.cluster_centers_)
print(kmeans.labels_)
```

plt.title('KMEANS')

plt1.scatter(X[:,0], X[:,1], c=kmeans.labels_, cmap='rainbow')

plt1.scatter(kmeans.cluster_centers_[:,0],kmeans.cluster_centers_[:,1], color='black')

OUTPUT:



EM predictions

 $[0\ 0\ 0\ 1\ 0\ 1\ 1\ 1\ 2\ 1\ 2\ 2\ 1\ 1\ 2\ 1\ 2\ 1\ 0\ 1\ 0\ 1\ 1]$

[[57.70629058 25.73574491]

[52.12044022 22.46250453]

[46.4364858 39.43288647]]

Covariances

[[[83.51878796 14.926902] [14.926902 2.70846907]]

[[29.95910352 15.83416554] [15.83416554 67.01175729]]

[[79.34811849 29.55835938]

[29.55835938 18.17157304]]]

[[71.24 28.]

[52.53 25.]

[64.54 27.]

[55.69 22.]

[54.58 25.]

[41.91 10.]

[58.64 20.]

[52.02 8.]

[31.25 34.]

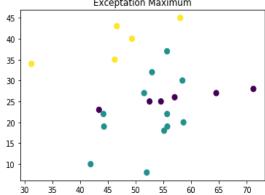
[44.31 19.]

[49.35 40.]

[58.07 45.]

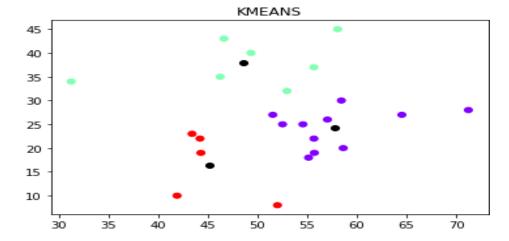
```
[44.22 22. ]
[55.73 19. ]
[46.63 43. ]
[52.97 32. ]
[46.25 35. ]
[51.55 27. ]
[57.05 26. ]
[58.45 30. ]
[43.42 23. ]
[55.68 37. ]
[55.15 18. ]

Exceptation Maximum
```



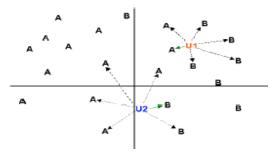
centroid and predications

[[57.74090909 24.27272727] [48.6 38.] [45.176 16.4]] [0 0 0 0 0 2 0 2 1 2 1 1 2 0 1 1 1 0 0 0 2 1 0]



9. Write a program to implement k-Nearest Neighbour algorithm to classify the iris data set. Print both correct and wrong predictions. Java/Python ML library classes can be used for this problem.

• Principle: points (documents) that are close in the space belong to the same class



Distance Metrics

Minkowsky:

$$D(x,y) = \left(\sum_{i=1}^{m} |x_i - y_i|^r\right)^{1/r} \qquad D(x,y) = \sqrt{\sum_{i=1}^{m} (x_i - y_i)^2} \qquad D(x,y) = \sum_{i=1}^{m} |x_i - y_i|$$

$$D(x,y) = \sqrt{\sum_{i=1}^{m} (x_i - y_i)^2}$$

Manhattan / city-block:

$$D(x,y) = \sum_{i=1}^{m} |x_i - y_i|$$

Camberra:

$$D(x,y) = \sum_{i=1}^{m} \frac{|x_i - y_i|}{|x_i + y_i|}$$

Chebychev:
$$D(x,y) = \max_{i=1}^{m} |x_i - y_i|$$

Quadratic:
$$D(x,y) = (x-y)^T Q(x-y) = \sum_{j=1}^m \left(\sum_{i=1}^m (x_i - y_i)q_{ji}\right)(x_j - y_j)$$

Q is a problem-specific positive definite $m \times m$ weight matrix

Mahalanobis:

$$D(x, y) = [\det V]^{1/m} (x - y)^{\mathrm{T}} V^{-1} (x - y)$$

V is the covariance matrix of $A_1.A_m$, and A_i is the vector of values for attribute j occuring in the training set instances 1..n.

Correlation: $D(x,y) = \frac{\sum_{i=1}^{m} (x_i - \overline{x_i})(y_i - \overline{y_i})}{\sqrt{\sum_{i=1}^{m} (x_i - \overline{x_i})^2 \sum_{i=1}^{m} (y_i - \overline{y_i})^2}}$

 $\overline{x_i} = \overline{y_i}$ and is the average value for attribute i occuring in the training set.

