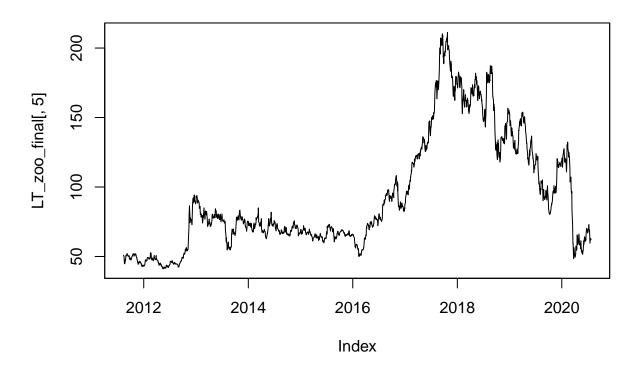
Untitled

me

7/26/2020

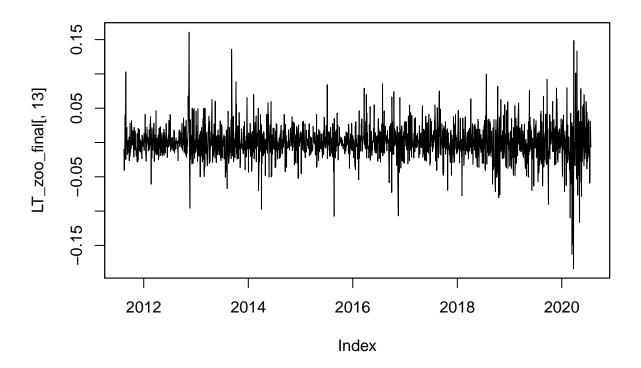
```
5+5
## [1] 10
library(zoo)
##
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
##
##
       as.Date, as.Date.numeric
library(tseries)
## Warning: package 'tseries' was built under R version 4.0.2
## Registered S3 method overwritten by 'quantmod':
    method
     as.zoo.data.frame zoo
library(FinTS)
## Warning: package 'FinTS' was built under R version 4.0.2
library(rugarch)
## Warning: package 'rugarch' was built under R version 4.0.2
## Loading required package: parallel
##
## Attaching package: 'rugarch'
## The following object is masked from 'package:stats':
##
##
       sigma
```

LT_zoo_final<-read.zoo("L&T housing Finance.csv",header=TRUE,sep=",",format="%d-%b-%y",FUN = as.Date) plot(LT_zoo_final[,5])



there is a trend in the closing price hence i am taking the differnce and considering the log return.

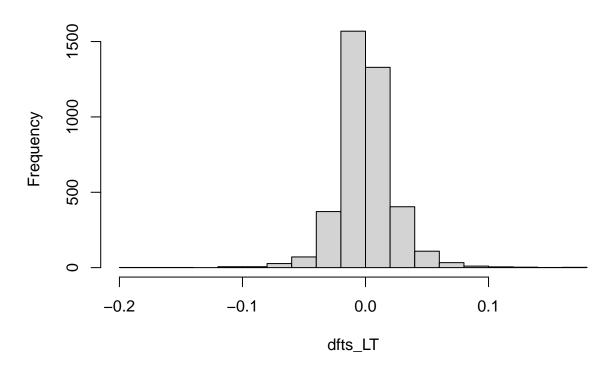
plot(LT_zoo_final[,13])



the return series seems to be constant at mean zero and volatility clustering is visible in graph

```
ret_LT<-LT_zoo_final[-1,13]
dfts_LT<- ts(ret_LT,start=c(2010,1),end=c(2020,300),frequency = 365)
hist(dfts_LT)</pre>
```

Histogram of dfts_LT



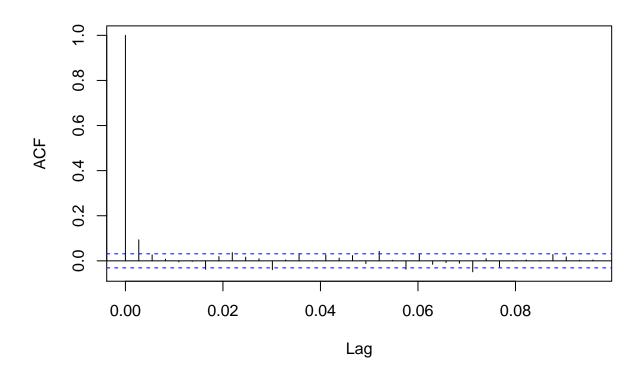
the return appears to be noormally distributed.

```
shapiro.test(dfts_LT)
##
    Shapiro-Wilk normality test
##
## data: dfts_LT
## W = 0.92625, p-value < 2.2e-16
the series is staionary.
mean(dfts_LT)
## [1] 0.0006501557
adf.test(ret_LT)
## Warning in adf.test(ret_LT): p-value smaller than printed p-value
##
    Augmented Dickey-Fuller Test
##
## data: ret_LT
## Dickey-Fuller = -12.043, Lag order = 13, p-value = 0.01
## alternative hypothesis: stationary
```

since p value is smaller than 0.05 hence we are rejecting the null hypothesis hence the series is stationary. also the series is normal around mean 0.

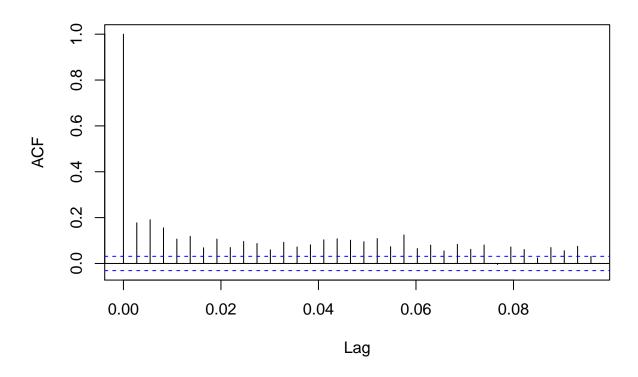
acf(dfts_LT)

Series dfts_LT



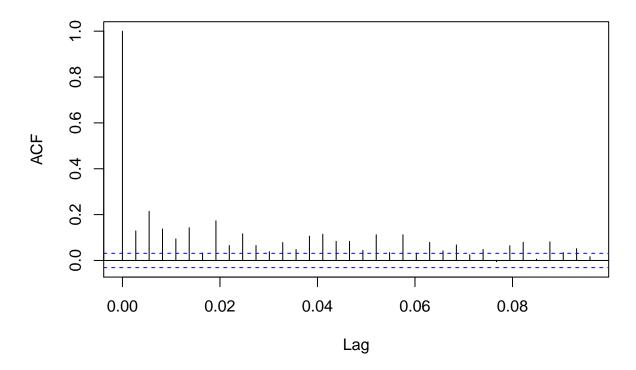
acf(abs(dfts_LT))

Series abs(dfts_LT)



acf(dfts_LT^2)

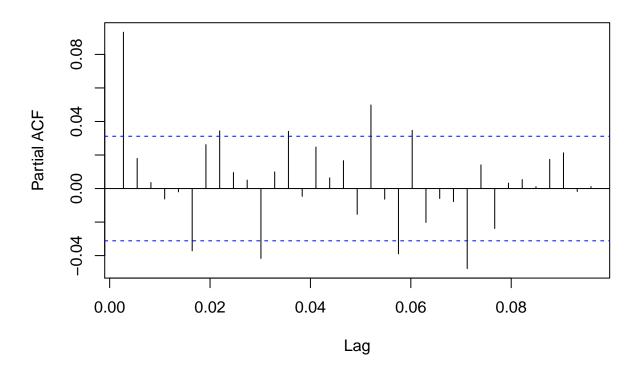
Series dfts_LT^2



by acf function of return we can say there is no auto correlation and there will be no need of MA model also by looking at the acf of absolute return we can say that the large return are followed by large returns regardless of sign MA(1) may be

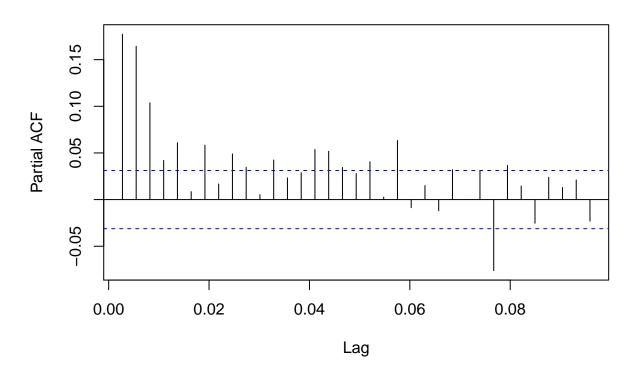
pacf(dfts_LT)

Series dfts_LT



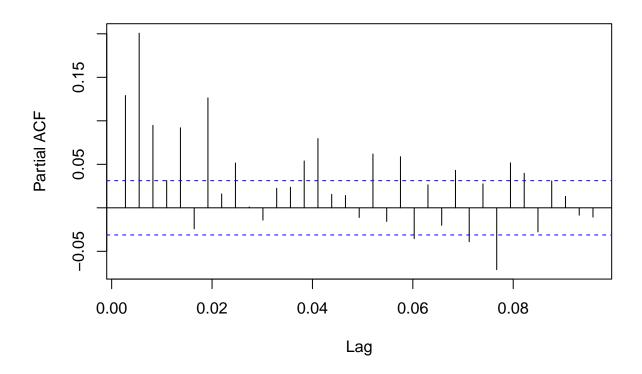
pacf(abs(dfts_LT))

Series abs(dfts_LT)



pacf(dfts_LT^2)

Series dfts_LT^2



there seems to be no need of any AR model to predict the log return series. AR(1).

Chi-squared = 295.61, df = 12, p-value < 2.2e-16

```
Box.test(ret_LT,lag=12,type="Ljung")

##

## Box-Ljung test

##

## data: ret_LT

## X-squared = 51.847, df = 12, p-value = 6.599e-07

ArchTest(ret_LT)

##

##

## ARCH LM-test; Null hypothesis: no ARCH effects
```

since p value is less than 0.05 we are rejecting the null hypothesis and thus we can say there is arch effect in the series.

```
arima001<-arima(ret_LT,order = c(0,0,1))
AIC(arima001)</pre>
```

```
## [1] -10158.81
```

data: ret_LT

##

```
"arima001"
## [1] "arima001"
arima010 < -arima(ret_LT, order = c(0,1,0))
AIC(arima010)
## [1] -8674.839
"arima010"
## [1] "arima010"
arima100 < -arima(ret_LT, order = c(1,0,0))
AIC(arima100); "arima100"
## [1] -10159.31
## [1] "arima100"
arima101 < -arima(ret_LT, order = c(1,0,1))
AIC(arima101); "arima101"
## [1] -10161.29
## [1] "arima101"
arima110<-arima(ret_LT,order = c(1,1,0))</pre>
AIC(arima110); "arima110"
## [1] -9308.291
## [1] "arima110"
arima011 < -arima(ret_LT, order = c(0,1,1))
AIC(arima011); "arima011"
## [1] -10137.74
## [1] "arima011"
arima111 < -arima(ret_LT, order = c(1,1,1))
AIC(arima111); "arima111"
## [1] -10146.16
## [1] "arima111"
```

```
arima200 < -arima(ret_LT, order = c(2,0,0))
AIC(arima200); "arima200"
## [1] -10158.8
## [1] "arima200"
arima210 < -arima(ret_LT, order = c(2,1,0))
AIC(arima210); "arima210"
## [1] -9550.121
## [1] "arima210"
arima201 < -arima(ret_LT, order = c(2,0,1))
## Warning in arima(ret_LT, order = c(2, 0, 1)): possible convergence problem:
## optim gave code = 1
AIC(arima201); "arima201"
## [1] -10159.14
## [1] "arima201"
arima211<-arima(ret_LT,order = c(2,1,1))</pre>
AIC(arima211); "arima211"
## [1] -10145.69
## [1] "arima211"
arima020 < -arima(ret_LT, order = c(0,2,0))
AIC(arima020); "arima020"
## [1] -5745.348
## [1] "arima020"
arima120 < -arima(ret_LT, order = c(1,2,0))
AIC(arima120); "arima120"
## [1] -7213.363
## [1] "arima120"
```

```
arima021 < -arima(ret_LT, order = c(0,2,1))
AIC(arima021); "arima021"
## [1] -8659.563
## [1] "arima021"
arima121 < -arima(ret_LT, order = c(1,2,1))
AIC(arima121); "arima121"
## [1] -9291.916
## [1] "arima121"
arima002 < -arima(ret_LT, order = c(0,0,2))
AIC(arima002); "arima002"
## [1] -10157.96
## [1] "arima002"
arima102 < -arima(ret_LT, order = c(1,0,2))
AIC(arima102); "arima102"
## [1] -10159.3
## [1] "arima102"
arima012 < -arima(ret_LT, order = c(0,1,2))
AIC(arima012); "arima012"
## [1] -10145.64
## [1] "arima012"
arima112 < -arima(ret_LT, order = c(1,1,2))
AIC(arima112); "arima112"
## [1] -10141.96
## [1] "arima112"
arima222 < -arima(ret_LT, order = c(2,2,2))
AIC(arima222); "arima222"
## [1] -10084.88
## [1] "arima222"
```

```
arima220 < -arima(ret_LT, order = c(2,2,0))
AIC(arima220); "arima220"
## [1] -7923.671
## [1] "arima220"
arima202 < -arima(ret_LT, order = c(2,0,2))
AIC(arima202); "arima202"
## [1] -10157.6
## [1] "arima202"
arima022 < -arima(ret_LT, order = c(0,2,2))
AIC(arima022); "arima022"
## [1] -10084
## [1] "arima022"
arima212 < -arima(ret_LT, order = c(2,1,2))
AIC(arima212); "arima212"
## [1] -10142.31
## [1] "arima212"
ARMA(1,0,1)<-(1,0,0) is the best choice since there was not any recommendation from acf and pacf function
we will ignore these model for now.
spec_of_garch_LT<- ugarchspec(variance.model = list(garchOrder=c(1,0)),mean.model = list(armaOrder=c(1,0))</pre>
my_model_LT<-ugarchfit(spec=spec_of_garch_LT,data=ret_LT,out.sample = 500)</pre>
my_model_LT
##
             GARCH Model Fit *
## Conditional Variance Dynamics
## -----
## GARCH Model : sGARCH(1,0)
## Mean Model : ARFIMA(1,0,0)
## Distribution : norm
##
## Optimal Parameters
           Estimate Std. Error t value Pr(>|t|)
##
```

```
## mu 0.067208 0.000326 206.32303 0.00000 ## ar1 -0.508998 0.006827 -74.55422 0.00000
## omega 0.000000 0.000003 0.11943 0.90494
## alpha1 0.999000 0.027706 36.05726 0.00000
## Robust Standard Errors:
## Estimate Std. Error t value Pr(>|t|)
        0.067208 0.001046 64.228361 0.00000
-0.508998 0.023013 -22.118140 0.00000
## mu
## ar1
## omega 0.000000 0.000005 0.069136 0.94488
## alpha1 0.999000 0.029493 33.871975 0.00000
## LogLikelihood: 1314.285
##
## Information Criteria
## -----
##
## Akaike
             -1.5316
             -1.5189
## Bayes
## Shibata -1.5316
## Hannan-Quinn -1.5269
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
                        statistic p-value
                          1.09 0.2965
## Lag[1]
## Lag[2*(p+q)+(p+q)-1][2] 56.28 0.0000
## Lag[4*(p+q)+(p+q)-1][5] 90.22 0.0000
## d.o.f=1
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                         statistic p-value
## Lag[1]
                           0.7394 0.3899
## Lag[2*(p+q)+(p+q)-1][2] 2.0945 0.2476
## Lag[4*(p+q)+(p+q)-1][5] 3.0181 0.4037
## d.o.f=1
##
## Weighted ARCH LM Tests
## -----
              Statistic Shape Scale P-Value
## ARCH Lag[2] 2.704 0.500 2.000 0.1001
## ARCH Lag[4] 2.802 1.397 1.611 0.2913
## ARCH Lag[6] 3.202 2.222 1.500 0.4339
##
## Nyblom stability test
## -----
## Joint Statistic: 25.9224
## Individual Statistics:
## mu
        0.05949
## ar1
         0.09513
## omega 1.49347
## alpha1 11.42401
```

```
## Asymptotic Critical Values (10% 5% 1%)
                  1.07 1.24 1.6
## Joint Statistic:
## Individual Statistic:
                       0.35 0.47 0.75
## Sign Bias Test
## -----
                  t-value prob sig
              13.18 7.702e-38 ***
## Sign Bias
## Negative Sign Bias 16.72 3.052e-58 ***
## Positive Sign Bias 10.45 7.876e-25 ***
## Joint Effect 526.39 9.100e-114 ***
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
##
   group statistic p-value(g-1)
## 1
      20
            7242
## 2
      30
            7586
                           0
## 3
      40
             7669
                            0
## 4
    50
             7808
                           0
##
##
## Elapsed time : 0.997993
spec_of_garch_LT<- ugarchspec(variance.model = list(garchOrder=c(0,1)),mean.model = list(armaOrder=c(1,0))</pre>
my_model_LT<-ugarchfit(spec=spec_of_garch_LT,data=ret_LT,out.sample = 500)</pre>
## Warning in .sgarchfit(spec = spec, data = data, out.sample = out.sample, :
## ugarchfit-->warning: solver failer to converge.
my_model_LT
##
## *----*
          GARCH Model Fit
## *----*
##
## Conditional Variance Dynamics
## -----
## GARCH Model : sGARCH(0,1)
## Mean Model : ARFIMA(1,0,0)
## Distribution : norm
## Convergence Problem:
## Solver Message:
spec_of_garch_LT<- ugarchspec(variance.model = list(garchOrder=c(1,1)),mean.model = list(armaOrder=c(1,0)</pre>
my_model_LT<-ugarchfit(spec=spec_of_garch_LT,data=ret_LT,out.sample = 500)
my_model_LT
##
```

