

# Databases

## Tag

Data: Known fact abt any <sup>entity</sup> object  
eg: Rno, name

— object — <sup>active</sup> ~~passive~~  
~~entity~~ data + qm  
character + behavior

Record: Collection of interrelated data.

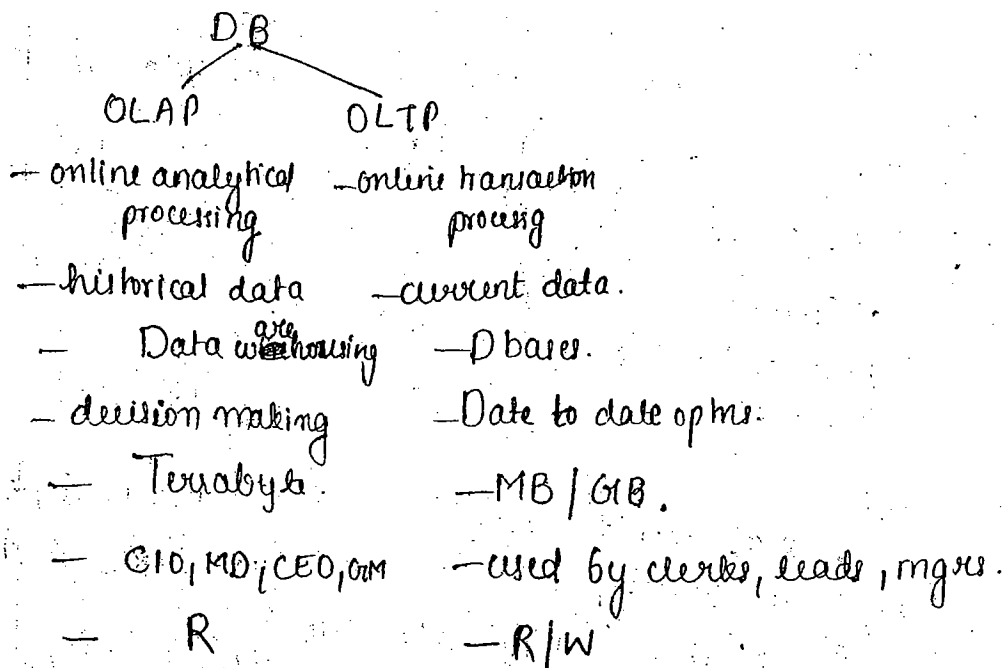
Rno	Name	G.no	mark
101	nyz	1	100

— entity — <sup>passive</sup> ~~active~~  
only characteristics  
no behaviour.

Database: collection of records

DBMS: s/w to collect create, modify manipulate & delete db.

DS: DB + DBMS  
(db & s) Eg: Oracle, SQL server

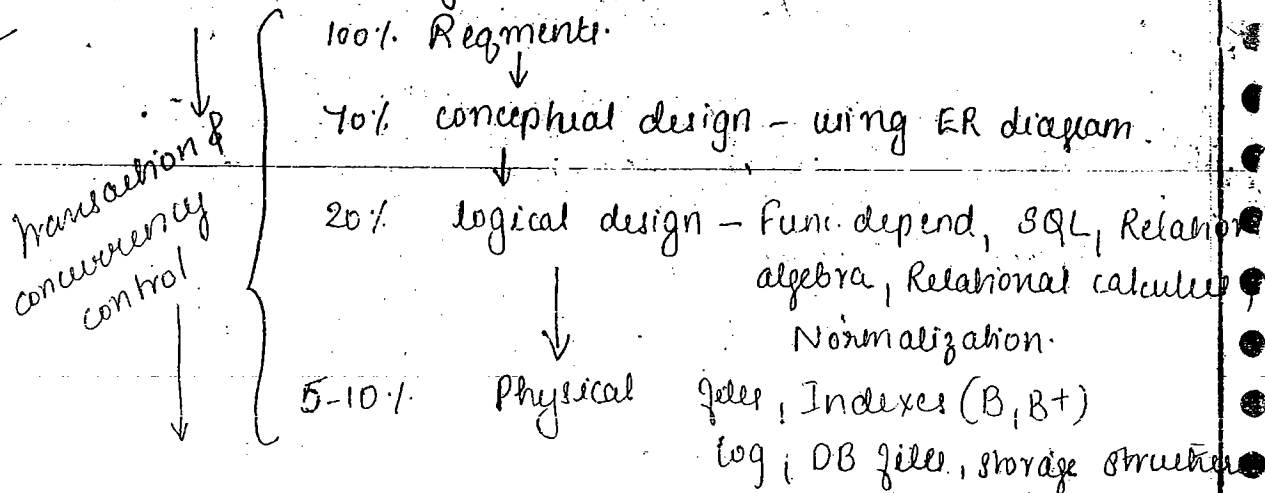


## Data Mining -

- DBase — commercial (inventory, material) (char, number.)  
multimedia (data stored as objects) (audio, video)  
Deductive (stores rules)  
Temporal (time aspect also involved)  
Geological Info System DB (Google maps — contains images)  
Distributed DB (eg. network dbs.)

13/9/10

## Database design



→ If users are more than 100, we use indexes for easy access

## E-R Diagrams:

- It gives graphical representation of reqmts in terms of entities, relationships and attributes (or)

It is a domain knowledge representation in terms of entities, relationships & attributes.

## ER diagram components

- Entities
- relationships
- attributes

### a) Entities:

A real world object or thing with independent existence is known as entities. There are 2 types of

- physical entity (tangible)
- conceptual entity (nontangible)

Physical entity: Person, vehicle, furniture

Conceptual : Sale, course, brand image

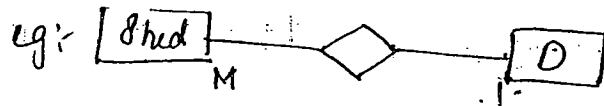
### b) Relationships:

It gives association among entities.

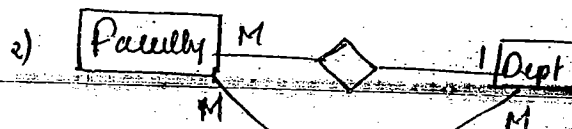
Btw entities, one/more relations are possible

## Types of relations

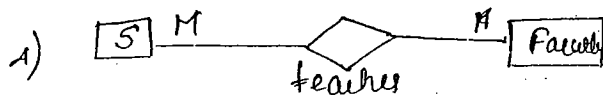
- one-one (10%)
- one-many (20%)
- many-many (70%)



(2)

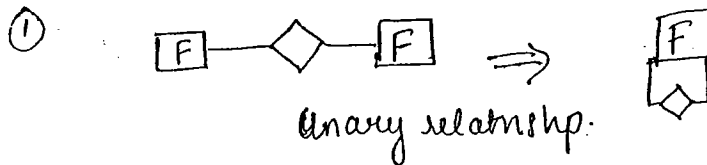


HOD  $\Rightarrow$  In general, it is one-one.



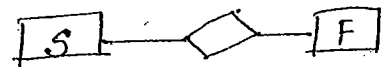
Degree of relationship:

It specifies no. of entities participating in a relationship.

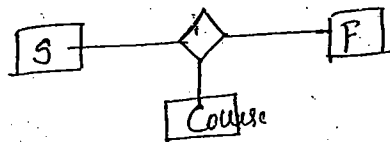


② Binary relationship

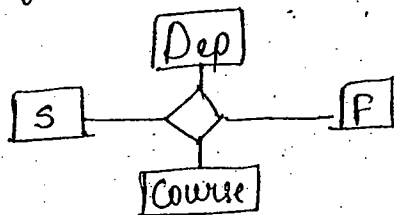
Only 2 entities participate.



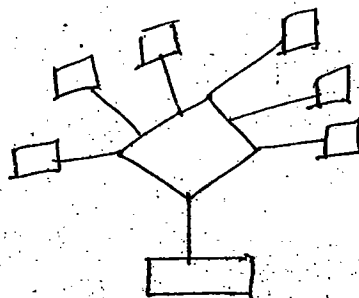
③ Ternary relationship



④ Quarternary relation

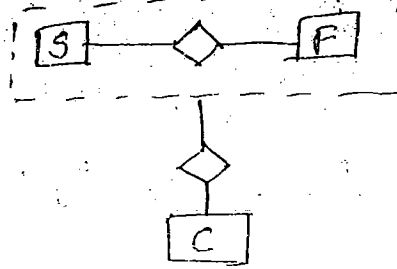
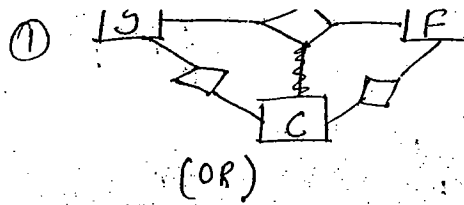


⑤ n-ary



ER diagrams are designed to take care of unary & binary relationships, not other type of relationships.

