1 Problem Statement

Find the equation of the line parallel to the Y-axis drawn through the point of intersection of the lines

$$(1-7)\tilde{\mathbf{x}} = -5 \text{ and } (31)\tilde{\mathbf{x}} = \mathbf{0} \tag{1}$$

2 Theory

consider the equation of the system of lines

$$x - 7y = -5 \tag{2}$$

$$3x + y = 0 (3)$$

consider the augmented matrix

$$\begin{pmatrix} 1 & -7 & -5 \\ 3 & 1 & 0 \end{pmatrix} \tag{4}$$

By applying row reduction reduction technique

$$\begin{pmatrix} 4 & -7 & -5 \\ 3 & 1 & 0 \end{pmatrix} \xrightarrow{R_2 \to R_2 - 3R_1} \begin{pmatrix} 1 & -7 & -5 \\ 0 & 1 & \frac{15}{22} \end{pmatrix} \xrightarrow{R_1 \to R_1 + 7R_2} \begin{pmatrix} 1 & 0 & \frac{-5}{22} \\ 0 & 1 & \frac{15}{22} \end{pmatrix}$$
(5)

Therefore the value of $x = \frac{-5}{22}(-0.2272)$ and $y = \frac{15}{22}(0.6818)$

The required x and y is the point of intersection of lines

Now the equation of line parallel to y-axis through the point of intersection

$$\vec{x} = \begin{pmatrix} 1 & 0 \end{pmatrix} \begin{pmatrix} \frac{-5}{22} \\ \frac{15}{22} \end{pmatrix} \tag{6}$$

$$\vec{x} = \left(\frac{-5}{22}\right) \tag{7}$$

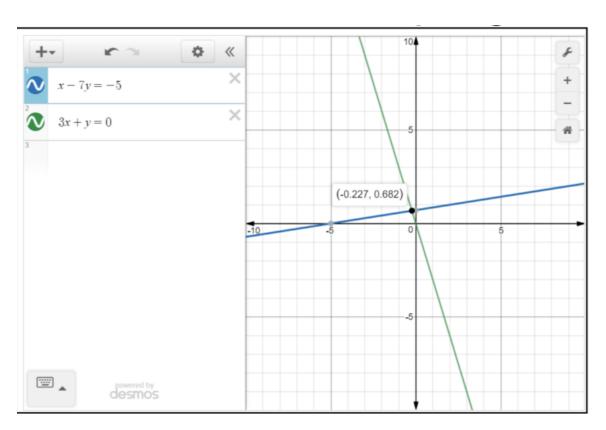


Figure 1: graphical representation of two lines