##

```
GARCH Model Fit *
## *----*
##
## Conditional Variance Dynamics
## -----
## GARCH Model : sGARCH(1,1)
## Mean Model : ARFIMA(1,0,0)
## Distribution : norm
##
## Optimal Parameters
        Estimate Std. Error t value Pr(>|t|)
         0.000612 0.000484 1.2634 0.206439
## ar1 0.057432 0.029936 1.9185 0.055047
## omega 0.000157 0.000026 5.9865 0.000000
## alpha1 0.223015 0.044341 5.0295 0.000000
## beta1 0.423046 0.080789 5.2364 0.000000
## Robust Standard Errors:
##
      Estimate Std. Error t value Pr(>|t|)
       0.000612 0.000495 1.2373 0.215989
## ar1 0.057432 0.029172 1.9687 0.048982
## omega 0.000157 0.000033 4.7184 0.000002
## alpha1 0.223015 0.069098 3.2275 0.001249
## beta1 0.423046 0.089208 4.7422 0.000002
##
## LogLikelihood : 4274.761
## Information Criteria
## -----
##
## Akaike
            -4.9910
## Bayes
            -4.9750
## Shibata
            -4.9910
## Hannan-Quinn -4.9851
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
                      statistic p-value
## Lag[1]
                        1.130 0.2877
                      1.738 0.3168
3.237 0.3739
## Lag[2*(p+q)+(p+q)-1][2]
## Lag[4*(p+q)+(p+q)-1][5]
## d.o.f=1
## HO : No serial correlation
##
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                      statistic p-value
                        0.9602 0.3271
## Lag[1]
## Lag[2*(p+q)+(p+q)-1][5] 1.2837 0.7928
## Lag[4*(p+q)+(p+q)-1][9] 1.7706 0.9306
## d.o.f=2
##
```

```
## Weighted ARCH LM Tests
## -----
            Statistic Shape Scale P-Value
## ARCH Lag[3] 0.3737 0.500 2.000 0.5410
            0.5888 1.440 1.667 0.8571
## ARCH Lag[5]
## ARCH Lag[7] 0.7085 2.315 1.543 0.9558
## Nyblom stability test
## -----
## Joint Statistic: 1.1166
## Individual Statistics:
        0.23104
## mu
## ar1
        0.05652
## omega 0.22648
## alpha1 0.15724
## beta1 0.12510
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 1.28 1.47 1.88
## Individual Statistic:
                      0.35 0.47 0.75
##
## Sign Bias Test
## -----
                  t-value prob sig
## Sign Bias
                  1.2153 0.2244
## Negative Sign Bias 0.4617 0.6443
## Positive Sign Bias 0.7643 0.4448
## Joint Effect
                  1.5318 0.6750
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
   group statistic p-value(g-1)
      20 108.8 1.306e-14
## 1
    30 118.5
40 127.4
## 2
                  8.671e-13
                  2.566e-11
## 3
## 4 50 137.5 2.498e-10
##
## Elapsed time : 1.163993
spec_of_garch_LT<- ugarchspec(variance.model = list(garchOrder=c(2,0)),mean.model =list(armaOrder=c(1,0))</pre>
my_model_LT<-ugarchfit(spec=spec_of_garch_LT,data=ret_LT,out.sample = 500)</pre>
my_model_LT
         GARCH Model Fit
## Conditional Variance Dynamics
## -----
```

GARCH Model : sGARCH(2,0)
Mean Model : ARFIMA(1,0,0)

```
## Distribution : norm
##
## Optimal Parameters
## -----
        Estimate Std. Error t value Pr(>|t|)
## mu
       0.000595 0.000470 1.2647 0.205962
## ar1 0.046435 0.028893 1.6071 0.108027
## alpha2 0.200278 0.040909 4.8957 0.000001
## Robust Standard Errors:
        Estimate Std. Error t value Pr(>|t|)
       0.000595 0.000495 1.2024 0.229193
## mu
## ar1 0.046435 0.028664 1.6200 0.105237
## omega 0.000271 0.000027 9.9740 0.000000
## alpha1 0.212705 0.078318 2.7159 0.006609
## alpha2 0.200278 0.070406 2.8446 0.004447
## LogLikelihood: 4277.724
##
## Information Criteria
## -----
## Akaike
           -4.9944
## Bayes
            -4.9785
## Shibata -4.9944
## Hannan-Quinn -4.9885
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
                     statistic p-value
## Lag[1]
                      1.579 0.2089
## Lag[2*(p+q)+(p+q)-1][2] 2.011 0.2095
## Lag[4*(p+q)+(p+q)-1][5] 3.530 0.3104
## d.o.f=1
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                     statistic p-value
## Lag[1]
                       0.8255 0.3636
## Lag[2*(p+q)+(p+q)-1][5] 2.3136 0.5464
## Lag[4*(p+q)+(p+q)-1][9] 3.0915 0.7438
## d.o.f=2
##
## Weighted ARCH LM Tests
## -----
            Statistic Shape Scale P-Value
## ARCH Lag[3] 0.03631 0.500 2.000 0.8489
## ARCH Lag[5] 0.95973 1.440 1.667 0.7449
## ARCH Lag[7] 1.16110 2.315 1.543 0.8860
##
## Nyblom stability test
```

```
## Joint Statistic: 0.9376
## Individual Statistics:
## mu
        0.17513
## ar1
        0.03447
## omega 0.20129
## alpha1 0.20597
## alpha2 0.08386
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 1.28 1.47 1.88
## Individual Statistic: 0.35 0.47 0.75
## Sign Bias Test
##
                   t-value prob sig
## Sign Bias
                   1.1028 0.2703
## Negative Sign Bias 0.8086 0.4189
## Positive Sign Bias 0.6122 0.5405
## Joint Effect
               1.3332 0.7213
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
## group statistic p-value(g-1)
## 1 20 103.1 1.460e-13
## 2
     30
            117.1 1.514e-12
    40 134.3 2.176e-12
50 155.2 5.705e-13
## 4
##
##
## Elapsed time: 1.343
spec_of_garch_LT<- ugarchspec(variance.model = list(garchOrder=c(0,2)),mean.model = list(armaOrder=c(1,0))</pre>
my_model_LT<-ugarchfit(spec=spec_of_garch_LT,data=ret_LT,out.sample = 500)</pre>
## Warning in .sgarchfit(spec = spec, data = data, out.sample = out.sample, :
## ugarchfit-->warning: solver failer to converge.
my_model_LT
      GARCH Model Fit *
## *----*
## Conditional Variance Dynamics
## GARCH Model : sGARCH(0,2)
## Mean Model : ARFIMA(1,0,0)
## Distribution : norm
##
## Convergence Problem:
## Solver Message:
```

```
spec_of_garch_LT<- ugarchspec(variance.model = list(garchOrder=c(2,2)),mean.model =list(armaOrder=c(1,0
my_model_LT<-ugarchfit(spec=spec_of_garch_LT,data=ret_LT,out.sample = 500)
my_model_LT</pre>
```

```
##
    GARCH Model Fit
## Conditional Variance Dynamics
## -----
## GARCH Model : sGARCH(2,2)
## Mean Model : ARFIMA(1,0,0)
## Distribution : norm
##
## Optimal Parameters
## -----
        Estimate Std. Error t value Pr(>|t|)
## mu
       ## ar1 0.077103 0.026907 2.865502 0.004163
## omega 0.000032 0.000013 2.495879 0.012565
## alpha1 0.088188 0.029163 3.023930 0.002495
## alpha2 0.000000 0.025606 0.000009 0.999993
## beta1 0.617055 0.093278 6.615193 0.000000
## beta2 0.220015 0.149331 1.473333 0.140661
## Robust Standard Errors:
     Estimate Std. Error t value Pr(>|t|)
      ## mu
## ar1
## omega 0.000032 0.000061 0.531186 0.595290
## alpha1 0.088188 0.120853 0.729710 0.465567
## alpha2 0.000000 0.075725 0.000003 0.999998
## beta1 0.617055 0.812446 0.759502 0.447552
## beta2 0.220015 0.977097 0.225172 0.821846
##
## LogLikelihood: 4268.83
##
## Information Criteria
## Akaike
            -4.9817
## Bayes
            -4.9594
## Shibata
           -4.9817
## Hannan-Quinn -4.9734
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
                    statistic p-value
## Lag[1]
                       0.7489 0.3868
## Lag[2*(p+q)+(p+q)-1][2] 1.6111 0.3782
                      2.8644 0.4662
## Lag[4*(p+q)+(p+q)-1][5]
## d.o.f=1
```

```
## HO : No serial correlation
##
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
                        statistic p-value
## Lag[1]
                           1.086 0.2974
## Lag[2*(p+q)+(p+q)-1][11] 4.378 0.6758
## Lag[4*(p+q)+(p+q)-1][19] 7.458 0.7355
## d.o.f=4
##
## Weighted ARCH LM Tests
## -----
    Statistic Shape Scale P-Value
## ARCH Lag[5] 1.750 0.500 2.000 0.1859
## ARCH Lag[7] 3.493 1.473 1.746 0.2538
## ARCH Lag[9] 3.829 2.402 1.619 0.4234
##
## Nyblom stability test
## -----
## Joint Statistic: 5.0916
## Individual Statistics:
## mu
       0.15697
## ar1 0.17148
## omega 0.21336
## alpha1 0.06715
## alpha2 0.05467
## beta1 0.12428
## beta2 0.12775
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 1.69 1.9 2.35 ## Individual Statistic: 0.35 0.47 0.75
## Sign Bias Test
## -----
                  t-value prob sig
## Sign Bias
                   1.0096 0.3128
## Negative Sign Bias 1.3934 0.1637
## Positive Sign Bias 0.8079 0.4192
## Joint Effect 3.5804 0.3105
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
## group statistic p-value(g-1)
## 1 20 110.7 5.847e-15
## 2 30 121.1 3.155e-13
## 3 40 140.0 2.627e-13
## 4 50 144.3 2.502e-11
##
## Elapsed time : 0.96825
```

```
spec_of_garch_LT<- ugarchspec(variance.model = list(garchOrder=c(1,2)),mean.model =list(armaOrder=c(1,0)
my_model_LT<-ugarchfit(spec=spec_of_garch_LT,data=ret_LT,out.sample = 500)
my_model_LT</pre>
```

```
##
    GARCH Model Fit *
## Conditional Variance Dynamics
## -----
## GARCH Model : sGARCH(1,2)
## Mean Model : ARFIMA(1,0,0)
## Distribution : norm
##
## Optimal Parameters
## -----
        Estimate Std. Error t value Pr(>|t|)
## mu
       ## ar1 0.077109 0.027003 2.8556 0.004296
## omega 0.000032 0.000023 1.4280 0.153284
## alpha1 0.088175 0.030417 2.8989 0.003745
## beta1 0.617015 0.174771 3.5304 0.000415
## beta2 0.220097 0.192434 1.1438 0.252727
##
## Robust Standard Errors:
   Estimate Std. Error t value Pr(>|t|)
##
       ## mu
## ar1 0.077109 0.029364 2.62597 0.00864
## omega 0.000032 0.000114 0.28436 0.77614
## alpha1 0.088175 0.145616 0.60553 0.54483
## beta1 0.617015 0.253365 2.43528 0.01488
## beta2  0.220097  0.618785  0.35569  0.72207
##
## LogLikelihood: 4268.83
##
## Information Criteria
##
## Akaike
            -4.9829
            -4.9638
## Bayes
## Shibata
            -4.9829
## Hannan-Quinn -4.9758
## Weighted Ljung-Box Test on Standardized Residuals
## -----
                     statistic p-value
                       0.7485 0.3870
## Lag[1]
## Lag[2*(p+q)+(p+q)-1][2] 1.6107 0.3783
## Lag[4*(p+q)+(p+q)-1][5] 2.8640 0.4663
## d.o.f=1
## HO : No serial correlation
##
```

```
## d.o.f=3
##
## Weighted ARCH LM Tests
             Statistic Shape Scale P-Value
## ARCH Lag[4] 0.06857 0.500 2.000 0.7934
             2.24991 1.461 1.711 0.4381
## ARCH Lag[6]
## ARCH Lag[8]
               3.29130 2.368 1.583 0.4904
## Nyblom stability test
## Joint Statistic: 1.239
## Individual Statistics:
## mu
       0.1569
## ar1
        0.1715
## omega 0.2138
## alpha1 0.0670
## beta1 0.1245
## beta2 0.1280
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 1.49 1.68 2.12
## Individual Statistic: 0.35 0.47 0.75
##
## Sign Bias Test
## -----
##
                  t-value prob sig
                   1.0095 0.3129
## Sign Bias
## Negative Sign Bias 1.3937 0.1636
## Positive Sign Bias 0.8083 0.4190
## Joint Effect 3.5818 0.3103
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
## group statistic p-value(g-1)
## 1 20 110.7 5.847e-15
## 2 30 121.1 3.155e-13
## 3
    40 140.0 2.627e-13
     50 143.7
## 4
                   3.052e-11
##
##
## Elapsed time : 0.819993
spec_of_garch_LT<- ugarchspec(variance.model = list(garchOrder=c(2,1)),mean.model = list(armaOrder=c(1,0)</pre>
my_model_LT<-ugarchfit(spec=spec_of_garch_LT,data=ret_LT,out.sample = 500)</pre>
my_model_LT
```