Ternary  $\Rightarrow$



Constraints on ER diagram:

① Structural constraints

- a) participation constraints:
- b) cardinality ratio.

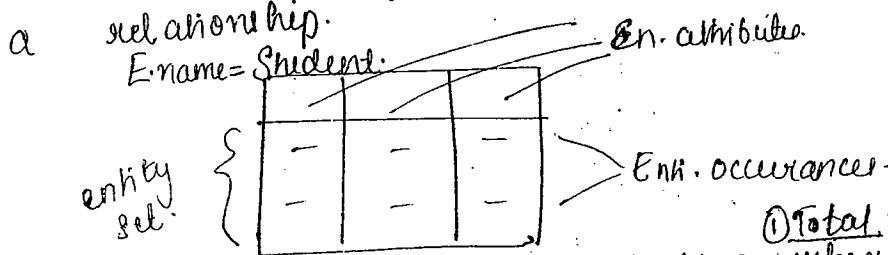
② Covering constraints

③ Overlapped constraints

② and ③ is used in EER (ER + OO)

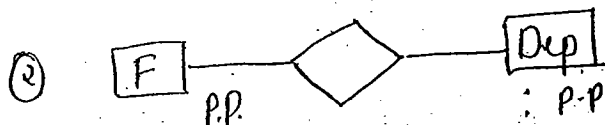
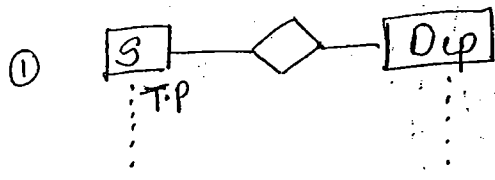
Participation constraints:

It defines participation of entity occurrences thru a relationship.



There are 2 types of participation where all entity occurrences participating through a relationship.

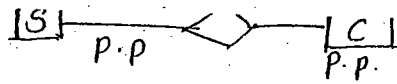
② Partial: Some of entities are not participating thru a relationship.



All students must have dept  
But all dept need not contain student

all students participate but depts do not.

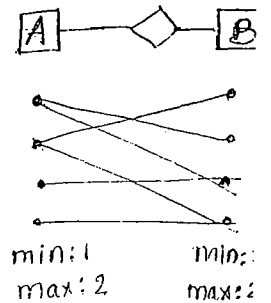
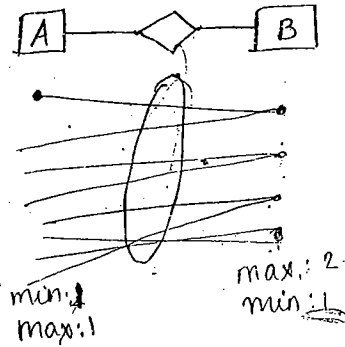
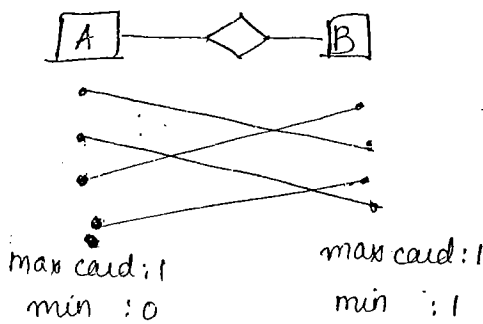
Dept may not contain a faculty. (p.p.)



(3)

Cardinality ratio:

defines maximum no. of times an entity occurs participating in a relationship.



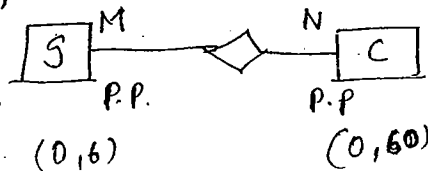
min cardinality : If 0  $\Rightarrow$  partial participation.

If 1  $\Rightarrow$  Total participation

max cardinality : If 1  $\Rightarrow$  entity occurrence is participating thru a relation only once.

If N  $\Rightarrow$  then N no. of times an entity occurrence participate in a relation.

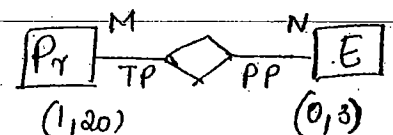
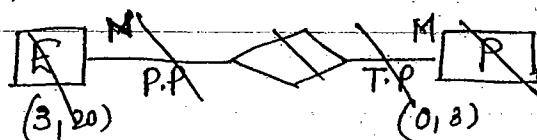
① Consider,



Description: All the students need not register courses but they can go max upto 6.

A course can allow max of 60 students to register, but all the courses need not have registration.

② Consider: A project suppose to have min 3 employees and max of 20 employees. All the employees need not be in proj, but they can participate upto 3 project at a time.



but (max 3 proj) cannot be represented.

### III Attributes:

3 categories:

- a) simple and composite attributes
- b) single valued & multivalued attr.
- c) stored and derived attr.

⇒ multivalued causes sm. probs.

a) Simple - atomic value and cant be divided further.

Rollno, age

Composite - can be divided further into simple attributes

Address → HNo  
              → Streetname  
              → State   City

Name → Firstname  
         → Lastname

b) Single valued : attr that holds single value is called single valued. Eg: PANcard no, blood group, voterID.

Multivalued : holds multiple values.

eg: address, telephone no, emailIDs

c) Stored : supplies values to derived attributes.

Derived : get value from stored attributes.

① DOB ← age.

② RNo. BNo → I/Date R/Date (line) defnd from

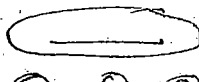
③

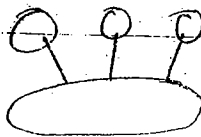
RNo.	Name	BNo
101	a	1
102	b	1
102	c	2

Bno	Bname	#
1	CSE	2
2	IT	1

instead of manually entering, # can be derived from 1st table.

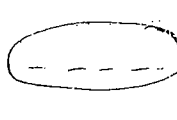
 Attr.


 1<sup>o</sup> key attr

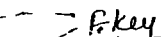
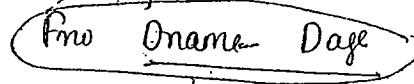
 CA (composite)

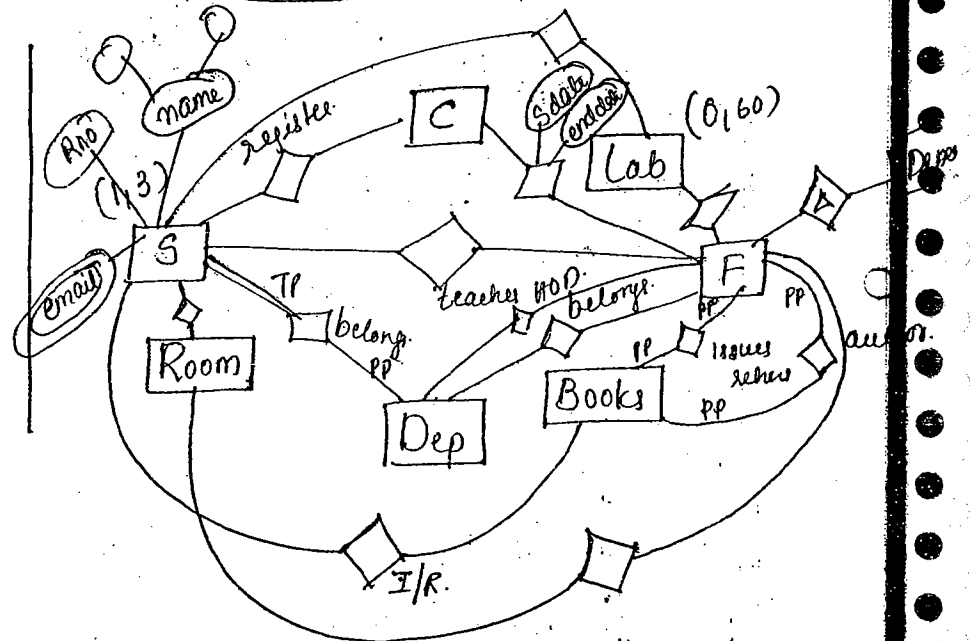
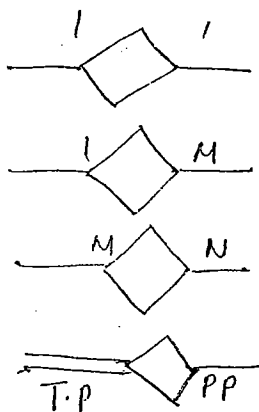
 Multi var. attr.



 DA

 discriminated  
~~designated~~ attr.

