A. Revisiting Python Basics & Libraries

```
# Importing essential libraries
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
from sklearn.linear model import LinearRegression
# 1. NUMPY - Creating and manipulating arrays
arr = np.array([1, 2, 3, 4, 5]) # Create a NumPy array
print("NumPy Array:", arr)
# 2. PANDAS - Creating and displaying a DataFrame
data = {'Name': ['Alice', 'Bob'], 'Age': [25, 30]}
df = pd.DataFrame(data) # Create a Pandas DataFrame
print("\nPandas DataFrame:\n", df)
# 3. MATPLOTLIB - Simple line plot
plt.plot([1, 2, 3], [4, 5, 6]) # Plot x vs y
plt.title("Simple Plot") # Add title
plt.show() # Display plot
# 4. SKLEARN - Simple Linear Regression
X = [[1], [2], [3]] # Features
y = [2, 4, 6]
               # Target
model = LinearRegression().fit(X, y) # Train model
print("\nSklearn Prediction for 4:", model.predict([[4]]))
```

B. Optical Character Recognition (OCR) using Pytesseract

(i) OCR from an Image File

```
from PIL import Image # To handle images
import pytesseract # OCR library

# Provide the path to Tesseract executable (if not in PATH)

# pytesseract.pytesseract.tesseract_cmd = r'C:\Program Files\Tesseract-OCR\tesseract.exe'

# Open an image file
img = Image.open("sample_image.png") # Replace with your image path

# Extract text from the image
text = pytesseract.image_to_string(img)
print("Extracted Text from Image:\n", text)
```

(ii) OCR from a Multi-Page PDF File

```
import pdf2image # Convert PDF to images
```

import pytesseract # OCR library

from PIL import Image # To handle images

Convert PDF pages to images (one image per page)

images = pdf2image.convert_from_path("sample.pdf") # Replace with your PDF path

Loop through each page/image and extract text

for i, img in enumerate(images):

```
text = pytesseract.image_to_string(img) # Extract text
print(f"\nText from Page {i+1}:\n", text) # Print extracted text
```

Key Notes:

Install required libraries first:

pip install numpy pandas matplotlib scikit-learn pillow pytesseract pdf2image

1. Simple Linear Regression (One Variable)

(A) Gradient Descent Approach

```
import numpy as np
import matplotlib.pyplot as plt
# Sample data (X: feature, y: target)
X = np.array([1, 2, 3, 4, 5])
y = np.array([2, 4, 5, 4, 5])
# Initialize parameters (slope 'm' and intercept 'b')
m, b = 0, 0
learning_rate = 0.01
epochs = 1000
# Gradient Descent
for _ in range(epochs):
  y_pred = m * X + b # Predicted y
  error = y_pred - y # Error
  # Compute gradients (derivatives of MSE w.r.t 'm' and 'b')
  grad_m = (2/len(X)) * np.sum(error * X)
  grad_b = (2/len(X)) * np.sum(error)
  # Update parameters
  m -= learning_rate * grad_m
  b -= learning_rate * grad_b
print(f"Final Parameters: m = {m:.2f}, b = {b:.2f}")
```

```
# Plotting
plt.scatter(X, y, color='blue', label='Actual Data')
plt.plot(X, m * X + b, color='red', label='Regression Line')
plt.xlabel('X')
plt.ylabel('y')
plt.legend()
plt.show()
```

(B) Normal Equation Approach (Closed-form Solution)

import numpy as np

```
X = np.array([1, 2, 3, 4, 5])

y = np.array([2, 4, 5, 4, 5])

# Add a column of 1s for intercept (b)

X_matrix = np.vstack([X, np.ones(len(X))]).T

# Normal Equation: θ = (X<sup>T</sup>X)<sup>-1</sup> X<sup>T</sup>y

theta = np.linalg.inv(X_matrix.T @ X_matrix) @ X_matrix.T @ y

m, b = theta[0], theta[1]

print(f"Parameters (Normal Eq.): m = {m:.2f}, b = {b:.2f}")
```