Weighted Ljung-Box Test on Standardized Squared Residuals

statistic p-value 1.087 0.2971

Lag[2*(p+q)+(p+q)-1][8] 3.426 0.6075 ## Lag[4*(p+q)+(p+q)-1][14] 5.356 0.7243

##

Lag[1]

```
## *----*
           GARCH Model Fit
## *----*
## Conditional Variance Dynamics
## -----
## GARCH Model : sGARCH(2,1)
## Mean Model : ARFIMA(1,0,0)
## Distribution : norm
## Optimal Parameters
##
         Estimate Std. Error t value Pr(>|t|)
## mu
       0.000616 0.000477 1.2919 0.196396
## ar1 0.056330 0.029043 1.9395 0.052436
## omega 0.000240 0.000029 8.2300 0.000000
## alpha1 0.195406 0.043451 4.4972 0.000007
## alpha2 0.164282 0.051325 3.2008 0.001370
## beta1 0.110576 0.092433 1.1963 0.231588
##
## Robust Standard Errors:
        Estimate Std. Error t value Pr(>|t|)
##
       0.000616 0.000489 1.25895 0.208047
## mu
## ar1 0.056330 0.028890 1.94979 0.051201
## omega 0.000240 0.000047 5.12772 0.000000
## alpha1 0.195406 0.069115 2.82726 0.004695
## alpha2 0.164282 0.085338 1.92506 0.054222
## beta1 0.110576 0.132606 0.83387 0.404355
##
## LogLikelihood: 4279.017
##
## Information Criteria
## Akaike
            -4.9948
## Bayes
            -4.9757
## Shibata -4.9948
## Hannan-Quinn -4.9877
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
                      statistic p-value
## Lag[1]
                        0.9815 0.3218
## Lag[2*(p+q)+(p+q)-1][2] 1.4297 0.4771
## Lag[4*(p+q)+(p+q)-1][5] 2.7985 0.4837
## d.o.f=1
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                       statistic p-value
## Lag[1]
                         0.5678 0.4511
## Lag[2*(p+q)+(p+q)-1][8] 1.7476 0.8957
```

```
## Lag[4*(p+q)+(p+q)-1][14] 3.1086 0.9494
## d.o.f=3
##
## Weighted ARCH LM Tests
## -----
    Statistic Shape Scale P-Value
## ARCH Lag[4] 0.3549 0.500 2.000 0.5514
## ARCH Lag[6] 0.4682 1.461 1.711 0.9008
## ARCH Lag[8] 0.5085 2.368 1.583 0.9812
##
## Nyblom stability test
## -----
## Joint Statistic: 1.2291
## Individual Statistics:
## mu
        0.16622
## ar1
        0.05782
## omega 0.21149
## alpha1 0.17124
## alpha2 0.09298
## beta1 0.11060
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 1.49 1.68 2.12
## Individual Statistic: 0.35 0.47 0.75
##
## Sign Bias Test
## -----
                  t-value prob sig
                   1.0786 0.2809
## Sign Bias
## Negative Sign Bias 0.8013 0.4231
## Positive Sign Bias 0.5036 0.6146
## Joint Effect 1.2537 0.7402
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
## group statistic p-value(g-1)
## 1 20 97.83 1.324e-12
      30 113.49
                  6.093e-12
## 2
## 3 40 123.51 1.037e-10
## 4 50 140.11 1.037e-10
##
## Elapsed time : 1.122009
spec_of_garch_LT<- ugarchspec(variance.model = list(garchOrder=c(0,1)),mean.model = list(armaOrder=c(1,0))</pre>
my_model_LT<-ugarchfit(spec=spec_of_garch_LT,data=ret_LT,out.sample = 500)</pre>
## Warning in .sgarchfit(spec = spec, data = data, out.sample = out.sample, :
## ugarchfit-->warning: solver failer to converge.
my_model_LT
```

