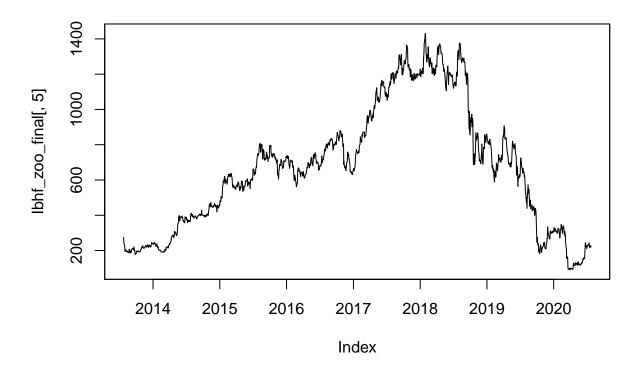
Untitled

me

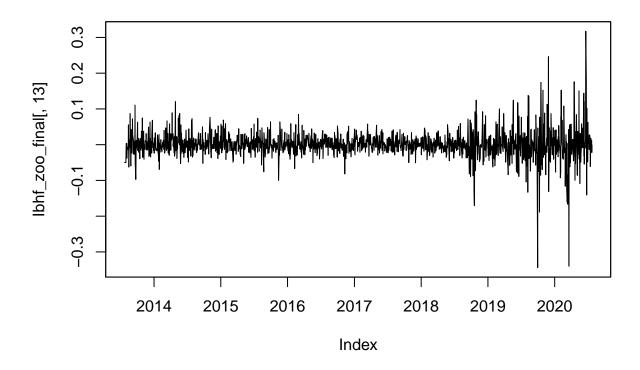
7/26/2020

```
5+5
## [1] 10
library(zoo)
##
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
##
##
       as.Date, as.Date.numeric
library(tseries)
## Warning: package 'tseries' was built under R version 4.0.2
## Registered S3 method overwritten by 'quantmod':
    method
     as.zoo.data.frame zoo
library(FinTS)
## Warning: package 'FinTS' was built under R version 4.0.2
library(rugarch)
## Warning: package 'rugarch' was built under R version 4.0.2
## Loading required package: parallel
##
## Attaching package: 'rugarch'
## The following object is masked from 'package:stats':
##
##
       sigma
```



there is a trend in the closing price hence i am taking the differnce and considering the log return.

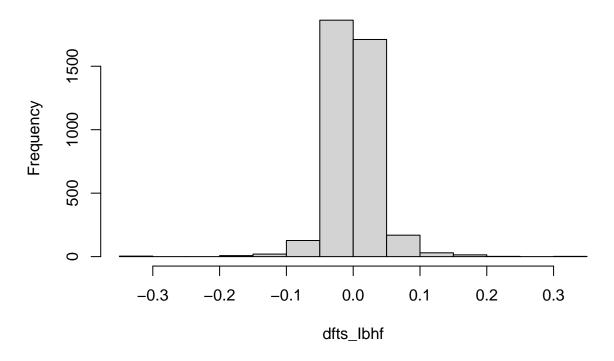
plot(Ibhf_zoo_final[,13])



the return series seems to be constant at mean zero and volatility clustering is visible in graph

```
ret_Ibhf<-Ibhf_zoo_final[-1,13]
dfts_Ibhf<- ts(ret_Ibhf,start=c(2010,1),end=c(2020,300),frequency = 365)
hist(dfts_Ibhf)</pre>
```

Histogram of dfts_lbhf



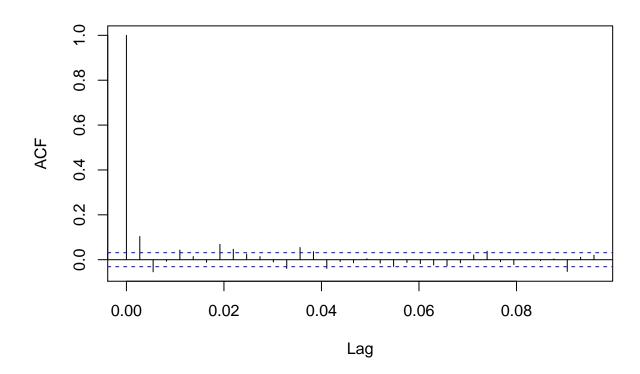
the return appears to be noormally distributed.

```
shapiro.test(dfts_Ibhf)
##
    Shapiro-Wilk normality test
##
## data: dfts_Ibhf
## W = 0.85063, p-value < 2.2e-16
the series is staionary.
mean(dfts_Ibhf)
## [1] 0.000748546
adf.test(ret_Ibhf)
## Warning in adf.test(ret_Ibhf): p-value smaller than printed p-value
##
    Augmented Dickey-Fuller Test
##
## data: ret_Ibhf
## Dickey-Fuller = -11.61, Lag order = 11, p-value = 0.01
## alternative hypothesis: stationary
```

since p value is smaller than 0.05 hence we are rejecting the null hypothesis hence the series is stationary. also the series is normal around mean 0.

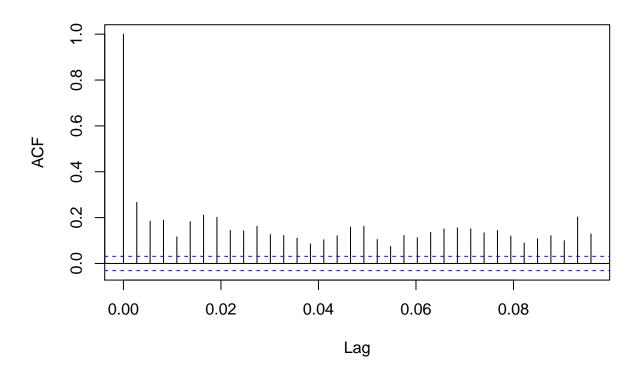
acf(dfts_Ibhf)

Series dfts_lbhf



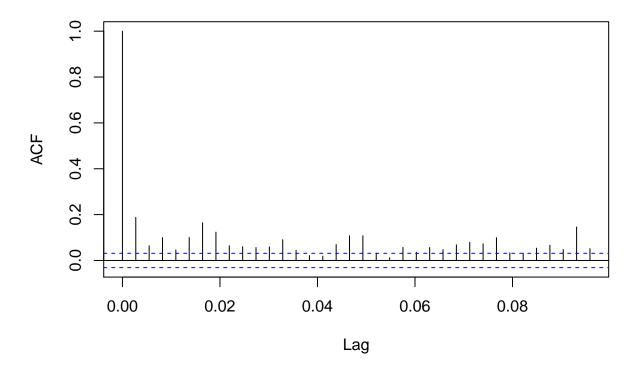
acf(abs(dfts_Ibhf))

Series abs(dfts_lbhf)



acf(dfts_Ibhf^2)

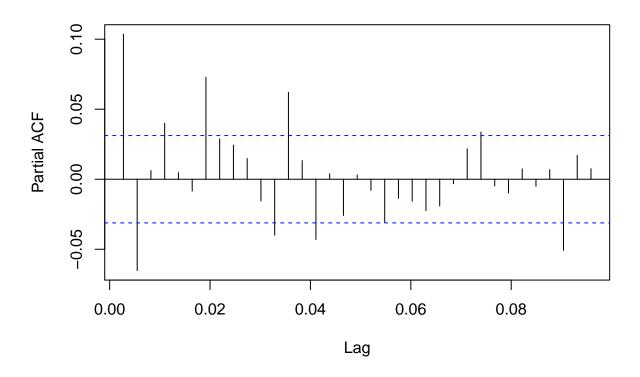
Series dfts_lbhf^2



by acf function of return we can say there is no auto correlation and there will be no need of MA model also by looking at the acf of absolute return we can say that the large return are followed by large returns regardless of sign MA(2) may be

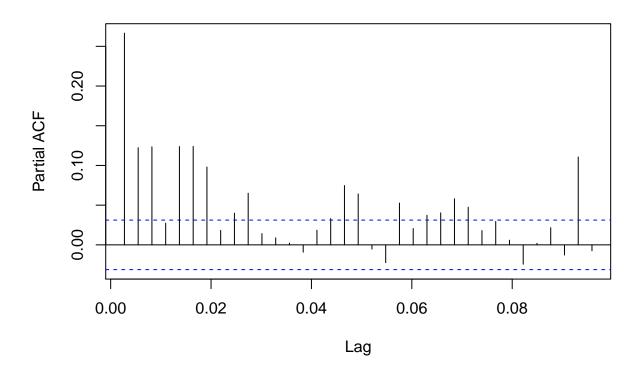
pacf(dfts_Ibhf)

Series dfts_lbhf



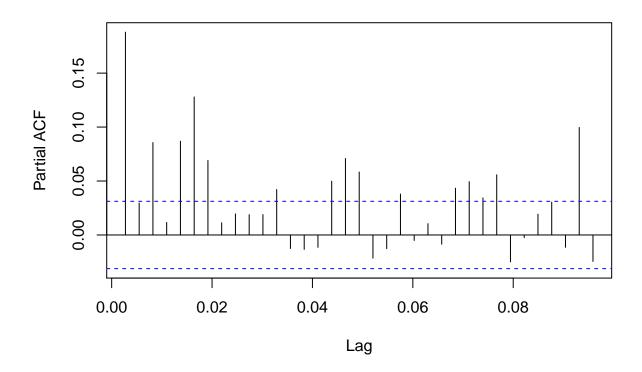
pacf(abs(dfts_Ibhf))

Series abs(dfts_lbhf)



pacf(dfts_Ibhf^2)

Series dfts_lbhf^2



there seems to be no need of any AR model to predict the log return series. AR(2)

```
Box.test(ret_Ibhf^2,lag=12,type="Ljung")

##
## Box-Ljung test
##
## data: ret_Ibhf^2
## X-squared = 323.19, df = 12, p-value < 2.2e-16

ArchTest(ret_Ibhf)

##
## ARCH LM-test; Null hypothesis: no ARCH effects
##
## data: ret_Ibhf
## Chi-squared = 125.67, df = 12, p-value < 2.2e-16</pre>
```

since p value is less than 0.05 we are rejecting the null hypothesis and thus we can say there is arch effect in the series.

```
arima001<-arima(ret_Ibhf,order = c(0,0,1))
AIC(arima001)</pre>
```

```
## [1] -6530.104
```

```
"arima001"
## [1] "arima001"
arima010 < -arima(ret_Ibhf, order = c(0,1,0))
AIC(arima010)
## [1] -5354.403
"arima010"
## [1] "arima010"
arima100 < -arima(ret_Ibhf, order = c(1,0,0))
AIC(arima100); "arima100"
## [1] -6530.003
## [1] "arima100"
arima101 < -arima(ret_Ibhf, order = c(1,0,1))
AIC(arima101); "arima101"
## [1] -6534.22
## [1] "arima101"
arima110<-arima(ret_Ibhf,order = c(1,1,0))</pre>
AIC(arima110); "arima110"
## [1] -5819.849
## [1] "arima110"
arima011<-arima(ret_Ibhf,order = c(0,1,1))</pre>
AIC(arima011); "arima011"
## [1] -6517.821
## [1] "arima011"
arima111<-arima(ret_Ibhf,order = c(1,1,1))</pre>
AIC(arima111); "arima111"
## [1] -6517.973
## [1] "arima111"
```

```
arima200 < -arima(ret_Ibhf, order = c(2,0,0))
AIC(arima200); "arima200"
## [1] -6528.452
## [1] "arima200"
arima210 < -arima(ret_Ibhf, order = c(2,1,0))
AIC(arima210); "arima210"
## [1] -6069.564
## [1] "arima210"
arima201 < -arima(ret_Ibhf, order = c(2,0,1))
AIC(arima201); "arima201"
## [1] -6534.478
## [1] "arima201"
arima211 < -arima(ret_Ibhf, order = c(2,1,1))
AIC(arima211); "arima211"
## [1] -6516.427
## [1] "arima211"
arima020 < -arima(ret_Ibhf, order = c(0,2,0))
AIC(arima020); "arima020"
## [1] -3112.169
## [1] "arima020"
arima120 < -arima(ret_Ibhf, order = c(1,2,0))
AIC(arima120); "arima120"
## [1] -4170.702
## [1] "arima120"
arima021 < -arima(ret_Ibhf, order = c(0,2,1))
AIC(arima021); "arima021"
## [1] -5340.191
## [1] "arima021"
```

```
arima121 < -arima(ret_Ibhf, order = c(1,2,1))
AIC(arima121); "arima121"
## [1] -5804.567
## [1] "arima121"
arima002 < -arima(ret_Ibhf, order = c(0,0,2))
AIC(arima002); "arima002"
## [1] -6529.362
## [1] "arima002"
arima102 < -arima(ret_Ibhf, order = c(1,0,2))
AIC(arima102); "arima102"
## [1] -6533.848
## [1] "arima102"
arima012 < -arima(ret_Ibhf, order = c(0,1,2))
AIC(arima012); "arima012"
## [1] -6518.08
## [1] "arima012"
arima112<-arima(ret_Ibhf,order = c(1,1,2))</pre>
AIC(arima112); "arima112"
## [1] -6522.213
## [1] "arima112"
arima222 < -arima(ret_Ibhf, order = c(2,2,2))
AIC(arima222); "arima222"
## [1] -6470.112
## [1] "arima222"
arima220 < -arima(ret_Ibhf, order = c(2,2,0))
AIC(arima220); "arima220"
## [1] -4739.029
## [1] "arima220"
```

```
arima202 < -arima(ret_Ibhf, order = c(2,0,2))
## Warning in arima(ret_Ibhf, order = c(2, 0, 2)): possible convergence problem:
## optim gave code = 1
AIC(arima202); "arima202"
## [1] -6533.011
## [1] "arima202"
arima022 < -arima(ret_Ibhf, order = c(0,2,2))
AIC(arima022); "arima022"
## [1] -6473.54
## [1] "arima022"
arima212 < -arima(ret_Ibhf, order = c(2,1,2))
AIC(arima212); "arima212"
## [1] -6522.415
## [1] "arima212"
ARIMA201<-ARIMA101<-ARIMA102 is the best choice since there was not any recomendation from acf
and pacf function we will ignore these model for now .
spec_of_garch_Ibhf<- ugarchspec(variance.model = list(garchOrder=c(1,0)),mean.model = list(armaOrder=c(2</pre>
my_model_Ibhf<-ugarchfit(spec=spec_of_garch_Ibhf,data=ret_Ibhf)</pre>
my_model_Ibhf
## *----*
            GARCH Model Fit
## *----*
##
## Conditional Variance Dynamics
## GARCH Model : sGARCH(1,0)
## Mean Model : ARFIMA(2,0,0)
## Distribution : norm
##
## Optimal Parameters
## -----
##
          Estimate Std. Error t value Pr(>|t|)
## mu
        0.051852 0.000013 4106.777
        -0.908190 0.000207 -4390.275
                                               0
## ar1
```

0

-0.657896 0.000228 -2887.384

ar2

```
## omega 0.000003 0.000000 16.589
## alpha1 0.969902 0.000248 3918.735
## Robust Standard Errors:
      Estimate Std. Error t value Pr(>|t|)
## mu
       0.051852 1.113817 0.046553 0.96287
## ar1 -0.908190 13.234454 -0.068623 0.94529
## ar2 -0.657896 27.239340 -0.024152 0.98073
## omega 0.000003 0.003241 0.000866 0.99931
## alpha1 0.969902 26.597721 0.036466 0.97091
## LogLikelihood : 572.2388
## Information Criteria
## -----
##
            -0.65729
## Akaike
## Bayes
            -0.64149
## Shibata
           -0.65730
## Hannan-Quinn -0.65144
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
                      statistic p-value
## Lag[1]
                         0.3014 0.58299
## Lag[2*(p+q)+(p+q)-1][5] 4.1406 0.04613
## Lag[4*(p+q)+(p+q)-1][9] 5.3982 0.36750
## d.o.f=2
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                      statistic p-value
                       0.003434 0.9533
## Lag[1]
## Lag[2*(p+q)+(p+q)-1][2] 0.008550 0.9910
## Lag[4*(p+q)+(p+q)-1][5] 0.018127 0.9999
## d.o.f=1
##
## Weighted ARCH LM Tests
## -----
           Statistic Shape Scale P-Value
## ARCH Lag[2] 0.01021 0.500 2.000 0.9195
## ARCH Lag[4] 0.01787 1.397 1.611 0.9985
## ARCH Lag[6] 0.01988 2.222 1.500 1.0000
## Nyblom stability test
## -----
## Joint Statistic: 1.6806
## Individual Statistics:
## mu
       0.0336
## ar1
        0.0336
## ar2 0.0336
## omega 0.0805
## alpha1 0.0336
```

```
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 1.28 1.47 1.88
## Individual Statistic:
                      0.35 0.47 0.75
## Sign Bias Test
## -----
                  t-value prob sig
## Sign Bias
                  0.3742 7.083e-01
## Negative Sign Bias 4.3736 1.295e-05 ***
## Positive Sign Bias 0.4795 6.317e-01
## Joint Effect 19.4867 2.168e-04 ***
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
   group statistic p-value(g-1)
## 1
      20 6003
## 2
      30
            6148
                          0
## 3 40 6309
## 4 50 6360
                          0
                          Ω
##
##
## Elapsed time : 0.9449871
spec_of_garch_Ibhf<- ugarchspec(variance.model = list(garchOrder=c(0,1)),mean.model = list(armaOrder=c(2</pre>
my_model_Ibhf<-ugarchfit(spec=spec_of_garch_Ibhf,data=ret_Ibhf)</pre>
my_model_Ibhf
##
          GARCH Model Fit
## *----*
## Conditional Variance Dynamics
## -----
## GARCH Model : sGARCH(0,1)
## Mean Model : ARFIMA(2,0,0)
## Distribution : norm
##
## Optimal Parameters
## -----
      Estimate Std. Error t value Pr(>|t|)
## mu
       0.000586 0.000896 0.6539 0.513174
## ar1 0.110229 0.024026 4.5880 0.000004
## ar2 -0.067512 0.024014 -2.8114 0.004933
## omega 0.000002 0.000000 62.2454 0.000000
## beta1 0.999000 0.000012 81262.7707 0.000000
```