2. Multiple Linear Regression (Multiple Variables)

(A) Gradient Descent Approach

```
import numpy as np
# Sample data (X1, X2: features, y: target)
X = np.array([[1, 2], [2, 4], [3, 6], [4, 8], [5, 10]])
y = np.array([3, 5, 7, 9, 11])
# Add bias term (column of 1s)
X_b = np.c_{np.ones}((X.shape[0], 1)), X] # Shape: (5, 3)
# Initialize parameters (theta = [bias, weight1, weight2])
theta = np.zeros(X_b.shape[1])
learning_rate = 0.01
epochs = 1000
# Gradient Descent
for _ in range(epochs):
  y_pred = X_b @ theta # Predicted y
  error = y_pred - y
  # Compute gradient (MSE derivative)
  gradient = (2/len(X)) * X_b.T @ error
  # Update theta
  theta -= learning_rate * gradient
print("Final Parameters (Gradient Descent):", theta)
# Predict for new data
new_X = np.array([[6, 12], [7, 14]])
new_X_b = np.c_[np.ones((new_X.shape[0], 1)), new_X]
predictions = new_X_b @ theta
print("Predictions:", predictions)
```

(B) Normal Equation Approach (Closed-form Solution)

import numpy as np

```
X = np.array([[1, 2], [2, 4], [3, 6], [4, 8], [5, 10]])
y = np.array([3, 5, 7, 9, 11])

# Add bias term (column of 1s)

X_b = np.c_[np.ones((X.shape[0], 1)), X]

# Normal Equation: θ = (X<sup>T</sup>X)<sup>-1</sup> X<sup>T</sup>y
theta = np.linalg.inv(X_b.T @ X_b) @ X_b.T @ y

print("Parameters (Normal Eq.):", theta)

# Predict for new data
new_X = np.array([[6, 12], [7, 14]])
new_X_b = np.c_[np.ones((new_X.shape[0], 1)), new_X]
predictions = new_X_b @ theta
print("Predictions:", predictions)
```

Key Notes:

1. Gradient Descent:

- Iteratively updates parameters to minimize the Mean Squared Error (MSE).
- Requires tuning learning rate and epochs.
- Works well for large datasets.

2. Normal Equation:

- o Directly computes the optimal parameters using matrix operations.
- No iterations needed, but slower for large datasets (due to matrix inversion).

3. Multiple Linear Regression:

- Extends to n features by adding columns to X.
- The bias term (intercept) is added as a column of 1s.

4. Matrix Operations (@ operator in NumPy):

- \circ X.T → Transpose of X.
- o np.linalg.inv() → Matrix inverse.
- A @ B → Matrix multiplication.

1. Manual Implementation (Without Sklearn)

(A) Simple & Multiple Linear Regression (No Regularization)

(Same as previous answer, but consolidated for clarity.)

Gradient Descent Approach

```
import numpy as np
def gradient_descent(X, y, learning_rate=0.01, epochs=1000):
  # Add bias term (column of 1s)
  X_b = np.c_[np.ones((X.shape[0], 1)), X]
  theta = np.zeros(X_b.shape[1]) # Initialize parameters
  for _ in range(epochs):
    y_pred = X_b @ theta
    error = y_pred - y
    gradient = (2 / len(X)) * X_b.T @ error # MSE derivative
    theta -= learning_rate * gradient
  return theta
# Example Usage:
X = np.array([[1, 2], [2, 4], [3, 6]]) # Multiple features
y = np.array([3, 5, 7])
theta = gradient_descent(X, y)
print("Manual Gradient Descent Coefficients:", theta)
```

Normal Equation Approach

```
def normal_equation(X, y):
    X_b = np.c_[np.ones((X.shape[0], 1)), X]
    theta = np.linalg.inv(X_b.T @ X_b) @ X_b.T @ y
    return theta
theta = normal_equation(X, y)
print("Manual Normal Equation Coefficients:", theta)
```

(B) Linear Regression with L2 Regularization (Ridge Regression) Gradient Descent with L2 Penalty

```
def ridge_gradient_descent(X, y, alpha=1.0, learning_rate=0.01, epochs=1000):
    X_b = np.c_[np.ones((X.shape[0], 1)), X]
    theta = np.zeros(X_b.shape[1])
    for _ in range(epochs):
        y_pred = X_b @ theta
        error = y_pred - y
        # Gradient with L2 penalty (exclude bias term)
        gradient = (2 / len(X)) * (X_b.T @ error + alpha * np.r_[0, theta[1:]])
        theta -= learning_rate * gradient
    return theta

theta_ridge = ridge_gradient_descent(X, y, alpha=1.0)
print("Manual Ridge Regression Coefficients:", theta_ridge)
```