##

```
GARCH Model Fit *
## *----*
##
## Conditional Variance Dynamics
## -----
## GARCH Model : sGARCH(0,1)
## Mean Model : ARFIMA(1,0,0)
## Distribution : sstd
##
## Convergence Problem:
## Solver Message:
spec_of_garch_LT<- ugarchspec(variance.model = list(garchOrder=c(1,0)),mean.model = list(armaOrder=c(1,0))</pre>
my_model_LT<-ugarchfit(spec=spec_of_garch_LT,data=ret_LT,out.sample = 500)
my_model_LT
##
      GARCH Model Fit *
## *----*
## Conditional Variance Dynamics
## -----
## GARCH Model : sGARCH(1,0)
## Mean Model : ARFIMA(1,0,0)
## Distribution : sstd
##
## Optimal Parameters
##
        Estimate Std. Error t value Pr(>|t|)
## mu
      0.000765 0.000505 1.5128 0.130342
## ar1 0.070225 0.025190 2.7878 0.005306
## omega 0.000367 0.000034 10.7693 0.000000
## alpha1 0.204628 0.058827 3.4784 0.000504
        1.119668 0.036645 30.5547 0.000000
## skew
## shape 3.793486 0.372673 10.1791 0.000000
## Robust Standard Errors:
     Estimate Std. Error t value Pr(>|t|)
##
## mu
      0.000765 0.000488 1.5675 0.116991
## ar1 0.070225 0.021495 3.2670 0.001087
## skew 1.119668 0.038722 28.9154 0.000000
## shape
        ## LogLikelihood : 4379.536
## Information Criteria
## -----
##
## Akaike
           -5.1123
           -5.0932
## Bayes
```

```
## Shibata -5.1123
## Hannan-Quinn -5.1052
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
                      statistic p-value
                        0.4428 0.5058
## Lag[1]
## Lag[2*(p+q)+(p+q)-1][2] 1.0804 0.6908
## Lag[4*(p+q)+(p+q)-1][5] 3.2467 0.3718
## d.o.f=1
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                      statistic p-value
## Lag[1]
                        0.02726 0.8689
## Lag[2*(p+q)+(p+q)-1][2] 2.92215 0.1473
## Lag[4*(p+q)+(p+q)-1][5] 7.33418 0.0430
## d.o.f=1
##
## Weighted ARCH LM Tests
## -----
## Statistic Shape Scale P-Value
## ARCH Lag[2] 5.776 0.500 2.000 0.016244
## ARCH Lag[4]
              9.093 1.397 1.611 0.008427
## ARCH Lag[6] 9.987 2.222 1.500 0.013883
## Nyblom stability test
## Joint Statistic: 1.7312
## Individual Statistics:
## mu
      0.3504
      0.2732
## ar1
## omega 0.4229
## alpha1 0.3953
## skew 0.1794
## shape 0.3658
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 1.49 1.68 2.12
## Individual Statistic: 0.35 0.47 0.75
## Sign Bias Test
## -----
                 t-value prob sig
               1.350 0.1771
## Sign Bias
## Negative Sign Bias 1.054 0.2921
## Positive Sign Bias 0.162 0.8713
## Joint Effect 2.221 0.5279
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
  group statistic p-value(g-1)
```

```
20
## 1
            7.773
                        0.9888
## 2
       30 16.884
                        0.9639
## 3
       40 23.868
                        0.9729
## 4
       50 34.733
                        0.9384
##
##
## Elapsed time : 1.591997
spec_of_garch_LT<- ugarchspec(variance.model = list(garchOrder=c(1,1)),mean.model = list(armaOrder=c(1,0))</pre>
my_model_LT<-ugarchfit(spec=spec_of_garch_LT,data=ret_LT,out.sample = 500)</pre>
my_model_LT
##
## *----*
           GARCH Model Fit
## *----*
## Conditional Variance Dynamics
## -----
## GARCH Model : sGARCH(1,1)
## Mean Model : ARFIMA(1,0,0)
## Distribution : sstd
## Optimal Parameters
##
         Estimate Std. Error t value Pr(>|t|)
## mu
        0.000813 0.000494 1.6468 0.099608
         0.072547 0.024666 2.9411 0.003270
## ar1
## omega 0.000124 0.000044 2.8469 0.004415
## alpha1 0.180462 0.054705 3.2988 0.000971
## beta1 0.555789 0.128328 4.3310 0.000015
## skew 1.133749 0.037615 30.1407 0.000000
## shape 3.965729 0.398564 9.9500 0.000000
## Robust Standard Errors:
##
         Estimate Std. Error t value Pr(>|t|)
         0.000813 0.000495 1.6405 0.100893
## mu
        0.072547 0.021200 3.4220 0.000622
## ar1
## omega 0.000124 0.000062 2.0073 0.044722
## alpha1 0.180462 0.069694 2.5893 0.009616
## beta1 0.555789 0.179956 3.0885 0.002012
## skew 1.133749 0.039854 28.4476 0.000000
## shape 3.965729 0.358611 11.0586 0.000000
##
## LogLikelihood: 4392.533
## Information Criteria
## Akaike
              -5.1263
## Bayes
             -5.1040
## Shibata
            -5.1263
## Hannan-Quinn -5.1180
##
```

```
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
                      statistic p-value
                        0.4988 0.4800
## Lag[1]
                       1.1307 0.6596
## Lag[2*(p+q)+(p+q)-1][2]
## Lag[4*(p+q)+(p+q)-1][5] 2.4769 0.5730
## d.o.f=1
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                      statistic p-value
## Lag[1]
                        0.2320 0.6300
## Lag[2*(p+q)+(p+q)-1][5] 0.6754 0.9276
## Lag[4*(p+q)+(p+q)-1][9] 1.3928 0.9639
## d.o.f=2
##
## Weighted ARCH LM Tests
## -----
           Statistic Shape Scale P-Value
## ARCH Lag[3] 0.4087 0.500 2.000 0.5226
## ARCH Lag[5] 0.8641 1.440 1.667 0.7737
## ARCH Lag[7] 1.1878 2.315 1.543 0.8812
## Nyblom stability test
## -----
## Joint Statistic: 2.097
## Individual Statistics:
## mu
      0.2933
## ar1
       0.2286
## omega 0.3721
## alpha1 0.3216
## beta1 0.3014
## skew 0.3256
## shape 0.2895
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 1.69 1.9 2.35
## Individual Statistic: 0.35 0.47 0.75
##
## Sign Bias Test
## -----
                 t-value prob sig
## Sign Bias
                 1.1782 0.2389
## Negative Sign Bias 0.7603 0.4472
## Positive Sign Bias 0.3373 0.7359
## Joint Effect 1.4769 0.6876
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
## group statistic p-value(g-1)
## 1 20 4.50 0.9997
## 2 30 17.94
                    0.9456
```

```
## 3
       40
             28.45
                        0.8936
## 4
       50
             31.93
                        0.9719
##
##
## Elapsed time : 2.060997
spec_of_garch_LT<- ugarchspec(variance.model = list(garchOrder=c(2,0)),mean.model = list(armaOrder=c(1,0))</pre>
my_model_LT<-ugarchfit(spec=spec_of_garch_LT,data=ret_LT,out.sample = 500)</pre>
my_model_LT
##
            GARCH Model Fit
## Conditional Variance Dynamics
## -----
## GARCH Model : sGARCH(2,0)
## Mean Model : ARFIMA(1,0,0)
## Distribution : sstd
##
## Optimal Parameters
## -----
         Estimate Std. Error t value Pr(>|t|)
##
## mu
         0.000710 0.000490 1.4485 0.147482
         0.069505 0.024827 2.7996 0.005117
## ar1
## omega 0.000306 0.000029 10.4123 0.000000
## alpha1 0.178493 0.054134 3.2972 0.000976
## alpha2 0.167582 0.050412 3.3243 0.000887
## skew
         1.125224 0.037178 30.2661 0.000000
         3.979253 0.401070 9.9216 0.000000
## shape
## Robust Standard Errors:
        Estimate Std. Error t value Pr(>|t|)
         0.000710 0.000478 1.4838 0.137852
## mu
         0.069505 0.021234 3.2733 0.001063
## ar1
## omega 0.000306 0.000032 9.6318 0.000000
## alpha1 0.178493 0.061019 2.9252 0.003442
                  0.054077 3.0989 0.001942
## alpha2 0.167582
## skew
         1.125224 0.038922 28.9100 0.000000
## shape
         3.979253 0.361976 10.9931 0.000000
## LogLikelihood: 4391.129
##
## Information Criteria
##
## Akaike
             -5.1246
## Bayes
              -5.1024
## Shibata
            -5.1247
## Hannan-Quinn -5.1164
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
```

```
##
                      statistic p-value
## Lag[1]
                         0.3108 0.5772
## Lag[2*(p+q)+(p+q)-1][2]
                         0.7304 0.8845
## Lag[4*(p+q)+(p+q)-1][5] 2.2401 0.6415
## d.o.f=1
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                      statistic p-value
## Lag[1]
                        0.1229 0.7260
                         1.5885 0.7181
## Lag[2*(p+q)+(p+q)-1][5]
## Lag[4*(p+q)+(p+q)-1][9]
                      2.6634 0.8130
## d.o.f=2
##
## Weighted ARCH LM Tests
## Statistic Shape Scale P-Value
## ARCH Lag[3] 0.3343 0.500 2.000 0.5631
            2.1223 1.440 1.667 0.4448
## ARCH Lag[5]
## ARCH Lag[7] 2.4019 2.315 1.543 0.6327
## Nyblom stability test
## -----
## Joint Statistic: 2.1103
## Individual Statistics:
## mu
       0.2685
## ar1
       0.2312
## omega 0.4077
## alpha1 0.2303
## alpha2 0.3538
## skew 0.3121
## shape 0.3120
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 1.69 1.9 2.35
## Individual Statistic: 0.35 0.47 0.75
##
## Sign Bias Test
## -----
                 t-value prob sig
## Sign Bias
                  1.0724 0.2837
## Negative Sign Bias 1.2127 0.2254
## Positive Sign Bias 0.1255 0.9001
## Joint Effect 1.8018 0.6145
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
## group statistic p-value(g-1)
## 1 20 3.565 1.0000
## 2 30 18.147
                     0.9412
## 3 40 15.686
                     0.9997
## 4 50 32.629
                  0.9653
```

```
##
##
## Elapsed time : 1.768996
spec_of_garch_LT<- ugarchspec(variance.model = list(garchOrder=c(0,2)),mean.model =list(armaOrder=c(1,0))</pre>
my_model_LT<-ugarchfit(spec=spec_of_garch_LT,data=ret_LT,out.sample = 500)</pre>
my_model_LT
##
           GARCH Model Fit
## Conditional Variance Dynamics
## -----
## GARCH Model : sGARCH(0,2)
## Mean Model : ARFIMA(1,0,0)
## Distribution : sstd
##
## Optimal Parameters
## -----
##
        Estimate Std. Error t value Pr(>|t|)
## mu
       0.000927 0.000546 1.6977 0.089570
## ar1 0.076181 0.021991
                             3.4642 0.000532
## omega 0.000001 0.000000 28.4084 0.000000
## beta1 0.992975 0.000372 2667.4657 0.000000
## beta2 0.004153 0.000536 7.7530 0.000000
## skew 1.119364 0.037521 29.8330 0.000000
## shape 3.553275 0.318034 11.1726 0.000000
##
## Robust Standard Errors:
        Estimate Std. Error t value Pr(>|t|)
## mu
        0.000927 0.000584 1.5892 0.112014
## ar1 0.076181 0.024200 3.1480 0.001644
## omega 0.000001 0.000000 24.3052 0.000000
## beta1 0.992975 0.000421 2355.9950 0.000000
## beta2 0.004153 0.000567 7.3301 0.000000
## skew 1.119364 0.042388 26.4074 0.000000
## shape 3.553275 0.390237 9.1054 0.000000
## LogLikelihood : 4366.008
##
## Information Criteria
##
## Akaike
             -5.0953
## Bayes
              -5.0730
             -5.0953
## Shibata
## Hannan-Quinn -5.0870
## Weighted Ljung-Box Test on Standardized Residuals
## -----
                       statistic p-value
                           1.339 0.2473
## Lag[1]
```

```
## Lag[2*(p+q)+(p+q)-1][2] 2.237 0.1444
## Lag[4*(p+q)+(p+q)-1][5] 3.945 0.2344
## d.o.f=1
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                        statistic p-value
## Lag[1]
                           50.16 1.414e-12
## Lag[2*(p+q)+(p+q)-1][5]
                        76.18 0.000e+00
## Lag[4*(p+q)+(p+q)-1][9] 84.96 0.000e+00
## d.o.f=2
## Weighted ARCH LM Tests
   Statistic Shape Scale P-Value
## ARCH Lag[3] 25.57 0.500 2.000 4.258e-07
               35.92 1.440 1.667 1.944e-09
## ARCH Lag[5]
## ARCH Lag[7] 36.72 2.315 1.543 2.664e-09
## Nyblom stability test
## -----
## Joint Statistic: 61.7706
## Individual Statistics:
## mu
      0.2950
## ar1
        0.4703
## omega 16.6375
## beta1 0.4902
## beta2 0.4902
## skew 0.1874
## shape 0.3946
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 1.69 1.9 2.35
## Individual Statistic: 0.35 0.47 0.75
## Sign Bias Test
## -----
             t-value prob sig
0.226 8.212e-01
##
## Sign Bias
## Negative Sign Bias 4.018 6.130e-05 ***
## Positive Sign Bias 5.534 3.607e-08 ***
## Joint Effect 48.430 1.725e-10 ***
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
## group statistic p-value(g-1)
## 1 20 12.10 0.8814
    30 22.74
40 32.57
## 2
                       0.7883
## 3 40 32.57
## 4 50 39.06
                      0.7569
                       0.8445
##
##
```

```
## Elapsed time : 1.444995
spec_of_garch_LT<- ugarchspec(variance.model = list(garchOrder=c(2,2)),mean.model = list(armaOrder=c(1,0)</pre>
my_model_LT<-ugarchfit(spec=spec_of_garch_LT,data=ret_LT,out.sample = 500)</pre>
my_model_LT
##
            GARCH Model Fit
## Conditional Variance Dynamics
## -----
## GARCH Model : sGARCH(2,2)
## Mean Model : ARFIMA(1,0,0)
## Distribution : sstd
## Optimal Parameters
          Estimate Std. Error t value Pr(>|t|)
## mu
         0.000874 0.000489 1.786262 0.074057
## ar1 0.068724 0.023445 2.931225 0.003376
## omega 0.000045 0.000026 1.711098 0.087063
## alpha1 0.080410 0.030705 2.618770 0.008825
## alpha2 0.031911 0.025027 1.275054 0.202290
## beta1 0.000000 0.086724 0.000005 0.999996
## beta2  0.790606  0.038274  20.656548  0.000000
          1.129509 0.037273 30.303463 0.000000
## skew
## shape 3.938386 0.387438 10.165192 0.000000
##
## Robust Standard Errors:
         Estimate Std. Error t value Pr(>|t|)
## mu
          0.000874 0.000488 1.788415 0.073709
## ar1 0.068724 0.022558 3.046556 0.002315
## omega 0.000045 0.000050 0.898644 0.368842
## alpha1 0.080410 0.055472 1.449570 0.147179
## alpha2 0.031911 0.048269 0.661109 0.508543
## beta1 0.000000 0.126173 0.000003 0.999998
## beta2 0.790606 0.155110 5.097077 0.000000
## skew 1.129509 0.039707 28.446227 0.000000
## shape 3.938386 0.371290 10.607315 0.000000
## LogLikelihood : 4392.035
##
## Information Criteria
##
## Akaike
              -5.1234
## Bayes
              -5.0947
          -5.1234
## Shibata
## Hannan-Quinn -5.1128
##
## Weighted Ljung-Box Test on Standardized Residuals
```

```
##
                         statistic p-value
## Lag[1]
                           1.302 0.2538
## Lag[2*(p+q)+(p+q)-1][2] 2.318 0.1257
## Lag[4*(p+q)+(p+q)-1][5] 3.761 0.2661
## d.o.f=1
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                          statistic p-value
## Lag[1]
                             1.793 0.1805
## Lag[2*(p+q)+(p+q)-1][11] 5.868 0.4539
## Lag[4*(p+q)+(p+q)-1][19] 8.648 0.6019
## d.o.f=4
##
## Weighted ARCH LM Tests
## Statistic Shape Scale P-Value
## ARCH Lag[5] 2.006 0.500 2.000 0.1567
## ARCH Lag[7] 3.477 1.473 1.746 0.2557
## ARCH Lag[9] 3.631 2.402 1.619 0.4551
## Nyblom stability test
## -----
## Joint Statistic: 2.525
## Individual Statistics:
## mu
        0.2261
## ar1
        0.3109
## omega 0.2900
## alpha1 0.1677
## alpha2 0.2015
## beta1 0.2760
## beta2 0.2333
## skew 0.2677
## shape 0.2227
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 2.1 2.32 2.82
## Individual Statistic: 0.35 0.47 0.75
##
## Sign Bias Test
## -----
                   t-value prob sig
## Sign Bias
                   1.179 0.23875
## Negative Sign Bias 1.648 0.09944
## Positive Sign Bias 1.032 0.30230
## Joint Effect 5.216 0.15668
##
## Adjusted Pearson Goodness-of-Fit Test:
## group statistic p-value(g-1)
## 1 20 8.638 0.9790
## 2 30 13.167 0.9948
```

```
## 3
      40 38.784
                       0.4796
      50
## 4
            37.071
                       0.8945
##
##
## Elapsed time : 2.485992
spec_of_garch_LT<- ugarchspec(variance.model = list(garchOrder=c(1,2)),mean.model =list(armaOrder=c(1,0))</pre>
my_model_LT<-ugarchfit(spec=spec_of_garch_LT,data=ret_LT,out.sample = 500)</pre>
## Warning in .sgarchfit(spec = spec, data = data, out.sample = out.sample, :
## ugarchfit-->warning: solver failer to converge.
my model LT
##
## *----*
          GARCH Model Fit *
## *----*
##
## Conditional Variance Dynamics
## -----
## GARCH Model : sGARCH(1,2)
## Mean Model : ARFIMA(1,0,0)
## Distribution : sstd
##
## Convergence Problem:
## Solver Message:
spec_of_garch_LT<- ugarchspec(variance.model = list(garchOrder=c(2,1)),mean.model = list(armaOrder=c(1,0)</pre>
my_model_LT<-ugarchfit(spec=spec_of_garch_LT,data=ret_LT,out.sample = 500)</pre>
my model LT
##
     GARCH Model Fit *
## *----*
##
## Conditional Variance Dynamics
## -----
## GARCH Model : sGARCH(2,1)
## Mean Model : ARFIMA(1,0,0)
## Distribution : sstd
##
## Optimal Parameters
##
         Estimate Std. Error t value Pr(>|t|)
       0.000763 0.000491 1.5525 0.120536
## mu
## ar1 0.071499 0.024572 2.9098 0.003617
## omega 0.000207 0.000068 3.0277 0.002465
## alpha1 0.169869 0.052999 3.2052 0.001350
## alpha2 0.102666 0.080833 1.2701 0.204050
## beta1 0.284713 0.205866 1.3830 0.166664
```

```
1.130440 0.037598 30.0668 0.000000
## skew
## shape 3.996384 0.403277 9.9098 0.000000
##
## Robust Standard Errors:
        Estimate Std. Error t value Pr(>|t|)
## mu
        ## ar1 0.071499 0.021243 3.36576 0.000763
## omega 0.000207 0.000094 2.19969 0.027829
## alpha1 0.169869 0.057160 2.97184 0.002960
## alpha2 0.102666 0.104290 0.98443 0.324906
## beta1
         1.130440 0.040078 28.20571 0.000000
## skew
## shape 3.996384 0.359668 11.11133 0.000000
##
## LogLikelihood : 4393.18
##
## Information Criteria
##
## Akaike
            -5.1259
            -5.1004
## Bayes
## Shibata -5.1259
## Hannan-Quinn -5.1164
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
                      statistic p-value
## Lag[1]
                        0.3448 0.5571
## Lag[2*(p+q)+(p+q)-1][2] 0.8379 0.8319
## Lag[4*(p+q)+(p+q)-1][5] 2.1306 0.6734
## d.o.f=1
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                      statistic p-value
## Lag[1]
                       0.1326 0.7158
## Lag[2*(p+q)+(p+q)-1][8] 0.7286 0.9891
## Lag[4*(p+q)+(p+q)-1][14] 2.0602 0.9900
## d.o.f=3
##
## Weighted ARCH LM Tests
## -----
## Statistic Shape Scale P-Value
## ARCH Lag[4] 0.0532 0.500 2.000 0.8176
## ARCH Lag[6] 0.2805 1.461 1.711 0.9500
## ARCH Lag[8] 0.3122 2.368 1.583 0.9935
##
## Nyblom stability test
## -----
## Joint Statistic: 2.3241
## Individual Statistics:
## mu 0.2652
      0.2279
## ar1
```

```
## omega 0.3983
## alpha1 0.2836
## alpha2 0.3715
## beta1 0.2993
## skew 0.3486
## shape 0.2957
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 1.89 2.11 2.59
## Individual Statistic: 0.35 0.47 0.75
## Sign Bias Test
## -----
##
                t-value prob sig
                 1.0784 0.2810
## Sign Bias
## Negative Sign Bias 0.9879 0.3234
## Positive Sign Bias 0.1876 0.8512
## Joint Effect 1.4835 0.6861
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
## group statistic p-value(g-1)
## 1 20 2.606 1.0000
## 2
      30 11.870
                    0.9979
## 3 40 16.341
                    0.9995
## 4 50 32.162
                    0.9698
##
##
## Elapsed time : 3.998
spec_of_garch_LT<-ugarchspec(variance.model =list(model="eGARCH",garchOrder=c(1,1)),mean.model = list(a</pre>
my_model_LT<-ugarchfit(spec=spec_of_garch_LT,data=ret_LT,out.sample = 500)</pre>
my_model_LT
## *----*
         GARCH Model Fit *
## *----*
##
## Conditional Variance Dynamics
## -----
## GARCH Model : eGARCH(1,1)
## Mean Model : ARFIMA(1,0,0)
## Distribution : sstd
##
## Optimal Parameters
## -----
       Estimate Std. Error t value Pr(>|t|)
## mu
       0.000789 0.000434 1.81683 0.069244
     0.072742 0.021324 3.41126 0.000647
## ar1
## omega -1.144660 0.647472 -1.76789 0.077079
```

beta1 0.853174 0.083032 10.27522 0.000000

```
## gamma1 0.284346 0.079616 3.57145 0.000355
## skew 1.134137 0.036736 30.87285 0.000000
## shape 3.979434 0.396459 10.03743 0.000000
##
## Robust Standard Errors:
        Estimate Std. Error t value Pr(>|t|)
        0.000789 0.000416 1.89810 0.057683
## mu
## ar1 0.072742 0.017036 4.26982 0.000020
## omega -1.144660 1.261303 -0.90752 0.364131
## beta1
         ## gamma1 0.284346 0.140800 2.01950 0.043435
## skew 1.134137 0.038876 29.17351 0.000000
## shape 3.979434 0.350628 11.34945 0.000000
##
## LogLikelihood : 4397.777
##
## Information Criteria
## Akaike -5.1312
## Bayes
            -5.1058
## Shibata -5.1313
## Hannan-Quinn -5.1218
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
                      statistic p-value
## Lag[1]
                         1.059 0.3033
## Lag[2*(p+q)+(p+q)-1][2] 1.847 0.2701
## Lag[4*(p+q)+(p+q)-1][5] 3.000 0.4314
## d.o.f=1
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
          statistic p-value
##
## Lag[1]
                         0.2798 0.5969
## Lag[2*(p+q)+(p+q)-1][5] 0.7422 0.9147
## Lag[4*(p+q)+(p+q)-1][9] 2.0050 0.9044
## d.o.f=2
##
## Weighted ARCH LM Tests
## -----
            Statistic Shape Scale P-Value
## ARCH Lag[3] 0.05946 0.500 2.000 0.8074
## ARCH Lag[5] 1.00700 1.440 1.667 0.7308
## ARCH Lag[7] 1.91089 2.315 1.543 0.7362
## Nyblom stability test
## -----
## Joint Statistic: 2.8802
## Individual Statistics:
## mu 0.2882
```

```
## ar1
      0.2858
## omega 0.2152
## alpha1 0.9880
## beta1 0.2200
## gamma1 0.6411
## skew 0.3692
## shape 0.2086
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic:
                 1.89 2.11 2.59
## Individual Statistic:
                      0.35 0.47 0.75
## Sign Bias Test
## -----
                  t-value prob sig
## Sign Bias
                  0.9758 0.3293
## Negative Sign Bias 0.7299 0.4656
## Positive Sign Bias 0.5182 0.6044
## Joint Effect
                  2.2833 0.5157
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
    group statistic p-value(g-1)
##
## 1
     20
                    0.9892
           7.726
## 2
      30 17.936
                      0.9456
     40 30.601
## 3
                      0.8295
## 4
    50 41.221
                      0.7774
##
## Elapsed time : 1.763997
```