Robust Standard Errors:

mu

Estimate Std. Error t value Pr(>|t|)

0.000586 0.000810 0.72389 0.469133

ar1 0.110229 0.032580 3.38334 0.000716 ## ar2 -0.067512 0.031253 -2.16015 0.030761

```
## omega 0.000002 0.000000 9.58574 0.000000
## beta1 0.999000 0.000129 7742.41689 0.000000
## LogLikelihood : 3295.311
## Information Criteria
## -----
## Akaike -3.8126
## Bayes -3.7968
## Shibata -3.8127
## Hannan-Quinn -3.8068
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
                        statistic p-value
## Lag[1]
                         0.005183 0.9426
## Lag[2*(p+q)+(p+q)-1][5] 1.228208 0.9998
## Lag[4*(p+q)+(p+q)-1][9] 5.849434 0.2819
## d.o.f=2
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                       statistic p-value
## Lag[1]
                         69.02 1.11e-16
## Lag[2*(p+q)+(p+q)-1][2] 72.94 0.00e+00
## Lag[4*(p+q)+(p+q)-1][5] 93.46 0.00e+00
## d.o.f=1
##
## Weighted ARCH LM Tests
## -----
            Statistic Shape Scale P-Value
## ARCH Lag[2] 7.826 0.500 2.000 5.150e-03
## ARCH Lag[4] 25.109 1.397 1.611 5.846e-07 
## ARCH Lag[6] 55.656 2.222 1.500 5.884e-15
##
## Nyblom stability test
## -----
## Joint Statistic: 91.011
## Individual Statistics:
## mu 0.23104
## ar1 0.01861
## ar2 0.05093
## omega 1.68055
## beta1 3.91347
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 1.28 1.47 1.88
## Individual Statistic: 0.35 0.47 0.75
##
## Sign Bias Test
## -----
                   t-value prob sig
##
```

```
## Sign Bias
                    1.309 1.906e-01
## Negative Sign Bias 8.936 1.015e-18 ***
## Positive Sign Bias 5.254 1.670e-07 ***
## Joint Effect
               107.465 3.854e-23 ***
##
## Adjusted Pearson Goodness-of-Fit Test:
    group statistic p-value(g-1)
## 1
      20 473.6 1.881e-88
## 2
      30
             504.1
                    4.104e-88
## 3
      40
            530.4
                    1.809e-87
## 4
      50
             530.8
                    4.290e-82
##
##
## Elapsed time : 0.5749929
spec_of_garch_Ibhf<- ugarchspec(variance.model = list(garchOrder=c(1,1)),mean.model = list(armaOrder=c(2,1))</pre>
my_model_Ibhf<-ugarchfit(spec=spec_of_garch_Ibhf,data=ret_Ibhf)</pre>
my_model_Ibhf
##
## *----*
          GARCH Model Fit
##
## Conditional Variance Dynamics
## -----
## GARCH Model : sGARCH(1,1)
## Mean Model : ARFIMA(2,0,0)
## Distribution : norm
## Optimal Parameters
## -----
##
         Estimate Std. Error t value Pr(>|t|)
## mu
       0.001464 0.000638 2.2932 0.021835
       ## ar1
## ar2 -0.059922 0.025063 -2.3909 0.016808
## omega 0.000003 0.000002 1.3372 0.181154
## alpha1 0.038525 0.004036 9.5451 0.000000
## beta1 0.960475 0.003967 242.1159 0.000000
## Robust Standard Errors:
         Estimate Std. Error t value Pr(>|t|)
## mu
         0.001464 0.000614 2.38389 0.017131
         0.128655
                   0.022901 5.61792 0.000000
## ar1
## ar2
        -0.059922
                  0.024237 -2.47237 0.013422
## omega 0.000003 0.000005
                            0.54413 0.586350
## alpha1 0.038525
                    0.006450 5.97315 0.000000
                  0.006617 145.14962 0.000000
## beta1
         0.960475
##
## LogLikelihood: 3668.325
## Information Criteria
```

```
##
## Akaike
            -4.2437
## Bayes
            -4.2248
## Shibata
            -4.2437
## Hannan-Quinn -4.2367
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
                       statistic p-value
## Lag[1]
                       0.0003936 0.9842
## Lag[2*(p+q)+(p+q)-1][5] 0.4976853 1.0000
## Lag[4*(p+q)+(p+q)-1][9] 2.6103883 0.9407
## d.o.f=2
## HO : No serial correlation
##
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                      statistic p-value
## Lag[1]
                         4.770 0.02895
## Lag[2*(p+q)+(p+q)-1][5] 5.348 0.12755
## Lag[4*(p+q)+(p+q)-1][9] 8.011 0.12825
## d.o.f=2
## Weighted ARCH LM Tests
## -----
            Statistic Shape Scale P-Value
## ARCH Lag[3] 0.01699 0.500 2.000 0.8963
## ARCH Lag[5] 1.51686 1.440 1.667 0.5879
## ARCH Lag[7] 3.79340 2.315 1.543 0.3773
## Nyblom stability test
## -----
## Joint Statistic: 8.4195
## Individual Statistics:
## mu
       0.09759
## ar1
      0.07617
## ar2 0.03520
## omega 3.15249
## alpha1 0.31160
## beta1 0.21569
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 1.49 1.68 2.12
## Individual Statistic: 0.35 0.47 0.75
##
## Sign Bias Test
## -----
                  t-value prob sig
##
                   1.7253 8.465e-02
## Sign Bias
## Negative Sign Bias 4.2314 2.445e-05 ***
## Positive Sign Bias 0.5506 5.820e-01
## Joint Effect 18.2476 3.910e-04 ***
##
```

```
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
## group statistic p-value(g-1)
## 1 20 132.5 4.962e-19
## 2 30 163.8 9.456e-21
## 3 40 154.1 1.313e-15
## 4 50 177.8 1.649e-16
##
##
## Elapsed time : 0.4490039
spec_of_garch_Ibhf<- ugarchspec(variance.model = list(garchOrder=c(2,0)),mean.model = list(armaOrder=c(2,0))</pre>
my_model_Ibhf<-ugarchfit(spec=spec_of_garch_Ibhf,data=ret_Ibhf)</pre>
my model Ibhf
## *----*
      GARCH Model Fit *
## *----*
## Conditional Variance Dynamics
## -----
## GARCH Model : sGARCH(2,0)
## Mean Model : ARFIMA(2,0,0)
## Distribution : norm
## Optimal Parameters
         Estimate Std. Error t value Pr(>|t|)
## mu
       0.000099 0.000728 0.13621 0.891654
        0.132040 0.033024 3.99825 0.000064
## ar1
## ar2 -0.077868 0.027470 -2.83465 0.004588
## omega 0.000587 0.000038 15.50221 0.000000
## alpha1 0.535597 0.076161 7.03247 0.000000
## alpha2 0.182075 0.034032 5.35003 0.000000
##
## Robust Standard Errors:
        Estimate Std. Error t value Pr(>|t|)
       0.000099 0.001178 0.084194 0.932903
## mu
## ar1 0.132040 0.040042 3.297513 0.000975
## ar2 -0.077868 0.047532 -1.638218 0.101376
## omega 0.000587 0.000112 5.250831 0.000000 ## alpha1 0.535597 0.222083 2.411701 0.015878
## alpha2 0.182075 0.058915 3.090464 0.001998
## LogLikelihood: 3485.264
## Information Criteria
## -----
## Akaike
            -4.0316
## Bayes
            -4.0126
## Shibata
```

-4.0316

```
## Hannan-Quinn -4.0246
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
                     statistic p-value
## Lag[1]
                       0.1309 0.7175
## Lag[2*(p+q)+(p+q)-1][5] 0.4526 1.0000
## Lag[4*(p+q)+(p+q)-1][9] 3.2659 0.8463
## d.o.f=2
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
          statistic p-value
##
## Lag[1]
                       0.2836 0.5944
## Lag[2*(p+q)+(p+q)-1][5] 1.4943 0.7413
## Lag[4*(p+q)+(p+q)-1][9] 8.1743 0.1191
## d.o.f=2
## Weighted ARCH LM Tests
## -----
    Statistic Shape Scale P-Value
## ARCH Lag[3] 0.8537 0.500 2.000 0.3555
## ARCH Lag[5] 1.9992 1.440 1.667 0.4714
## ARCH Lag[7] 6.2146 2.315 1.543 0.1274
## Nyblom stability test
## -----
## Joint Statistic: 4.4081
## Individual Statistics:
## mu
       0.5044
## ar1
      0.2630
## ar2 0.0955
## omega 2.3134
## alpha1 1.8973
## alpha2 2.1244
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 1.49 1.68 2.12
## Individual Statistic: 0.35 0.47 0.75
## Sign Bias Test
## -----
##
                t-value prob sig
## Sign Bias
                 1.4180 0.1564
## Negative Sign Bias 0.4517 0.6516
## Positive Sign Bias 1.0782 0.2811
## Joint Effect 2.2465 0.5228
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
## group statistic p-value(g-1)
## 1 20 218.6 6.683e-36
```

```
30 231.2 2.202e-33
40 245.1 1.103e-31
## 2
## 3
## 4
      50 264.3 2.773e-31
##
## Elapsed time : 0.9519989
spec_of_garch_Ibhf<- ugarchspec(variance.model = list(garchOrder=c(0,2)),mean.model = list(armaOrder=c(2))</pre>
my_model_Ibhf<-ugarchfit(spec=spec_of_garch_Ibhf,data=ret_Ibhf)</pre>
my_model_Ibhf
##
## *----*
          GARCH Model Fit *
## *----*
##
## Conditional Variance Dynamics
## -----
## GARCH Model : sGARCH(0,2)
## Mean Model : ARFIMA(2,0,0)
## Distribution : norm
##
## Optimal Parameters
## -----
        Estimate Std. Error t value Pr(>|t|)
      0.000587 0.000891 6.5898e-01 0.509909
## mu
      ## ar1
## ar2 -0.067279 0.024016 -2.8014e+00 0.005089
## omega 0.000002 0.000000 1.0094e+02 0.000000
## beta1 0.000000 0.000098 1.1660e-03 0.999069
## beta2 0.999000 0.000009 1.1341e+05 0.000000
## Robust Standard Errors:
      Estimate Std. Error t value Pr(>|t|)
      0.000587 0.000766 7.6606e-01 0.443641 0.110027 0.031048 3.5437e+00 0.000394
## mu
## ar1
## ar2 -0.067279 0.029921 -2.2486e+00 0.024541
## omega 0.000002 0.000000 2.2070e+01 0.000000
## beta1 0.000000 0.000390 2.9300e-04 0.999766
## beta2 0.999000 0.000041 2.4411e+04 0.000000
##
## LogLikelihood: 3302.52
##
## Information Criteria
## -----
## Akaike
            -3.8198
## Bayes
            -3.8009
## Shibata -3.8199
## Hannan-Quinn -3.8128
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
                       statistic p-value
```

```
0.006226 0.9371
## Lag[1]
## Lag[2*(p+q)+(p+q)-1][5] 1.175991 0.9999
## Lag[4*(p+q)+(p+q)-1][9] 5.655275 0.3170
## d.o.f=2
## HO : No serial correlation
##
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                      statistic p-value
                        68.24 1.11e-16
## Lag[1]
## Lag[2*(p+q)+(p+q)-1][5]
                          92.18 0.00e+00
## Lag[4*(p+q)+(p+q)-1][9] 141.12 0.00e+00
## d.o.f=2
##
## Weighted ARCH LM Tests
## -----
      Statistic Shape Scale P-Value
##
## ARCH Lag[3] 18.12 0.500 2.000 2.073e-05
## ARCH Lag[5] 35.98 1.440 1.667 1.872e-09
## ARCH Lag[7] 81.28 2.315 1.543 0.000e+00
##
## Nyblom stability test
## -----
## Joint Statistic: 217.2647
## Individual Statistics:
## mu
     0.24131
## ar1 0.01851
## ar2 0.05280
## omega 5.02034
## beta1 3.49068
## beta2 3.49036
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 1.49 1.68 2.12
## Individual Statistic: 0.35 0.47 0.75
## Sign Bias Test
## -----
## t-value prob sig
## Sign Bias 1.318 1.878e-01
## Negative Sign Bias 8.933 1.043e-18 ***
## Positive Sign Bias 5.236 1.840e-07 ***
## Joint Effect 107.219 4.352e-23 ***
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
## group statistic p-value(g-1)
## 1 20 488.6 1.405e-91
## 2 30 519.0 3.567e-91
## 3 40 540.2 1.865e-89
## 4 50 549.7 7.699e-86
##
##
```

```
## Elapsed time : 0.7850039
spec_of_garch_Ibhf<- ugarchspec(variance.model = list(garchOrder=c(2,2)),mean.model =list(armaOrder=c(2,2))</pre>
my_model_Ibhf<-ugarchfit(spec=spec_of_garch_Ibhf,data=ret_Ibhf)</pre>
my_model_Ibhf
##
           GARCH Model Fit
## Conditional Variance Dynamics
## -----
## GARCH Model : sGARCH(2,2)
## Mean Model : ARFIMA(2,0,0)
## Distribution : norm
## Optimal Parameters
        Estimate Std. Error t value Pr(>|t|)
        ## mu
## ar1 0.130690 0.025658 5.093581 0.000000
## ar2 -0.057840 0.023850 -2.425148 0.015302
## omega 0.000005 0.000005 0.926337 0.354271  
## alpha1 0.074790 0.015770 4.742433 0.000002
## alpha2 0.000000 0.014027 0.000004 0.999996
## beta1 0.064199 0.037909 1.693474 0.090365
          ## beta2
##
## Robust Standard Errors:
##
       Estimate Std. Error t value Pr(>|t|)
        0.001529 0.000633 2.414582 0.015753
## mu
## ar1 0.130690 0.022405 5.833194 0.000000
## ar2 -0.057840 0.025054 -2.308627 0.020964
## omega 0.000005 0.000017 0.286172 0.774746
## alpha1 0.074790 0.033820 2.211418 0.027007
## alpha2 0.000000 0.023448 0.000003 0.999998
## beta1 0.064199 0.055488 1.156987 0.247278
## beta2  0.860012  0.036503 23.560014 0.000000
## LogLikelihood : 3676.309
##
## Information Criteria
##
## Akaike
             -4.2506
## Bayes
              -4.2254
              -4.2507
## Shibata
## Hannan-Quinn -4.2413
## Weighted Ljung-Box Test on Standardized Residuals
## -----
                        statistic p-value
```