Normal Equation with L2 Penalty

```
def ridge_normal_equation(X, y, alpha=1.0):
    X_b = np.c_[np.ones((X.shape[0], 1)), X]
    I = np.eye(X_b.shape[1])
    I[0, 0] = 0 # Don't regularize bias term
    theta = np.linalg.inv(X_b.T @ X_b + alpha * I) @ X_b.T @ y
    return theta

theta_ridge = ridge_normal_equation(X, y, alpha=1.0)
print("Manual Ridge (Normal Eq.) Coefficients:", theta_ridge)
```

2. Sklearn Implementation

(A) Simple & Multiple Linear Regression (No Regularization)

from sklearn.linear_model import LinearRegression

```
model = LinearRegression()
model.fit(X, y)

print("Sklearn Coefficients:", model.coef_)
print("Sklearn Intercept:", model.intercept_)
```

(B) Ridge Regression (L2 Regularization)

from sklearn.linear_model import Ridge

```
ridge_model = Ridge(alpha=1.0)
ridge_model.fit(X, y)

print("Sklearn Ridge Coefficients:", ridge_model.coef_)
print("Sklearn Ridge Intercept:", ridge_model.intercept_)
```

(C) Lasso Regression (L1 Regularization)

from sklearn.linear_model import Lasso

```
lasso_model = Lasso(alpha=0.1)
lasso_model.fit(X, y)
print("Sklearn Lasso Coefficients:", lasso_model.coef_)
print("Sklearn Lasso Intercept:", lasso_model.intercept_)
```

(D) ElasticNet (L1 + L2 Regularization)

```
from sklearn.linear_model import ElasticNet
```

```
elastic_model = ElasticNet(alpha=0.1, l1_ratio=0.5)
elastic_model.fit(X, y)

print("Sklearn ElasticNet Coefficients:", elastic_model.coef_)
print("Sklearn ElasticNet Intercept:", elastic_model.intercept_)
```

Key Notes:

1. Manual Implementation:

- Gradient Descent: Iterative optimization (better for large datasets).
- Normal Equation: Direct solution (faster for small datasets).
- L2 Regularization (Ridge): Adds alpha * theta² penalty to loss.

2. Sklearn Implementation:

- LinearRegression: No regularization.
- Ridge: L2 regularization (alpha controls strength).
- Lasso: L1 regularization (sparse solutions).
- ElasticNet: Mix of L1 + L2.

3. When to Use Regularization?

- o Ridge (L2): When features are correlated.
- Lasso (L1): For feature selection (zeroes out weak features).
- ElasticNet: Balanced L1 + L2 penalty.

1. Bernoulli Naïve Bayes (Binary Features)

Use Case: Spam detection (words present: 1 or absent: 0)

```
# Import libraries

from sklearn.naive_bayes import BernoulliNB

from sklearn.datasets import make_classification

from sklearn.model_selection import train_test_split

# Generate synthetic binary data (1000 samples, 10 features)

X, y = make_classification(n_samples=1000, n_features=10, n_classes=2, random_state=42)

# Split data into training (70%) and testing (30%)

X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.3, random_state=42)

# Initialize and train Bernoulli Naïve Bayes

bnb = BernoulliNB() # Default settings

bnb.fit(X_train, y_train) # Train model

# Evaluate accuracy on test data

print("BernoulliNB Accuracy:", bnb.score(X_test, y_test)) # Output: ~0.87
```

2. Multinomial Naïve Bayes (Discrete Counts)

Use Case: Sentiment analysis (word frequencies)

```
from sklearn.naive_bayes import MultinomialNB

from sklearn.feature_extraction.text import CountVectorizer

# Sample dataset: 4 movie reviews

corpus = ["good movie", "bad movie", "great film", "poor film"]

labels = [1, 0, 1, 0] # 1=Positive, 0=Negative

# Convert text to word counts (e.g., "good movie" → [1, 1, 0, 0, 0])

vectorizer = CountVectorizer()

X = vectorizer.fit_transform(corpus) # X = word count matrix

# Train Multinomial Naïve Bayes

mnb = MultinomialNB()

mnb.fit(X, labels)

# Predict sentiment for new text

new_text = ["good film"]

X_new = vectorizer.transform(new_text) # Convert to word counts

print("Predicted sentiment (1=Positive, 0=Negative):", mnb.predict(X_new)) # Output: [1]
```

3. Gaussian Naïve Bayes (Continuous Features)

Use Case: Iris flower classification (sepal/petal measurements)

```
from sklearn.naive_bayes import GaussianNB
from sklearn.datasets import load_iris
from sklearn.model_selection import train_test_split

# Load Iris dataset (150 samples, 4 features)
X, y = load_iris(return_X_y=True) # X = features, y = labels (0,1,2)

# Split data (70% train, 30% test)
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.3, random_state=42)

# Train Gaussian Naïve Bayes (assumes features are normally distributed)
gnb = GaussianNB()
gnb.fit(X_train, y_train)

# Evaluate accuracy
print("GaussianNB Accuracy:", gnb.score(X_test, y_test)) # Output: ~0.93
```

Key Notes for Easy Recall

1. BernoulliNB:

- Input: Binary data (0 or 1).
- Example: [1, 0, 1] = "Word1 present, Word2 absent, Word3 present".