this model is rejected since there is no leverage effect.

```
spec_of_garch_LT<-ugarchspec(variance.model =list(model="gjrGARCH",garchOrder=c(1,1)),mean.model = list
my_model_LT<-ugarchfit(spec=spec_of_garch_LT,data=ret_LT,out.sample = 500)
my_model_LT</pre>
```

```
## ## *-----*
## * GARCH Model Fit *
## *-----*
##
## Conditional Variance Dynamics
## ------
## GARCH Model : gjrGARCH(1,1)
## Mean Model : ARFIMA(1,0,0)
## Distribution : sstd
##
## Optimal Parameters
## Estimate Std. Error t value Pr(>|t|)
## mu 0.001033 0.000505 2.0466 0.040697
```

```
## ar1
          ## omega 0.000001 0.000001 1.1834 0.236641
## alpha1 0.014400 0.003130 4.6010 0.000004
## beta1 0.989979 0.000417 2373.1610 0.000000 ## gamma1 -0.014165 0.005694 -2.4876 0.012859
## skew 1.134564 0.038823 29.2243 0.000000
## shape 3.752190 0.501981 7.4748 0.000000
##
## Robust Standard Errors:
##
        Estimate Std. Error t value Pr(>|t|)
## mu
          0.001033 0.000539 1.91604 0.055359
          0.069303 0.024166 2.86775 0.004134
## ar1
## omega 0.000001 0.000005 0.21812 0.827336
## alpha1 0.014400 0.006998 2.05770 0.039619
## beta1 0.989979 0.000266 3718.02486 0.000000 ## gamma1 -0.014165 0.009683 -1.46282 0.143515
## skew 1.134564 0.053372 21.25779 0.000000
## shape 3.752190 2.034840 1.84397 0.065187
##
## LogLikelihood: 4387.81
##
## Information Criteria
## -----
## Akaike
             -5.1196
## Bayes
              -5.0941
## Shibata -5.1196
## Hannan-Quinn -5.1102
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
                         statistic p-value
## Lag[1]
                          1.759 0.18474
## Lag[2*(p+q)+(p+q)-1][2] 3.480 0.01319
## Lag[4*(p+q)+(p+q)-1][5] 5.400 0.07697
## d.o.f=1
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                         statistic p-value
## Lag[1]
                            48.24 3.774e-12
## Lag[2*(p+q)+(p+q)-1][5] 62.19 0.000e+00
## Lag[4*(p+q)+(p+q)-1][9] 67.18 0.000e+00
## d.o.f=2
##
## Weighted ARCH LM Tests
## -----
              Statistic Shape Scale P-Value
## ARCH Lag[3] 11.93 0.500 2.000 5.512e-04
## ARCH Lag[5] 18.71 1.440 1.667 4.513e-05
## ARCH Lag[7] 19.37 2.315 1.543 9.253e-05
##
## Nyblom stability test
```

```
## Joint Statistic: 328.8651
## Individual Statistics:
        0.06815
## mu
## ar1
        0.36858
## omega 33.01721
## alpha1 0.12167
## beta1
         0.17204
## gamma1 0.16287
## skew
         0.32744
## shape
         0.14329
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 1.89 2.11 2.59
## Individual Statistic: 0.35 0.47 0.75
##
## Sign Bias Test
## -----
                 t-value prob sig
##
## Sign Bias
                  0.5377 5.909e-01
## Negative Sign Bias 3.3919 7.099e-04 ***
## Positive Sign Bias 4.2305 2.455e-05 ***
## Joint Effect 31.0162 8.434e-07 ***
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
##
  group statistic p-value(g-1)
## 1 20 21.00 0.3365
## 2
    30 19.58
                       0.9054
     40 46.92
## 3
                      0.1797
## 4
    50 44.79
                       0.6445
##
##
## Elapsed time : 2.653998
spec_of_garch_LT<-ugarchspec(variance.model =list(model="gjrGARCH",garchOrder=c(1,2)),mean.model = list</pre>
my_model_LT<-ugarchfit(spec=spec_of_garch_LT,data=ret_LT,out.sample = 500)</pre>
my_model_LT
       GARCH Model Fit *
## *----*
##
## Conditional Variance Dynamics
## -----
## GARCH Model : gjrGARCH(1,2)
## Mean Model : ARFIMA(1,0,0)
## Distribution : sstd
## Convergence Problem:
## Solver Message:
```

```
spec_of_garch_LT<-ugarchspec(variance.model =list(model="gjrGARCH",garchOrder=c(2,1)),mean.model = list
my_model_LT<-ugarchfit(spec=spec_of_garch_LT,data=ret_LT,out.sample = 500)
my_model_LT</pre>
```

```
##
            GARCH Model Fit
## Conditional Variance Dynamics
## -----
## GARCH Model : gjrGARCH(2,1)
## Mean Model : ARFIMA(1,0,0)
## Distribution : sstd
##
## Optimal Parameters
## -----
         Estimate Std. Error t value Pr(>|t|)
## mu
         0.001016 0.000510 1.99436 0.046113
## ar1
          ## omega 0.000001 0.000001 0.96774 0.333177
## alpha1 0.013574 0.007948 1.70783 0.087667
## alpha2 0.000000 0.010214 0.00000 1.000000
## beta1
          0.991444 0.000290 3421.77075 0.000000
## gamma1 0.159525 0.003386 47.11427 0.000000
## gamma2 -0.174462 0.000785 -222.16132 0.000000
## skew 1.138457 0.039542 28.79112 0.000000
## shape 3.821576 0.573914 6.65879 0.000000
##
## Robust Standard Errors:
##
        Estimate Std. Error t value Pr(>|t|)
         0.001016 0.000616 1.64979 0.098987
## mu
## ar1
         0.064837 0.027528 2.35535 0.018505
## omega 0.000001 0.000006 0.14773 0.882555
## alpha1 0.013574 0.033336 0.40718 0.683874
## alpha2 0.000000 0.042037 0.00000 1.000000
## beta1 0.991444 0.000443 2236.70850 0.000000
## gamma1 0.159525 0.010856 14.69484 0.000000
1.138457 0.058633 19.41673 0.000000
## skew
          3.821576 2.987533
## shape
                              1.27917 0.200836
##
## LogLikelihood: 4393.135
##
## Information Criteria
## -----
## Akaike
             -5.1235
## Bayes
              -5.0917
## Shibata
            -5.1235
## Hannan-Quinn -5.1117
##
## Weighted Ljung-Box Test on Standardized Residuals
```

```
statistic p-value
##
## Lag[1]
                         2.974 0.084596
## Lag[2*(p+q)+(p+q)-1][2] 4.578 0.001169
## Lag[4*(p+q)+(p+q)-1][5] 6.409 0.032671
## d.o.f=1
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                          statistic p-value
## Lag[1]
                            31.51 1.984e-08
## Lag[2*(p+q)+(p+q)-1][8] 47.75 2.192e-12
## Lag[4*(p+q)+(p+q)-1][14] 50.90 2.078e-11
## d.o.f=3
##
## Weighted ARCH LM Tests
## -----
## Statistic Shape Scale P-Value
## ARCH Lag[4] 7.242 0.500 2.000 0.007123
## ARCH Lag[6] 7.560 1.461 1.711 0.029565
## ARCH Lag[8] 7.807 2.368 1.583 0.068270
##
## Nyblom stability test
## -----
## Joint Statistic: 352.0509
## Individual Statistics:
        0.05894
## mu
## ar1
        0.29288
## omega 40.78036
## alpha1 0.14762
## alpha2 0.18165
## beta1 0.19707
## gamma1 0.18855
## gamma2 0.18714
## skew 0.38635
## shape 0.20879
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 2.29 2.54 3.05
## Individual Statistic: 0.35 0.47 0.75
## Sign Bias Test
## -----
                   t-value prob sig
## Sign Bias
                    0.1285 8.978e-01
## Negative Sign Bias 0.7564 4.495e-01
## Positive Sign Bias 4.3759 1.283e-05 ***
## Joint Effect 25.0857 1.482e-05 ***
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
## group statistic p-value(g-1)
```

```
## 1
      20
           6.65
                     0.9959
## 2
      30
           10.26
                     0.9995
## 3
      40
          27.84
                     0.9085
## 4
           25.44
      50
                     0.9978
##
##
## Elapsed time : 7.127001
spec_of_garch_LT<-ugarchspec(variance.model =list(model="gjrGARCH",garchOrder=c(2,2)),mean.model = list</pre>
my_model_LT<-ugarchfit(spec=spec_of_garch_LT,data=ret_LT,out.sample = 500)</pre>
my_model_LT
## *----*
          GARCH Model Fit
## *----*
## Conditional Variance Dynamics
## -----
## GARCH Model : gjrGARCH(2,2)
## Mean Model : ARFIMA(1,0,0)
## Distribution : sstd
## Optimal Parameters
##
        Estimate Std. Error t value Pr(>|t|)
## mu
        0.001187 0.000126 9.4439 0.00000
        0.070110 0.010252 6.8385 0.00000
## ar1
        0.000001 0.000001
                         0.9483 0.34298
## omega
## alpha1 0.019326 0.000867 22.2948 0.00000
## alpha2 0.003138 0.000016 193.6857 0.00000
        0.501790 0.000611 820.8856 0.00000
## beta1
## beta2
        0.484405 0.001499 323.1059 0.00000
## gamma1 0.033767 0.001465 23.0444 0.00000
## skew
## shape
        3.723429 0.324133 11.4873 0.00000
## Robust Standard Errors:
##
        Estimate Std. Error t value Pr(>|t|)
## mu
        ## ar1
        0.070110 0.043188 1.62337 0.104511
## omega 0.000001 0.000012 0.11915 0.905154
## alpha1 0.019326 0.002159 8.95056 0.000000
## alpha2 0.003138 0.000029 107.80242 0.000000
        ## beta1
        0.484405 0.008359 57.94782 0.000000
## beta2
## gamma1 0.033767 0.001713 19.71466 0.000000
## skew
## shape
        3.723429
                0.909329
                         4.09470 0.000042
##
## LogLikelihood: 4390.719
```

##

```
## Information Criteria
## -----
##
            -5.1195
## Akaike
            -5.0845
## Bayes
## Shibata -5.1196
## Hannan-Quinn -5.1065
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
                     statistic p-value
                        1.618 0.20341
## Lag[1]
## Lag[2*(p+q)+(p+q)-1][2] 3.330 0.01804
## Lag[4*(p+q)+(p+q)-1][5] 5.259 0.08641
## d.o.f=1
## HO : No serial correlation
##
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                       statistic
                                 p-value
                         29.16 6.668e-08
## Lag[1]
## Lag[2*(p+q)+(p+q)-1][11] 47.09 2.976e-11
## Lag[4*(p+q)+(p+q)-1][19] 50.36 7.264e-10
## d.o.f=4
##
## Weighted ARCH LM Tests
## -----
    Statistic Shape Scale P-Value
## ARCH Lag[5] 0.3517 0.500 2.000 0.5532
## ARCH Lag[7] 0.5455 1.473 1.746 0.8849
## ARCH Lag[9] 0.7603 2.402 1.619 0.9607
##
## Nyblom stability test
## -----
## Joint Statistic: 245.5898
## Individual Statistics:
## mu 0.3456
## ar1
       0.2557
## omega 19.9165
## alpha1 0.1883
## alpha2 0.1976
## beta1 0.1480
## beta2 0.1430
## gamma1 0.2098
## gamma2 0.2730
## skew
         0.4331
## shape 0.1060
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 2.49 2.75 3.27
## Individual Statistic: 0.35 0.47 0.75
##
## Sign Bias Test
## -----
```

```
##
                    t-value prob sig
## Sign Bias
                      0.415 0.6781661
## Negative Sign Bias 2.055 0.0400457 **
## Positive Sign Bias 3.696 0.0002256 ***
## Joint Effect
                     20.686 0.0001223 ***
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
    group statistic p-value(g-1)
## 1
       20
             9.90
                        0.9554
## 2
       30
             12.12
                        0.9975
## 3
       40
             23.07
                        0.9800
## 4
       50
             34.62
                        0.9402
##
##
## Elapsed time : 4.739013
```

 $sGARCH(0,2) \ Akaike \ -4.5795 \ sstd \ sGARCH(2,0) \ Akaike \ -4.6343 \ sstd \ sGARCH(2,1) \ Akaike \ -4.6599 \ sstd \ sGARCH(2,2) \ Akaike \ -4.6650 \ sstd \ sGARCH(1,1) \ Akaike \ -4.6611 \ sstd \ sGARCH(1,2) \ Akaike \ -4.6657 \ sstd \ gjrGARCH(2,1) \ Akaike \ -4.6685 \ sstd \ gjrGARCH(1,1) \ Akaike \ -4.6703 \ sstd \ gjrGARCH(1,2) \ Akaike \ -4.6730 \ sstd \ gjrGARCH(2,2) \ Akaike \ -4.6742 \ sstd$