0.00147 0.9694

Lag[1]

```
## Lag[2*(p+q)+(p+q)-1][5] 0.40511 1.0000
## Lag[4*(p+q)+(p+q)-1][9] 2.75905 0.9238
## d.o.f=2
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                        statistic p-value
## Lag[1]
                          1.741 0.1870
## Lag[2*(p+q)+(p+q)-1][11]
                          7.842 0.2299
## Lag[4*(p+q)+(p+q)-1][19] 10.595 0.3894
## d.o.f=4
## Weighted ARCH LM Tests
   Statistic Shape Scale P-Value
## ARCH Lag[5] 1.101 0.500 2.000 0.29402
               8.474 1.473 1.746 0.02025
## ARCH Lag[7]
## ARCH Lag[9] 9.212 2.402 1.619 0.03927
## Nyblom stability test
## -----
## Joint Statistic: 1.9918
## Individual Statistics:
## mu
       0.09025
## ar1
        0.05767
## ar2 0.02572
## omega 0.59493
## alpha1 0.36050
## alpha2 0.45380
## beta1 0.29134
## beta2 0.25725
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 1.89 2.11 2.59
## Individual Statistic: 0.35 0.47 0.75
##
## Sign Bias Test
## -----
##
                   t-value
                             prob sig
                  1.52911 0.126420
## Sign Bias
## Negative Sign Bias 3.40781 0.000670 ***
## Positive Sign Bias 0.05022 0.959955
## Joint Effect 11.62663 0.008778 ***
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
   group statistic p-value(g-1)
## 1 20 125.7 9.437e-18
## 2 30 144.9 2.331e-17
## 3 40 160.3 1.208e-16
## 4 50 168.6 4.922e-15
##
```

```
##
## Elapsed time : 1.050993
spec_of_garch_Ibhf<- ugarchspec(variance.model = list(garchOrder=c(1,2)),mean.model = list(armaOrder=c(2</pre>
my_model_Ibhf<-ugarchfit(spec=spec_of_garch_Ibhf,data=ret_Ibhf)</pre>
my_model_Ibhf
       GARCH Model Fit *
## *----*
##
## Conditional Variance Dynamics
## -----
## GARCH Model : sGARCH(1,2)
## Mean Model : ARFIMA(2,0,0)
## Distribution : norm
##
## Optimal Parameters
## -----
        Estimate Std. Error t value Pr(>|t|)
       0.001529 0.000636 2.40298 0.016262
## ar1
       ## ar2 -0.057841 0.023758 -2.43454 0.014911
## omega 0.000005 0.000005 0.98359 0.325315
## alpha1 0.074788 0.014741 5.07350 0.000000
## beta1 0.064183 0.028573 2.24626 0.024687
         ## beta2
##
## Robust Standard Errors:
##
       Estimate Std. Error t value Pr(>|t|)
       0.001529 0.000631 2.42338 0.015377
## mu
## ar1 0.130689 0.022372 5.84152 0.000000
## ar2 -0.057841 0.024025 -2.40758 0.016059
## omega 0.000005 0.000015 0.32937 0.741879
## alpha1 0.074788 0.040127 1.86380 0.062349
## beta1 0.064183 0.037406 1.71585 0.086190
## beta2 0.860028 0.050400 17.06403 0.000000
##
## LogLikelihood: 3676.309
## Information Criteria
## -----
##
## Akaike
            -4.2518
## Bayes
            -4.2297
## Shibata
             -4.2518
## Hannan-Quinn -4.2436
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
                      statistic p-value
                      0.001467 0.9695
## Lag[1]
## Lag[2*(p+q)+(p+q)-1][5] 0.405103 1.0000
```

```
## Lag[4*(p+q)+(p+q)-1][9] 2.759070 0.9238
## d.o.f=2
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                      statistic p-value
                          1.741 0.1870
## Lag[1]
## Lag[2*(p+q)+(p+q)-1][8] 5.921 0.2431
## Lag[4*(p+q)+(p+q)-1][14] 9.079 0.2738
## d.o.f=3
## Weighted ARCH LM Tests
## -----
    Statistic Shape Scale P-Value
## ARCH Lag[4] 0.05479 0.500 2.000 0.81494
## ARCH Lag[6] 6.60905 1.461 1.711 0.04898
## ARCH Lag[8] 7.81084 2.368 1.583 0.06813
## Nyblom stability test
## -----
## Joint Statistic: 1.941
## Individual Statistics:
## mu
       0.09022
## ar1 0.05766
## ar2 0.02572
## omega 0.59496
## alpha1 0.36048
## beta1 0.29134
## beta2 0.25725
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 1.69 1.9 2.35
## Individual Statistic: 0.35 0.47 0.75
## Sign Bias Test
## -----
##
                  t-value prob sig
            1.52910 0.1264239
## Sign Bias
## Negative Sign Bias 3.40783 0.0006699 ***
## Positive Sign Bias 0.05027 0.9599146
## Joint Effect 11.62681 0.0087773 ***
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
##
   group statistic p-value(g-1)
## 1 20 125.7 9.437e-18
## 2 30 144.9 2.331e-17
## 3 40 160.3 1.208e-16
## 4 50 168.6 4.922e-15
##
##
## Elapsed time : 0.733999
```

```
spec_of_garch_Ibhf<- ugarchspec(variance.model = list(garchOrder=c(2,1)),mean.model =list(armaOrder=c(2
my_model_Ibhf<-ugarchfit(spec=spec_of_garch_Ibhf,data=ret_Ibhf)
my_model_Ibhf</pre>
```

```
##
     GARCH Model Fit
## Conditional Variance Dynamics
## -----
## GARCH Model : sGARCH(2,1)
## Mean Model : ARFIMA(2,0,0)
## Distribution : norm
##
## Optimal Parameters
## -----
          Estimate Std. Error t value Pr(>|t|)
        0.001464 0.000639 2.2921 0.021902
## mu
## ar1 0.128655 0.024964 5.1537 0.000000
## ar2 -0.059924 0.025063 -2.3909 0.016807
## omega 0.000003 0.000002 1.3335 0.182353
## alpha1 0.038525 0.017125 2.2497 0.024470
## alpha2 0.000000 0.018250 0.0000 1.000000
## beta1 0.960474 0.004143 231.8220 0.000000
## Robust Standard Errors:
      Estimate Std. Error t value Pr(>|t|)

      0.001464
      0.000617
      2.37139
      0.017721

      0.128655
      0.022872
      5.62493
      0.000000

## mu
## ar1
## ar2 -0.059924 0.024235 -2.47265 0.013412
## omega 0.000003 0.000005 0.54047 0.588872
## alpha1 0.038525 0.019528 1.97283 0.048515
## alpha2 0.000000 0.019433 0.00000 1.000000
## beta1 0.960474 0.006722 142.89428 0.000000
##
## LogLikelihood : 3668.325
##
## Information Criteria
## Akaike
              -4.2426
## Bayes
              -4.2204
## Shibata
             -4.2426
## Hannan-Quinn -4.2344
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
                          statistic p-value
## Lag[1]
                          0.0003934 0.9842
## Lag[2*(p+q)+(p+q)-1][5] 0.4976742 1.0000
## Lag[4*(p+q)+(p+q)-1][9] 2.6103753 0.9407
## d.o.f=2
```

```
## HO : No serial correlation
##
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
                        statistic p-value
## Lag[1]
                            4.770 0.02895
## Lag[2*(p+q)+(p+q)-1][8] 7.516 0.11917
## Lag[4*(p+q)+(p+q)-1][14] 9.771 0.21617
## d.o.f=3
##
## Weighted ARCH LM Tests
## -----
    Statistic Shape Scale P-Value
## ARCH Lag[4] 0.05668 0.500 2.000 0.8118
## ARCH Lag[6] 4.13479 1.461 1.711 0.1760
## ARCH Lag[8] 5.29945 2.368 1.583 0.2186
##
## Nyblom stability test
## -----
## Joint Statistic: 10.5076
## Individual Statistics:
## mu
       0.09760
## ar1 0.07617
## ar2 0.03520
## omega 3.15250
## alpha1 0.31160
## alpha2 0.36434
## beta1 0.21570
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 1.69 1.9 2.35 ## Individual Statistic: 0.35 0.47 0.75
## Sign Bias Test
## -----
                  t-value prob sig
              1.7253 8.465e-02 *
## Sign Bias
## Negative Sign Bias 4.2314 2.445e-05 ***
## Positive Sign Bias 0.5506 5.820e-01
## Joint Effect 18.2476 3.910e-04 ***
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
## group statistic p-value(g-1)
## 1 20 132.5
                     4.962e-19
## 2 30 163.8 9.456e-21
## 3 40 154.1 1.313e-15
## 4 50 177.8 1.649e-16
##
## Elapsed time : 0.707999
```

```
spec_of_garch_Ibhf<- ugarchspec(variance.model = list(garchOrder=c(0,1)),mean.model =list(armaOrder=c(2
my_model_Ibhf<-ugarchfit(spec=spec_of_garch_Ibhf,data=ret_Ibhf)
my_model_Ibhf</pre>
```

```
##
          GARCH Model Fit
## Conditional Variance Dynamics
## -----
## GARCH Model : sGARCH(0,1)
## Mean Model : ARFIMA(2,0,0)
## Distribution : sstd
##
## Optimal Parameters
## -----
       Estimate Std. Error t value Pr(>|t|) 0.000760 0.000787 0.96572 0.334183
## mu
## ar1 0.037882 0.020875 1.81475 0.069563
## ar2 -0.061884 0.020616 -3.00168 0.002685
## omega 0.000003 0.000000 24.79209 0.000000
## beta1 0.999000 0.000023 43526.56745 0.000000
## skew 1.068887 0.032866 32.52297 0.000000
## shape 2.419737 0.032367 74.76004 0.000000
## Robust Standard Errors:
     Estimate Std. Error t value Pr(>|t|)
       0.000760 0.000881 0.86294 0.38817
## mu
## ar1
      0.037882 0.025619 1.47867 0.13923
## ar2 -0.061884 0.027627 -2.24001 0.02509
## omega 0.000003 0.000000 16.83959 0.00000
## beta1 0.999000 0.000101 9881.14250 0.00000
## skew 1.068887 0.038390 27.84317 0.00000
## shape 2.419737 0.033012 73.29969 0.00000
##
## LogLikelihood : 3667.818
##
## Information Criteria
## Akaike
             -4.2420
## Bayes
            -4.2198
            -4.2420
## Shibata
## Hannan-Quinn -4.2338
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
                      statistic
                                  p-value
## Lag[1]
                         9.396 2.174e-03
## Lag[2*(p+q)+(p+q)-1][5] 10.530 1.799e-14
## Lag[4*(p+q)+(p+q)-1][9] 14.777 4.959e-05
## d.o.f=2
```

```
## HO : No serial correlation
##
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
                      statistic p-value
## Lag[1]
                         59.09 1.51e-14
## Lag[2*(p+q)+(p+q)-1][2] 62.48 0.00e+00
## Lag[4*(p+q)+(p+q)-1][5] 79.11 0.00e+00
## d.o.f=1
##
## Weighted ARCH LM Tests
## -----
    Statistic Shape Scale P-Value
## ARCH Lag[2] 6.751 0.500 2.000 9.367e-03
## ARCH Lag[4] 20.431 1.397 1.611 9.882e-06
## ARCH Lag[6] 46.568 2.222 1.500 2.042e-12
##
## Nyblom stability test
## -----
## Joint Statistic: 36.3398
## Individual Statistics:
## mu
     0.2432
## ar1 0.4119
## ar2 0.2960
## omega 7.0333
## beta1 6.9445
## skew 0.2794
## shape 4.5879
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 1.69 1.9 2.35 ## Individual Statistic: 0.35 0.47 0.75
## Sign Bias Test
## -----
                 t-value prob sig
              1.037 2.998e-01
## Sign Bias
## Negative Sign Bias 8.416 8.061e-17 ***
## Positive Sign Bias 5.190 2.357e-07 ***
## Joint Effect 97.780 4.664e-21 ***
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
## group statistic p-value(g-1)
## 1 20 8.044
                     0.9862
## 2
      30 16.294
                      0.9720
## 3 40 28.206
                     0.8997
## 4 50 43.409
                      0.6984
##
## Elapsed time : 1.697006
```

```
spec_of_garch_Ibhf<- ugarchspec(variance.model = list(garchOrder=c(1,0)),mean.model =list(armaOrder=c(2
my_model_Ibhf<-ugarchfit(spec=spec_of_garch_Ibhf,data=ret_Ibhf)
my_model_Ibhf</pre>
```

```
##
     GARCH Model Fit
## Conditional Variance Dynamics
## -----
## GARCH Model : sGARCH(1,0)
## Mean Model : ARFIMA(2,0,0)
## Distribution : sstd
##
## Optimal Parameters
## -----
         Estimate Std. Error t value Pr(>|t|)
## mu
        0.000930 0.000703 1.3238 0.185583
## ar1 0.083488 0.026361 3.1671 0.001540
## ar2 -0.081537 0.021742 -3.7502 0.000177
## omega 0.000924 0.000145 6.3746 0.000000
## alpha1 0.558086 0.122056 4.5724 0.000005
## skew 1.092280 0.034497 31.6634 0.000000
## shape 2.825290 0.211006 13.3896 0.000000
## Robust Standard Errors:
     Estimate Std. Error t value Pr(>|t|)
        0.000930 0.000788 1.1799 0.238035
0.083488 0.027005 3.0916 0.001991
## mu
## ar1
## ar2 -0.081537 0.027129 -3.0055 0.002652
## omega 0.000924 0.000176 5.2422 0.000000
## alpha1 0.558086 0.150909 3.6982 0.000217
## skew 1.092280 0.041804 26.1284 0.000000
## shape 2.825290 0.229188 12.3274 0.000000
##
## LogLikelihood : 3712.902
##
## Information Criteria
## Akaike
             -4.2942
## Bayes
             -4.2721
## Shibata
            -4.2942
## Hannan-Quinn -4.2860
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
                       statistic p-value
## Lag[1]
                          2.057 0.1516
## Lag[2*(p+q)+(p+q)-1][5] 3.569 0.1794
## Lag[4*(p+q)+(p+q)-1][9] 7.113 0.1176
## d.o.f=2
```

```
## HO : No serial correlation
##
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
                     statistic p-value
## Lag[1]
                       0.1422 7.061e-01
## Lag[2*(p+q)+(p+q)-1][2] 0.6993 6.070e-01
## Lag[4*(p+q)+(p+q)-1][5] 21.4706 7.625e-06
## d.o.f=1
##
## Weighted ARCH LM Tests
## -----
   Statistic Shape Scale P-Value
## ARCH Lag[2] 1.112 0.500 2.000 2.917e-01
## ARCH Lag[4] 25.720 1.397 1.611 4.037e-07
## ARCH Lag[6] 34.571 2.222 1.500 4.279e-09
##
## Nyblom stability test
## -----
## Joint Statistic: 9.7862
## Individual Statistics:
## mu
      0.3441
## ar1 0.1033
## ar2 0.3947
## omega 4.7227
## alpha1 2.9823
## skew 0.4918
## shape 3.1054
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 1.69 1.9 2.35 ## Individual Statistic: 0.35 0.47 0.75
## Sign Bias Test
## -----
                 t-value prob sig
             1.869 0.06186
## Sign Bias
## Negative Sign Bias 1.042 0.29746
## Positive Sign Bias 1.098 0.27231
## Joint Effect 3.683 0.29777
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
## group statistic p-value(g-1)
## 1 20 16.27
                    0.6391
## 2 30 24.74
                      0.6916
                    0.1618
## 3 40 47.63
## 4 50 42.83
                     0.7202
##
## Elapsed time : 1.550998
```

```
spec_of_garch_Ibhf<- ugarchspec(variance.model = list(garchOrder=c(1,1)),mean.model =list(armaOrder=c(2
my_model_Ibhf<-ugarchfit(spec=spec_of_garch_Ibhf,data=ret_Ibhf)
my_model_Ibhf</pre>
```

```
##
    GARCH Model Fit
## Conditional Variance Dynamics
## -----
## GARCH Model : sGARCH(1,1)
## Mean Model : ARFIMA(2,0,0)
## Distribution : sstd
##
## Optimal Parameters
## -----
        Estimate Std. Error t value Pr(>|t|)
       ## mu
## ar1 0.078582 0.023730 3.3115 0.000928
## ar2 -0.058648 0.022725 -2.5808 0.009858
## omega 0.000038 0.000015 2.4526 0.014184
## alpha1 0.112180 0.032114 3.4931 0.000477
## beta1 0.863133 0.036793 23.4594 0.000000
        ## skew
## shape 3.711351 0.361108 10.2777 0.000000
##
## Robust Standard Errors:
##
       Estimate Std. Error t value Pr(>|t|)
## mu
      0.078582 0.023942 3.2821 0.001030
## ar1
## ar2 -0.058648 0.022224 -2.6390 0.008315
## omega 0.000038 0.000024 1.5958 0.110542
## alpha1 0.112180 0.049732 2.2557 0.024092
## beta1 0.863133 0.060847 14.1852 0.000000
## skew
        0.365498 10.1542 0.000000
## shape 3.711351
##
## LogLikelihood: 3780.194
##
## Information Criteria
## Akaike
           -4.3710
## Baves
           -4.3457
## Shibata
           -4.3711
## Hannan-Quinn -4.3617
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
                    statistic p-value
## Lag[1]
                      3.630 0.05676
## Lag[2*(p+q)+(p+q)-1][5] 3.839 0.09873
```

```
## Lag[4*(p+q)+(p+q)-1][9] 5.845 0.28261
## d.o.f=2
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                      statistic p-value
                         0.7135 0.3983
## Lag[1]
## Lag[2*(p+q)+(p+q)-1][5] 1.7019 0.6903
## Lag[4*(p+q)+(p+q)-1][9] 3.8694 0.6110
## d.o.f=2
## Weighted ARCH LM Tests
## -----
    Statistic Shape Scale P-Value
## ARCH Lag[3] 0.287 0.500 2.000 0.5921
## ARCH Lag[5] 1.037 1.440 1.667 0.7219
## ARCH Lag[7] 2.827 2.315 1.543 0.5468
## Nyblom stability test
## -----
## Joint Statistic: 2.9855
## Individual Statistics:
## mu
       0.09051
## ar1 0.09553
## ar2 0.13339
## omega 0.20357
## alpha1 0.59979
## beta1 0.34604
## skew 0.53950
## shape 0.08304
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 1.89 2.11 2.59
## Individual Statistic: 0.35 0.47 0.75
## Sign Bias Test
## -----
                  t-value prob sig
##
## Sign Bias
                  1.47004 0.141734
## Negative Sign Bias 2.89728 0.003812 ***
## Positive Sign Bias 0.08144 0.935103
## Joint Effect 8.47115 0.037215 **
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
## group statistic p-value(g-1)
## 1 20 14.90 0.72869
## 2 30 27.11 0.56602
## 3 40 38.08 0.51173
## 4 50 62.30 0.09613
##
##
```

```
## Elapsed time : 1.229993
spec_of_garch_Ibhf<- ugarchspec(variance.model = list(garchOrder=c(2,0)),mean.model = list(armaOrder=c(2,0))</pre>
my_model_Ibhf<-ugarchfit(spec=spec_of_garch_Ibhf,data=ret_Ibhf)</pre>
my_model_Ibhf
##
            GARCH Model Fit
## Conditional Variance Dynamics
## -----
## GARCH Model : sGARCH(2,0)
## Mean Model : ARFIMA(2,0,0)
## Distribution : sstd
## Optimal Parameters
         Estimate Std. Error t value Pr(>|t|)
## mu
        0.000875 0.000683 1.2821 0.199810
        0.080844 0.025279 3.1981 0.001384
## ar1
## ar2 -0.056839 0.025182 -2.2571 0.024001
## omega 0.000678 0.000094 7.2239 0.000000
## alpha1 0.407239 0.088810 4.5855 0.000005
## alpha2 0.270127 0.069837 3.8680 0.000110
          1.096863 0.034959 31.3754 0.000000
## skew
                   0.244396 12.4630 0.000000
## shape
          3.045918
##
## Robust Standard Errors:
##
       Estimate Std. Error t value Pr(>|t|)
        0.000875 0.000740 1.1826 0.236960
## mu
## ar1 0.080844 0.024169 3.3449 0.000823
## ar2 -0.056839 0.027250 -2.0858 0.036997
## omega 0.000678 0.000104 6.5374 0.000000
## alpha1 0.407239 0.098584 4.1309 0.000036
## alpha2 0.270127 0.070770 3.8169 0.000135
## skew
          1.096863 0.040383 27.1614 0.000000
          3.045918 0.249834 12.1918 0.000000
## shape
## LogLikelihood : 3734.563
##
## Information Criteria
##
## Akaike
              -4.3181
## Bayes
              -4.2929
## Shibata
              -4.3182
## Hannan-Quinn -4.3088
## Weighted Ljung-Box Test on Standardized Residuals
## -----
                         statistic p-value
```