Chi-square: $D(x,y) = \sum_{i=1}^{m} \frac{1}{sum_i} \left(\frac{x_i}{size_x} - \frac{y_i}{size_y} \right)^2$

sum_i is the sum of all values for attribute i occurring in the training set, and $size_x$ is the sum of all values in the vector x.

 $D(x,y) = 1 - \frac{2}{n(n-1)} \sum_{i=1}^{m} \sum_{j=1}^{i-1} \operatorname{sign}(x_i - x_j) \operatorname{sign}(y_i - y_j)$ **Kendall's Rank Correlation:** sign(x)=-1, 0 or 1 if x < 0,x = 0, or x > 0, respectively.

Figure 1. Equations of selected distance functions. (x and y are vectors of m attribute values).

K-Nearest-Neighbour Algorithm:

- 1. Load the data
- 2. Initialize the value of k
- 3. For getting the predicted class, iterate from 1 to total number of training data points
 - 1. Calculate the distance between test data and each row of training data. Here we will use Euclidean distance as our distance metric since it's the most popular method. The other metrics that can be used are Chebyshev, cosine, etc.
 - 2. Sort the calculated distances in ascending order based on distance values
 - 3. Get top k rows from the sorted array
 - 4. Get the most frequent class of these rows i.e Get the labels of the selected K entries
 - 5. Return the predicted class
 - If regression, return the mean of the K labels
 - If classification, return the mode of the K labels

Confusion matrix:

Note,

• Class 1 : Positive

• Class 2 : Negative

	Class 1 Predicted	Class 2 Predicted
Class 1 Actual	TP	FN
Class 2 Actual	FP	TN

- Positive (P): Observation is positive (for example: is an apple).
- Negative (N): Observation is not positive (for example: is not an apple).
- True Positive (TP): Observation is positive, and is predicted to be positive.
- False Negative (FN): Observation is positive, but is predicted negative. (Also known as a "Type II error.")
- True Negative (TN): Observation is negative, and is predicted to be negative.
- False Positive (FP): Observation is negative, but is predicted positive. (Also known as a "Type I error.")

Accuracy =
$$\frac{TP + TN}{TP + TN + FP + FN}$$
 Recall = $\frac{TP}{TP + FN}$

$$Precision = \frac{TP}{TP + FP}$$

Example:

n=165	Predicted: NO	Predicted: YES	
Actual: NO	TN = 50	FP = 10	60
Actual: YES	FN = 5	TP = 100	105
	55	110	

Accuracy: Overall, how often is the classifier correct?

(TP+TN)/total = (100+50)/165 = 0.91

Misclassification Rate: Overall, how often is it wrong?

(FP+FN)/total = (10+5)/165 = 0.09

equivalent to 1 minus Accuracy

also known as "Error Rate"

True Positive Rate: When it's actually yes, how often does it predict yes?

TP/actual yes = 100/105 = 0.95

also known as "Sensitivity" or "Recall"

False Positive Rate: When it's actually no, how often does it predict yes?

FP/actual no = 10/60 = 0.17

True Negative Rate: When it's actually no, how often does it predict no?

TN/actual no = 50/60 = 0.83

equivalent to 1 minus False Positive Rate

also known as "Specificity"

Precision: When it predicts yes, how often is it correct?

TP/predicted yes = 100/110 = 0.91

Prevalence: How often does the yes condition actually occur in our sample?

