1 Problem Statement

Find the equation of the line parallel to the Y-axis drawn through the point of intersection of the lines

$$\begin{pmatrix} 1 & -7 \end{pmatrix} \mathbf{x} = -5 \text{ and } \begin{pmatrix} 3 & 1 \end{pmatrix} \mathbf{x} = \mathbf{0} \tag{1}$$

2 Theory

consider the equation of the system of lines

$$x - 7y = -5 \tag{2}$$

$$3x + y = 0 (3)$$

consider the augmented matrix

$$\begin{pmatrix} 1 & -7 & -5 \\ 3 & 1 & 0 \end{pmatrix} \tag{4}$$

By applying row reduction reduction technique

$$\begin{pmatrix} 4 & -7 & -5 \\ 3 & 1 & 0 \end{pmatrix} \xrightarrow{R_2 \to R_2 - 3R_1} \begin{pmatrix} 1 & -7 & -5 \\ 0 & 1 & \frac{15}{22} \end{pmatrix} \xrightarrow{R_1 \to R_1 + 7R_2} \begin{pmatrix} 1 & 0 & \frac{-5}{22} \\ 0 & 1 & \frac{15}{22} \end{pmatrix}$$
(5)

The value of
$$\mathbf{A} = \begin{pmatrix} \frac{-5}{22} \\ \frac{15}{22} \end{pmatrix}$$
; A is the point of intersection. (6)

Now the equation of line parallel to y-axis through the point of intersection

$$\mathbf{n}^{\mathbf{T}}\mathbf{x} - \mathbf{A} = \mathbf{0} \tag{7}$$

where \vec{n} is the vector normal to the Y-axis and A is the point of intersection.

$$\begin{pmatrix} 1 \\ 0 \end{pmatrix} \boldsymbol{x} = \begin{pmatrix} \frac{-5}{22} \\ \frac{15}{22} \end{pmatrix} \tag{8}$$

$$\boldsymbol{x} = \left(\frac{-5}{22}\right) \tag{9}$$

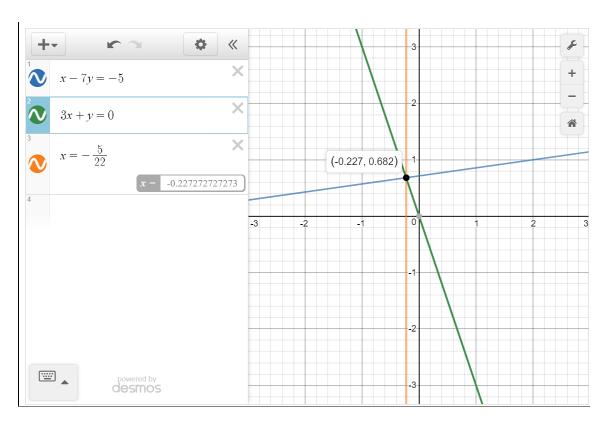


Figure 1: graphical representation of systems of lines