2.990 0.08377

Lag[1]

```
## Lag[2*(p+q)+(p+q)-1][5] 3.354 0.27119
## Lag[4*(p+q)+(p+q)-1][9] 6.255 0.21723
## d.o.f=2
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                       statistic p-value
                         0.02933 0.8640
## Lag[1]
## Lag[2*(p+q)+(p+q)-1][5] 1.23632 0.8043
## Lag[4*(p+q)+(p+q)-1][9] 8.49526 0.1029
## d.o.f=2
## Weighted ARCH LM Tests
   Statistic Shape Scale P-Value
## ARCH Lag[3] 0.5651 0.500 2.000 0.45223
## ARCH Lag[5] 1.8779 1.440 1.667 0.49886
## ARCH Lag[7] 6.8677 2.315 1.543 0.09272
## Nyblom stability test
## -----
## Joint Statistic: 7.4833
## Individual Statistics:
## mu
       0.27124
## ar1
        0.06662
## ar2
      0.15560
## omega 3.02916
## alpha1 2.61515
## alpha2 1.56947
## skew 0.54649
## shape 1.85533
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 1.89 2.11 2.59
## Individual Statistic: 0.35 0.47 0.75
##
## Sign Bias Test
## -----
##
                  t-value prob sig
## Sign Bias
                  1.6124 0.1071
## Negative Sign Bias 1.0484 0.2946
## Positive Sign Bias 0.7389 0.4601
## Joint Effect 2.7688 0.4287
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
   group statistic p-value(g-1)
## 1 20 10.01 0.9526
## 2 30 17.58
## 3 40 33.86
                      0.9524
                      0.7030
## 4 50 37.96 0.8735
##
```

```
##
## Elapsed time : 1.710991
spec_of_garch_Ibhf<- ugarchspec(variance.model = list(garchOrder=c(0,2)),mean.model = list(armaOrder=c(2))</pre>
my_model_Ibhf<-ugarchfit(spec=spec_of_garch_Ibhf,data=ret_Ibhf)</pre>
my_model_Ibhf
        GARCH Model Fit *
## *----*
##
## Conditional Variance Dynamics
## -----
## GARCH Model : sGARCH(0,2)
## Mean Model : ARFIMA(2,0,0)
## Distribution : sstd
##
## Optimal Parameters
## -----
        Estimate Std. Error
                             t value Pr(>|t|)
## mu
       0.000810 0.000793 1.020563 0.307462
## ar1 0.038674 0.020978 1.843567 0.065246
## ar2 -0.060987 0.020699 -2.946360 0.003215
## omega 0.000004 0.000000 20.836023 0.000000
## beta1 0.000033 0.000446 0.074037 0.940981
## beta2 0.998967 0.000117 8552.019111 0.000000
## skew 1.071637 0.033210 32.268263 0.000000
                 0.062867
                             38.166111 0.000000
## shape 2.399407
##
## Robust Standard Errors:
        Estimate Std. Error t value Pr(>|t|)
## mu
       0.000810 0.000877 0.92312 0.355946
## ar1 0.038674 0.025687 1.50557 0.132177
## ar2 -0.060987 0.027316 -2.23265 0.025572
## omega 0.000004 0.000000 11.72830 0.000000
## beta1 0.000033 0.000816 0.04053 0.967671
## beta2 0.998967 0.000142 7049.41290 0.000000
## skew 1.071637 0.038105 28.12360 0.000000
## shape 2.399407 0.113344 21.16931 0.000000
## LogLikelihood : 3672.526
##
## Information Criteria
## -----
##
## Akaike
            -4.2463
             -4.2210
## Bayes
## Shibata -4.2463
## Hannan-Quinn -4.2369
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
                       statistic p-value
##
```

```
## Lag[1]
                        9.164 2.468e-03
## Lag[2*(p+q)+(p+q)-1][5] 10.181 1.213e-13
## Lag[4*(p+q)+(p+q)-1][9] 14.113 1.081e-04
## d.o.f=2
## HO : No serial correlation
##
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
            statistic p-value
##
                      57.49 3.397e-14
## Lag[1]
## Lag[2*(p+q)+(p+q)-1][5]
                       76.80 0.000e+00
## Lag[4*(p+q)+(p+q)-1][9] 117.21 0.000e+00
## d.o.f=2
##
## Weighted ARCH LM Tests
## -----
      Statistic Shape Scale P-Value
##
## ARCH Lag[3] 14.94 0.500 2.000 1.113e-04
## ARCH Lag[5]
              28.22 1.440 1.667 1.781e-07
## ARCH Lag[7] 66.22 2.315 1.543 0.000e+00
##
## Nyblom stability test
## -----
## Joint Statistic: 36.4137
## Individual Statistics:
## mu
     0.2257
## ar1 0.4085
## ar2 0.2991
## omega 7.1976
## beta1 6.1269
## beta2 6.1251
## skew 0.2639
## shape 4.0902
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 1.89 2.11 2.59
## Individual Statistic: 0.35 0.47 0.75
##
## Sign Bias Test
## -----
      t-value prob sig
            1.055 2.918e-01
## Sign Bias
## Negative Sign Bias 8.393 9.725e-17 ***
## Positive Sign Bias 5.133 3.181e-07 ***
## Joint Effect 96.805 7.556e-21 ***
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
## group statistic p-value(g-1)
## 1 20 8.322 0.9831
## 2 30 14.139
                    0.9907
## 3 40 28.809
                    0.8841
                 0.7989
## 4 50 40.570
```

```
##
##
## Elapsed time : 1.49299
spec_of_garch_Ibhf<- ugarchspec(variance.model = list(garchOrder=c(2,2)),mean.model = list(armaOrder=c(2,2))</pre>
my_model_Ibhf<-ugarchfit(spec=spec_of_garch_Ibhf,data=ret_Ibhf)</pre>
my_model_Ibhf
##
## *----*
           GARCH Model Fit
## Conditional Variance Dynamics
## -----
## GARCH Model : sGARCH(2,2)
## Mean Model : ARFIMA(2,0,0)
## Distribution : sstd
##
## Optimal Parameters
## -----
##
         Estimate Std. Error t value Pr(>|t|)
## mu
       0.001527 0.000622 2.45424 0.014118
        0.084888
                   0.024305 3.49264 0.000478
## ar1
## ar2 -0.059482 0.021516 -2.76455 0.005700
## omega 0.000052 0.000024 2.16371 0.030487
## alpha1 0.153469 0.040707 3.77006 0.000163
## alpha2 0.009711 0.046847 0.20729 0.835780
## beta1 0.102440 0.155474 0.65889 0.509966
## beta2 0.698308 0.129679 5.38491 0.000000
         1.150844 0.036863 31.21990 0.000000
## skew
## shape 3.796226
                 0.377508 10.05602 0.000000
##
## Robust Standard Errors:
         Estimate Std. Error t value Pr(>|t|)
##
## mu
        0.001527 0.000642 2.37809 0.017402
## ar1
       0.084888 0.024803 3.42246 0.000621
## ar2 -0.059482 0.022234 -2.67524 0.007467
## omega 0.000052 0.000040 1.30621 0.191479
## alpha1 0.153469 0.056251 2.72829 0.006366
## alpha2 0.009711 0.063464 0.15302 0.878385
## beta1 0.102440 0.211230 0.48497 0.627696
         ## beta2
## skew
         1.150844 0.038191 30.13419 0.000000
## shape 3.796226 0.383279 9.90460 0.000000
##
## LogLikelihood: 3783.868
##
## Information Criteria
## -----
##
## Akaike
             -4.3730
## Bayes
            -4.3414
```

Shibata

-4.3730

```
## Hannan-Quinn -4.3613
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
                     statistic p-value
## Lag[1]
                         2.745 0.09757
## Lag[2*(p+q)+(p+q)-1][5] 3.040 0.44696
## Lag[4*(p+q)+(p+q)-1][9] 5.434 0.36028
## d.o.f=2
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
            statistic p-value
##
## Lag[1]
                         0.1455 0.7029
## Lag[2*(p+q)+(p+q)-1][11] 4.2611 0.6936
## Lag[4*(p+q)+(p+q)-1][19] 6.7017 0.8124
## d.o.f=4
## Weighted ARCH LM Tests
## -----
    Statistic Shape Scale P-Value
## ARCH Lag[5] 0.08302 0.500 2.000 0.7732
## ARCH Lag[7] 4.60559 1.473 1.746 0.1475
## ARCH Lag[9] 5.99632 2.402 1.619 0.1757
## Nyblom stability test
## -----
## Joint Statistic: 4.4199
## Individual Statistics:
## mu
       0.10056
## ar1
      0.09808
## ar2 0.11824
## omega 0.16804
## alpha1 0.55518
## alpha2 0.29977
## beta1 0.29620
## beta2 0.24209
## skew 0.48054
## shape 0.08948
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 2.29 2.54 3.05
## Individual Statistic: 0.35 0.47 0.75
## Sign Bias Test
## -----
      t-value
##
                           prob sig
## Sign Bias
                  1.4793 0.139230
## Negative Sign Bias 2.6517 0.008082 ***
## Positive Sign Bias 0.5126 0.608267
## Joint Effect 7.3167 0.062459
##
##
```

```
## Adjusted Pearson Goodness-of-Fit Test:
## -----
    group statistic p-value(g-1)
## 1
      20
           15.07
                     0.7184
          23.84
## 2
      30
                       0.7369
## 3
     40 34.00
                       0.6970
## 4
      50
            42.31
                       0.7393
##
##
## Elapsed time : 1.626997
spec_of_garch_Ibhf<- ugarchspec(variance.model = list(garchOrder=c(1,2)),mean.model =list(armaOrder=c(2,2))</pre>
my_model_Ibhf<-ugarchfit(spec=spec_of_garch_Ibhf,data=ret_Ibhf)</pre>
my model Ibhf
##
## *----*
    GARCH Model Fit
## Conditional Variance Dynamics
## -----
## GARCH Model : sGARCH(1,2)
## Mean Model : ARFIMA(2,0,0)
## Distribution : sstd
##
## Optimal Parameters
## -----
##
         Estimate Std. Error t value Pr(>|t|)
## mu
       0.001525 0.000622 2.4492 0.014316
        ## ar1
      -0.059388 0.021413 -2.7734 0.005547
## ar2
## omega 0.000049 0.000019 2.5439 0.010963
## alpha1 0.155235 0.039975 3.8833 0.000103
## beta1 0.132330 0.096293 1.3742 0.169365
## beta2 0.678010 0.107461 6.3093 0.000000
## skew 1.150933 0.036846 31.2363 0.000000
## shape 3.799033 0.377991 10.0506 0.000000
## Robust Standard Errors:
       Estimate Std. Error t value Pr(>|t|)
## mu
        0.084687 0.024573 3.4464 0.000568
-0.059388 0.022222 -2.6724 0.007530
## ar1
## ar2
## omega 0.000049 0.000029 1.7200 0.085435
## alpha1 0.155235 0.060550 2.5637 0.010356
                  0.117707
                            1.1242 0.260917
## beta1 0.132330
## beta2 0.678010 0.159830
                            4.2421 0.000022
## skew 1.150933 0.038088 30.2175 0.000000
## shape 3.799033 0.386256 9.8355 0.000000
##
## LogLikelihood : 3783.848
```

Information Criteria

```
##
## Akaike
           -4.3741
## Bayes
            -4.3457
## Shibata
           -4.3742
## Hannan-Quinn -4.3636
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
                        statistic p-value
## Lag[1]
                          2.782 0.09533
## Lag[2*(p+q)+(p+q)-1][5] 3.077 0.42409
## Lag[4*(p+q)+(p+q)-1][9] 5.482 0.35049
## d.o.f=2
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                        statistic p-value
## Lag[1]
                          0.1275 0.7210
## Lag[2*(p+q)+(p+q)-1][8]
                          2.5216 0.7721
## Lag[4*(p+q)+(p+q)-1][14] 5.2201 0.7418
## d.o.f=3
## Weighted ARCH LM Tests
## -----
            Statistic Shape Scale P-Value
## ARCH Lag[4] 0.09077 0.500 2.000 0.7632
## ARCH Lag[6] 2.66116 1.461 1.711 0.3618
## ARCH Lag[8] 4.44764 2.368 1.583 0.3136
## Nyblom stability test
## -----
## Joint Statistic: 3.1329
## Individual Statistics:
## mu
       0.09982
## ar1 0.10035
## ar2 0.11962
## omega 0.16232
## alpha1 0.53027
## beta1 0.26809
## beta2 0.23248
## skew 0.47471
## shape 0.09024
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 2.1 2.32 2.82
## Individual Statistic: 0.35 0.47 0.75
## Sign Bias Test
## t-value prob sig
## Sign Bias 1.4977 0.134404
## Negative Sign Bias 2.6562 0.007975 ***
```

```
## Positive Sign Bias 0.5418 0.588008
## Joint Effect
                  7.3726 0.060924
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
  group statistic p-value(g-1)
                    0.6869
## 1
      20 15.55
## 2
      30
           21.72
                      0.8317
## 3
    40 33.95
                      0.6990
## 4
      50 39.01
                      0.8459
##
##
## Elapsed time : 1.369995
spec_of_garch_Ibhf<- ugarchspec(variance.model = list(garchOrder=c(2,1)),mean.model = list(armaOrder=c(2,1))</pre>
my_model_Ibhf<-ugarchfit(spec=spec_of_garch_Ibhf,data=ret_Ibhf)</pre>
my_model_Ibhf
##
## *----*
           GARCH Model Fit
##
## Conditional Variance Dynamics
## -----
## GARCH Model : sGARCH(2,1)
## Mean Model : ARFIMA(2,0,0)
## Distribution : sstd
##
## Optimal Parameters
##
         Estimate Std. Error t value Pr(>|t|)
       ## ar1
      -0.058649 0.022726 -2.580718 0.009859
## ar2
## omega 0.000038 0.000024 1.556688 0.119545
## alpha1 0.112187 0.034638 3.238871 0.001200
## alpha2 0.000000 0.060685 0.000001 1.000000
## beta1 0.863136 0.063723 13.545195 0.000000
## skew 1.146631 0.036558 31.364614 0.000000
## shape 3.710569 0.411244 9.022781 0.000000
##
## Robust Standard Errors:
##
       Estimate Std. Error t value Pr(>|t|)
         ## mu
## ar1
        ## ar2
## omega 0.000038 0.000055 0.68562 0.492954
## alpha1 0.112187 0.035410 3.16826 0.001534
## alpha2 0.000000 0.114209 0.00000 1.000000
## beta1 0.863136 0.149943 5.75644 0.000000
## skew 1.146631 0.037314 30.72912 0.000000
## shape 3.710569 0.568399 6.52810 0.000000
```

```
##
## LogLikelihood: 3780.194
## Information Criteria
## -----
##
            -4.3699
## Akaike
            -4.3414
## Bayes
## Bayes -4.3414
## Shibata -4.3699
## Hannan-Quinn -4.3593
## Weighted Ljung-Box Test on Standardized Residuals
## -----
          statistic p-value
##
## Lag[1]
                           3.628 0.05680
## Lag[2*(p+q)+(p+q)-1][5] 3.838 0.09903
## Lag[4*(p+q)+(p+q)-1][9] 5.844 0.28282
## d.o.f=2
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                       statistic p-value
## Lag[1] 0.7139 0.3982
## Lag[2*(p+q)+(p+q)-1][8] 3.2430 0.6409
## Lag[4*(p+q)+(p+q)-1][14] 5.9339 0.6477
## d.o.f=3
## Weighted ARCH LM Tests
   Statistic Shape Scale P-Value
## ARCH Lag[4] 0.7843 0.500 2.000 0.3758
## ARCH Lag[6] 2.4251 1.461 1.711 0.4041
## ARCH Lag[8] 3.7462 2.368 1.583 0.4142
## Nyblom stability test
## -----
## Joint Statistic: 4.414
## Individual Statistics:
## mu 0.09039
## ar1 0.09541
## ar2 0.13339
## omega 0.20395
## alpha1 0.59992
## alpha2 0.74035
## beta1 0.34637
## skew 0.53917
## shape 0.08312
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 2.1 2.32 2.82
## Individual Statistic: 0.35 0.47 0.75
##
## Sign Bias Test
```

```
t-value prob sig
1.47003 0.141737
##
## Sign Bias
## Negative Sign Bias 2.89759 0.003808 ***
## Positive Sign Bias 0.08116 0.935323
## Joint Effect 8.47286 0.037186 **
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
    group statistic p-value(g-1)
      20 14.90 0.72869
## 1
## 2
      30 27.11
                     0.56602
## 3 40 38.08
                     0.51173
## 4
    50 63.05
                     0.08558
##
##
## Elapsed time : 1.307997
spec_of_garch_Ibhf<-ugarchspec(variance.model =list(model="eGARCH",garchOrder=c(1,1)),mean.model = list</pre>
my_model_Ibhf<-ugarchfit(spec=spec_of_garch_Ibhf,data=ret_Ibhf)</pre>
my_model_Ibhf
##
       GARCH Model Fit
##
## Conditional Variance Dynamics
## -----
## GARCH Model : eGARCH(1,1)
## Mean Model : ARFIMA(2,0,0)
## Distribution : sstd
## Optimal Parameters
##
        Estimate Std. Error t value Pr(>|t|)
## mu
       0.001113 0.000691 1.6104 0.107312
## ar1
        ## ar2 -0.064705 0.022594 -2.8638 0.004185
## omega -0.114240 0.013041 -8.7598 0.000000
## beta1 0.983717 0.001829 537.9391 0.000000 ## gamma1 0.154018 0.030718 5.0139 0.000001
## skew 1.136959 0.036898 30.8136 0.000000
## shape 3.813267 0.379349 10.0521 0.000000
## Robust Standard Errors:
       Estimate Std. Error t value Pr(>|t|)
        0.001113 0.000845 1.3179 0.187527
## mu
        0.071473 0.028885 2.4744 0.013347
## ar1
## ar2 -0.064705 0.023418 -2.7631 0.005726
## omega -0.114240 0.005671 -20.1434 0.000000
```

```
## beta1 0.983717 0.000702 1400.6722 0.000000 ## gamma1 0.154018 0.038399 4.0110 0.000060
## skew 1.136959 0.039907 28.4904 0.000000
## shape 3.813267 0.382342 9.9734 0.000000
## LogLikelihood : 3782.215
## Information Criteria
## -----
##
## Akaike
              -4.3722
## Bayes
              -4.3438
## Shibata -4.3723
## Hannan-Quinn -4.3617
## Weighted Ljung-Box Test on Standardized Residuals
##
                        statistic p-value
## Lag[1]
                           5.090 0.0240635
## Lag[2*(p+q)+(p+q)-1][5] 5.351 0.0009535
## Lag[4*(p+q)+(p+q)-1][9] 7.426 0.0922214
## d.o.f=2
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                         statistic p-value
## Lag[1]
                          5.763 0.01637
## Lag[2*(p+q)+(p+q)-1][5] 6.291 0.07678
## Lag[4*(p+q)+(p+q)-1][9] 8.035 0.12686
## d.o.f=2
##
## Weighted ARCH LM Tests
             Statistic Shape Scale P-Value
## ARCH Lag[3] 0.2783 0.500 2.000 0.5978
## ARCH Lag[5] 0.9309 1.440 1.667 0.7536
## ARCH Lag[7] 2.2952 2.315 1.543 0.6550
##
## Nyblom stability test
## -----
## Joint Statistic: 3.1446
## Individual Statistics:
## mu 0.03751
## ar1 0.12979
## ar2 0.15495
## omega 0.21612
## alpha1 0.63860
## beta1 0.19054
## gamma1 0.16817
## skew 0.39736
## shape 0.21785
##
## Asymptotic Critical Values (10% 5% 1%)
```

```
## Joint Statistic: 2.1 2.32 2.82 ## Individual Statistic: 0.35 0.47 0.75
## Sign Bias Test
## -----
##
                  t-value prob sig
                 1.277 0.20185
## Sign Bias
## Negative Sign Bias 2.662 0.00783 ***
## Positive Sign Bias 1.514 0.13019
## Joint Effect 10.599 0.01410 **
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
## group statistic p-value(g-1)
## 1
      20
            21.14
                    0.3292
## 2
      30
          34.65
                       0.2163
## 3 40 38.54
                     0.4906
## 4 50 58.70
                     0.1614
##
##
## Elapsed time : 2.056005
```