actual yes/total = 105/165 = 0.64

Source Code:

from sklearn.neighbors import KNeighborsClassifier

from sklearn.metrics import confusion_matrix

from sklearn.metrics import accuracy_score

from sklearn.metrics import classification_report

from sklearn.model selection import train test split

import pandas as pd

dataset=pd.read_csv("iris.csv")

X_train,X_test,y_train,y_test=train_test_split(X,y,random_state=0,test_size=0.25)

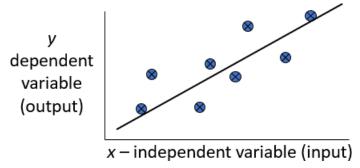
classifier=KNeighborsClassifier(n_neighbors=8,p=3,metric='euclidean')

```
classifier.fit(X_train,y_train)
#predict the test resuts
y_pred=classifier.predict(X_test)
cm=confusion_matrix(y_test,y_pred)
print('Confusion matrix is as follows\n',cm)
print('Accuracy Metrics')
print(classification_report(y_test,y_pred))
print(" correct predicition",accuracy_score(y_test,y_pred))
print(" worng predicition",(1-accuracy_score(y_test,y_pred)))
Output:
Confusion matrix is as follows
[[13 0 0]
[0151]
[0\ 0\ 9]]
Accuracy Metrics
          precision recall f1-score support
  Iris-setosa
                 1.00
                         1.00
                                 1.00
                                           13
Iris-versicolor
                  1.00
                          0.94
                                   0.97
                                            16
Iris-virginica
                  0.90
                                  0.95
                                            9
                          1.00
  avg / total
                0.98
                         0.97
                                 0.97
                                          38
```

correct predicition 0.9736842105263158 worng predicition 0.02631578947368418

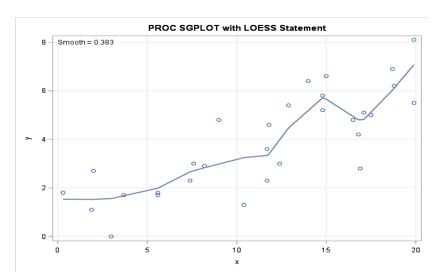
10. Implement the non-parametric Locally Weighted Regression algorithm in order to fit data points. Select appropriate data set for your experiment and draw graphs.

- **Regression** is a technique from statistics that is used to predict values of a desired target quantity when the target quantity is continuous.
- In regression, we seek to identify (or estimate) a continuous variable y associated with a given input vector x.
- y is called the dependent variable.
- x is called the independent variable.



Loess/Lowess Regression: Loess regression is a nonparametric technique that uses *local* weighted regression to fit a smooth curve through points in a scatter plot.

Lowess Algorithm: Locally weighted regression is a very powerful non-parametric model used in statistical learning . Given a *dataset* X, y, we attempt to find a *model* parameter $\beta(x)$ that minimizes *residual sum of weighted squared errors*. The weights are given by a *kernel function*(k or w) which can be chosen arbitrarily .



Locally Weighted Regression Algorithm:

- 1. Read the Given data Sample to X and the curve (linear or non linear) to Y
- 2. Set the value for Smoothening parameter or free parameter say τ
- 3. Set the bias /Point of interest set X0 which is a subset of X
- 4. Determine the weight matrix using:

$$w(x, x_o) = e^{-\frac{(x - x_o)^2}{2\tau^2}}$$

5. Determine the value of model term parameter β using :

$$\hat{\beta}(x_0) = (X^T W X)^{-1} X^T W y$$

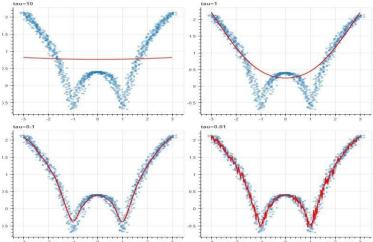
6. Prediction = $x0*\beta$

Source Code:

jitter X

```
import numpy as np
from bokeh.plotting import figure, show, output notebook
from bokeh.layouts import gridplot
from bokeh.io import push_notebook
def local_regression(x0, X, Y, tau):
# add bias term
x0 = np.r_{1}, x0 # Add one to avoid the loss in information
X = np.c_[np.ones(len(X)), X]
# fit model: normal equations with kernel
xw = X.T * radial kernel(x0, X, tau) # XTranspose * W
beta = np.linalg.pinv(xw @ X) @ xw @ Y # @ Matrix Multiplication or Dot Product
# predict value
return x0 @ beta # @ Matrix Multiplication or Dot Product for prediction
def radial_kernel(x0, X, tau):