2. MultinomialNB:

o Input: Word counts (e.g., [3, 0, 2] = "Word1 appears 3 times, Word2 appears 0 times...").

3. GaussianNB:

o Input: Continuous numbers (e.g., [5.1, 3.5, 1.4, 0.2] = sepal length, width, etc.).

4. Preprocessing:

For text, always use CountVectorizer (as above) or TfidfVectorizer.

5. Why Naïve Bayes?

- Fast training/prediction.
- Works well with high-dimensional data (e.g., text).

k-NN Algorithm from Scratch

```
import numpy as np
from collections import Counter
from sklearn.datasets import load_iris
from sklearn.model_selection import train_test_split
from sklearn.metrics import accuracy_score
# Load the Iris dataset (real-world data)
iris = load_iris()
X, y = iris.data, iris.target # Features (sepal/petal measurements) and labels (0,1,2)
# Split into training (70%) and testing (30%)
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.3, random_state=42)
# --- k-NN Implementation ---
def euclidean_distance(x1, x2):
  """Calculate Euclidean distance between two points."""
  return np.sqrt(np.sum((x1 - x2) ** 2))
class KNN:
  def __init__(self, k=3):
    self.k = k # Number of neighbors to consider
  def fit(self, X, y):
    """Store the training data (k-NN is a lazy learner)."""
    self.X_train = X
    self.y_train = y
  def predict(self, X):
```

```
"""Predict labels for test data."""
    y_pred = [self._predict(x) for x in X]
    return np.array(y_pred)
  def _predict(self, x):
    """Helper function to predict a single data point."""
    # 1. Compute distances between 'x' and all training points
    distances = [euclidean_distance(x, x_train) for x_train in self.X_train]
    # 2. Get indices of the k-nearest neighbors
    k_indices = np.argsort(distances)[:self.k] # Sort and pick top-k
    # 3. Get labels of these neighbors
    k_nearest_labels = [self.y_train[i] for i in k_indices]
    # 4. Majority vote (most common label)
    most_common = Counter(k_nearest_labels).most_common(1)
    return most_common[0][0] # Return the predicted label
# --- Testing the k-NN ---
knn = KNN(k=3) # Initialize with k=3
knn.fit(X_train, y_train) # "Train" (just stores the data)
predictions = knn.predict(X_test) # Predict on test data
# Calculate accuracy
accuracy = accuracy_score(y_test, predictions)
print(f"k-NN Accuracy (k=3): {accuracy:.2f}") # Output: ~0.98
```

Key Steps Explained

1. Euclidean Distance:

- Measures straight-line distance between two points.
- o Formula: $sqrt((x1 x2)^2 + (y1 y2)^2 + ...)$.

2. k-NN Class Workflow:

- o fit(): Stores training data (no actual training, hence "lazy learner").
- o predict(): For each test point:
 - Computes distances to all training points.
 - Finds the k nearest neighbors.
 - Predicts the majority label among them.

3. Testing on Iris Dataset:

- Features: [sepal_length, sepal_width, petal_length, petal_width].
- Labels: 0=setosa, 1=versicolor, 2=virginica.

4. Accuracy:

Achieves ~98% accuracy for k=3 on the Iris dataset.

Why k-NN?

- **Simple**: No complex math, just distance calculations.
- No Training: Works directly on stored data.
- Works for Any Data Type: As long as you can define a distance metric.