this model is rejected since there is no leverage effect.

```
spec_of_garch_Ibhf<-ugarchspec(variance.model =list(model="gjrGARCH",garchOrder=c(1,1)),mean.model = li
my_model_Ibhf<-ugarchfit(spec=spec_of_garch_Ibhf,data=ret_Ibhf)
my_model_Ibhf</pre>
```

```
## *----*
          GARCH Model Fit
## *----*
##
## Conditional Variance Dynamics
## -----
## GARCH Model : gjrGARCH(1,1)
## Mean Model : ARFIMA(2,0,0)
## Distribution : sstd
##
## Optimal Parameters
         Estimate Std. Error t value Pr(>|t|)
       0.001128 0.000615 1.8344 0.066591
## mu
        0.072700 0.023257 3.1260 0.001772
## ar1
## ar2 -0.063966 0.022349 -2.8622 0.004207
## omega 0.000031 0.000013 2.3563 0.018459
## alpha1 0.055090 0.025378 2.1708 0.029949
## beta1 0.881337 0.035789 24.6257 0.000000
## gamma1 0.088309 0.032357 2.7292 0.006349
## skew
         1.139250 0.035895 31.7381 0.000000
         3.802084 0.378112 10.0554 0.000000
## shape
##
```

```
## Robust Standard Errors:
##
   Estimate Std. Error t value Pr(>|t|)
## mu
       ## ar1
        0.072700 0.023696 3.0681 0.002154
## ar2 -0.063966 0.022397 -2.8561 0.004289
## omega 0.000031 0.000020 1.5732 0.115675
## alpha1 0.055090 0.035473 1.5530 0.120425
## beta1 0.881337 0.057729 15.2668 0.000000 ## gamma1 0.088309 0.045111 1.9576 0.050281
## skew 1.139250 0.036522 31.1938 0.000000
## shape 3.802084 0.377641 10.0680 0.000000
##
## LogLikelihood : 3785.318
##
## Information Criteria
## -----
##
## Akaike
            -4.3758
## Bayes
            -4.3474
## Shibata -4.3759
## Hannan-Quinn -4.3653
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
                      statistic p-value
## Lag[1]
                        4.434 0.035223
## Lag[2*(p+q)+(p+q)-1][5] 4.771 0.007087
## Lag[4*(p+q)+(p+q)-1][9] 6.774 0.151230
## d.o.f=2
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                       statistic p-value
## Lag[1]
                        1.155 0.2826
## Lag[2*(p+q)+(p+q)-1][5] 1.922 0.6369
## Lag[4*(p+q)+(p+q)-1][9] 3.549 0.6659
## d.o.f=2
##
## Weighted ARCH LM Tests
## -----
            Statistic Shape Scale P-Value
## ARCH Lag[3] 0.06199 0.500 2.000 0.8034
## ARCH Lag[5] 0.88827 1.440 1.667 0.7664
## ARCH Lag[7] 1.83488 2.315 1.543 0.7522
##
## Nyblom stability test
## -----
## Joint Statistic: 2.999
## Individual Statistics:
## mu 0.06350
## ar1 0.10567
## ar2 0.14288
## omega 0.14136
```

```
## alpha1 0.24330
## beta1 0.20776
## gamma1 0.59706
## skew 0.42940
## shape 0.08892
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 2.1 2.32 2.82
## Individual Statistic: 0.35 0.47 0.75
## Sign Bias Test
## -----
                 t-value prob sig
## Sign Bias
                  1.2075 0.22739
## Negative Sign Bias 2.1272 0.03355 **
## Positive Sign Bias 0.5657 0.57168
## Joint Effect 5.3906 0.14533
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
## group statistic p-value(g-1)
## 1 20 19.79
                    0.4071
## 2
      30 38.23
                      0.1173
## 3 40 35.71
                     0.6205
## 4 50 45.49
                     0.6160
##
## Elapsed time : 2.941003
spec_of_garch_Ibhf<-ugarchspec(variance.model =list(model="gjrGARCH",garchOrder=c(1,2)),mean.model = li</pre>
my_model_Ibhf<-ugarchfit(spec=spec_of_garch_Ibhf,data=ret_Ibhf)</pre>
my_model_Ibhf
##
    GARCH Model Fit *
## *----*
##
## Conditional Variance Dynamics
## -----
## GARCH Model : gjrGARCH(1,2)
## Mean Model : ARFIMA(2,0,0)
## Distribution : sstd
##
## Optimal Parameters
```

Estimate Std. Error t value Pr(>|t|)

0.001176 0.000614 1.9140 0.055619 0.074666 0.023715 3.1484 0.001642

-0.062259 0.021289 -2.9245 0.003450

omega 0.000046 0.000016 2.7952 0.005186 ## alpha1 0.081039 0.030579 2.6502 0.008045 ## beta1 0.132748 0.089503 1.4832 0.138028

##

mu

ar1

ar2

```
## skew 1.145098 0.036294 31.5507 0.000000
## shape 3.886072 0.393244 9.8821 0.000000
## Robust Standard Errors:
## Estimate Std. Error t value Pr(>|t|)
        0.001176 0.000667 1.7630 0.077899
0.074666 0.023527 3.1737 0.001505
## mu
## ar1
## ar2 -0.062259 0.021840 -2.8506 0.004363
## omega 0.000046 0.000020 2.2558 0.024083
## alpha1 0.081039 0.033495 2.4194 0.015546
## beta1 0.132748 0.096597 1.3742 0.169364
## beta2 0.688527 0.117267 5.8715 0.000000
## gamma1 0.135229 0.062732 2.1557 0.031110
## skew 1.145098 0.037356 30.6539 0.000000
## shape 3.886072 0.388444 10.0042 0.000000
##
## LogLikelihood : 3789.341
## Information Criteria
## -----
##
             -4.3793
## Akaike
## Bayes
             -4.3477
## Shibata
            -4.3794
## Hannan-Quinn -4.3676
## Weighted Ljung-Box Test on Standardized Residuals
##
                        statistic p-value
## Lag[1]
                           3.967 0.04639
## Lag[2*(p+q)+(p+q)-1][5] 4.305 0.02934
## Lag[4*(p+q)+(p+q)-1][9]
                         6.643 0.16620
## d.o.f=2
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                         statistic p-value
## Lag[1]
                          0.240 0.6242
                            1.677 0.9052
## Lag[2*(p+q)+(p+q)-1][8]
## Lag[4*(p+q)+(p+q)-1][14] 5.167 0.7485
## d.o.f=3
## Weighted ARCH LM Tests
             Statistic Shape Scale P-Value
## ARCH Lag[4] 0.3792 0.500 2.000 0.5381
              0.9852 1.461 1.711 0.7520
## ARCH Lag[6]
## ARCH Lag[8] 3.0087 2.368 1.583 0.5418
## Nyblom stability test
## -----
```

```
## Joint Statistic: 3.2005
## Individual Statistics:
        0.07537
      0.11418
## ar1
      0.14029
## ar2
## omega 0.13357
## alpha1 0.22450
## beta1 0.18048
## beta2 0.15467
## gamma1 0.56775
## skew 0.41779
## shape 0.09810
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic:
                  2.29 2.54 3.05
## Individual Statistic: 0.35 0.47 0.75
## Sign Bias Test
## -----
                  t-value prob sig
## Sign Bias
                  1.2852 0.1989
## Negative Sign Bias 1.6418 0.1008
## Positive Sign Bias 0.1031 0.9179
## Joint Effect 3.3820 0.3364
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
## group statistic p-value(g-1)
## 1 20 19.82
                       0.4057
      30 31.90
## 2
                       0.3242
    40 36.64
## 3
                      0.5779
## 4
    50 48.91
                      0.4766
##
## Elapsed time : 2.927001
spec_of_garch_Ibhf<-ugarchspec(variance.model =list(model="gjrGARCH",garchOrder=c(2,1)),mean.model = li</pre>
my_model_Ibhf<-ugarchfit(spec=spec_of_garch_Ibhf,data=ret_Ibhf)</pre>
my_model_Ibhf
      GARCH Model Fit *
## *----*
## Conditional Variance Dynamics
## GARCH Model : gjrGARCH(2,1)
## Mean Model : ARFIMA(2,0,0)
```

Distribution : sstd

Optimal Parameters

##

```
Estimate Std. Error t value Pr(>|t|)
## mu
       ## ar1
       -0.064073 0.021659 -2.958298 0.003093
## ar2
## omega 0.000017 0.000004 3.862489 0.000112
## alpha1 0.028375 0.023074 1.229725 0.218800
## alpha2 0.000000 0.024914 0.000002 0.999999
## beta1 0.930930 0.012259 75.939441 0.000000 ## gamma1 0.247948 0.082573 3.002765 0.002675
## gamma2 -0.189105 0.079559 -2.376913 0.017458
## skew
         1.142575 0.036207 31.556739 0.000000
         ## shape
##
## Robust Standard Errors:
##
         Estimate Std. Error t value Pr(>|t|)
        0.001068 0.000695 1.535811 0.124585
## mu
        ## ar1
## ar2
      ## omega 0.000017 0.000006 2.638972 0.008316
## alpha1 0.028375 0.021355 1.328736 0.183935
## alpha2 0.000000 0.028990 0.000001 0.999999
## beta1
         ## gamma1 0.247948 0.090199 2.748889 0.005980
## gamma2 -0.189105 0.084132 -2.247702 0.024595
## skew 1.142575 0.036935 30.934405 0.000000
## shape
         3.896390 0.401058 9.715279 0.000000
##
## LogLikelihood: 3788.295
## Information Criteria
## -----
##
## Akaike
            -4.3769
## Bayes
            -4.3422
## Shibata
             -4.3770
## Hannan-Quinn -4.3641
##
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
                      statistic p-value
## Lag[1]
                        6.348 1.175e-02
                       6.734 3.473e-06
8.635 3 3265 00
## Lag[2*(p+q)+(p+q)-1][5]
## Lag[4*(p+q)+(p+q)-1][9]
## d.o.f=2
## HO : No serial correlation
##
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                       statistic p-value
## Lag[1]
                          1.909 0.1670
## Lag[2*(p+q)+(p+q)-1][8] 3.395 0.6131
## Lag[4*(p+q)+(p+q)-1][14] 6.036 0.6339
## d.o.f=3
##
```

```
## Weighted ARCH LM Tests
## -----
    Statistic Shape Scale P-Value
## ARCH Lag[4] 0.6678 0.500 2.000 0.4138
## ARCH Lag[6] 1.2966 1.461 1.711 0.6646
## ARCH Lag[8] 2.5757 2.368 1.583 0.6254
## Nyblom stability test
## -----
## Joint Statistic: 6.285
## Individual Statistics:
## mu
       0.07951
## ar1
      0.11005
## ar2 0.18933
## omega 0.61938
## alpha1 0.12178
## alpha2 0.14502
## beta1 0.11808
## gamma1 0.31942
## gamma2 0.27047
## skew 0.38894
## shape 0.11086
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 2.49 2.75 3.27
## Individual Statistic: 0.35 0.47 0.75
## Sign Bias Test
                  t-value prob sig
                1.458 0.14513
## Sign Bias
## Negative Sign Bias 1.398 0.16216
## Positive Sign Bias 1.174 0.24047
## Joint Effect 6.647 0.08404
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## group statistic p-value(g-1)
## 1 20 20.91 0.3420
## 2 30 32.11
                      0.3150
## 3 40 40.12
                      0.4204
    50 56.21
## 4
                     0.2229
##
## Elapsed time : 4.289004
spec_of_garch_Ibhf<-ugarchspec(variance.model =list(model="gjrGARCH",garchOrder=c(2,2)),mean.model = li</pre>
my_model_Ibhf<-ugarchfit(spec=spec_of_garch_Ibhf,data=ret_Ibhf)</pre>
my_model_Ibhf
##
## *----*
```