so we are taking (1,2) instead of (2,2) because many terms in it are not significant

```
spec_of_garch_LT<-ugarchspec(variance.model =list(model="gjrGARCH",garchOrder=c(1,3)),mean.model = list
my_model_LT<-ugarchfit(spec=spec_of_garch_LT,data=ret_LT,out.sample = 500)
my_model_LT</pre>
```

```
##
          GARCH Model Fit
## *----*
## Conditional Variance Dynamics
## -----
## GARCH Model : gjrGARCH(1,3)
## Mean Model : ARFIMA(1,0,0)
## Distribution : sstd
##
## Optimal Parameters
##
        Estimate Std. Error t value Pr(>|t|)
## mu
        0.001002 0.000496
                         2.0206 0.043321
## ar1
        0.068221
                 0.022856
                        2.9848 0.002838
                          2.4388 0.014734
## omega
        0.000003 0.000001
## alpha1 0.035149
               0.006150
                         5.7155 0.000000
## beta1
        0.134265 0.006487 20.6981 0.000000
## beta2
        0.445062 0.004263 104.4113 0.000000
## beta3
## skew
        1.134488 0.037318 30.4002 0.000000
## shape
        3.802105 0.360754 10.5393 0.000000
##
```

```
## Robust Standard Errors:
##
      Estimate Std. Error t value Pr(>|t|)
## mu
        0.001002 0.000522 1.9211 0.054717
## ar1
          0.068221 0.023034 2.9617 0.003059
## omega 0.000003 0.000002 1.1354 0.256213
## alpha1 0.035149 0.013164 2.6700 0.007584
## beta1 0.134265 0.009667 13.8892 0.000000
## beta2  0.392030  0.005323  73.6454  0.000000  ## beta3  0.445062  0.001196  372.0647  0.000000
## gamma1 -0.025375 0.022260 -1.1399 0.254312
## skew 1.134488 0.040282 28.1633 0.000000
## shape 3.802105 0.393369 9.6655 0.000000
## LogLikelihood: 4389.106
##
## Information Criteria
##
## Akaike
             -5.1188
             -5.0869
## Bayes
## Shibata -5.1188
## Hannan-Quinn -5.1070
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
                        statistic p-value
## Lag[1]
                           1.794 0.18044
## Lag[2*(p+q)+(p+q)-1][2] 3.428 0.01470
## Lag[4*(p+q)+(p+q)-1][5] 5.386 0.07788
## d.o.f=1
## HO : No serial correlation
##
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
                       statistic p-value
##
## Lag[1]
                           29.85 4.673e-08
## Lag[2*(p+q)+(p+q)-1][11] 46.44 4.544e-11
## Lag[4*(p+q)+(p+q)-1][19] 49.36 1.335e-09
## d.o.f=4
##
## Weighted ARCH LM Tests
## -----
            Statistic Shape Scale P-Value
## ARCH Lag[5] 0.5495 0.500 2.000 0.4585
## ARCH Lag[7] 0.8048 1.473 1.746 0.8124
## ARCH Lag[9] 0.9863 2.402 1.619 0.9332
##
## Nyblom stability test
## -----
## Joint Statistic: 93.1594
## Individual Statistics:
## mu
       0.09787
## ar1 0.37615
## omega 5.61479
```

```
## alpha1 0.10599
## beta1 0.15753
## beta2 0.15784
## beta3 0.15837
## gamma1 0.15470
## skew 0.31131
## shape 0.12551
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 2.29 2.54 3.05
## Individual Statistic:
                      0.35 0.47 0.75
## Sign Bias Test
## -----
                  t-value prob sig
## Sign Bias
                  0.9691 0.3326233
## Negative Sign Bias 3.1047 0.0019359 ***
## Positive Sign Bias 2.9164 0.0035868 ***
## Joint Effect 19.5202 0.0002134 ***
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
   group statistic p-value(g-1)
##
## 1 20 12.64 0.8567
## 2 30 14.32
                     0.9896
## 3 40 27.66
## 4 50 31.87
                      0.9128
                     0.9724
##
## Elapsed time : 3.796001
spec_of_garch_LT<-ugarchspec(variance.model =list(model="gjrGARCH",garchOrder=c(3,1)),mean.model = list</pre>
my_model_LT<-ugarchfit(spec=spec_of_garch_LT,data=ret_LT,out.sample = 500)</pre>
my_model_LT
##
## *----*
    GARCH Model Fit
## *----*
## Conditional Variance Dynamics
## -----
## GARCH Model : gjrGARCH(3,1)
## Mean Model : ARFIMA(1,0,0)
## Distribution : sstd
## Optimal Parameters
```

Estimate Std. Error t value Pr(>|t|)
mu 0.000954 0.000327 2.917866 0.003524
ar1 0.063416 0.022260 2.848911 0.004387
omega 0.000001 0.000001 1.616038 0.106086
alpha1 0.012018 0.003844 3.126464 0.001769

```
## alpha2 0.000000 0.038529 0.000001 0.999999  
## alpha3 0.000000 0.044948 0.000001 0.999999
## beta1 0.993397 0.000820 1210.942981 0.000000
## gamma1 0.176610 0.000990 178.350844 0.000000 ## gamma2 -0.048113 0.004169 -11.541650 0.000000
## gamma3 -0.144040 0.003578 -40.260104 0.000000
## skew 1.143089 0.030641 37.306096 0.000000
## shape 3.963093 0.473081 8.377197 0.000000
##
## Robust Standard Errors:
          Estimate Std. Error t value Pr(>|t|)
## mu 0.000954 0.002897 0.32941 0.741845
## ar1 0.063416 0.050715 1.25045 0.211135
## omega 0.000001 0.000003 0.31643 0.751675
## alpha1 0.012018 0.037353 0.32175 0.747643
## alpha2 0.000000 0.231181 0.00000 1.000000
## alpha3 0.000000 0.261977 0.00000 1.000000
           ## beta1
## gamma1 0.176610 0.005890 29.98556 0.000000 ## gamma2 -0.048113 0.024916 -1.93104 0.053478
## gamma3 -0.144040 0.017625 -8.17231 0.000000
## skew 1.143089 0.152989 7.47172 0.000000
## shape 3.963093 2.901808 1.36573 0.172023
##
## LogLikelihood: 4397.704
## Information Criteria
##
## Akaike -5.1265
## Bayes -5.0883
## Shibata -5.1266
## Hannan-Quinn -5.1123
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
                          statistic p-value
## Lag[1]
                              3.638 0.0564701
## Lag[2*(p+q)+(p+q)-1][2] 5.304 0.0002138
## Lag[4*(p+q)+(p+q)-1][5] 7.106 0.0175208
## d.o.f=1
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                             statistic p-value
                                37.94 7.288e-10
## Lag[1]
## Lag[2*(p+q)+(p+q)-1][11] 57.20 3.941e-14
## Lag[4*(p+q)+(p+q)-1][19] 61.17 8.932e-13
## d.o.f=4
##
## Weighted ARCH LM Tests
## -----
                Statistic Shape Scale P-Value
```

```
## ARCH Lag[5]
            0.4281 0.500 2.000 0.5129
## ARCH Lag[7] 0.8721 1.473 1.746 0.7933
## ARCH Lag[9] 1.5645 2.402 1.619 0.8405
##
## Nyblom stability test
## -----
## Joint Statistic: 352.593
## Individual Statistics:
## mu
       0.05672
## ar1
        0.28967
## omega 48.59588
## alpha1 0.15962
## alpha2 0.18816
## alpha3 0.20461
## beta1
         0.17454
## gamma1 0.19180
## gamma2 0.19083
## gamma3 0.19158
## skew
         0.40980
## shape 0.19717
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 2.69 2.96 3.51
## Individual Statistic: 0.35 0.47 0.75
##
## Sign Bias Test
## -----
                          prob sig
                 t-value
## Sign Bias
                  0.4466 6.552e-01
## Negative Sign Bias 0.6008 5.481e-01
## Positive Sign Bias 4.7319 2.408e-06 ***
## Joint Effect 27.7099 4.179e-06 ***
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
## group statistic p-value(g-1)
## 1
      20 4.406
                    0.9998
## 2
      30 17.445
                      0.9548
## 3 40 27.095
                     0.9249
## 4 50 30.993
                      0.9792
##
## Elapsed time : 10.171
spec_of_garch_LT<-ugarchspec(variance.model =list(model="gjrGARCH",garchOrder=c(2,3)),mean.model = list</pre>
my_model_LT<-ugarchfit(spec=spec_of_garch_LT,data=ret_LT,out.sample = 500)
my model LT
## *----*
          GARCH Model Fit
## *----*
```

##

```
## Conditional Variance Dynamics
## -----
## GARCH Model : gjrGARCH(2,3)
## Mean Model : ARFIMA(1,0,0)
## Distribution : sstd
##
## Convergence Problem:
## Solver Message:
spec_of_garch_LT<-ugarchspec(variance.model =list(model="gjrGARCH",garchOrder=c(3,2)),mean.model = list</pre>
my_model_LT<-ugarchfit(spec=spec_of_garch_LT,data=ret_LT,out.sample = 500)</pre>
my_model_LT
##
## *----*
          GARCH Model Fit
## *----*
##
## Conditional Variance Dynamics
## -----
## GARCH Model : gjrGARCH(3,2)
## Mean Model : ARFIMA(1,0,0)
## Distribution : sstd
## Optimal Parameters
## -----
         Estimate Std. Error t value Pr(>|t|)
## mu
         0.001003 0.000482
                             2.082159 0.037328
## ar1
         0.063491 0.024091
                           2.635489 0.008402
## omega
         0.000001 0.000000 16.954286 0.000000
## alpha1 0.020915 0.000689 30.361910 0.000000 ## alpha2 0.000058 0.008532 0.006805 0.994570
## alpha3 0.000041 0.007534
                            0.005482 0.995626
## beta1
         0.394564 0.000399 988.297737 0.000000
## beta2  0.592488  0.002257  262.560779  0.000000  ## gamma1  0.162475  0.001257  129.222067  0.000000
## skew
                   0.037897 30.090295 0.000000
         1.140339
## shape
         3.912920
                   0.360636
                           10.850041 0.000000
##
## Robust Standard Errors:
##
         Estimate Std. Error
                            t value Pr(>|t|)
## mu
         ## ar1
         0.063491 0.024641
                           2.576626 0.009977
## omega
         0.000001
                 0.000000
                           9.416683 0.000000
## alpha1 0.020915
                 0.003015
                            6.936393 0.000000
## alpha2 0.000058 0.008448
                            0.006873 0.994516
## alpha3 0.000041 0.007073
                           0.005839 0.995341
         0.394564 0.000522 755.392371 0.000000
0.592488 0.002802 211.485181 0.000000
## beta1
## beta2
## gamma1 0.162475 0.000411 395.659575 0.000000
```

0.001935 -68.429630 0.000000

gamma3 -0.132414

```
1.140339 0.041576 27.427841 0.000000
## skew
## shape 3.912920 0.352966 11.085839 0.000000
##
## LogLikelihood: 4395.481
## Information Criteria
## -----
## Akaike -5.1227
## Bayes -5.0813
## Shibata -5.1228
## Hannan-Quinn -5.1074
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
                       statistic p-value
                          2.948 0.085999
## Lag[1]
## Lag[2*(p+q)+(p+q)-1][2] 4.619 0.001065
## Lag[4*(p+q)+(p+q)-1][5] 6.417 0.032448
## d.o.f=1
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                         statistic p-value
## Lag[1]
                          25.96 3.481e-07
## Lag[2*(p+q)+(p+q)-1][14] 44.67 1.077e-09
## Lag[4*(p+q)+(p+q)-1][24] 49.80 1.708e-08
## d.o.f=5
##
## Weighted ARCH LM Tests
## -----
     Statistic Shape Scale P-Value
## ARCH Lag[6] 0.2357 0.500 2.000 0.6273
## ARCH Lag[8] 0.5323 1.480 1.774 0.8922
## ARCH Lag[10] 1.0158 2.424 1.650 0.9342
##
## Nyblom stability test
## -----
## Joint Statistic: 230.9085
## Individual Statistics:
## mu
       0.05955
## ar1
        0.28414
## omega 20.49630
## alpha1 0.13273
## alpha2 0.17170
## alpha3 0.18120
## beta1
          0.16803
## beta2
          0.16820
## gamma1 0.17193
## gamma2 0.17303
## gamma3 0.16815
## skew
         0.37563
## shape 0.16733
```

```
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 2.89 3.15 3.69
## Individual Statistic:
                         0.35 0.47 0.75
## Sign Bias Test
## -----
                     t-value prob sig
## Sign Bias
                     0.01682 9.866e-01
## Negative Sign Bias 0.65317 5.137e-01
## Positive Sign Bias 3.91795 9.283e-05 ***
## Joint Effect 20.78570 1.166e-04 ***
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
   group statistic p-value(g-1)
## 1 20 11.68
## 2
       30 17.06
                        0.9612
     40 29.15
## 3
                        0.8746
## 4 50 33.80
                       0.9517
##
##
## Elapsed time : 5.876993
spec_of_garch_LT<-ugarchspec(variance.model =list(model="gjrGARCH",garchOrder=c(3,3)),mean.model = list</pre>
my_model_LT<-ugarchfit(spec=spec_of_garch_LT,data=ret_LT,out.sample = 500)</pre>
my_model_LT
##
           GARCH Model Fit
## Conditional Variance Dynamics
## -----
## GARCH Model : gjrGARCH(3,3)
## Mean Model : ARFIMA(1,0,0)
## Distribution : sstd
##
## Optimal Parameters
## -----
        Estimate Std. Error t value Pr(>|t|) 0.000530 0.000456 1.161636 0.245384
##
## mu
## ar1 0.055797 0.021936 2.543678 0.010969
## omega 0.000009 0.000002 3.701944 0.000214
## alpha1 0.030182 0.003360 8.982847 0.000000
## alpha2 0.000000 0.017878 0.000002 0.999999
## alpha3 0.000000 0.015133 0.000000 1.000000
## beta1 0.527362 0.000407 1295.181143 0.000000
## beta2 0.145327 0.001459 99.624414 0.000000
## beta3 0.262306 0.001984 132.204228 0.000000
```

gamma1 0.157617 0.010851 14.525269 0.000000 ## gamma2 0.144342 0.012985 11.115758 0.000000

```
1.119412 0.036398 30.755182 0.000000
## skew
## shape 4.055594 0.335250 12.097223 0.000000
##
## Robust Standard Errors:
         Estimate Std. Error t value Pr(>|t|)
##
         0.000530 0.000474 1.118218 0.263474
## mu

      0.055797
      0.022451
      2.485269
      0.012945

      0.000009
      0.000003
      2.599090
      0.009347

## ar1
## omega
## alpha1 0.030182 0.004086 7.386280 0.000000
## alpha2 0.000000 0.021046 0.000002 0.999999
## beta2
         ## gamma3 -0.262287 0.001029 -254.944764 0.000000
## skew
         1.119412 0.038984 28.714363 0.000000
                  0.327123 12.397752 0.000000
## shape
         4.055594
##
## LogLikelihood : 4387.786
##
## Information Criteria
## -----
## Akaike
             -5.1125
             -5.0680
## Bayes
## Shibata
         -5.1127
## Hannan-Quinn -5.0961
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
                       statistic p-value
## Lag[1]
                        4.931 2.638e-02
## Lag[2*(p+q)+(p+q)-1][2] 6.281 1.985e-05
## Lag[4*(p+q)+(p+q)-1][5] 7.780 9.417e-03
## d.o.f=1
## HO : No serial correlation
##
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
                        statistic
                                  p-value
## Lag[1]
                         22.62 1.978e-06
## Lag[2*(p+q)+(p+q)-1][17]
                        43.43 1.484e-08
## Lag[4*(p+q)+(p+q)-1][29] 49.75 2.094e-07
## d.o.f=6
##
## Weighted ARCH LM Tests
## -----
##
             Statistic Shape Scale P-Value
## ARCH Lag[7] 0.1426 0.500 2.000 0.7057
## ARCH Lag[9] 0.6289 1.485 1.796 0.8696
## ARCH Lag[11] 1.2523 2.440 1.677 0.9059
```

```
##
## Nyblom stability test
## -----
## Joint Statistic: 24.4062
## Individual Statistics:
## mu
       0.1594
## ar1
      0.4324
## omega 1.7146
## alpha1 0.1266
## alpha2 0.1583
## alpha3 0.1910
## beta1 0.1690
## beta2 0.1714
## beta3 0.1723
## gamma1 0.1604
## gamma2 0.1569
## gamma3 0.1421
## skew 0.3474
## shape 0.1763
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 3.08 3.34 3.9
## Individual Statistic: 0.35 0.47 0.75
## Sign Bias Test
## -----
              t-value prob sig
##
                   0.2944 0.7684637
## Sign Bias
## Negative Sign Bias 0.6573 0.5110458
## Positive Sign Bias 3.4846 0.0005053 ***
## Joint Effect 18.0790 0.0004236 ***
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
## group statistic p-value(g-1)
## 1 20 7.819 0.9884
## 2
      30 21.443
                       0.8425
     40 22.279
## 3
                      0.9855
## 4
    50 30.175
                      0.9842
##
## Elapsed time : 9.422992
going further is not leading any good results
spec_of_garch_LT<-ugarchspec(variance.model =list(model="gjrGARCH",garchOrder=c(3,1)),mean.model = list</pre>
my_model_LT<-ugarchfit(spec=spec_of_garch_LT,data=ret_LT,out.sample = 500)</pre>
my_model_LT
## *----*
## *
```