An attr/attrs in weak entity that are combined with primary key of S.E to declare the combination as a 1<sup>o</sup> key for the W.E is known as 

1<sup>o</sup> key  Fkey  




Participation:  TP  
 PP.

Cardinality ratio — (0,60) (1,3) ....

## Stronger classification of entities

Strong entity  
Weak entity

Associative entity.

<sup>1<sup>st</sup> key</sup>  

FNo	FName
101	a
102	b
103	c

Dependent table.

FNo	Dep name	age
101	X	5
101	X	60
102	Y	10

when 102 is removed, its dependent table entry also removed.

<sup>1<sup>st</sup> key</sup>  

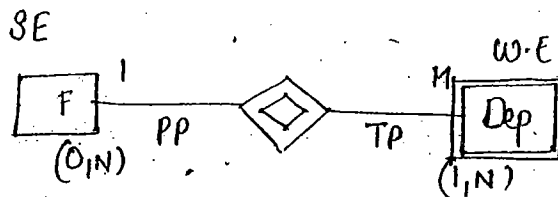
PNo	Pname
101	a
102	b
103	c

<sup>1<sup>st</sup> key</sup>  

PNo	LNo	Ltype
101	1A1	LMV
101	1B1	IDL
102	1L1	HMV

Strong entity

strong entity.



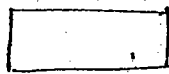
E-R Diagram notations:

Chen

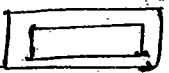
Crow's  
Feet  
↓  
UML

Idexis  
X

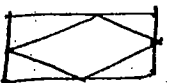
Rein5  
X



SE



WE



AE

looks like relationship but actually its entity.



Relation



Identifying relation



## • Conversion of ER diagrams to tables:

⑤

### Step 1: Conversion of strong entities

- a) for each strong entity create a separate table with same name.
- b) Include all attr, if there is any composite attr. split it into simple attr and include them.  
Ignore multivalued attr at this stage.
- c) Select 1<sup>o</sup> key for the table.

### Step 2: Conversion of weak entity.

- a) for each weak entity create a separate table with same name.
- b) Same as step (1)
- c) ~~Create~~ Include 1<sup>o</sup> key of strong entity as foreign key in the weak entity.
- d) Declare the combination of foreign key & discriminator attributes as 1<sup>o</sup> key for the weak entity.

### Step 3: Conversion of one to one relationship.

- a) For each one to one relation, say A and B, modify either A side or B side to include 1<sup>o</sup> key of other side as a foreign key.
- b) If A or B is having total participation, then that shd be the modified table.  
If both PP, either A/B
- c) If relationship consists attributes include them also in the modified table.

### Step 4: Conversion of one to many relationship

- a) For each one to many relationship, modify M side to include 1<sup>o</sup> key of one side as a foreign key.
- b) If relationship consists attr, include them also

### Step 5: Conversion of many-many relationship

① For each many-many, create a separate table & include 1<sup>o</sup> keys of M side and N side as foreign keys in the new table.

② Declare the combination of foreign keys as 1<sup>o</sup> key for new table.

③ If relationship consists attr, include them also in the new table.

### Step 6: Conversion of multivalued attr:

a) For each multivalued attr, create a separate table and include 1<sup>o</sup> key of parent table as foreign key.

b) Declare the combination of foreign key & Multivalued attr as 1<sup>o</sup> key.

### Step 7: Conversion of n-ary relationships.

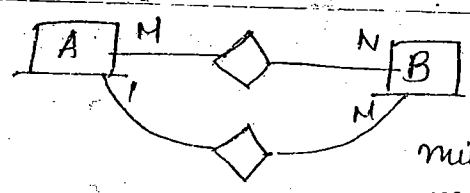
a) For each n-ary relationship, create a separate table & include 1<sup>o</sup> keys of all entities as foreign keys.

b) Declare the combination of foreign keys as 1<sup>o</sup> key.

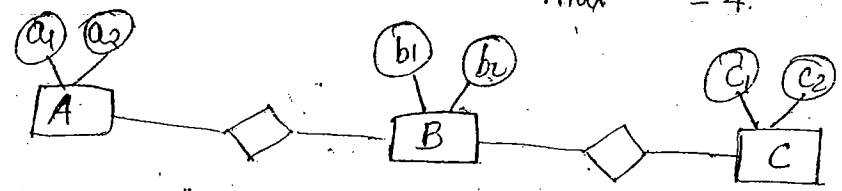
• Note:

1-1 and 1-M relations can also be separated as tables but its not advisable due to performance reasons.

(6)



min table = 3  
max = 4.

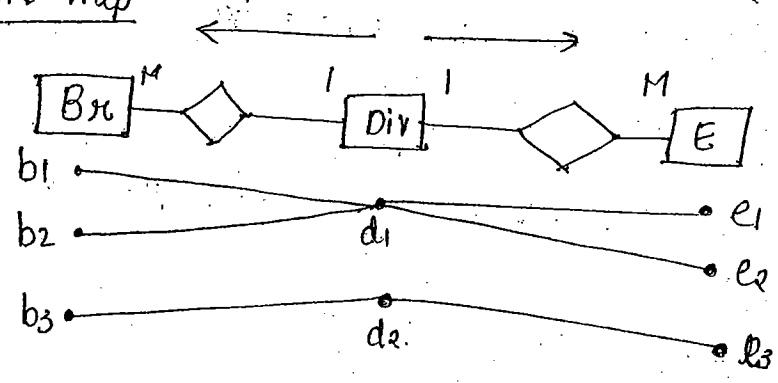


- a)  $a_1 a_2 b_1$
- b)  $b_1 b_2 c_1$
- c)  $a_1 a_2 c_1$
- d)  $a_1 a_2 b_2$

### Trap

- 1) FAN trap
- 2) CHASM trap.

#### FAN trap



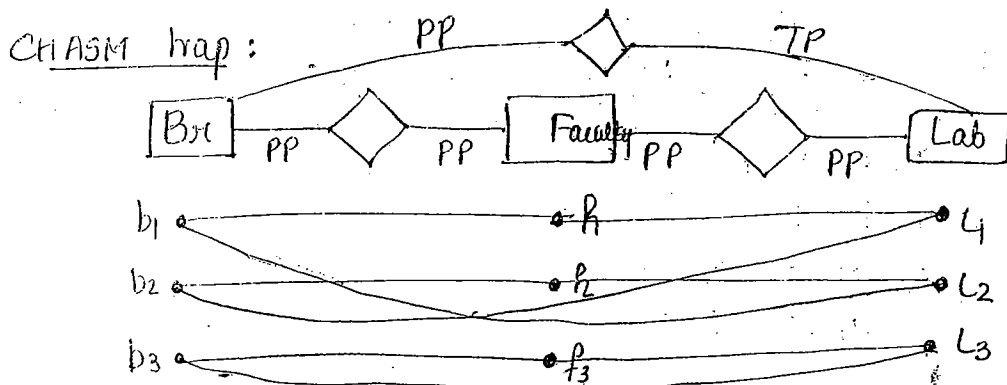
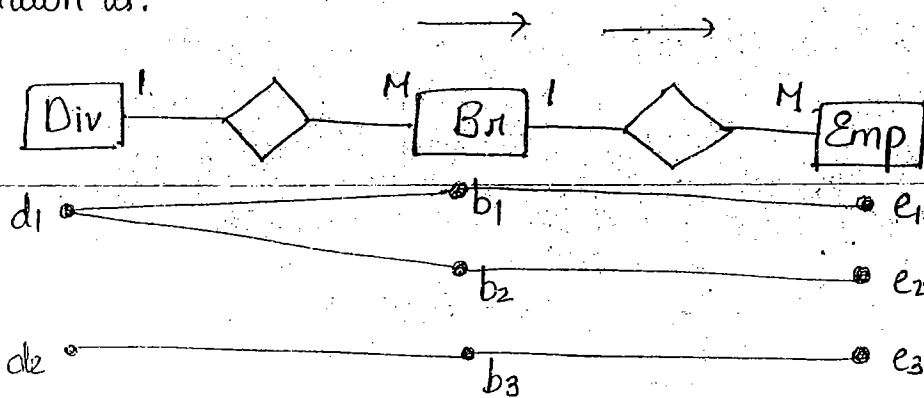
we cant say whether  $e_1$  belong to  $b_1$  or  $b_2$ .  
since  $d_1$  has both

If this E-R diagram is converted into tables, we are able to retrieve all info except  $e_1$  belongs to which branch ( $b_1/b_2$ ).  
This is due to FAN trap.

#### How to identify FAN trap?

If two 1-M relationships are emerging out from single entity, then there will be a FAN trap.