*

GARCH Model Fit

```
##
## Conditional Variance Dynamics
## -----
## GARCH Model : gjrGARCH(2,2)
## Mean Model : ARFIMA(2,0,0)
## Distribution : sstd
##
## Optimal Parameters
## -----
          Estimate Std. Error t value Pr(>|t|)
         ## mu
## ar1
        0.080032 0.023894 3.349518 0.000810
## ar2 -0.064973 0.021383 -3.038545 0.002377
## omega 0.000050 0.000022 2.289569 0.022046
## alpha1 0.086544 0.031143 2.778957 0.005453
## alpha2 0.000000 0.033103 0.000001 0.999999
## beta1 0.023486 0.076991 0.305043 0.760333
## beta2 0.779441 0.069364 11.236920 0.000000 ## gamma1 0.093383 0.046147 2.023621 0.043009
## gamma2 0.061723 0.041724 1.479310 0.139057
## skew
          1.144768 0.036412 31.438966 0.000000
          3.906202 0.405303 9.637741 0.000000
## shape
##
## Robust Standard Errors:
        Estimate Std. Error t value Pr(>|t|)
## mu
          0.080032 0.024471 3.270554 0.001073
## ar1
## ar2 -0.064973 0.021941 -2.961306 0.003063
## omega 0.000050 0.000034 1.479695 0.138955
## alpha1 0.086544 0.038282 2.260673 0.023780
## alpha2 0.000000 0.045678 0.000001 0.999999
## beta1 0.023486 0.094216 0.249274 0.803149
## beta2 0.779441 0.077534 10.052887 0.000000 ## gamma1 0.093383 0.058930 1.584656 0.113045
## gamma2 0.061723 0.051062 1.208780 0.226747
## skew
          1.144768 0.037602 30.444167 0.000000
## shape 3.906202 0.406742 9.603639 0.000000
##
## LogLikelihood: 3790.081
## Information Criteria
## -----
##
             -4.3778
## Akaike
             -4.3399
## Bayes
             -4.3779
## Shibata
## Hannan-Quinn -4.3638
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
                         statistic p-value
## Lag[1]
                          3.203 0.07352
## Lag[2*(p+q)+(p+q)-1][5] 3.662 0.14734
```

```
## Lag[4*(p+q)+(p+q)-1][9] 6.113 0.23846
## d.o.f=2
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                       statistic p-value
                         0.2491 0.6177
## Lag[1]
## Lag[2*(p+q)+(p+q)-1][11] 3.3787 0.8211
## Lag[4*(p+q)+(p+q)-1][19] 5.8503 0.8853
## d.o.f=4
## Weighted ARCH LM Tests
## -----
    Statistic Shape Scale P-Value
## ARCH Lag[5] 0.01706 0.500 2.000 0.8961
## ARCH Lag[7] 2.70624 1.473 1.746 0.3673
## ARCH Lag[9] 4.62861 2.402 1.619 0.3115
## Nyblom stability test
## -----
## Joint Statistic: 4.4235
## Individual Statistics:
## mu
      0.07253
## ar1 0.09682
## ar2 0.13138
## omega 0.13805
## alpha1 0.21120
## alpha2 0.20130
## beta1 0.24254
## beta2 0.15807
## gamma1 0.44652
## gamma2 0.59091
## skew 0.40483
## shape 0.10190
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 2.69 2.96 3.51
## Individual Statistic: 0.35 0.47 0.75
##
## Sign Bias Test
## -----
                 t-value prob sig
## Sign Bias
                 1.21520 0.22445
## Negative Sign Bias 1.98547 0.04725 **
## Positive Sign Bias 0.06256 0.95013
## Joint Effect 4.20879 0.23978
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
## group statistic p-value(g-1)
## 1 20 18.33 0.5003
## 2 30 29.54
                    0.4373
```

```
## 3 40 38.73 0.4822
## 4 50 43.76 0.6850
##
## ## Elapsed time : 5.736991
sGARCH(0,2) Akaike -4.5795 sstd sGA
```

 $sGARCH(0,2) \ Akaike \ -4.5795 \ sstd \ sGARCH(2,0) \ Akaike \ -4.6343 \ sstd \ sGARCH(2,1) \ Akaike \ -4.6599 \ sstd \ sGARCH(2,2) \ Akaike \ -4.6650 \ sstd \ sGARCH(1,1) \ Akaike \ -4.6611 \ sstd \ sGARCH(1,2) \ Akaike \ -4.6657 \ sstd \ gjrGARCH(2,1) \ Akaike \ -4.6685 \ sstd \ gjrGARCH(1,1) \ Akaike \ -4.6703 \ sstd \ gjrGARCH(1,2) \ Akaike \ -4.6730 \ sstd \ gjrGARCH(2,2) \ Akaike \ -4.6742 \ sstd$

so we are taking (1,2) instead of (2,2) because many terms in it are not significant

```
spec_of_garch_Ibhf<-ugarchspec(variance.model =list(model="gjrGARCH",garchOrder=c(1,3)),mean.model = li
my_model_Ibhf<-ugarchfit(spec=spec_of_garch_Ibhf,data=ret_Ibhf)
my_model_Ibhf</pre>
```

```
##
          GARCH Model Fit
## *----*
##
## Conditional Variance Dynamics
## -----
## GARCH Model : gjrGARCH(1,3)
## Mean Model : ARFIMA(2,0,0)
## Distribution : sstd
##
## Optimal Parameters
        Estimate Std. Error t value Pr(>|t|)
##
               0.000614 1.88807 0.059016
## mu
        0.001159
        ## ar1
       ## ar2
        ## omega
## alpha1 0.080863 0.030367 2.66290 0.007747
## beta1
        ## beta2
        0.678787 0.114138 5.94708 0.000000
## beta3
        0.037753
                0.150791 0.25037 0.802305
## gamma1 0.136979 0.048811 2.80630 0.005011
## skew
        1.144234 0.036187 31.61988 0.000000
## shape
        3.904269
                0.394161 9.90527 0.000000
##
## Robust Standard Errors:
##
        Estimate Std. Error t value Pr(>|t|)
                 0.000671 1.72762 0.084055
## mu
        0.001159
        0.074602
                 0.024063 3.10025 0.001934
## ar1
                0.022186 -2.77764 0.005475
## ar2
       -0.061624
        0.000046 0.000020 2.29470 0.021750
## omega
## alpha1 0.080863 0.032649 2.47677 0.013258
               0.115176 0.89331 0.371694
## beta1
        0.102887
## beta2
        ## beta3
        ## gamma1 0.136979
               0.065939 2.07736 0.037768
```

```
## skew
         1.144234 0.037312 30.66685 0.000000
## shape 3.904269 0.393285 9.92732 0.000000
##
## LogLikelihood: 3789.087
## Information Criteria
## -----
## Akaike -4.3779
## Bayes -4.3431
## Shibata -4.3779
## Hannan-Quinn -4.3650
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
                      statistic p-value
## Lag[1] 4.028 0.04475
## Lag[2*(p+q)+(p+q)-1][5] 4.356 0.02534
## Lag[4*(p+q)+(p+q)-1][9] 6.702 0.15933
## d.o.f=2
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                        statistic p-value
## Lag[1]
                         0.2255 0.6349
## Lag[2*(p+q)+(p+q)-1][11] 3.6837 0.7790
## Lag[4*(p+q)+(p+q)-1][19] 6.7316 0.8096
## d.o.f=4
##
## Weighted ARCH LM Tests
## -----
            Statistic Shape Scale P-Value
## ARCH Lag[5] 0.06196 0.500 2.000 0.8034
## ARCH Lag[7] 2.36803 1.473 1.746 0.4283
## ARCH Lag[9] 5.38132 2.402 1.619 0.2287
##
## Nyblom stability test
## -----
## Joint Statistic: 4.3258
## Individual Statistics:
## mu
       0.07563
## ar1 0.11648
## ar2 0.14344
## omega 0.13431
## alpha1 0.22036
## beta1 0.16966
## beta2 0.14923
## beta3 0.17200
## gamma1 0.57598
## skew 0.40381
## shape 0.10360
##
## Asymptotic Critical Values (10% 5% 1%)
```

```
## Joint Statistic: 2.49 2.75 3.27 ## Individual Statistic: 0.35 0.47 0.75
## Sign Bias Test
## -----
##
                  t-value prob sig
## Sign Bias
                 1.29583 0.19521
## Negative Sign Bias 1.65051 0.09902
## Positive Sign Bias 0.08869 0.92934
## Joint Effect 3.40964 0.33267
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
## group statistic p-value(g-1)
## 1
     20
            18.47
                      0.4911
## 2
      30
           29.50
                       0.4391
## 3 40 36.97
                      0.5630
## 4 50 51.23
                      0.3862
##
##
## Elapsed time : 3.334995
spec_of_garch_Ibhf<-ugarchspec(variance.model =list(model="gjrGARCH",garchOrder=c(3,1)),mean.model = li</pre>
my_model_Ibhf<-ugarchfit(spec=spec_of_garch_Ibhf,data=ret_Ibhf)</pre>
my_model_Ibhf
##
          GARCH Model Fit
## *----*
## Conditional Variance Dynamics
## -----
## GARCH Model : gjrGARCH(3,1)
## Mean Model : ARFIMA(2,0,0)
## Distribution : sstd
## Optimal Parameters
## -----
         Estimate Std. Error t value Pr(>|t|)
## mu
       0.001046 0.000691 1.51348 0.130159
        ## ar1
## ar2
      -0.065384 0.022169 -2.94936 0.003184
## omega 0.000015 0.000011 1.39766 0.162216
## alpha1 0.026395 0.023150 1.14013 0.254232
## alpha2 0.000000 0.043886 0.00000 1.000000
## alpha3 0.000000 0.050487 0.00000 1.000000
## beta1
         ## gamma1 0.239626 0.081890 2.92618 0.003432
## gamma2 -0.154367 0.119950 -1.28692 0.198121
```

```
##
## Robust Standard Errors:
        Estimate Std. Error t value Pr(>|t|)
         0.001046 0.002239 0.467084 0.640440
## mu
        0.063812 0.028813 2.214686 0.026782
## ar1
## ar2 -0.065384 0.023088 -2.831986 0.004626
## omega 0.000015 0.000068 0.225717 0.821421
## alpha1 0.026395 0.039604 0.666467 0.505113
## alpha2 0.000000 0.053154 0.000000 1.000000
## alpha3 0.000000 0.217890 0.000000 1.000000
## beta1
         ## gamma1 0.239626 0.113748 2.106648 0.035148
## gamma2 -0.154367 0.310395 -0.497323 0.618961
## skew
          1.141148 0.082483 13.834942 0.000000
         3.923325 1.549805 2.531496 0.011358
## shape
##
## LogLikelihood: 3788.104
##
## Information Criteria
## -----
             -4.3744
## Akaike
## Bayes -4.3333
## Shibata -4.3745
## Hannan-Quinn -4.3592
## Weighted Ljung-Box Test on Standardized Residuals
##
                       statistic p-value
## Lag[1]
                          6.365 1.164e-02
## Lag[2*(p+q)+(p+q)-1][5] 6.808 2.508e-06
## Lag[4*(p+q)+(p+q)-1][9] 8.690 3.165e-02
## d.o.f=2
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                         statistic p-value
## Lag[1]
                           2.103 0.1470
## Lag[2*(p+q)+(p+q)-1][11]
                           5.176 0.5540
## Lag[4*(p+q)+(p+q)-1][19] 7.533 0.7274
## d.o.f=4
##
## Weighted ARCH LM Tests
## -----
             Statistic Shape Scale P-Value
## ARCH Lag[5] 0.5109 0.500 2.000 0.4748
## ARCH Lag[7]
             1.7354 1.473 1.746 0.5647
                3.8659 2.402 1.619 0.4177
## ARCH Lag[9]
##
## Nyblom stability test
## -----
## Joint Statistic: 10.294
```

```
## Individual Statistics:
## mu
       0.08077
      0.10491
## ar1
## ar2 0.19377
## omega 1.12666
## alpha1 0.11537
## alpha2 0.13699
## alpha3 0.17216
## beta1 0.11160
## gamma1 0.30548
## gamma2 0.25790
## gamma3 0.26878
## skew 0.38307
## shape 0.12168
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 2.89 3.15 3.69
## Individual Statistic:
                       0.35 0.47 0.75
## Sign Bias Test
## -----
                  t-value prob sig
                1.405 0.16025
## Sign Bias
## Negative Sign Bias 1.450 0.14719
## Positive Sign Bias 1.264 0.20657
## Joint Effect 6.857 0.07659
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
   group statistic p-value(g-1)
## 1 20 22.34
                       0.2675
      30 30.51
                       0.3888
## 2
    40 43.64
## 3
                       0.2807
      50 58.59
## 4
                      0.1640
##
##
## Elapsed time : 5.733994
spec_of_garch_Ibhf<-ugarchspec(variance.model =list(model="gjrGARCH",garchOrder=c(2,3)),mean.model = li</pre>
my_model_Ibhf<-ugarchfit(spec=spec_of_garch_Ibhf,data=ret_Ibhf)</pre>
my_model_Ibhf
## *----*
          GARCH Model Fit
##
## Conditional Variance Dynamics
## -----
## GARCH Model : gjrGARCH(2,3)
```

Mean Model : ARFIMA(2,0,0)

Distribution : sstd

##

```
## Optimal Parameters
## -----
          Estimate Std. Error t value Pr(>|t|)
          0.001054 0.000609 1.730468 0.083547
## mu
## ar1
         ## ar2 -0.062652 0.021994 -2.848549 0.004392
## omega 0.000033 0.000019 1.714037 0.086522
## alpha1 0.059523 0.031811 1.871111 0.061330
## alpha2 0.000000 0.039124 0.000000 1.000000
## beta1 0.646480 0.260381 2.482827 0.013034
## beta2
          ## beta3  0.201100  0.134967  1.489994 0.136226
## gamma1  0.190469  0.078855  2.415441 0.015716
## gamma2 -0.088559 0.034382 -2.575757 0.010002
## skew
          1.140811 0.036142 31.565090 0.000000
                   0.379058 10.246871 0.000000
## shape
          3.884155
##
## Robust Standard Errors:
##
         Estimate Std. Error t value Pr(>|t|)
## mu
         0.001054 0.000676 1.558484 0.119119
## ar1
        ## ar2
       ## omega 0.000033 0.000034 0.961252 0.336425
## alpha1 0.059523 0.029175 2.040181 0.041332
## alpha2 0.000000 0.067032 0.000000 1.000000
## beta1 0.646480 1.212700 0.533091 0.593970
## beta2  0.020015  1.457941  0.013728  0.989047  ## beta3  0.201100  0.529722  0.379633  0.704218
## gamma1 0.190469 0.131200 1.451742 0.146573
## gamma2 -0.088559 0.139867 -0.633165 0.526626
                   0.036937 30.885610 0.000000
## skew
          1.140811
## shape
          3.884155
                   0.433811 8.953565 0.000000
##
## LogLikelihood: 3788.483
## Information Criteria
## -----
##
## Akaike
             -4.3748
## Bayes
             -4.3338
## Shibata
             -4.3749
## Hannan-Quinn -4.3596
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
                         statistic p-value
## Lag[1]
                           5.180 0.0228521
## Lag[2*(p+q)+(p+q)-1][5]
                         5.525 0.0005007
## Lag[4*(p+q)+(p+q)-1][9]
                         7.442 0.0910641
## d.o.f=2
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
```

```
##
                        statistic p-value
                         0.4493 0.5027
## Lag[1]
## Lag[2*(p+q)+(p+q)-1][14] 4.9965 0.7699
## Lag[4*(p+q)+(p+q)-1][24] 7.8556 0.8835
## d.o.f=5
##
## Weighted ARCH LM Tests
## -----
##
            Statistic Shape Scale P-Value
## ARCH Lag[6] 0.3099 0.500 2.000 0.5777
## ARCH Lag[8]
              2.2315 1.480 1.774 0.4650
## ARCH Lag[10] 4.9553 2.424 1.650 0.2885
## Nyblom stability test
## -----
## Joint Statistic: 4.2696
## Individual Statistics:
## mu
        0.07754
## ar1
        0.10780
      0.18422
## ar2
## omega 0.11819
## alpha1 0.16731
## alpha2 0.16467
## beta1 0.15399
## beta2 0.15665
## beta3 0.14496
## gamma1 0.46409
## gamma2 0.34330
## skew 0.38176
## shape 0.09801
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 2.89 3.15 3.69
## Individual Statistic: 0.35 0.47 0.75
## Sign Bias Test
## -----
##
                  t-value prob sig
## Sign Bias
                  1.4753 0.1403
## Negative Sign Bias 1.4532 0.1464
## Positive Sign Bias 0.4157 0.6777
## Joint Effect 4.1384 0.2469
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
  group statistic p-value(g-1)
##
## 1 20 16.22
                    0.6422
    30 27.04
40 33.95
## 2
                      0.5698
## 3
                      0.6990
## 4
    50 58.24
                     0.1718
##
##
## Elapsed time : 5.343994
```

```
spec_of_garch_Ibhf<-ugarchspec(variance.model =list(model="gjrGARCH",garchOrder=c(3,2)),mean.model = li
my_model_Ibhf<-ugarchfit(spec=spec_of_garch_Ibhf,data=ret_Ibhf)
my_model_Ibhf</pre>
```

```
##
             GARCH Model Fit
## Conditional Variance Dynamics
## -----
## GARCH Model : gjrGARCH(3,2)
## Mean Model : ARFIMA(2,0,0)
## Distribution : sstd
##
## Optimal Parameters
## -----
          Estimate Std. Error t value Pr(>|t|)
## mu
          0.001128 0.000615 1.8347 0.066549
## ar1
        0.072365 0.024140 2.9978 0.002720
## ar2 -0.065047 0.021383 -3.0420 0.002350
## omega 0.000037 0.000021 1.7309 0.083463
## alpha1 0.065068 0.032236 2.0185 0.043540
## alpha2 0.000000 0.034374 0.0000 1.000000
## alpha3 0.000000 0.040866 0.0000 1.000000
## beta1 0.009208 0.076606 0.1202 0.904327
## beta2 0.840739 0.085386 9.8463 0.000000
## gamma1 0.224510 0.086102 2.6075 0.009121
## gamma2 0.057248 0.031493 1.8178 0.069095
## gamma3 -0.162727 0.082800 -1.9653 0.049380
## skew
          1.146201 0.036578 31.3362 0.000000
## shape
          ##
## Robust Standard Errors:
        Estimate Std. Error t value Pr(>|t|)
          ## mu
         0.072365 0.024010 3.013906 0.002579
-0.065047 0.021620 -3.008660 0.002624
## ar1
## ar2
## omega 0.000037 0.000038 0.958047 0.338039
## alpha1 0.065068 0.031524 2.064079 0.039010 ## alpha2 0.000000 0.053673 0.000000 1.000000
## alpha3 0.000000 0.054717 0.000000 1.000000
## beta1
          ## beta2  0.840739  0.118692  7.083374  0.000000  ## gamma1  0.224510  0.098281  2.284360  0.022350
## gamma2 0.057248 0.039464 1.450654 0.146876
## skew
                     0.038277 29.944745 0.000000
          1.146201
## shape
          ##
## LogLikelihood: 3792.226
##
## Information Criteria
```

```
##
## Akaike
            -4.3780
             -4.3338
## Bayes
## Shibata
            -4.3781
## Hannan-Quinn -4.3617
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
                        statistic p-value
## Lag[1]
                          4.445 0.034997
                        4.918 0.004366
7.053 0.122989
## Lag[2*(p+q)+(p+q)-1][5]
## Lag[4*(p+q)+(p+q)-1][9]
## d.o.f=2
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                         statistic p-value
## Lag[1]
                          0.2083 0.6481
## Lag[2*(p+q)+(p+q)-1][14] 3.3350 0.9349
## Lag[4*(p+q)+(p+q)-1][24] 5.7123 0.9764
## d.o.f=5
## Weighted ARCH LM Tests
## -----
              Statistic Shape Scale P-Value
## ARCH Lag[6] 0.6952 0.500 2.000 0.4044
## ARCH Lag[8] 2.6183 1.480 1.774 0.3921
## ARCH Lag[10] 3.7404 2.424 1.650 0.4548
## Nyblom stability test
## -----
## Joint Statistic: 4.7519
## Individual Statistics:
## mu
       0.08286
## ar1
      0.09231
      0.15823
## ar2
## omega 0.12329
## alpha1 0.12605
## alpha2 0.25059
## alpha3 0.13050
## beta1 0.20013
## beta2 0.12400
## gamma1 0.27244
## gamma2 0.52551
## gamma3 0.18678
## skew 0.38310
## shape 0.11013
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 3.08 3.34 3.9
## Individual Statistic: 0.35 0.47 0.75
##
```

```
## Sign Bias Test
## -----
                  t-value prob sig
##
## Sign Bias
                   1.3639 0.1728
## Negative Sign Bias 1.3069 0.1914
## Positive Sign Bias 0.4086 0.6829
## Joint Effect 3.5346 0.3163
##
##
## Adjusted Pearson Goodness-of-Fit Test:
  _____
##
    group statistic p-value(g-1)
## 1
      20 20.42 0.3697
      30 29.54
## 2
                       0.4373
## 3
      40 39.19
                       0.4613
## 4
      50 52.39
                       0.3439
##
##
## Elapsed time : 7.984991
spec_of_garch_Ibhf<-ugarchspec(variance.model =list(model="gjrGARCH",garchOrder=c(3,3)),mean.model = li</pre>
my_model_Ibhf<-ugarchfit(spec=spec_of_garch_Ibhf,data=ret_Ibhf)</pre>
my_model_Ibhf
## *----*
           GARCH Model Fit *
## *----*
##
## Conditional Variance Dynamics
## -----
## GARCH Model : gjrGARCH(3,3)
## Mean Model : ARFIMA(2,0,0)
## Distribution : sstd
##
## Optimal Parameters
## -----
         Estimate Std. Error t value Pr(>|t|)
         0.001129 0.000600 1.880848 0.059993
## mu
## ar1
        0.072422 0.024171 2.996234 0.002733
## ar2 -0.065078 0.021308 -3.054144 0.002257
## omega 0.000037 0.000022 1.724661 0.084589
## alpha1 0.067015 0.032471 2.063865 0.039030 ## alpha2 0.000000 0.013698 0.000000 1.000000
## alpha3 0.000000 0.024725 0.000001 1.000000
         0.000000 0.220539 0.000002 0.999999
## beta1
        0.830322 0.055624 14.927350 0.000000
## beta2
## beta3  0.016518  0.178791  0.092389  0.926389
## gamma1 0.223160 0.085007 2.625197 0.008660
## gamma2 0.056567 0.016273 3.476099 0.000509
                 0.073495 -2.173693 0.029728
## gamma3 -0.159757
```