GARCH Model Fit

```
##
## Conditional Variance Dynamics
## -----
## GARCH Model : gjrGARCH(3,1)
## Mean Model : ARFIMA(1,0,0)
## Distribution : sstd
##
## Optimal Parameters
## -----
           Estimate Std. Error
                                   t value Pr(>|t|)
                                 2.917866 0.003524
           0.000954 0.000327
## mu
## ar1 0.063416 0.022260 2.848911 0.004387
## omega 0.000001 0.000001 1.616038 0.106086
## alpha1 0.012018 0.003844 3.126464 0.001769
## alpha2 0.000000 0.038529 0.000001 0.999999
## alpha3 0.000000 0.044948 0.000001 0.999999
           ## beta1
## gamma1 0.176610 0.000990 178.350844 0.000000 ## gamma2 -0.048113 0.004169 -11.541650 0.000000
## gamma3 -0.144040 0.003578 -40.260104 0.000000
## skew 1.143089 0.030641 37.306096 0.000000
## shape 3.963093 0.473081
                                 8.377197 0.000000
##
## Robust Standard Errors:
         Estimate Std. Error t value Pr(>|t|)
## mu
           0.000954 0.002897 0.32941 0.741845
## ar1 0.063416 0.050715 1.25045 0.211135
## omega 0.000001 0.000003 0.31643 0.751675
## alpha1 0.012018 0.037353 0.32175 0.747643
## alpha2 0.000000 0.231181 0.00000 1.000000
## alpha3 0.000000 0.261977 0.00000 1.000000
## beta1 0.993397 0.004584 216.70656 0.000000
## gamma1 0.176610 0.005890 29.98556 0.000000
## gamma2 -0.048113 0.024916 -1.93104 0.053478
## gamma3 -0.144040 0.017625 -8.17231 0.000000
## skew 1.143089 0.152989 7.47172 0.000000
## shape 3.963093
                     2.901808 1.36573 0.172023
##
## LogLikelihood: 4397.704
## Information Criteria
## -----
##
## Akaike
               -5.1265
               -5.0883
## Bayes
             -5.1266
## Shibata
## Hannan-Quinn -5.1123
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
                           statistic p-value
## Lag[1]
                           3.638 0.0564701
## Lag[2*(p+q)+(p+q)-1][2] 5.304 0.0002138
```

```
## Lag[4*(p+q)+(p+q)-1][5] 7.106 0.0175208
## d.o.f=1
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                     statistic p-value
## Lag[1]
                         37.94 7.288e-10
## Lag[2*(p+q)+(p+q)-1][11] 57.20 3.941e-14
## Lag[4*(p+q)+(p+q)-1][19] 61.17 8.932e-13
## d.o.f=4
## Weighted ARCH LM Tests
## -----
    Statistic Shape Scale P-Value
## ARCH Lag[5] 0.4281 0.500 2.000 0.5129
## ARCH Lag[7] 0.8721 1.473 1.746 0.7933
## ARCH Lag[9] 1.5645 2.402 1.619 0.8405
## Nyblom stability test
## -----
## Joint Statistic: 352.593
## Individual Statistics:
## mu
       0.05672
## ar1
       0.28967
## omega 48.59588
## alpha1 0.15962
## alpha2 0.18816
## alpha3 0.20461
## beta1 0.17454
## gamma1 0.19180
## gamma2 0.19083
## gamma3 0.19158
## skew
        0.40980
## shape 0.19717
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 2.69 2.96 3.51
## Individual Statistic: 0.35 0.47 0.75
##
## Sign Bias Test
## -----
                 t-value prob sig
## Sign Bias
                 0.4466 6.552e-01
## Negative Sign Bias 0.6008 5.481e-01
## Positive Sign Bias 4.7319 2.408e-06 ***
## Joint Effect 27.7099 4.179e-06 ***
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
## group statistic p-value(g-1)
## 1 20 4.406 0.9998
## 2 30 17.445
                    0.9548
```

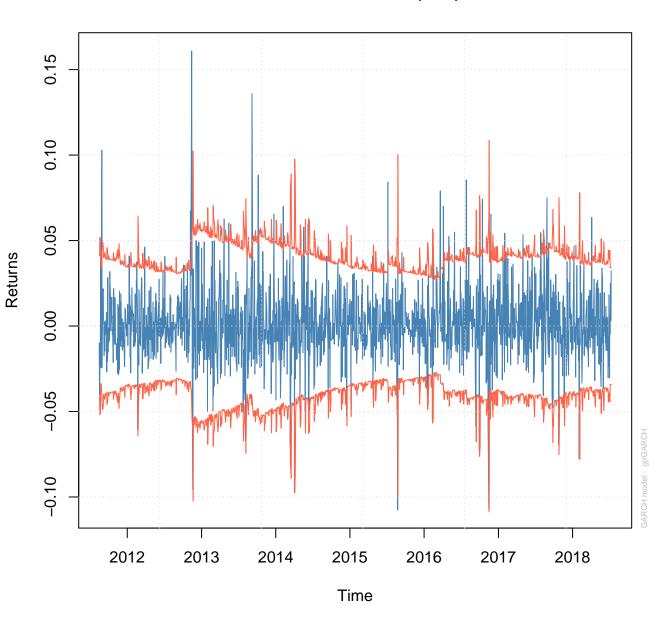
```
## 3
       40
             27.095
                          0.9249
## 4
       50
             30.993
                          0.9792
##
##
## Elapsed time : 6.320003
back_testing<-ugarchroll(spec_of_garch_LT,ret_LT,n.ahead=1,n.start = 2000,refit.every =30,refit.window
##
## Iter: 1 fn: -5023.2196
                                   4.993e-04 5.821e-02 1.317e-05 3.797e-02 1.354e-08 1.183e-11
                           Pars:
## Iter: 2 fn: -5023.2196
                           Pars: 4.992e-04 5.820e-02 1.317e-05 3.797e-02 1.351e-08
                                                                                         8.533e-16
## Iter: 3 fn: -5023.2196
                           Pars:
                                   4.993e-04 5.820e-02 1.317e-05 3.797e-02 1.351e-08
                                                                                         2.548e-16
## Iter: 4 fn: -5023.2196
                           Pars: 4.993e-04 5.820e-02 1.317e-05 3.797e-02 1.351e-08 2.214e-16
## solnp--> Completed in 4 iterations
##
## Iter: 1 fn: -5014.9800
                           Pars:
                                   0.00059160111 \quad 0.05790410750 \quad 0.00001161126 \quad 0.03958245825 \quad 0.0000
## Iter: 2 fn: -5014.9800
                                   Pars:
## solnp--> Completed in 2 iterations
##
## Iter: 1 fn: -4997.4099
                           Pars:
                                   0.0006767004 0.0548740817 0.0000123802 0.0436199545 0.00000023
## Iter: 2 fn: -4997.4099
                                   6.767e-04 5.487e-02 1.238e-05 4.361e-02 9.912e-09 2.697e-12
                           Pars:
## Iter: 3 fn: -4997.4099
                                   6.767e-04 5.487e-02 1.238e-05 4.361e-02 9.912e-09 2.697e-12
                           Pars:
## solnp--> Completed in 3 iterations
##
## Iter: 1 fn: -4982.1370
                           Pars:
                                   0.0007629200018 \quad 0.0495050756343 \quad 0.0000109168954 \quad 0.0376035543855
## Iter: 2 fn: -4982.1370
                           Pars:
                                   7.629e-04 4.950e-02 1.092e-05 3.760e-02 9.651e-09 3.525e-11
## Iter: 3 fn: -4982.1370
                           Pars:
                                   7.629e-04 4.950e-02 1.092e-05 3.760e-02 9.651e-09 3.525e-11
## solnp--> Completed in 3 iterations
##
## Iter: 1 fn: -4953.0579
                                   0.0006006073277 \quad 0.0526367770131 \quad 0.0000106095125 \quad 0.0377947188657
                           Pars:
## Iter: 2 fn: -4953.0579
                           Pars:
                                   0.0006006073277 \quad 0.0526367770131 \quad 0.0000106095125 \quad 0.0377947188657
## solnp--> Completed in 2 iterations
##
## Iter: 1 fn: -4910.8614
                                   0.00055561111 \quad 0.04515577736 \quad 0.00001158362 \quad 0.04121526381 \quad 0.0000
                           Pars:
## Iter: 2 fn: -4910.8614
                           Pars:
                                   0.0005556184546 \quad 0.0451556335504 \quad 0.0000115834053 \quad 0.0412150276547
                                   0.0005556184546 \quad 0.0451556335504 \quad 0.0000115834053 \quad 0.0412150276547
## Iter: 3 fn: -4910.8614
                           Pars:
## solnp--> Completed in 3 iterations
##
                                   0.00063291226 0.04767755780 0.00001221280 0.04228984550 0.0000
## Iter: 1 fn: -4880.0984
                           Pars:
## Iter: 2 fn: -4880.0984
                                   Pars:
## solnp--> Completed in 2 iterations
##
                                   0.0006535851752 \quad 0.0523427924861 \quad 0.0000130225823 \quad 0.0425814848666
## Iter: 1 fn: -4852.6915
                           Pars:
## Iter: 2 fn: -4852.6915
                                   0.0006535851752 \quad 0.0523427924861 \quad 0.0000130225823 \quad 0.0425814848666
                           Pars:
## solnp--> Completed in 2 iterations
report(back_testing)
## VaR Backtest Report
## Model:
                       gjrGARCH-sstd
## Backtest Length: 211
```

Data:

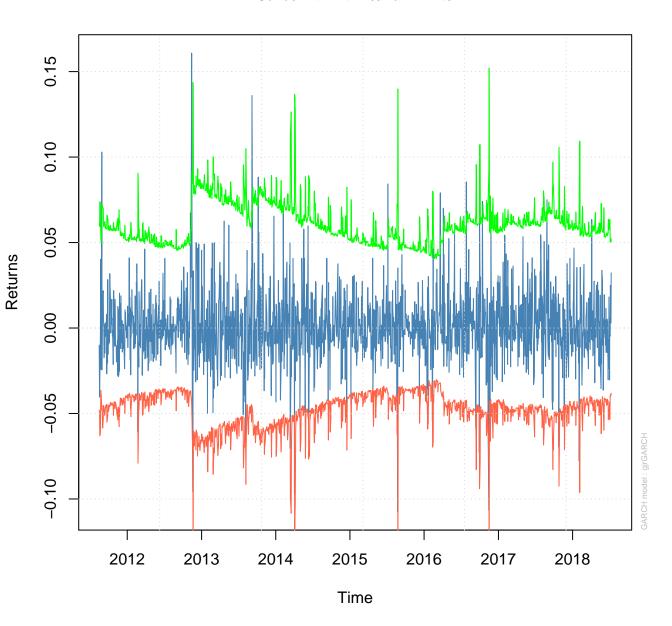
```
## ==============
## alpha:
                       1%
## Expected Exceed: 2.1
## Actual VaR Exceed:
## Actual %:
                       2.8%
## Unconditional Coverage (Kupiec)
## Null-Hypothesis: Correct Exceedances
## LR.uc Statistic: 4.834
## LR.uc Critical:
                       3.841
## LR.uc p-value:
                       0.028
## Reject Null:
                   YES
##
## Conditional Coverage (Christoffersen)
## Null-Hypothesis: Correct Exceedances and
                   Independence of Failures
## LR.cc Statistic: 5.187
## LR.cc Critical:
                       5.991
## LR.cc p-value:
                       0.075
## Reject Null:
                   NO
forecast<- ugarchforecast(my_model_LT,data=ret_LT,out.sample = 500,n.ahead =100,n.roll = 100)</pre>
```

##

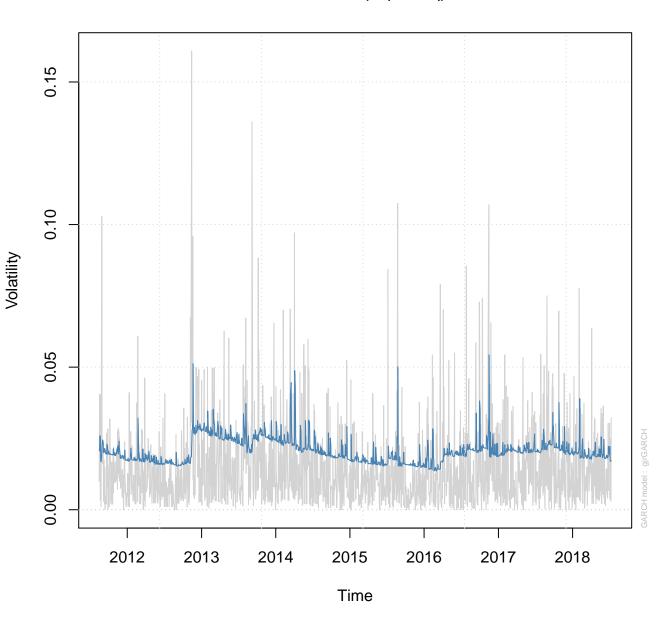
Series with 2 Conditional SD Superimposed