1. Basic Decision Tree with Default Parameters

```
from sklearn.tree import DecisionTreeClassifier
from sklearn.datasets import load_iris
from sklearn.model_selection import train_test_split
from sklearn.metrics import accuracy_score
# Load dataset
iris = load_iris()
X, y = iris.data, iris.target
# Split into train (70%) and test (30%)
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.3, random_state=42)
# Initialize and train Decision Tree (default: Gini impurity, unlimited depth)
dt_default = DecisionTreeClassifier(random_state=42)
dt_default.fit(X_train, y_train)
# Predict and evaluate
y_pred = dt_default.predict(X_test)
accuracy_default = accuracy_score(y_test, y_pred)
print(f"Default Decision Tree Accuracy: {accuracy_default:.2f}") # Output: ~0.98
```

2. Comparing Different Parameters

We will test the impact of:

- Criterion ("gini" vs "entropy")
- min_samples_split (minimum samples required to split a node)
- min_samples_leaf (minimum samples required to be a leaf node)
- max_depth (maximum depth of the tree)

A. Criterion: Gini vs Entropy

```
# Gini (default, faster)

dt_gini = DecisionTreeClassifier(criterion="gini", random_state=42)

dt_gini.fit(X_train, y_train)

y_pred_gini = dt_gini.predict(X_test)

accuracy_gini = accuracy_score(y_test, y_pred_gini)

# Entropy (sometimes more accurate but slower)

dt_entropy = DecisionTreeClassifier(criterion="entropy", random_state=42)

dt_entropy.fit(X_train, y_train)

y_pred_entropy = dt_entropy.predict(X_test)

accuracy_entropy = accuracy_score(y_test, y_pred_entropy)

print(f"Gini Accuracy: {accuracy_gini:.2f}") # Output: ~0.98

print(f"Entropy Accuracy: {accuracy_entropy:.2f}") # Output: ~0.98
```

Effect:

- Gini is slightly faster but Entropy may sometimes generalize better.
- For Iris dataset, both perform similarly.

B. min_samples_split (Controls Overfitting)

```
# min_samples_split = 2 (default)

dt_min_split_2 = DecisionTreeClassifier(min_samples_split=2, random_state=42)

dt_min_split_2.fit(X_train, y_train)

y_pred_split_2 = dt_min_split_2.predict(X_test)

accuracy_split_2 = accuracy_score(y_test, y_pred_split_2)

# min_samples_split = 5 (fewer splits \rightarrow simpler tree)

dt_min_split_5 = DecisionTreeClassifier(min_samples_split=5, random_state=42)

dt_min_split_5.fit(X_train, y_train)

y_pred_split_5 = dt_min_split_5.predict(X_test)

accuracy_split_5 = accuracy_score(y_test, y_pred_split_5)

print(f"min_samples_split=2 Accuracy: {accuracy_split_2:.2f}") # Output: ~0.98

print(f"min_samples_split=5 Accuracy: {accuracy_split_5:.2f}") # Output: ~0.96
```

Effect:

• Higher min_samples_split → simpler tree, less overfitting, but may reduce accuracy if too restrictive.

C. min_samples_leaf (Controls Leaf Size)

```
# min_samples_leaf = 1 (default)

dt_min_leaf_1 = DecisionTreeClassifier(min_samples_leaf=1, random_state=42)

dt_min_leaf_1.fit(X_train, y_train)

y_pred_leaf_1 = dt_min_leaf_1.predict(X_test)

accuracy_leaf_1 = accuracy_score(y_test, y_pred_leaf_1)

# min_samples_leaf = 3 (larger leaves \rightarrow smoother decisions)

dt_min_leaf_3 = DecisionTreeClassifier(min_samples_leaf=3, random_state=42)

dt_min_leaf_3.fit(X_train, y_train)

y_pred_leaf_3 = dt_min_leaf_3.predict(X_test)

accuracy_leaf_3 = accuracy_score(y_test, y_pred_leaf_3)

print(f"min_samples_leaf=1 Accuracy: {accuracy_leaf_1:.2f}") # Output: ~0.98

print(f"min_samples_leaf=3 Accuracy: {accuracy_leaf_3:.2f}") # Output: ~0.96
```

Effect:

 Higher min_samples_leaf → prevents tiny leaves, reduces overfitting, but may underfit if too large.

D. max_depth (Controls Tree Depth)

```
# max_depth = None (default, unlimited depth → overfits)

dt_depth_none = DecisionTreeClassifier(max_depth=None, random_state=42)

dt_depth_none.fit(X_train, y_train)

y_pred_depth_none = dt_depth_none.predict(X_test)

accuracy_depth_none = accuracy_score(y_test, y_pred_depth_none)

# max_depth = 3 (shallower tree → less overfitting)

dt_depth_3 = DecisionTreeClassifier(max_depth=3, random_state=42)

dt_depth_3.fit(X_train, y_train)

y_pred_depth_3 = dt_depth_3.predict(X_test)

accuracy_depth_3 = accuracy_score(y_test, y_pred_depth_3)

print(f"max_depth=None Accuracy: {accuracy_depth_none:.2f}") # Output: ~0.98

print(f"max_depth=3 Accuracy: {accuracy_depth_3:.2f}") # Output: ~0.98
```

Effect:

- Smaller max_depth → simpler tree, less overfitting.
- Too shallow → underfitting, too deep → overfitting.

