Assignment-10

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Satyam Singh EE20MTECH14015

Abstract—This assignment deals with vector spaces.

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https://github.com/satyam463/Assignment-10/blob/main/Assignment%2010.tex

1 Problem Statement

Let V be the set of all pairs (x,y) of real numbers and let F be the field of real numbers. Define

$$(x, y) + (x_1, y_1) = (x + x_1, y + y_1)$$
 (1.0.1)

$$c(x, y) = (cx, y)$$
 (1.0.2)

Is V with these operations, a vector space over the field of real numbers?

2 Solution

 $V=\{(x,y) \mid x,y\in R\}$, consider $u=(x_1,y_1)\in V,a,b,c\in R$. Axioms with respect to addition and scalar multiplication.

1)

$$(a+b)u = (a+b)(x_1, y_1)$$
 (2.0.1)

$$= ((a+b)x_1, y_1) \neq au + bu$$
 (2.0.2)

Since V with the given operations the equation 2.0.2 contradicts the axioms of scalar multiplication . Hence it is not vector space over real number with these operations.