Redrawn as:



If we convert this ER diagram into tables we face the 2 probs:

- 1) we are unable to identify branch details of <sup>lab</sup> branch 2.
- 2) it shows lab1 belongs to branch1 since f1 is operating this lab — may/may<sup>n</sup>t be correct.

This is due to CHASM trap.

How to identify?

If two directly related entities are connected through another entity with partial participation then there is a CHASM trap.

How to eliminate?

Create a direct relationship b/w these 2 entities.

Advantages of ER diagrams

- 1) It is an effective communication tool among database designer, domain expert & stakeholders.
- 2) It is tightly integrated with relational DB model.
- 3) It is easy to understand.

## Disadvantages:

- 1) loss of information content.
- 2) limited constraint representation.
- 3) it is overly complex for small projects.

## Various dB design concepts:

- 1) Top down design
- 2) Bottom up design
- 3) Mixed design
- 4) Inside-Outside design

### top down

Entity  
Relation  
Attr  
ER  
↓  
tables.  
- big projt  
- x  
- easy

### Bottom up

all attr  
relation b/w attr.  
Entities  
FD, normalization  
↓  
tables.  
- small projt  
- powerful  
- difficult

### Mixed

E  
R  
A  
ER  
↓  
tables  
↓  
FD, norm  
↓  
tables.

### in/out

1:1  
1:M  
M:N } attributes

## Defn: Functional Dependency:

It defines association amng entities.

RNo, name, C<sup>ouse</sup>no, V<sup>ehi</sup>no

Course credit (Cc)

RNo → name  
name ↗ RNo.

RNo → CNo.

39 Q.2.

A → B

B ↗ C

A ↗ C

AC → B

AB ↗ C

RNo → BrNo

R<sub>no</sub> → BrNo

	A	B
t <sub>1</sub>	101	A
t <sub>2</sub>	102 101	B

If t<sub>1</sub> & t<sub>2</sub>  
agree

then t<sub>1</sub> & t<sub>2</sub>  
must also  
agree

if t<sub>1</sub> & t<sub>2</sub>  
disagree

t<sub>1</sub> & t<sub>2</sub>  
must not agree

39 3)  $A \rightarrow B$   
 $B \rightarrow C$   
 $C \nrightarrow A$   
 $AC \rightarrow B$   
 $AB \rightarrow C$   
 $BC \rightarrow A$

39 4)  $B \rightarrow C$  ✓ solve 5th hw.

Characteristics of func. dependancies:

FDs must hold always,  $\therefore$  they shd be defnd on schema not on ~~depen~~ instances.

RNo	Name	age

Rno  $\rightarrow$  name  
age  $\rightarrow$  Rno.

$A \rightarrow B.$

A	B	C
1	2	3
4	5	6
7	8	5
3	4	6

3 4 6

3 5 6 X not possible

2) deals with 1-1 relationship.

3) It shd be non ~~trivial~~ ~~or~~ completely non trivial.

$AB \rightarrow CD$  — completely nontrivial

$AB \rightarrow BC$  — non trivial

Some are subset of left.  
<sub>attr</sub>

$ABC \rightarrow BC$  — trivial

all attr of it are subset of left.

Req.



$F_1$



$F_2$  (additional FDs)  $A \rightarrow C$

$A \rightarrow B$

$B \rightarrow C$

$$F = F_1 + F_2$$

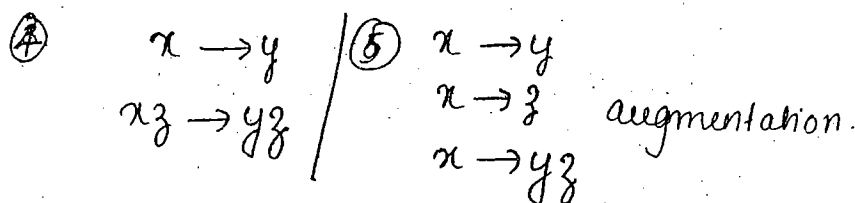
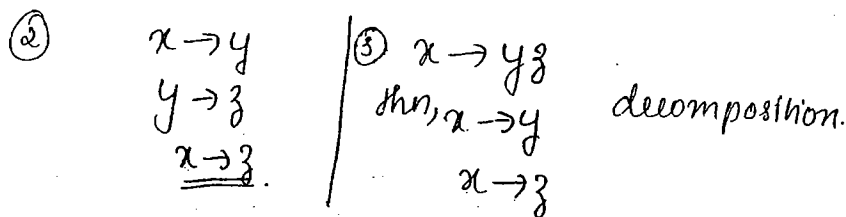
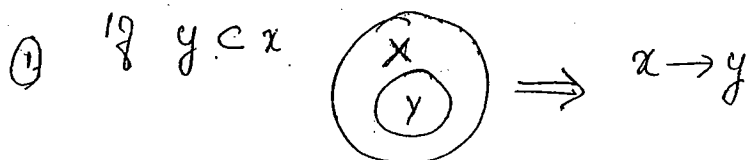
From the segments, once FDs are identified. I call it as  $F_1$ ; From  $F_1$  addtnl fn depn. can be identified

Total func. dependancies =  $F_1 + F_2$ .

This shd be i/p for normalisation process.

To identify  $F_2$  we use following two methods, inference

- 1) inference rules
- 2) closure set of attr



Eg:-

Req.



$F_1 = A \rightarrow B$

$B \rightarrow C$

$C \rightarrow DE$

$E \rightarrow F$

$C \rightarrow D$

$C \rightarrow E$

$F_2 : A \rightarrow C$

$B \rightarrow DE$

$C \rightarrow F$

X

we don use inference rules to identify addn. FDs

neg. as it is a tedious process.

① time consuming.

② error prone.

## ② Closure set method

$A^+$

$X = A$

$= AB$

$= ABC$

$= ABCDE$

$= ABCDEF$

$C^+$

$X = C$

$= CDE$

$= CDEF$

Algorithm to identify closure set of attributes:

① Equate an attribute or attributes to  $X$  for which closure ~~is~~ needs to be identified.

② Repeatedly take func. dependencies one by one and check whether left hand side attr is available or not. If available, add r.h side attr of func dependency to  $X$ .

③ Repeat step 2 as many times as possible to cover all possible FDs.

④ Stop the process if no more attributes can be added to  $X$ .

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6.

$A \rightarrow B$  ✓

$BC \rightarrow DE$  ✓

$AE \rightarrow G$  ✗

compute  $AC^+$

$X = AC$

$= ABC$

$= ABCDE$

$AC^+ = ABCDE$

i.e.  $AC \rightarrow BDE$

(repeatedly go for 2 cycle)

→ determine



$$\begin{array}{lcl}
 7. & A \rightarrow BC & \times \mid \times \quad X = B \\
 & CD \rightarrow E & \times \mid \times \quad = BD \\
 & B \rightarrow D & \checkmark \mid \times \\
 & E \rightarrow A & \times \mid \times \\
 & B^+ = ? &
 \end{array}$$

8 HW

Apples of closure set of attr

- ① To identify attribute functional dependencies.
- ② To identify equivalences.
- ③ To identify candidate keys.
- ④ To identify irreducible set of FDs or canonical form of FDs. (std form of FDs)

pg 41  
9.

$A = ABCDEFGHI$

$$\begin{array}{lcl}
 A \rightarrow BC & \cdot & \checkmark \\
 CD \rightarrow E & & \\
 E \rightarrow C & \checkmark & \\
 D \rightarrow AEH & \checkmark & \\
 ABH \rightarrow BD & \checkmark & \\
 DH \rightarrow BC & &
 \end{array}
 \quad BCD \rightarrow H \Rightarrow ?$$

$BCD^+$

$$X = BCD$$

$$= BCDE$$

$$= ABCDEH$$

$$= ABCDEH \rightarrow \text{hence possible.}$$

$$BCD^+ \rightarrow ABCDEH$$

$$\rightarrow AEH$$

ie,

$$BCD \rightarrow A$$

$$BCD \rightarrow E$$

$$ACD \rightarrow H \quad \checkmark \quad \text{hence possible}$$

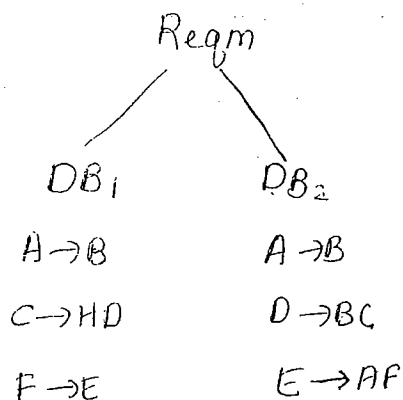
1.  $AED \rightarrow H$  ? true.

$BH \rightarrow AC$  X

$BH^+ \neq BH$

$BH^+ = BH$

$BH \rightarrow \underline{BH}$



From the same reqm, database designers might come with diff sets of f.d.s. By evaluating which is wrong/right, it is necessary to chk whether both are equivalent or not. For this purpose, we use closure set of attributes.