3. Best Parameter Combination

```
# Optimal parameters (prevents overfitting while maintaining accuracy)
dt_optimal = DecisionTreeClassifier(
    criterion="gini",
    max_depth=3,
    min_samples_split=2,
    min_samples_leaf=1,
    random_state=42
)
dt_optimal.fit(X_train, y_train)
y_pred_optimal = dt_optimal.predict(X_test)
accuracy_optimal = accuracy_score(y_test, y_pred_optimal)
print(f"Optimal Decision Tree Accuracy: {accuracy_optimal:.2f}") # Output: ~0.98
```

Summary of Parameter Effects

Parameter	Effect	Too Low	Too High	Ideal Value (for Iris)
criterion	Splitting method	Gini (faster)	Entropy (sometimes better)	"gini"
min_samples_split	Minimum samples to split	Overfitting (tiny splits)	Underfitting (too few splits)	2 (default)
min_samples_leaf	Minimum samples in a leaf	Overfitting (noisy leaves)	Underfitting (large leaves)	1 (default)
max_depth	Maximum tree depth	Overfitting (deep tree)	Underfitting (shallow tree)	3

Key Takeaways

- 1. **Default settings often overfit** (unlimited depth, small leaves).
- 2. Tune max_depth first to control complexity.
- 3. **Use** min_samples_split **and** min_samples_leaf to prevent tiny splits/noisy leaves.
- 4. **Gini vs Entropy**: Usually similar accuracy, but Gini is faster.

1. SVM with Grid Search (Best Parameters)

```
import numpy as np
import matplotlib.pyplot as plt
from sklearn import datasets
from sklearn.svm import SVC
from sklearn.model_selection import GridSearchCV, train_test_split
from sklearn.metrics import accuracy_score
# Load sample dataset (3D for visualization)
X, y = datasets.make_classification(
  n_samples=100, n_features=3, n_redundant=0, n_informative=3,
  n_classes=2, random_state=42, n_clusters_per_class=1
)
# Split into train-test
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.3, random_state=42)
# Define SVM model
svm = SVC()
# Grid Search for best hyperparameters
param_grid = {
  'C': [0.1, 1, 10],
                  # Regularization strength
  'kernel': ['linear', 'rbf'], # Kernel type
  'gamma': ['scale', 'auto'] # Kernel coefficient (for 'rbf')
}
grid_search = GridSearchCV(svm, param_grid, cv=5, scoring='accuracy')
grid_search.fit(X_train, y_train)
```

```
# Best parameters and accuracy
best_params = grid_search.best_params_
best_svm = grid_search.best_estimator_
y_pred = best_svm.predict(X_test)
accuracy = accuracy_score(y_test, y_pred)
print(f"Best Parameters: {best_params}")
print(f"Test Accuracy: {accuracy:.2f}")
```

Output Example:

Best Parameters: {'C': 10, 'gamma': 'scale', 'kernel': 'rbf'}

Test Accuracy: 0.93

2. 3D Plot of SVM Decision Boundary

```
from mpl_toolkits.mplot3d import Axes3D
# Create a meshgrid for 3D plotting
def plot_3d_hyperplane(X, y, model):
  fig = plt.figure(figsize=(10, 7))
  ax = fig.add_subplot(111, projection='3d')
  # Plot data points
  ax.scatter(X[:, 0], X[:, 1], X[:, 2], c=y, cmap='coolwarm', s=50)
  # Create meshgrid for decision boundary
  x_{min}, x_{max} = X[:, 0].min() - 1, X[:, 0].max() + 1
  y_min, y_max = X[:, 1].min() - 1, X[:, 1].max() + 1
  z_{min}, z_{max} = X[:, 2].min() - 1, X[:, 2].max() + 1
  xx, yy = np.meshgrid(np.linspace(x_min, x_max, 10),
       np.linspace(y_min, y_max, 10)
  zz = np.linspace(z_min, z_max, 10)
  # Predict decision boundary
  Z = model.predict(np.c_[xx.ravel(), yy.ravel(), np.zeros_like(xx).ravel()])
  Z = Z.reshape(xx.shape)
  # Plot decision surface
  ax.plot_surface(xx, yy, Z, alpha=0.3, cmap='coolwarm')
  ax.set_xlabel('Feature 1')
  ax.set_ylabel('Feature 2')
  ax.set_zlabel('Feature 3')
  plt.title("SVM Decision Boundary (3D)")
  plt.show()
# Plot the best SVM model
plot_3d_hyperplane(X, y, best_svm)
```

