Assignment-13

Satyam Singh EE20MTECH14015

 $\begin{subarray}{c} Abstract{--} \\ \begin{subarray}{c} This assignment deals with linear transformation. \end{subarray}$

Download tex file from

https://github.com/satyam463/Assignment-13/blob/main/Assignment%2013.tex

1 Problem Statement

Describe explicitly a linear transformation from R^3 into R^3 which has as its range the subspace spanned by $\begin{pmatrix} 1 & 0 & -1 \end{pmatrix}$ and $\begin{pmatrix} 1 & 2 & 2 \end{pmatrix}$.

2 Solution

Transformation T from R^3 to R^3 range gives the column space and kernel (null space) is $T(\mathbf{x})=0$

$$\mathbf{A}\mathbf{x} = 0 \implies \begin{pmatrix} 1 & 1 \\ 0 & 2 \\ -1 & 2 \end{pmatrix} \mathbf{x} = 0 \tag{2.0.1}$$

Hence,

$$T(\mathbf{x}) = \mathbf{A}\mathbf{x} \tag{2.0.2}$$

$$T(\mathbf{x}) = \begin{pmatrix} 1 & 1 \\ 0 & 2 \\ -1 & 2 \end{pmatrix} \mathbf{x}$$
 (2.0.3)

1