$\frac{A}{10} F =$   
 $A \rightarrow C$   
 $AC \rightarrow D$   
 $E \rightarrow AD$   
 $E \rightarrow H$

$G_1 =$   $\begin{pmatrix} A \rightarrow CD \\ E \rightarrow AH \end{pmatrix}$

Take F set and verify all its FDs can be derived from  $G_1$  or not

$A \rightarrow C$  compute  $A^+$  from  $G_1$ .

$AC \rightarrow D$  compute  $AC^+$  from  $G_1$ .

$E \rightarrow AD$  compute  $E^+$  from  $G_1$ .

Take ' $G_1$ ' set and verify all its FD can be derived from F/no

$A \rightarrow CD$

$E \rightarrow AH$

compute  $A^+$  from  $F$  ✓  
 $E^+$  from  $F$  ✓

$A^+ \underline{\hspace{1cm}}$  ⑩

11.

$F = B \rightarrow CD$

$AD \rightarrow E$  ✓

$B \rightarrow A$  ✓

$G = B \rightarrow CDE$

$B \rightarrow ABC$

$AD \rightarrow E$

$F:$   
 $X = B$   
 $= BCD$   
 $= ABCD$   
 $= ABCDE$

$G:$   
 $X = B$   
 $= BCDE$   
 $= ABCDE$

both are equivalent.

Appm 3.

Types of keys

- 1) Primary key
- 2) Composite primary key.
- 3) Candidate key
- 4) Super key.
- 5) Surrogate key
- 6) Foreign key.

Primary key: - unique value column

- not null column

- only 1  $1^o$  key per table

- enforces entity integrity.

Composite  $1^o$  key: -  $1^o$  key with 2 or more attr.

- mainly in transaction table.

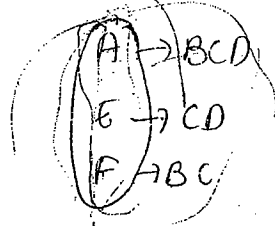
<u>FNo</u>	<u>CNo</u>	to uniquely identify	
		S/date	E/date
101	10		
101	11		
102	12		

Candidate key : If we have one or more unique value ~~col~~ columns in a table, then 1 of them can be elected as 1<sup>o</sup> key for a table. and these alternative keys are called candidate keys.

(or)

V.No	Engine No	DOP
-	-	-

R = ABCDEF



A  
E  
F

AE  
AF  
EF  
AEF

Superkey - union of all lefthand side attr in FD.

Surrogate key

If we are unable to identify 1<sup>o</sup> key from existing cols of table, we look for surrogate key.

App	RNo	BNo	S/date	E/date
1	101	1	1/1/2010	15/1/2010
2	101	2		
3	102	1	16/1/10	20/1/2010
4	101	1	21/1/2010	21/1/10
5	101	1	21/1/2010	21/1/2010

0/10 Foreign key: - used to implement referential integrity.

- can be a null column

- we can have more than 1 foreign key in a table.

- Foreign key shd refer always primary key either in its own table or in some other table.

RNo	Name	Bx no	Bno	Bname
1	a	101	101	CSE
2	b	101	102	IT
3	c	102	103	ECE
4	d	105X103		

*(Note: In the original image, an arrow labeled 'Fkey' points from Bx no to Bno, and an arrow labeled 'Prim key' points from Bno to Bname.)*

P-key	primary no	rname	HOD	rkey
	1	a	2	
	2	b	—	
	3	c	—	
	4	d	3	
	5	e	3	

Since they are HODs

Q10. how many addnl rows have to be removed if 3,1 is removed.

A	B
1	—
2	1
<del>3</del>	<del>1</del>
4	1
X 5	3
6	→ 5 X
X 7	3
8	→ 6 X

Totally 5 rows have to be removed.

⇒ Eg:-  
 $A \rightarrow B$   
 $C \rightarrow D$   
 $F \rightarrow CH$

If any closure can identify all attr then it is key.

$$A^+ = ABCDH$$

$$A \rightarrow \underline{BCDH}$$

12.  $R = ABCDEH$

$$\underline{A} \rightarrow BC$$

$$CD \rightarrow E$$

$$\underline{E} \rightarrow C$$

$$\underline{D} \rightarrow AEH$$

$$ABH \rightarrow BD$$

$$\underline{DH} \rightarrow BC$$

Single LHS first, find closure.

$$A^+ = ABC$$

$$E^+ = EC$$

$$D^+ \rightarrow DAEHBC$$

$A D$  - Superkey

$C D$  -

$B D$  -

∴ D is a key.

(13)  $R = ABCDE$

$A \rightarrow B$

$B \rightarrow E$

$E \rightarrow A$

$A^+ = AB$

$B^+ = BCE$

$E^+ = EDAB$

$AB^+ = AB$

$BD^+ = BD$

$AD^+ = ADB$

$BCD^+ = BCDEA$  (key)

$ACD^+ = ACDBE$  (key)

ACD is the key.

Note:

ABCDE

$A \rightarrow BDE$

$C \rightarrow E$

$D \rightarrow BC$

$A \times$

$C \times$

$D \times$

$AC \times$

$CD \times$

$AD \times$

$ACD \checkmark$

3 keys

(19)  $ABD \rightarrow E$

$AB \rightarrow G$

$B \rightarrow F$

$C \rightarrow J$

$CJ \rightarrow I$

$G \rightarrow H$

$B^+ = BF$

$C^+ = CJI$

now 2 attr;

$AB^+ = ABGFH$

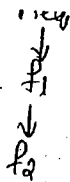
includes majority of attr.

$CJ = CJI$

$ABC^+ = ABGFHCJI$

$ABD^+ = ABGFHDE$

$ABCD^+ = ABGFHFEQI$



$$F = F_1 + F_2$$

$$A \rightarrow B$$

$$B \rightarrow D$$

$$E \rightarrow F$$

$$(G \rightarrow H) \times$$

 $\Rightarrow$ 

$$A \rightarrow B$$

$$B \rightarrow D$$

$$E \rightarrow F$$

Total func dependency  $F = F_1 + F_2$ . where  $F_1$  is derived from regm. and  $F_2$  is derived from  $F_1$ .  $F$  is i/p for normalization process.

Before making a move to normalization, we have to evaluate the following; i.e.

- 1) redundant func. dependency.
- 2) redundant left hand attr.
- 3) redundant right hand attr.

20)

$$R = ABCD$$

$$\begin{array}{l} A \rightarrow B \\ C \rightarrow B \\ D \rightarrow ABCD \\ AC \rightarrow D \end{array}$$

Step 1 make RHS single

- 1  $A \rightarrow B$  ✓
- 2  $C \rightarrow B$  ✓
- 3  $D \rightarrow A$  ✓
- 4  $D \rightarrow B \times$
- 5  $D \rightarrow C$  ✓
- 6  $AC \rightarrow D$  ✓

irreducible set

- $$\rightarrow \begin{array}{l} A \rightarrow B \\ C \rightarrow B \\ D \rightarrow A \\ D \rightarrow C \\ AC \rightarrow D \end{array}$$

Step 2

remove ①, compute  $A^+$  from 2, 3, 4, 5, 6  
 $A^+ = A$

remove ②, compute  $C^+$  from 1, 3, 4, 5, 6  
 $C^+ = C$

remv ③, compute  $B^+$  from 1, 2, 4, 5, 6  
 $B^+ = DBC$

remov. ④, compute  $D^+$  from 1, 2, 3, 5, 6  
 $D^+ = DCBA$

remove ⑤, compute  $D^+$  from 1, 2, 3, 4, 6.  
 $D^+ = DBA$

remove ⑥, compute  $AC^+$  from 1, 2, 3, 4, 5  
 $AC^+ = ABC$

Step 2 remove A

$A \rightarrow B$	$A \rightarrow B$
$C \rightarrow B$	$C \rightarrow B$
$D \rightarrow A$	$D \rightarrow A$
$D \rightarrow C$	$D \rightarrow C$
$AC \rightarrow D$	$\cancel{AC} \rightarrow D$
$C^+ = CB$	$C^+ = CDAB$

redundant left

not equivalent - so cant remove A

remove 'C'

$A \rightarrow B$	$A \rightarrow B$
$C \rightarrow B$	$C \rightarrow B$
$D \rightarrow A$	$D \rightarrow A$
$D \rightarrow C$	$D \rightarrow C$
$AC \rightarrow D$	$\cancel{AC} \rightarrow D$
$A^+ = AB$	$A^+ = ABCD$

$\neq$

cant remove C

Step 1

apply union rules.