1. Perceptron for AND & OR Gates (Linearly Separable)

Key Idea:

- A single-layer perceptron can solve AND and OR because they are linearly separable.
- Uses step activation (1 if w·x + b >= 0, else 0).

```
import numpy as np
# Define Perceptron class
class Perceptron:
  def __init__(self, learning_rate=0.1, epochs=100):
    self.lr = learning_rate # Learning rate
    self.epochs = epochs # Training iterations
    self.weights = None # Weights (w1, w2)
    self.bias = None
                         # Bias (b)
  def step_activation(self, x):
    return 1 if x >= 0 else 0 # Binary step function
  def fit(self, X, y):
    n_samples, n_features = X.shape
    self.weights = np.zeros(n_features) # Initialize weights
    self.bias = 0
                             # Initialize bias
    # Training loop
    for _ in range(self.epochs):
      for idx, x_i in enumerate(X):
         linear_output = np.dot(x_i, self.weights) + self.bias
         y_pred = self.step_activation(linear_output)
         update = self.lr * (y[idx] - y_pred) # Perceptron update rule
         self.weights += update * x_i
```

```
def predict(self, X):
    linear_output = np.dot(X, self.weights) + self.bias
    return [self.step_activation(x) for x in linear_output]
# --- Test AND Gate ---
# AND gate truth table: X = [[0,0], [0,1], [1,0], [1,1]], y = [0, 0, 0, 1]
X_{and} = np.array([[0, 0], [0, 1], [1, 0], [1, 1]])
y_and = np.array([0, 0, 0, 1])
# Train Perceptron on AND gate
p_and = Perceptron(epochs=100)
p_and.fit(X_and, y_and)
# Predict
print("AND Gate Predictions:", p_and.predict(X_and)) # Output: [0, 0, 0, 1]
# --- Test OR Gate ---
# OR gate truth table: X = same, y = [0, 1, 1, 1]
y_or = np.array([0, 1, 1, 1])
p_or = Perceptron(epochs=100)
p_or.fit(X_and, y_or)
print("OR Gate Predictions:", p_or.predict(X_and)) # Output: [0, 1, 1, 1]
```

self.bias += update

2. MLP for XOR Gate (Non-Linearly Separable)

Key Idea:

- XOR cannot be solved by a single perceptron (needs hidden layers).
- We use a **2-layer MLP** with:
 - Input layer (2 neurons)
 - Hidden layer (2 neurons, ReLU activation)
 - Output layer (1 neuron, sigmoid activation)

```
import numpy as np
class MLP:
  def __init__(self, learning_rate=0.1, epochs=10000):
    self.lr = learning_rate
    self.epochs = epochs
    self.weights1 = None # Input → Hidden weights
    self.weights2 = None # Hidden → Output weights
    self.bias1 = None # Hidden layer bias
    self.bias2 = None # Output layer bias
  def sigmoid(self, x):
    return 1/(1 + np.exp(-x)) # Sigmoid for output layer
  def relu(self, x):
    return np.maximum(0, x) # ReLU for hidden layer
  def fit(self, X, y):
    n_samples, n_features = X.shape
    # Initialize weights (small random values)
    self.weights1 = np.random.rand(n_features, 2) # 2 hidden neurons
    self.weights2 = np.random.rand(2, 1) # 1 output neuron
    self.bias1 = np.zeros(2)
    self.bias2 = np.zeros(1)
    # Training loop
    for _ in range(self.epochs):
```

```
# Forward pass
      hidden_input = np.dot(X, self.weights1) + self.bias1
      hidden_output = self.relu(hidden_input)
      output_input = np.dot(hidden_output, self.weights2) + self.bias2
      y_pred = self.sigmoid(output_input)
      # Backpropagation
      error = y.reshape(-1, 1) - y_pred
      d_output = error * (y_pred * (1 - y_pred)) # Sigmoid derivative
      d_hidden = np.dot(d_output, self.weights2.T) * (hidden_output > 0) # ReLU derivative
      # Update weights and biases
      self.weights2 += self.lr * np.dot(hidden_output.T, d_output)
      self.bias2 += self.lr * np.sum(d_output, axis=0)
      self.weights1 += self.lr * np.dot(X.T, d_hidden)
      self.bias1 += self.lr * np.sum(d_hidden, axis=0)
  def predict(self, X):
    hidden_output = self.relu(np.dot(X, self.weights1) + self.bias1)
    output = self.sigmoid(np.dot(hidden_output, self.weights2) + self.bias2)
    return [1 if x > 0.5 else 0 for x in output.flatten()]
# --- Test XOR Gate ---
# XOR truth table: X = [[0,0], [0,1], [1,0], [1,1]], y = [0, 1, 1, 0]
X_xor = np.array([[0, 0], [0, 1], [1, 0], [1, 1]])
y_xor = np.array([0, 1, 1, 0])
# Train MLP on XOR
mlp = MLP(epochs=10000)
mlp.fit(X_xor, y_xor)
# Predict
print("XOR Gate Predictions:", mlp.predict(X_xor)) # Output: [0, 1, 1, 0]
```

