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Challenge Problem-1(*EE*5600)

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Abstract—This assignment deals with basic coordinate geometry.

Download tex file from

https://github.com/satyam463/EE5600Ass1/blob/main/challengeproblem1.tex

1 Problem Statement

1.1 Vector2, Example-1, 21

Find the coordinates of the point which divides internally and externally, line joining the points (a + b, a - b) to the point (a - b, a + b) in the ratio a:b.

2 Solution

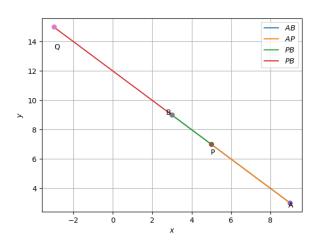


Fig. 0: Line joining AB with $\mathbf{A} \begin{pmatrix} 9 \\ 3 \end{pmatrix}$, $\mathbf{B} \begin{pmatrix} 3 \\ 9 \end{pmatrix}$ where as $\begin{pmatrix} a \\ b \end{pmatrix} = \begin{pmatrix} 6 \\ 3 \end{pmatrix}$ are used for python plot. The point of section $\mathbf{P}(internally) = \begin{pmatrix} 5 \\ 7 \end{pmatrix}$, $\mathbf{Q}(externally) = \begin{pmatrix} -3 \\ 15 \end{pmatrix}$.

Given:

$$\mathbf{A} = \begin{pmatrix} a+b \\ a-b \end{pmatrix}, \mathbf{B} = \begin{pmatrix} a-b \\ a+b \end{pmatrix}$$
 (2.0.1)

The line joining AB divided into the ratio a:b at point of division P(say) internally can be written by using section formula

$$\mathbf{P} = \frac{a\mathbf{B} + b\mathbf{A}}{a + b} \tag{2.0.2}$$

$$\mathbf{P} = \frac{1}{a+b} \begin{pmatrix} \mathbf{B} & \mathbf{A} \end{pmatrix} \begin{pmatrix} a \\ b \end{pmatrix} \tag{2.0.3}$$

Now,the line joining AB divided into the ratio a:b at point of division $\mathbf{Q}(say)$ externally can be written by using section formula

$$\mathbf{Q} = \frac{a\mathbf{B} - b\mathbf{A}}{a - b} \tag{2.0.4}$$

$$\mathbf{Q} = \frac{1}{a - b} \begin{pmatrix} \mathbf{B} & \mathbf{A} \end{pmatrix} \begin{pmatrix} a \\ -b \end{pmatrix} \tag{2.0.5}$$