return np.exp(np.sum((X - x0) ** 2, axis=1) / (-2 * tau * tau))
# Weight or Radial Kernal Bias Function
n = 1000
# generate dataset
X = np.linspace(-3, 3, num=n)
print("The Data Set (10 Samples) X : n'', X[1:10])
Y = np.log(np.abs(X ** 2 - 1) + .5)
print("The Fitting Curve Data Set (10 Samples) Y:\n",Y[1:10])
```

```
X += np.random.normal(scale=.1, size=n)
print("Normalised (10 Samples) X:\n",X[1:10])
domain = np.linspace(-3, 3, num=300)
print(" Xo Domain Space(10 Samples) :\n",domain[1:10])
def plot_lwr(tau):
# prediction through regression
prediction = [local regression(x0, X, Y, tau) for x0 in domain]
plot = figure(plot_width=400, plot_height=400)
plot.title.text='tau=%g' % tau
plot.scatter(X, Y, alpha=.3)
plot.line(domain, prediction, line width=2, color='red')
return plot
# Plotting the curves with different tau
show(gridplot([
[plot_lwr(10.), plot_lwr(1.)],
[plot_lwr(0.1), plot_lwr(0.01)]
1))
Output:
The Data Set (10 Samples) X:
[-2.99399399 -2.98798799 -2.98198198 -2.97597598 -2.96996997 -2.96396396
-2.95795796 -2.95195195 -2.94594595]
The Fitting Curve Data Set (10 Samples) Y:
[2.13582188 2.13156806 2.12730467 2.12303166 2.11874898 2.11445659
2.11015444 2.10584249 2.10152068]
Normalised (10 Samples) X:
[-3.10518137 -3.00247603 -2.9388515 -2.79373602 -2.84946247 -2.85313888
-2.9622708 -3.09679502 -2.69778859]
Xo Domain Space(10 Samples):
[-2.97993311 -2.95986622 -2.93979933 -2.91973244 -2.89966555 -2.87959866
-2.85953177 -2.83946488 -2.81939799]
```



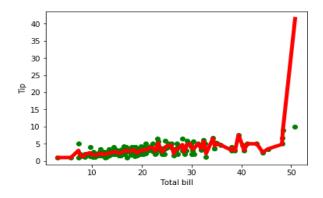
```
OR
from numpy import *
import operator
from os import listdir
import matplotlib
import matplotlib.pyplot as plt
import pandas as pd
import numpy.linalg
from scipy.stats.stats import pearsonr
def kernel(point,xmat, k):
  m,n = shape(xmat)
  weights = mat(eye((m)))
  for j in range(m):
     diff = point - X[j]
     weights[j,j] = \exp(\operatorname{diff*diff.T/(-2.0*k**2)})
  return weights
def localWeight(point,xmat,ymat,k):
  wei = kernel(point,xmat,k)
  W = (X.T*(wei*X)).I*(X.T*(wei*ymat.T))
  return W
def localWeightRegression(xmat,ymat,k):
  m,n = shape(xmat)
  ypred = zeros(m)
  for i in range(m):
     ypred[i] = xmat[i]*localWeight(xmat[i],xmat,ymat,k)
  return ypred
# load data points
data = pd.read_csv('tips.csv')
bill = array(data.total_bill)
tip = array(data.tip)
```

```
#preparing and add 1 in bill
mbill = mat(bill)
mtip = mat(tip)
m= shape(mbill)[1]
one = mat(ones(m))
X= hstack((one.T,mbill.T))
#set k here
ypred = localWeightRegression(X,mtip,0.2)
SortIndex = X[:,1].argsort(0)
xsort = X[SortIndex][:,0]
fig = plt.figure()
ax = fig.add\_subplot(1,1,1)
ax.scatter(bill,tip, color='green')
ax.plot(xsort[:,1],ypred[SortIndex], color = 'red', linewidth=5)
plt.xlabel('Total bill')
plt.ylabel('Tip')
plt.show();
```

Output:

Dataset

Add Tips.csv (256 rows)



VIVA Questions

- 1. What is machine learning?
- 2. Define supervised learning
- 3. Define unsupervised learning
- 4. Define semi supervised learning
- 5. Define reinforcement learning
- 6. What do you mean by hypotheses?
- 7. What is classification?
- 8. What is clustering?
- 9. Define precision, accuracy and recall
- 10. Define entropy
- 11. Define regression
- 12. How Knn is different from k-means clustering
- 13. What is concept learning?
- 14. Define specific boundary and general boundary
- 15. Define target function
- 16. Define decision tree
- 17. What is ANN
- 18. Explain gradient descent approximation
- 19. State Bayes theorem
- 20. Define Bayesian belief networks
- 21. Differentiate hard and soft clustering
- 22. Define variance
- 23. What is inductive machine learning?
- 24. Why K nearest neighbor algorithm is lazy learning algorithm
- 25. Why naïve Bayes is naïve
- 26. Mention classification algorithms
- 27. Define pruning
- 28. Differentiate Clustering and classification
- 29. Mention clustering algorithms
- 30. Define Bias
- 31. What is learning rate? Why it is need.