Key Takeaways

Logic Gate	Linearly Separable?	Model Used	Key Parameters
AND	Yes	Perceptron	step_activation, weights, bias
OR	Yes	Perceptron	Same as AND
XOR	No	MLP (2-layer)	sigmoid, ReLU, backpropagation

Why This Works?

1. Perceptron (AND/OR):

- Straight-line decision boundary works for AND/OR.
- o Adjusts weights until error is minimized.

2. MLP (XOR):

- Needs a **hidden layer** to learn non-linear separation.
- o **ReLU** introduces non-linearity.
- o **Backpropagation** adjusts weights iteratively.

```
# Import necessary libraries
from sklearn.datasets import load_iris
from sklearn.model_selection import train_test_split
from sklearn.preprocessing import StandardScaler
from sklearn.neural_network import MLPClassifier
from sklearn.metrics import classification_report, accuracy_score
# Step 1: Load a benchmark dataset (Iris)
iris = load_iris()
X = iris.data # Features
y = iris.target # Labels
# Step 2: Split into training and testing data (80% train, 20% test)
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2, random_state=42)
# Step 3: Standardize features (very important for neural networks)
scaler = StandardScaler()
X_train = scaler.fit_transform(X_train)
X_test = scaler.transform(X_test)
# Step 4: Create a simple MLP (Multilayer Perceptron) model
# hidden_layer_sizes=(10,): One hidden layer with 10 neurons
# max_iter=1000: Max number of training iterations
model = MLPClassifier(hidden_layer_sizes=(10,), activation='relu', solver='adam', max_iter=1000,
random_state=42)
```

```
# Step 5: Train the model using backpropagation
model.fit(X_train, y_train)

# Step 6: Predict and evaluate the model
y_pred = model.predict(X_test)

# Step 7: Print accuracy and classification report
print("Accuracy:", accuracy_score(y_test, y_pred))
print("Classification Report:\n", classification_report(y_test, y_pred))
```

Explanation:

- MLPClassifier uses backpropagation under the hood to train the neural network.
- We use Iris dataset: a well-known multiclass classification dataset.
- StandardScaler is used because neural networks perform better on scaled data.
- The model uses a single hidden layer with 10 neurons, ReLU activation, and Adam optimizer.

K Means Clustering using sklearn

```
# Import required libraries
import numpy as np
import matplotlib.pyplot as plt
from sklearn.cluster import KMeans
from sklearn.datasets import make_blobs
# Step 1: Create synthetic dataset for clustering
X, y_true = make_blobs(n_samples=300, centers=3, cluster_std=0.60, random_state=42)
# Step 2: Create KMeans model with k=3 clusters
kmeans = KMeans(n_clusters=3, random_state=42)
# Step 3: Fit the model to the data
kmeans.fit(X)
# Step 4: Get predicted cluster labels
y_kmeans = kmeans.predict(X)
# Step 5: Plot the clustered data
plt.scatter(X[:, 0], X[:, 1], c=y_kmeans, cmap='viridis', s=50)
# Plot the cluster centers
centers = kmeans.cluster_centers_
plt.scatter(centers[:, 0], centers[:, 1], c='red', s=200, alpha=0.75, marker='X', label='Centroids')
plt.title("K-Means Clustering")
plt.xlabel("Feature 1")
plt.ylabel("Feature 2")
plt.legend()
plt.grid(True)
plt.show()
```