1.146385 0.036316 31.567346 0.000000

3.967165 0.382898 10.360899 0.000000

skew

shape

##

```
## Robust Standard Errors:
##
   Estimate Std. Error t value Pr(>|t|)
## mu
       0.001129 0.000671 1.683727 0.092234
## ar1
        0.072422 0.024133 3.000897 0.002692
## ar2 -0.065078 0.021730 -2.994840 0.002746
## omega 0.000037 0.000037 1.012822 0.311145
## alpha1 0.067015 0.029701 2.256282 0.024053
## alpha2 0.000000 0.052267 0.000000 1.000000
## alpha3 0.000000 0.042346 0.000000 1.000000
## beta1 0.000000 0.479493 0.000001 0.999999
## beta2  0.830322  0.069474 11.951608 0.000000
## gamma2 0.056567 0.051172 1.105433 0.268972
1.146385 0.037583 30.502972 0.000000
## skew
## shape
         3.967165 0.406492 9.759518 0.000000
##
## LogLikelihood : 3792.271
## Information Criteria
## -----
##
## Akaike
            -4.3769
## Bayes
            -4.3295
## Shibata
            -4.3771
## Hannan-Quinn -4.3594
## Weighted Ljung-Box Test on Standardized Residuals
##
                       statistic p-value
## Lag[1]
                          4.422 0.035478
## Lag[2*(p+q)+(p+q)-1][5]
                         4.894 0.004739
## Lag[4*(p+q)+(p+q)-1][9]
                        7.041 0.124115
## d.o.f=2
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                        statistic p-value
## Lag[1]
                         0.1797 0.6717
## Lag[2*(p+q)+(p+q)-1][17] 4.1031 0.9497
## Lag[4*(p+q)+(p+q)-1][29] 6.9471 0.9848
## d.o.f=6
## Weighted ARCH LM Tests
             Statistic Shape Scale P-Value
## ARCH Lag[7] 1.374 0.500 2.000 0.2411
                3.485 1.485 1.796 0.2703
## ARCH Lag[9]
## ARCH Lag[11] 3.735 2.440 1.677 0.4694
## Nyblom stability test
## -----
```

```
## Joint Statistic: 5.5108
## Individual Statistics:
       0.08405
## ar1
      0.09504
      0.15991
## ar2
## omega 0.12216
## alpha1 0.13096
## alpha2 0.23145
## alpha3 0.13153
## beta1 0.19178
## beta2 0.12219
## beta3 0.19311
## gamma1 0.27985
## gamma2 0.50096
## gamma3 0.18707
## skew 0.37978
## shape 0.11024
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 3.26 3.54 4.07
## Individual Statistic: 0.35 0.47 0.75
## Sign Bias Test
## -----
                t-value prob sig
##
                  1.3850 0.1662
## Sign Bias
## Negative Sign Bias 1.3116 0.1898
## Positive Sign Bias 0.3619 0.7174
## Joint Effect 3.5021 0.3205
##
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
## group statistic p-value(g-1)
## 1 20 20.67 0.3551
## 2 30 29.68
                       0.4302
## 3 40 39.98
                       0.4265
## 4 50 52.91
                       0.3256
##
##
## Elapsed time : 8.577
going further is not leading any good results
spec_of_garch_Ibhf<-ugarchspec(variance.model =list(model="gjrGARCH",garchOrder=c(1,3)),mean.model = li</pre>
my_model_Ibhf<-ugarchfit(spec=spec_of_garch_Ibhf,data=ret_Ibhf,out.sample = 500)</pre>
my_model_Ibhf
## *----*
          GARCH Model Fit *
## *----*
##
```

```
## Conditional Variance Dynamics
## -----
## GARCH Model : gjrGARCH(1,3)
## Mean Model : ARFIMA(2,0,0)
## Distribution : sstd
##
## Optimal Parameters
## -----
##
         Estimate Std. Error t value Pr(>|t|)
## mu
        0.001560 0.000666 2.34266 0.019147
## ar1
        ## ar2
        -0.031310 0.027686 -1.13091 0.258095
## omega 0.000063 0.000045 1.39592 0.162738
## alpha1 0.100172 0.045661 2.19380 0.028250
## beta1 0.542046 0.116956 4.63462 0.000004
## beta2 0.000000 0.323474 0.00000 1.000000
## beta3 0.242930 0.110726 2.19397 0.028237
## skew
         1.189087 0.047416 25.07765 0.000000
## shape 5.199244
                  0.772588 6.72964 0.000000
##
## Robust Standard Errors:
         Estimate Std. Error t value Pr(>|t|)
##
         0.001560 0.000698 2.23697 0.025288
## mu
## ar1
        ## ar2 -0.031310 0.027768 -1.12755 0.259509
## omega 0.000063 0.000066 0.95419 0.339986
## alpha1 0.100172 0.056322 1.77856 0.075312
## beta1 0.542046 0.182118 2.97634 0.002917
## beta2  0.000000  0.300917  0.00000 1.000000
## beta3  0.242930  0.236647  1.02655  0.304632
## gamma1 -0.007170  0.045679 -0.15697  0.875270
## skew
         1.189087
                 0.049133 24.20158 0.000000
         5.199244
                    0.692375 7.50929 0.000000
## shape
## LogLikelihood : 2963.23
##
## Information Criteria
## -----
##
## Akaike
             -4.8160
## Bayes
             -4.7702
## Shibata
             -4.8162
## Hannan-Quinn -4.7988
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
                       statistic p-value
## Lag[1]
                         0.3346 0.5630
## Lag[2*(p+q)+(p+q)-1][5]
                         2.5356 0.7595
## Lag[4*(p+q)+(p+q)-1][9]
                       4.2306 0.6362
## d.o.f=2
## HO : No serial correlation
##
```

```
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                          statistic p-value
                         2.133e-05 0.9963
## Lag[1]
## Lag[2*(p+q)+(p+q)-1][11] 9.231e+00 0.1317
## Lag[4*(p+q)+(p+q)-1][19] 1.692e+01 0.0468
## d.o.f=4
##
## Weighted ARCH LM Tests
## -----
             Statistic Shape Scale P-Value
## ARCH Lag[5] 2.429 0.500 2.000 0.11915
## ARCH Lag[7] 3.652 1.473 1.746 0.23521
## ARCH Lag[9] 11.574 2.402 1.619 0.01202
## Nyblom stability test
## Joint Statistic: 5.5856
## Individual Statistics:
## mu
        0.12297
## ar1
       0.11597
## ar2 0.02438
## omega 0.53029
## alpha1 0.77417
## beta1 0.57518
## beta2 0.50637
## beta3 0.53744
## gamma1 0.48248
## skew 0.10816
## shape 0.10687
##
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 2.49 2.75 3.27
## Individual Statistic: 0.35 0.47 0.75
## Sign Bias Test
## -----
##
                   t-value prob sig
## Sign Bias
                   1.1275 0.2597
## Negative Sign Bias 1.1449 0.2525
## Positive Sign Bias 0.5204 0.6029
## Joint Effect 1.7125 0.6342
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
   group statistic p-value(g-1)
##
## 1 20 13.90
                      0.7894
## 2 30 28.57
## 3 40 33.77
## 4 50 53.93
                         0.4877
                    0.7069
0.2913
##
##
## Elapsed time : 3.696997
```

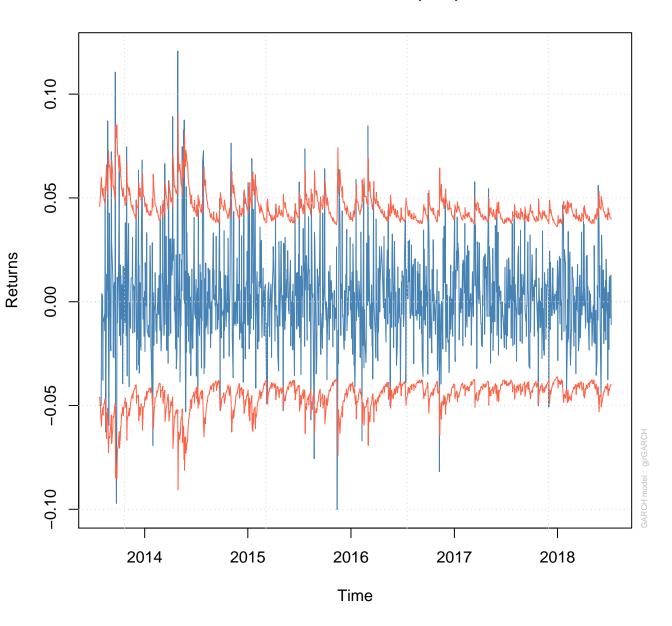
```
##
## Iter: 1 fn: -3469.3672
                    Pars:
                          0.00105627 0.09311132 -0.05976516 0.00002873 0.07005112 0.4656
## Iter: 2 fn: -3469.3672
                    Pars:
                          0.00105628 0.09311103 -0.05976585 0.00002873 0.07004858 0.4656
## Iter: 3 fn: -3469.3672
                          0.00105628 0.09311103 -0.05976585 0.00002873 0.07004858 0.4656
                    Pars:
## solnp--> Completed in 3 iterations
##
## Iter: 1 fn: -3464.5520
                           Pars:
## Iter: 2 fn: -3464.5520
                          Pars:
## solnp--> Completed in 2 iterations
##
## Iter: 1 fn: -3442.2912
                     Pars:
                          0.001207506 \quad 0.085185506 \quad -0.070550940 \quad 0.000034297 \quad 0.057424288 \quad 0
## Iter: 2 fn: -3442.2912
                     Pars: 0.001207506 0.085185506 -0.070550940 0.000034297 0.057424288 0
## solnp--> Completed in 2 iterations
##
## Iter: 1 fn: -3417.8987
                    Pars: 0.00131826 0.07967348 -0.05633088 0.00003327 0.06309338 0.1400
## Iter: 2 fn: -3417.8987
                     Pars:
                          ## Iter: 3 fn: -3417.8987
                     Pars:
                          ## solnp--> Completed in 3 iterations
##
## Iter: 1 fn: -3402.6756
                     Pars:
                          ## Iter: 2 fn: -3402.6756
                     Pars:
                          ## Iter: 3 fn: -3402.6756
                     Pars:
                          ## solnp--> Completed in 3 iterations
## Iter: 1 fn: -3359.8920
                          0.00123969 0.07869656 -0.05790131 0.00003522 0.06329162 0.1415
                    Pars:
## Iter: 2 fn: -3359.8920
                     Pars:
                          0.00123969 0.07869656 -0.05790131 0.00003522 0.06329162 0.1415
## solnp--> Completed in 2 iterations
## Iter: 1 fn: -3337.5695
                          Pars:
## Iter: 2 fn: -3337.5695
                    Pars: 0.00104078 0.07357411 -0.06306549 0.00003614 0.06159288 0.1127
## solnp--> Completed in 2 iterations
##
                          0.00107483 \quad 0.07048172 \quad -0.06831731 \quad 0.00004256 \quad 0.08153163 \quad 0.0742
## Iter: 1 fn: -3322.9101
                     Pars:
## Iter: 2 fn: -3322.9101
                     Pars:
                          ## solnp--> Completed in 2 iterations
```

report(back_testing)

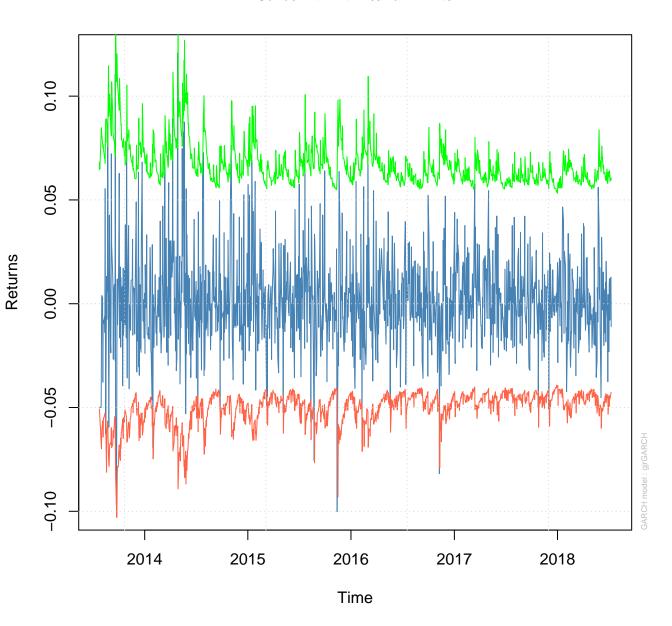
```
## Unconditional Coverage (Kupiec)
## Null-Hypothesis: Correct Exceedances
## LR.uc Statistic: 4.3
## LR.uc Critical:
                        3.841
## LR.uc p-value:
                        0.038
## Reject Null:
                    YES
## Conditional Coverage (Christoffersen)
## Null-Hypothesis: Correct Exceedances and
                    Independence of Failures
## LR.cc Statistic: 4.628
## LR.cc Critical:
                        5.991
## LR.cc p-value:
                        0.099
## Reject Null:
                    NO
```

forecast<- ugarchforecast(my_model_Ibhf,data=ret_Ibhf,n.ahead =100,n.roll = 100)</pre>