$A \rightarrow B$	$A \rightarrow B$
$C \rightarrow B$	$C \rightarrow B$
$D \rightarrow A$	$D \rightarrow AC$
$D \rightarrow C$	$D \rightarrow AC$
$AC \rightarrow D$	$AC \rightarrow D$

Q. 21

$AB \rightarrow C$	<u>Step 1</u>
$C \rightarrow B$	single attr on r
$A \rightarrow B$	① $AB = C$
	② $C \rightarrow B$
	③ $A \rightarrow B$

Step 2:

Remove ①, compute  $AB^+$  from 2, 3

$$AB^+ = AB$$

Remove ②, compute  $C^+$  from 1, 3.

$$C^+ = C$$

Remove ③, compute  $A^+$  from 1, 2

$$A^+ = A$$

Step 3

$AB \rightarrow C$	Remove A
$C \rightarrow B$	$B \rightarrow C$
$A \rightarrow B$	$C \rightarrow B$
	$A \rightarrow B$

$$B^+ = B \neq B^+ = BC \text{ cant remove A}$$

remove B

$AB \rightarrow C$	$A \rightarrow C$
$C \rightarrow B$	$C \rightarrow B$
$A \rightarrow B$	$A \rightarrow B$

$$A^+ = CAB = A^+ = ABC$$



now  
 $A \rightarrow C$   
 $C \rightarrow B$   
 $A \rightarrow B^X$

imp 4:

Remove ① & compute  $A^+$  from 2,3

$$A^+ = AB$$

remove ② compute  $C^+$  from 1,3

$$C^+ = C$$

remove ③ compute  $A^+$

$$A^+ = ACB$$

Step 4

$A \rightarrow C$   
 $C \rightarrow B$

$AB \rightarrow C$   
 $C \rightarrow B$   
 $A \rightarrow B$

Question: To check ans. correct  $\rightarrow$  equivalence chk.  
 left hand side removal - step 3.  
 right hand side " - step 2.

### Classification of FDs

Partial FDs

Transitive FDs

Full func. dependency

#### 1) Partial

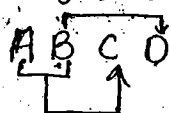
All nonkey attributes must depend totally on primary key attributes.

$R = ABCD$

$AB \rightarrow C$

$B \rightarrow D$  (partially dependant on  $AB$ )

key: AB



Note: Under the following circumstances a table ~~can~~ cannot have partial dependencies:

a) If 1<sup>st</sup> key consists single attribute.

b) If table has only 2 attr.

c) If all attr in a table are part of primary key.

## Transitive

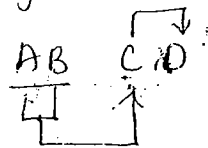
If there is a relation among monkey attr, then it is transitive dependency.

$R = ABCD$

$AB \rightarrow C$

$C \rightarrow D$

Key:  $AB$



here  $AB$  shd have identified  $D$   
but  $C \rightarrow D$ . not  $AB \rightarrow D$ .

Under the following circumstances, no transitive

a) If table consists only 2 attr.

b) If all attr in a table is part of prim. key.

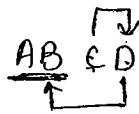
$ABCD$

$AB \rightarrow C$

$C \rightarrow D$ , (Trans)

$D \rightarrow B$

$BC \rightarrow D$



non key attr identifies  $B$ .

## Full functional

If there is a dependency of the form  $X \rightarrow Y$   
then the removal of attr/attrs from  $X$  makes  
 $X \rightarrow Y$  invalid.

## Normalization Tool

It is an evaluation tool to evaluate  
logic database design while insertion, deletion &  
modification problems.

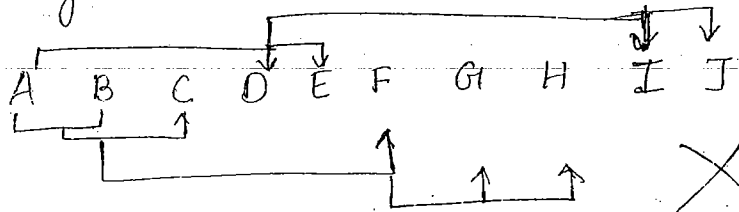
It is a process of reducing redundancy  
by eliminating ins, del & mod problems.



29.43

25. F:  $AB \rightarrow C$   $R = ABCDEFGHIJ$   
 $A \rightarrow DE$  (PD)  
 $B \rightarrow F$  (PD)  
 $F \rightarrow GH$   
 $D \rightarrow IJ$

(a) Key: AB.



use closure method

$$A^+ = \underline{ADEIJ}$$

$$B^+ = \underline{BFGH}$$

2NF

$$\begin{aligned} R_1 &= \underline{A} DEIJ \\ R_2 &= \underline{B} FGH \\ R_3 &= \underline{AB} C \end{aligned}$$

Note:

If there is a partial dependency remove partially dependent attr from original table along with copy of its determinant.

40)  $A \rightarrow B$   
 $B \rightarrow C$   
 $C \rightarrow D$

key: A

a) 2NF  $A^+ = \underline{ABCD}$

b) 3NF

$$\begin{aligned} &\underline{CD} \\ &\underline{BC} \\ &\underline{AB} \end{aligned}$$

c) 3NF = BCNF

Q. 42

FD Normal form

(15)

22.  $ABD \rightarrow AC$

$C \rightarrow BE$

$AD \rightarrow BF$

$B \rightarrow E$

Step 1:  $\alpha$ .

$ABD \rightarrow AX$

$ABD \rightarrow C \checkmark$

$C \rightarrow B \checkmark, C \rightarrow EX$

$AD \rightarrow B \checkmark$

$AD \rightarrow F \checkmark$

$B \rightarrow E \checkmark$

~~etc~~

Step 2:

①  $ABD^+ = ABCDEBF$

②  $ABD^+ = ABDEEF$  (C missing)

③  $C^+ = CE$  (no B)

④  $C^+ = CBE$  (E present)

⑤  $AD^+ = ADF$  (no B)

⑥  $AD^+ = ADBC E$  (no F)

⑦  $B^+ = B$  (no E)

ii.  $ABD \rightarrow C$

$C \rightarrow B$

$AD \rightarrow B$

$AD \rightarrow F$

$B \rightarrow E$

Remove A

$ABD \rightarrow C$

$C \rightarrow B$

$AD \rightarrow B$

$AD \rightarrow F$

$B \rightarrow E$

~~etc~~

$BD^+ = BDE$

$AD^+ = ABCDFE$

$D^+ = D$

$BD \rightarrow C$

$C \rightarrow B$

$AD \rightarrow B$

$AD \rightarrow F$

$B \rightarrow E$

~~etc~~

$BD^+ = BDC E$

not equal

Remove B

$AD \rightarrow C$

$C \rightarrow B$

$AD \rightarrow B$

$AD \rightarrow F$

$B \rightarrow E$

$AD^+ = ADCBEF$

equal  
hence B can be removed.

$ABD \rightarrow C$

$C \rightarrow B$

$AD \rightarrow B$

$D \rightarrow F$

$B \rightarrow E$

$D^+ = DBF$

can't remove A

can't remove D

iii.  $AD \rightarrow C$

$C \rightarrow B$

$AD \rightarrow F$

$B \rightarrow E$

$AD \rightarrow R$

Union.  $AD \rightarrow CFB$

$C \rightarrow B$

$B \rightarrow E$

23)  $A \rightarrow BC$   
 $ABE \rightarrow CDGH$   
 $C \rightarrow GD$   
 $D \rightarrow G$   
 $E \rightarrow F$

Step 1:

~~$A \rightarrow B$~~   
 ~~$A \rightarrow C$~~   
 $ABE \rightarrow CX$   
 $ABE \rightarrow DX$   
 $ABE \rightarrow GX$   
 $ABE \rightarrow H$   
 $C \rightarrow GX$   
 $C \rightarrow D$   
 $D \rightarrow G$   
 $E \rightarrow F$

Step 2:

- ①  $A^+ = ACGDG$  (no B)
- ②  $A^+ = AB$  no C
- ③  $ABE^+ = ABEDGHFC$  (all)
- ④  $ABE^+ = ABECGHDGF$  (all)
- ⑤  $ABE^+ = ABECDHGF$  (all)
- ⑥  $ABE^+ = ABEC DG F$  (no H)
- ⑦  $C^+ = CDG$
- ⑧  $C^+ = CG$  no D
- ⑨  $D^+ = D$  no G
- ⑩  $E^+ = E$  no F

i.  $A \rightarrow B$   
 $A \rightarrow C$   
 $ABE \rightarrow H$   
 $C \rightarrow D$   
 $D \rightarrow G$   
 $E \rightarrow F$

$BE^+ = BEF$   
 $AE^+ = AEB CF$   
 $AB^+ = ABCD$   
 $G$

Step 3:

remove A  
 $BE^+ = BEHF$   
 not remove A  
 remove B  
 $AE^+ = AEB CF$   
 equal.  
 remove E  
 $AB^+ = ABCDGH$   
 not equal

ii.  $A \rightarrow B$   
 $A \rightarrow C$   
 $AE \rightarrow H$   
 $C \rightarrow D$   
 $D \rightarrow G$   
 $E \rightarrow F$

Union

$A \rightarrow BC$   
 $C \rightarrow D$   
 $D \rightarrow G$   
 $E \rightarrow F$   
 $AB \rightarrow H$

24.  $BCD \rightarrow A \checkmark$   
 $BC \rightarrow E \checkmark$   
 $A \rightarrow F \checkmark$   
 $F \rightarrow G \checkmark$   
 $C \rightarrow D \checkmark$   
 $A \rightarrow G \times$   
Step 1 satisfied.

step 2.

