

Assignment 20

Satyam Singh
EE20MTECH14015

Abstract—This document explains the ideals of polynomial.

Download all latex codes from

<https://github.com/satyam463/Assignment-20/blob/main/Assignment%2020%20.tex>

1 PROBLEM STATEMENT

Let F be a field, show that the intersection of any numbers of ideals in $F[x]$ is an ideal.

2 SOLUTION

Given	F is a field.
To prove	$I = \bigcap_{\alpha \in A} I_{\alpha}$ is an ideal.
Proof	<p>Let A be a set and I_{α} be an ideal in $F[x]$ for each $\alpha \in A$</p> <p>Obviously I is the subspace since I_{α} is a subspace of $F[x]$ and arbitrary intersection of subspace is also a subspace.</p> <p>Let $g(x) \in F[x]$ and $f(x) \in I$</p> <p>Since $f(x) \in I$ and I_{α} is an ideal follows that</p> <p>$f(x)g(x) \in I_{\alpha} \forall \alpha \in A$</p> <p>Thus $f(x)g(x) \in I$.</p>

TABLE 0: solution