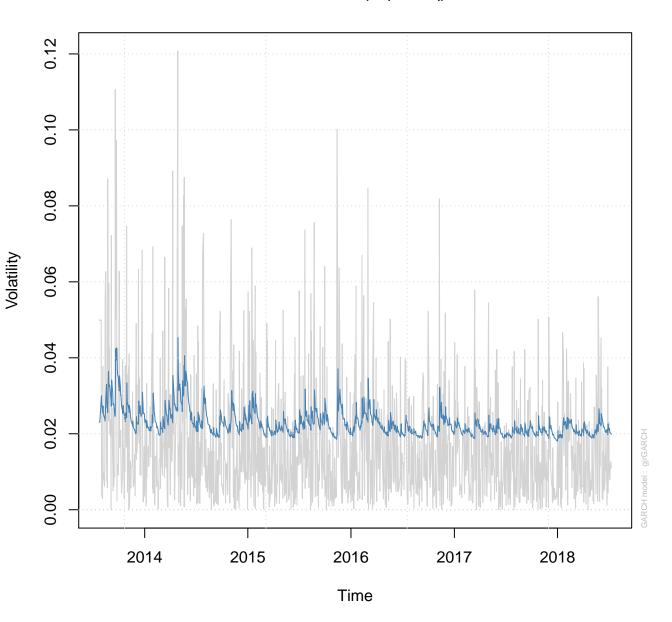
Series with 2 Conditional SD Superimposed



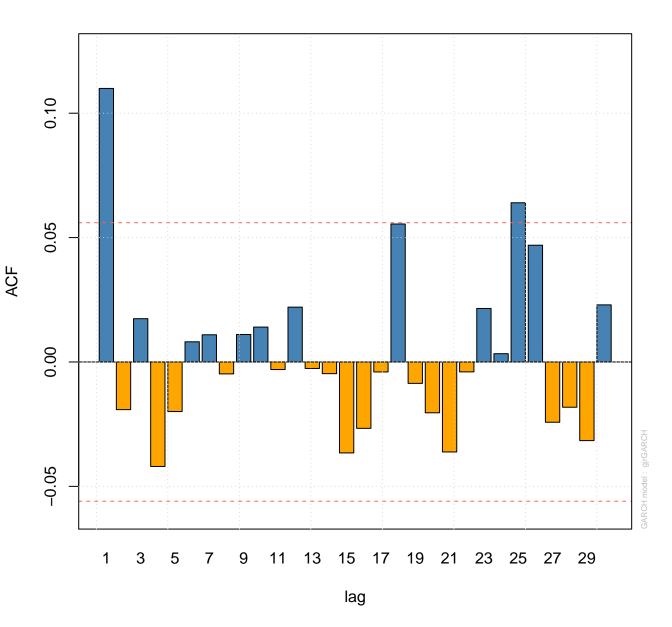
Series with with 1% VaR Limits



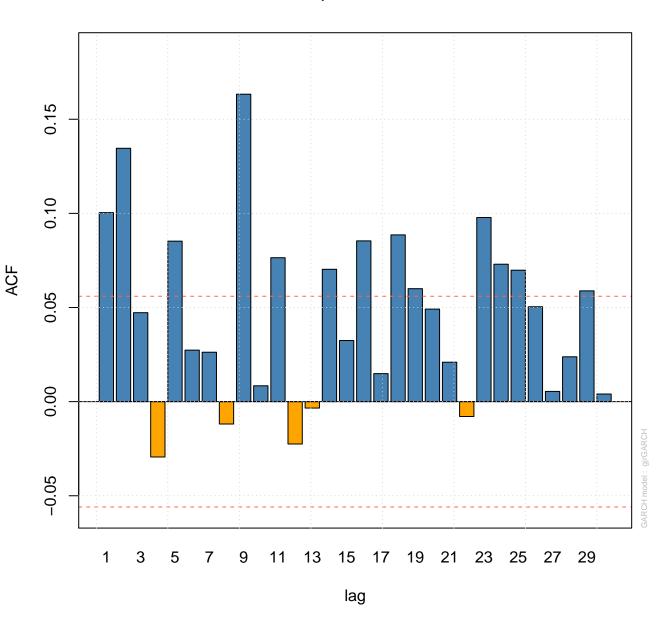
Conditional SD (vs |returns|)



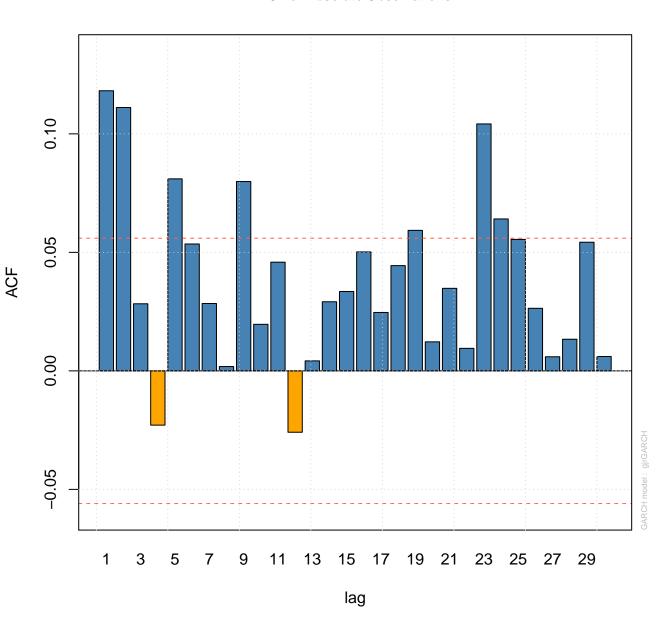
ACF of Observations



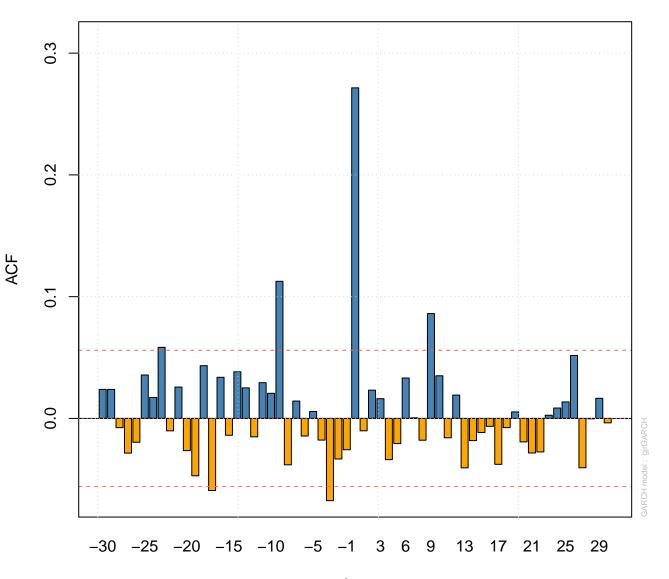
ACF of Squared Observations



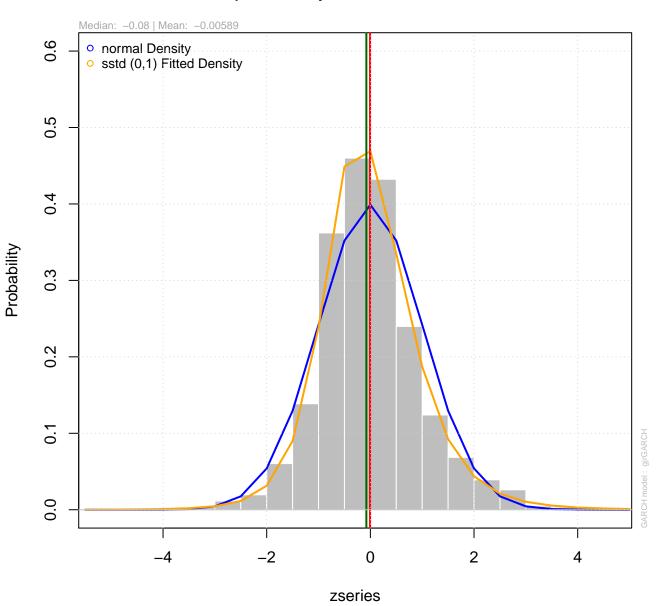
ACF of Absolute Observations



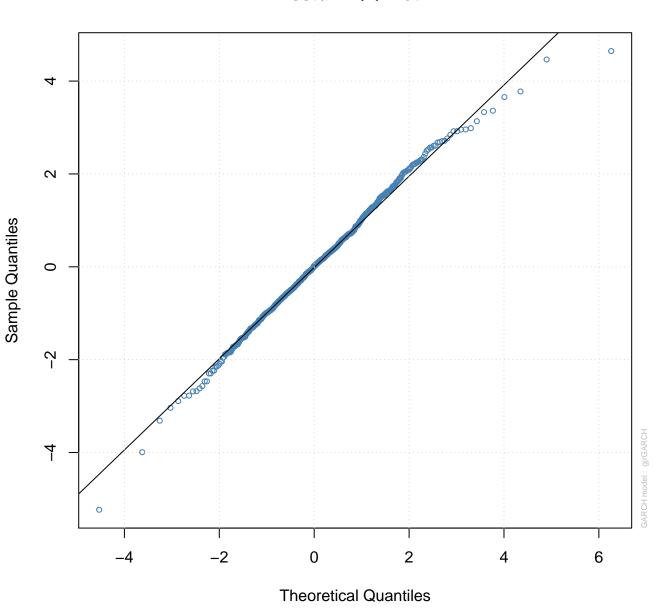
Cross-Correlations of Squared vs Actual Observations



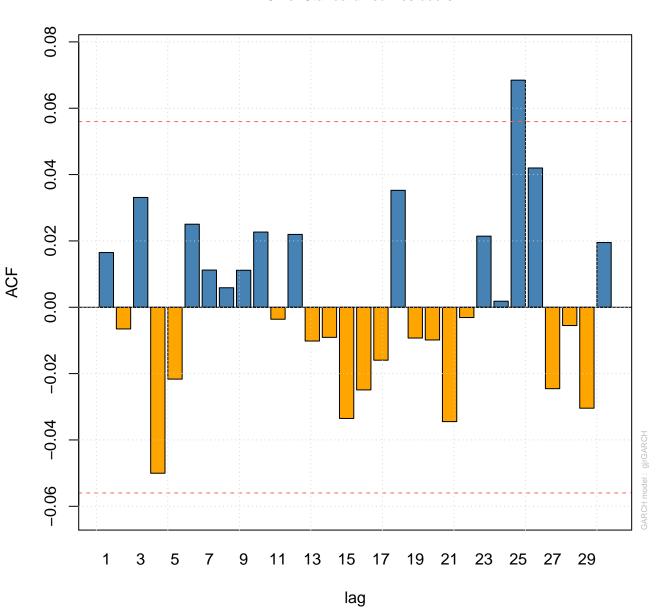
Empirical Density of Standardized Residuals



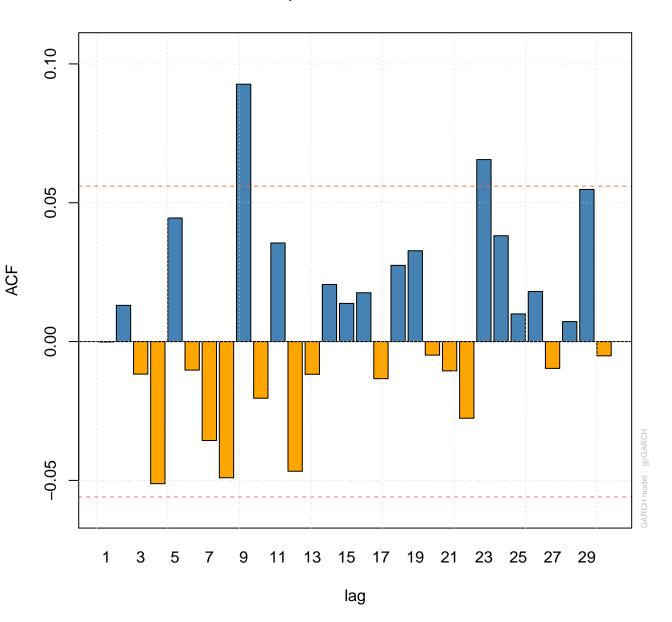
sstd - QQ Plot



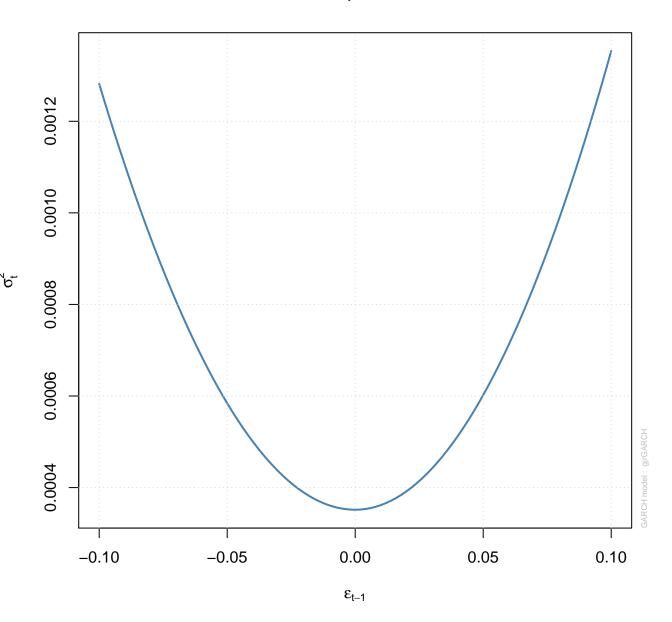
ACF of Standardized Residuals



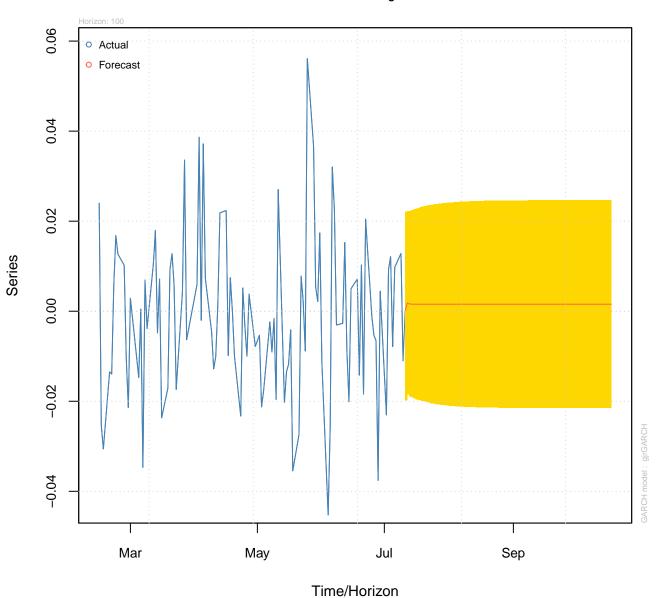
ACF of Squared Standardized Residuals



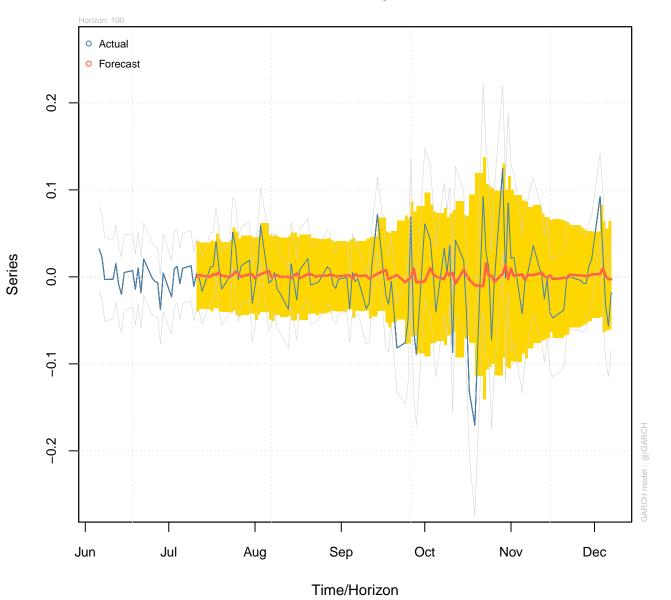
News Impact Curve



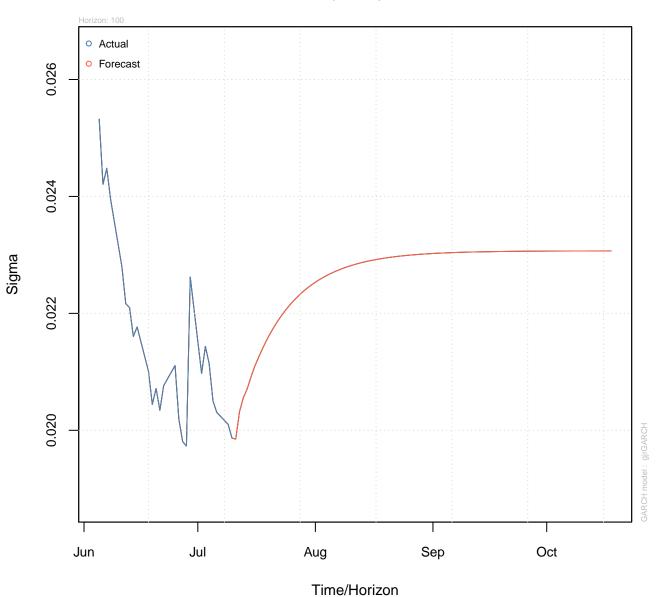
Forecast Series w/th unconditional 1-Sigma bands



Rolling Forecast vs Actual Series w/th conditional 2-Sigma bands



Forecast Unconditional Sigma (n.roll = 0)



Forecast Rolling Sigma vs |Series|