$BCD^+ = BCDE$  no A  
 $BC^+ = BCDA GF$  no E  
 $A^+ = A G$  no F  
 $F^+ = F$  no G.  
 $C^+ = C$  no D  
 $A^+ = A F G$  (G present)

(2) (16)

25.  $BCD \rightarrow A$   
 $BC \rightarrow E$   
 $A \rightarrow F$   
 $F \rightarrow G$   
 $C \rightarrow D$   
 $BC^+ = BCEDAFG$   
 $BD^+ = BD$   
 $CD^+ = CD$

remove D:

$BC \rightarrow B C A E F G$  not equal.

remove C:

$BD^+ = B D A F G$

remove B:

$CD = C$

cnt remove:

~~$BCD \rightarrow A$~~   
 $BC \rightarrow E$   
 ~~$A \rightarrow F$~~   
 ~~$F \rightarrow G$~~   
 $C \rightarrow D$

$BC \rightarrow A$

$BC \rightarrow E$

$A \rightarrow F$

$F \rightarrow G$

$C \rightarrow D$

$\equiv$

$BC \rightarrow AE$

$A \rightarrow F$

$F \rightarrow G$

$C \rightarrow D$

30)

$A \rightarrow B$

$BC \rightarrow E$

$ED \rightarrow A$

Key:  $ACD$

$A^+ = AB$

$C^+ = C$

$D^+ = D$

BCNF

2NF

$\begin{array}{|c|} \hline ACD E \\ \hline A B \\ \hline \end{array}$

no transitive dependency so in 3NF also.

$A \checkmark$

$ACD \checkmark$

$BC \checkmark$

$A \checkmark$

$ED \checkmark$

$BC \rightarrow E$

$E \rightarrow A$

$ACD$

$AB$

$AEC$

$BCE$

34)  $A \rightarrow BC$   
 $ABE \rightarrow CDGH$   
 $C \rightarrow GD$

$D \rightarrow G$

$E \rightarrow F$

Key: AE

$AE^+ = ABCDEFGH$

b) 2NF

$A^+ = ABCGD$

$E^+ = EF$

<u>ABC</u>	2NF
EF	
<u>AEH</u>	

c) 2 trans relations.

A BC  
D G  
C GD  
E F  
A EH

BCNF

Superkey ABE  
 A ✓  
 D ✓  
 C ✓  
 E ✓  
 AE ✓

BCNF

A BC  
D G  
C GD  
E F  
A EH

36)  $R = ABCDE$

$AB \rightarrow CDE$

$A \rightarrow C$

$C \rightarrow D \rightarrow E$

AB

b) 2NF

$A^+ = CA$

$B^+ = B$

<u>AC</u>	2NF
<u>ABDE</u>	

<u>AC</u>	3NF
<u>ABD</u>	
<u>DE</u>	

BCNF

AB A  
 A AB  
 D D

also BCNF.

37)  $AB \rightarrow CDE$

$A \rightarrow C$

$C \rightarrow D$

ABCDE

key: AB

b)  $A^+ = ACD$

$B^+ = B$

<u>ACD</u>	2NF
<u>ABE</u>	

<u>A</u> C	3NF	3NF <sub>2</sub>	BCNF
<u>C</u> D			
<u>ABE</u>			

d) BCNF: AB A  
 A C  
 C AB



26.

 $R = ABCDEF$  $A \rightarrow FC$  $C \rightarrow D$  $B \rightarrow E$ 

① Key: AB

②  $A^+ = \underline{AFCD}$  $B^+ = \underline{BE}$ ~~ABDEF~~ $R_1 = \underline{ACDF}$  $R_2 = \underline{BE}$  $R_3 = \underline{AB}$ 

27.

 $R = ABCDE$  $B \rightarrow E$  $C \rightarrow D$  $A \rightarrow B$ 

a) Key: AC

b)  $A^+ = \underline{ABE}$  $C^+ = \underline{CD}$ ~~ABCDE~~ $R_1 = ABE$  $R_2 = \overset{C}{\cancel{A}}D$  $R_3 = AC$

28)  $R = ABCDEFGHIJ$

$AB \rightarrow C$

$BD \rightarrow EF$

$AD \rightarrow GH$

$A \rightarrow I$

$H \rightarrow J$

Key: ABD

$AB^+ = \underline{ABC}I$

$BD^+ = \underline{BDEF}$

$AD^+ = \underline{AD}GHIJ$

$R = ABCDEFGHIJ$

$R_1 = \underline{ABC}I \leftarrow \begin{matrix} A^+ = AI \\ B^+ = B \end{matrix} \begin{matrix} R_1 = \underline{AI} \\ R_2 = \underline{ABC} \end{matrix}$   
 $R_2 = \underline{BDEF} \leftarrow \begin{matrix} B^+ = B \\ D^+ = D \end{matrix} \begin{matrix} R_3 = \underline{BDEF} \end{matrix}$   
 $R_3 = \underline{AD}GHIJ \leftarrow \begin{matrix} A^+ = AI \\ D^+ = D \end{matrix} \begin{matrix} R_4 = \underline{AI} \\ R_5 = \underline{AD}GHIJ \\ R_6 = \underline{ABD} \end{matrix}$   
 $R_4: ABD$

redundant

Finally,  $\begin{matrix} AI \\ ABC \\ BDEF \\ ADGHIJ \\ ABD \end{matrix}$

3NF

AI

3NF

A table is said to be in 3NF, if it is already in 2NF and shd be free from transitive dependencies.

Note:

If there is a transitive dependency, remove transitively dependent attr from 2NF table & place in separate table.

Q: 25:

$R_1 = \underline{ADE}IJ$

$R_2 = \underline{BFGH}$

$R_3 = \underline{ABC}$

$\Rightarrow \begin{matrix} DIJ \\ ADE \\ FGH \\ BF \\ ABC \end{matrix}$

Q: 26.

$R_1 = \underline{ACDE}$

$R_2 = \underline{BE}$

$R_3 = \underline{AB}$

$\underline{CU}$

$\underline{ACF}$

$\underline{BE}$

$\underline{AB}$

$A \rightarrow FC$

$C \rightarrow D$

$B \rightarrow E$

(18)  $AB$   $ACF$

$A^+ = AFCD$

$B^+ = BE$

10/10

while decomposing universal table, we are eliminating insertion, deletion and modification problem.

Beyond 3NF. if we make a move, these problems are further reduced but at the same time, we will invite few additional problems. Therefore they must be verified in BCNF and beyond that. They are:-

- ① Lossless join property. (mandatory)
- ② Dependency preserving property (optional)

Lossless join property:

A decomposition is said to be lossless if natural join of all decompositions = universal relations. (original table)

$R = \pi_{R_1}(R) \bowtie \pi_{R_2}(R) \dots \pi_{R_n}(R)$  - lossless

$R \subset \pi_{R_1}(R) \bowtie \pi_{R_2}(R) \dots \pi_{R_n}(R)$  - lossy

where  $R_1, R_2 \dots R_n$  are fragmentations of universal relation  $R$ .

A	B	C
$a_1$	$b_1$	$c_1$
$a_2$	$b_2$	$c_2$
$a_3$	$b_1$	$c_3$

$R_1$

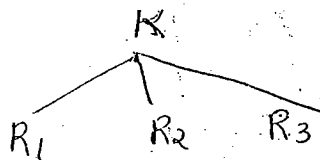
$R_2$

A	B	B	C
$a_1$	$b_1$	$b_1$	$c_1$
$a_2$	$b_2$	$b_2$	$c_2$
$a_3$	$b_1$	$b_1$	$c_3$

Check:  $R = \pi_{R_1}(R) \bowtie \pi_{R_2}(R)$

A	B	C
$a_1$	$b_1$	$c_1$
$a_1$	$b_1$	$c_3$
$a_2$	$b_2$	$c_2$
$a_3$	$b_1$	$c_1$
$a_3$	$b_1$	$c_3$

Hence not equal.