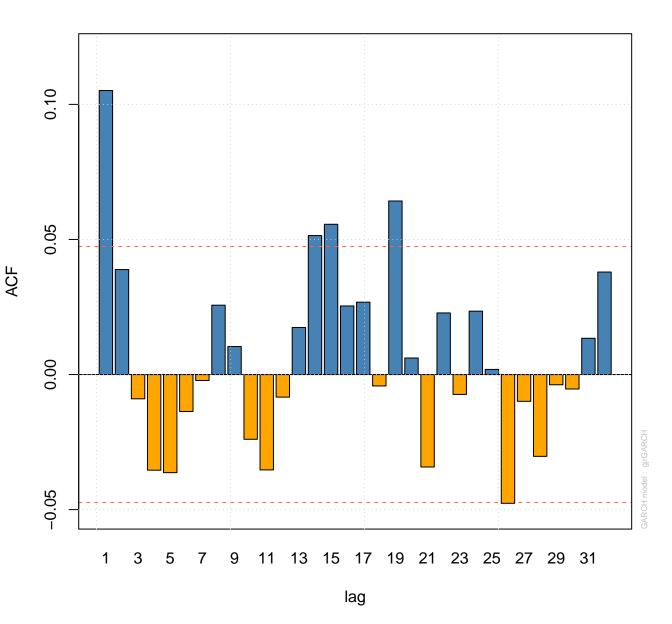
Series with with 1% VaR Limits



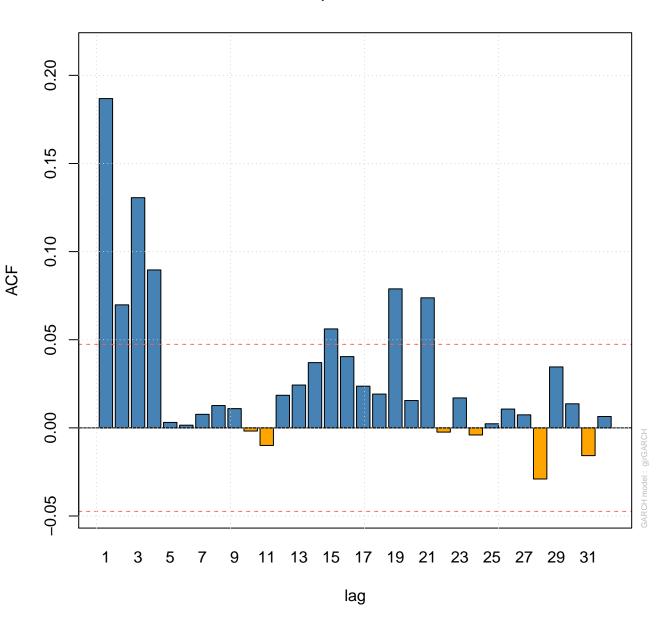
Conditional SD (vs |returns|)



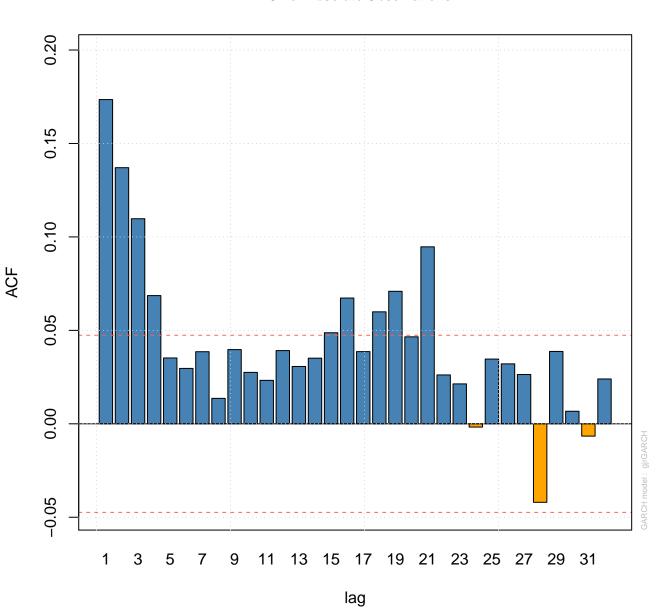
ACF of Observations



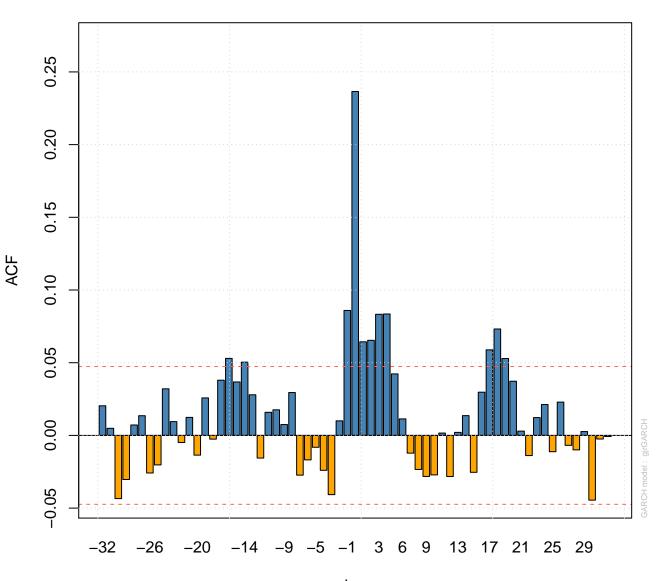
ACF of Squared Observations



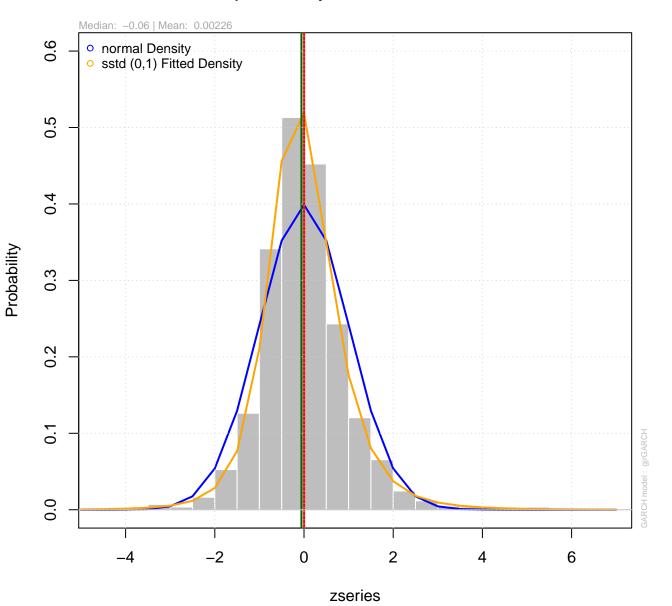
ACF of Absolute Observations



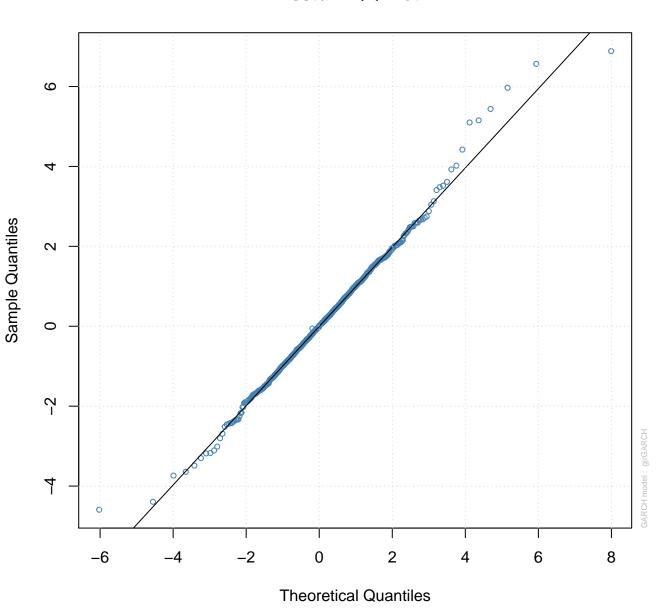
Cross-Correlations of Squared vs Actual Observations



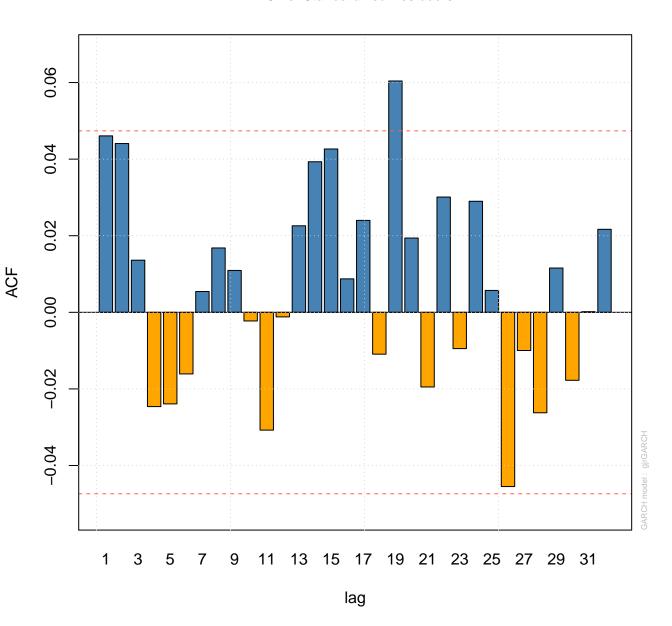
Empirical Density of Standardized Residuals



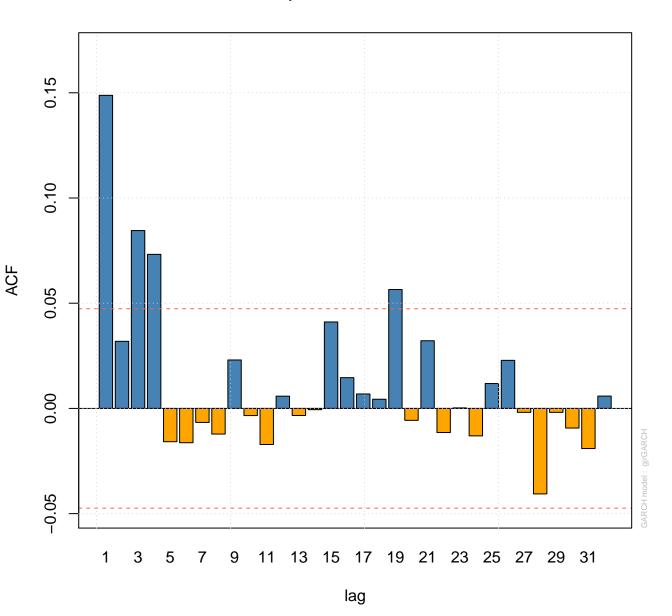
sstd - QQ Plot



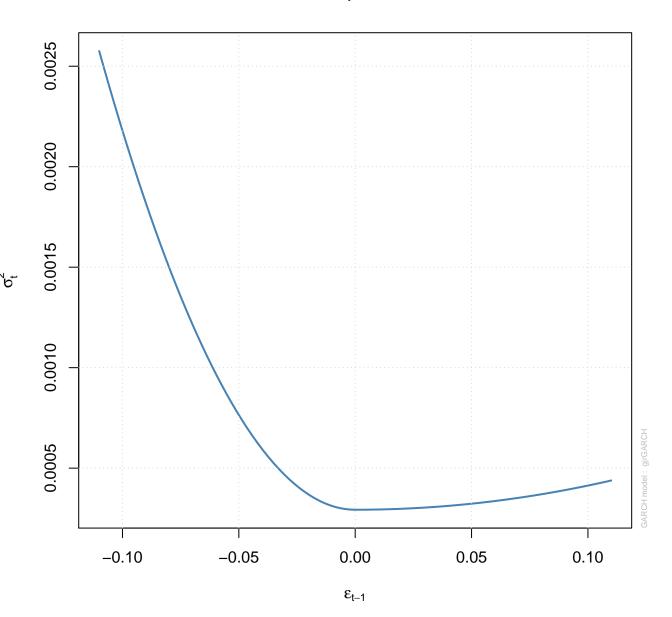
ACF of Standardized Residuals



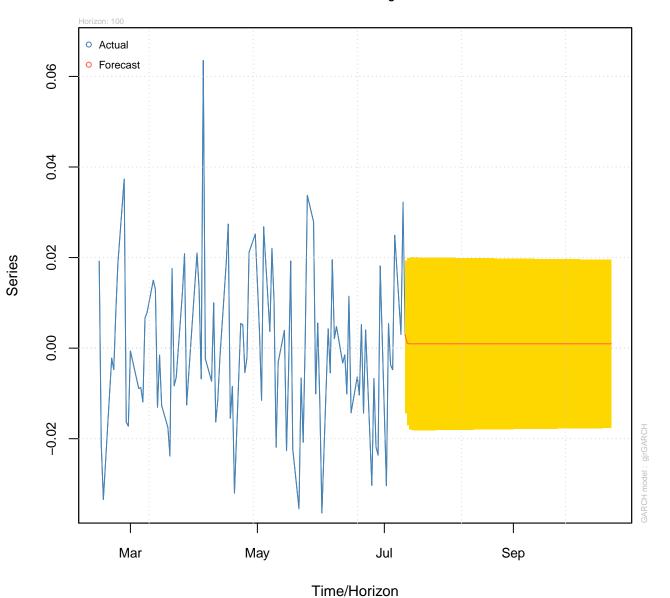
ACF of Squared Standardized Residuals



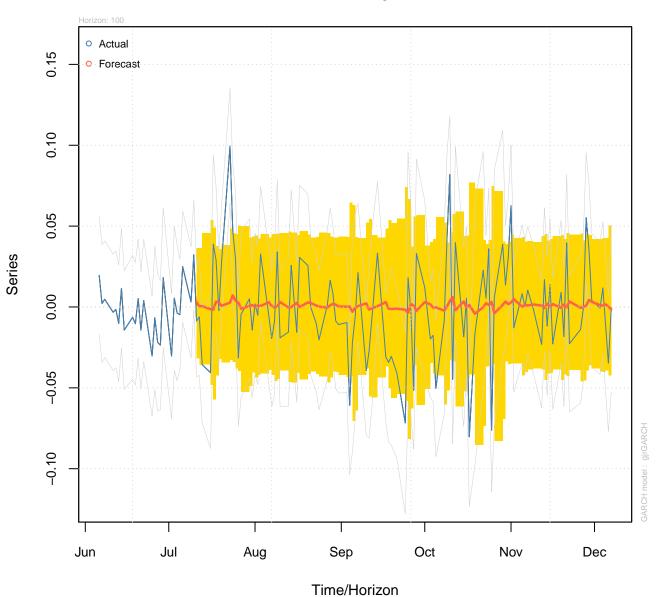
News Impact Curve



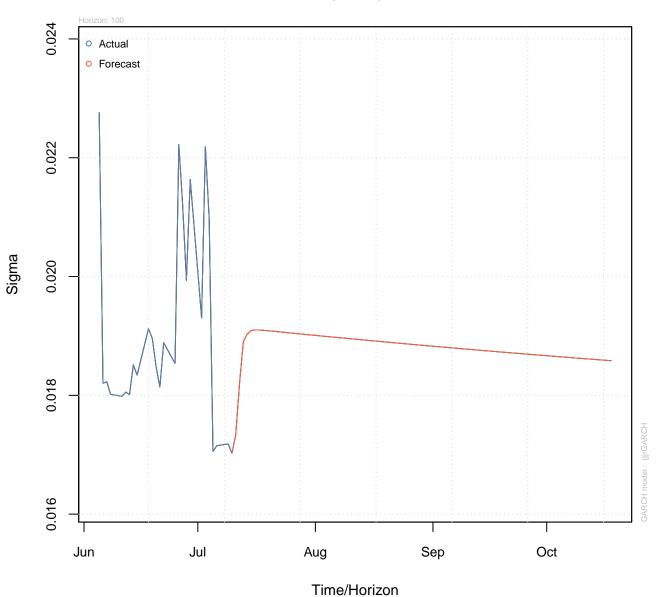
Forecast Series w/th unconditional 1-Sigma bands



Rolling Forecast vs Actual Series w/th conditional 2-Sigma bands



Forecast Unconditional Sigma (n.roll = 0)



Forecast Rolling Sigma vs |Series|