9-30-1 calculus  
807

$R_1 \cap R_2 \rightarrow R_1$   
 $R_1 \cap R_2 \rightarrow R_2$

*If common column is key*

$R_1 \cap R_2 \rightarrow R_1$  key.

$R_1 \cap R_2 \rightarrow R_2$  key.

2-5 digital  
312.

$(R_1 \cup R_2) \cap R_3 \rightarrow R_3$

$(R_1 \cup R_2) \cap R_3 \rightarrow (R_1 \cup R_2)$

if  $R_1 \cap R_2$  is a key  
either in  $R_1$  or  $R_2$   
then it is lossless  
otherwise lossy.

Dependency preserving properties

① a decomposition is said to be dependency preserving decomposition if  $(F_1 \cup F_2 \dots F_n)^+ = F^+$

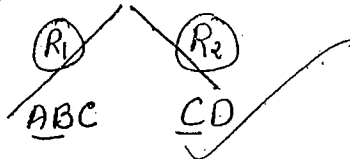
$F_1 \Rightarrow$  set of func. dependencies in  $R_1$

$F_2 \Rightarrow$  " " " " in  $R_2$  & so on.

Eg:- A table  $R = ABCD$

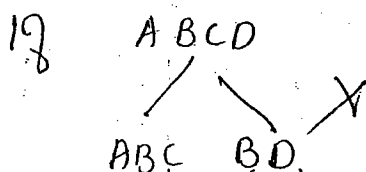
$AB \rightarrow C$   
 $C \rightarrow D$

decomposed into



$F_1: AB \rightarrow C$

$F_2: C \rightarrow D$



$F_1: AB \rightarrow C$

$F_2: \phi$

The following cases are not properly handled by 3NF: (E)

① If table consists composite primary keys (AB, CD, EF)

② If composite prim. keys consists overlapping attributes

Differences b/w 3NF and BCNF:

3NF

BCNF

1) Its focus is on 1<sup>st</sup> key

1) Its focus is on candidate key.

2) In 3NF, possibility for high degree of insertion, deletion & mod. problems due to candidate keys.

2) They are very much reduced as BCNF is taking care of candidate keys.

3) If there is a dependency,  $X \rightarrow Y$ , it is allowed in 3NF, if X is a superkey or Y is part of some key

3) If there is a dependency of the form  $X \rightarrow Y$ , X should be a superkey.

BCNF

more

reduces problems less comp. to 3NF  
dependency

A table is said to be in BCNF if it is already in 3<sup>rd</sup> normal form and all determinants are keys.

NOTE:

① If any dependency violates BCNF rule, then place RHS attributes of that dependency in a separate table along with copy of LHS, then remove <sup>max</sup> RHS attr from 3NF tables.

1<sup>st</sup> → Primary

32.

$R(ABCDEFGH)$

$AB \rightarrow CEFGH$

$A \rightarrow D$

$F \rightarrow G$

$FB \rightarrow H$

$HBC \rightarrow ADEFG$

$FBC \rightarrow ADE$

a) key: AB

b) 2NF

$A^+ = AD$

$B^+ = B$

$R_1 = AD$

$R_2 = ABCEFGH$

partial

c) 3NF

$R_1 = AD$

$R_2 = FG$

$R_3 = ABCEFGH$

transitive

d) BCNF

keys

A

F

AB

determine

$AB^+$

$A^+$

$F^+$

$FB^+$

$HBC^+$

$EBC^+$

AD

FG

FBH

ABCEFG

33.

$R = ABCDEFG$

$BCD \rightarrow A$

$BC \rightarrow E$

$A \rightarrow F$  (TD)

$F \rightarrow G$  (TD)

$C \rightarrow D$

$A \rightarrow G$  (TD)

a) key: BC

b) 2F

$B^+ = B$

$C^+ = CD$

$R_1 = CD$

$R_2 = ABCDEFG$

transitive

(c)  $R_1 = \underline{CD}$

$R_2 = \underline{AF}$

$R_3 = \underline{EG}$

$R_4 = \underline{AG}$

$R_5 = A \underline{BCE}$

can't be combined since they have trans-depen.

(20)

(d) BCNF

(all other's key)

C-

BCD (superkey)

A-

BC-

F-

A-

A-

F-

BC-

C-

A-

3NF = BCNF.

39.

$R_2 = ABCDE$

$AB \rightarrow CDE$

$C \rightarrow A$

$D \rightarrow E$

(a) key = AB

(b) 2NF = AB CDE

(c) 3NF

$R_1 = \underline{D.E}$

$R_2 = \underline{ABCD}$

d) BCNF

key  
D-

diff.  
AB-

AB-

C-? check whether C is superkey

D-

$R_1 = \underline{CA}$

$R_2 = \underline{DE}$

$R_3 = \underline{ABCD}$

One table is subset of another table

41.

 $R \rightarrow ABCD$  $AB \rightarrow CD$  $(C \rightarrow A)$  $A \rightarrow C \text{ (PD)}$ 

(a) key = AB

(b)  $A^+ = AC$  $B^+ = B$  $R_1 = \underline{AC}$  $R_2 = \underline{ABD}$ 

(c) 3NF

 $R_1 = \underline{AC}$  $R_2 = \underline{ABD}$ 

3NF = 2NF

(d) BCNF

key: A

AB

 $R_1 = \underline{AC}$  $R_2 = \underline{ABD}$ 

degenerate

AB

C?

A

same.

38)  $A \rightarrow BCDEF$  $B \rightarrow CD$  $C \rightarrow D$  $E \rightarrow F$  $E \rightarrow B$ 

key: A

b)  $A^+ = \underline{ABCDEF}$ 

in 2NF

P.D.

T.O.

<u>B</u>	C	D
<u>C</u>	D	
<u>E</u>	B	
<u>E</u>	F	
<u>A</u>	C	E

3NF

d) A  
B  
C  
E  
EB  
C  
E  
E  
A

BCNF

15/10/10

35) (1)  $R = ABCD$ (i)  $B \rightarrow C$  $D \rightarrow A$ 

It is preserving dependencies but lossless join property is not preserved. hence decomposition is bad.

(2)  $AB \rightarrow C$  $C \rightarrow A$  $C \rightarrow D$  $\bar{C}$  can det A & D

So Lossless join.

A	<u>C</u>	D

B	C



It satisfies lossless join property, BCNF but not dependency preserving property.

5)  $R = ABCD$

$A \rightarrow B$

$B \rightarrow C$

$C \rightarrow D$

A	B

$R_1$

A	D

$R_2$

C	D

$R_3$

It is not preserving lossless join property.

$\therefore$  decomposition is bad.

Q. 43 31.)  $R = ABCD$

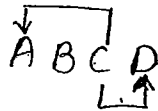
I)  $C \rightarrow D$

$C \rightarrow A$

$B \rightarrow C$

a) Key: B

b) transitive dependency present,  $\therefore$  it is in 2NF but not 3NF.



c)

<u>CD</u>
<u>CA</u>
<u>BC</u>

C    C-  
C    C-  
B    B-

$\Downarrow$   
BCNF

II)  $B \rightarrow C$

$D \rightarrow A$

Key: BD

1NF but not 2NF

BD AC

<u>BC</u>
<u>DA</u>
<u>BD</u>

2NF = 3NF = BCNF

B | B  
D | D

5)  $AB \rightarrow C$

$AB \rightarrow D$

$C \rightarrow A$

$D \rightarrow B$

a) Key:  $AB$

b)  $\overline{AB} \overline{CD} = 2NF = 3NF$

$C \rightarrow A$

$D \rightarrow B$

are not allowed in BCNF

CA

DB

ABCD

ABCD

↓

2 tables are subsets of ABCD.

Rakhu

Advantages of normalization:

① It improves query retrieval performance.

② It eliminates insertion, deletion and mod. problems to great extent.

Disadvantages:

① It degrades query retrieval performance.

② Normalized tables will lose real world meaning.

## Fundamental SQL queries: SQL

(22)

Queries based on logical ops , AND, OR,  $\leq$ ,  $\geq$ ,

- 1) SELECT \* <sup>from</sup> student where age  $> 17$  or branch = IT.
- 2) SELECT \* from student where (city = Hyd and branch = CSE)  
or age  <sup>$> 20$</sup>  ~~is greater~~

Queries based on range ops (between / not between)

- ① Select \* from student where marks b/w 300 and 400;
- ② " " " " name b/w 'A' and 'K';
- ③ " " " " marks b/w 17 and 15;

b/w is inclusive.

$$\textcircled{B} \quad \begin{array}{c} 17 - 15 \times \\ \underline{15 - 17} \end{array}$$

Queries based on set membership IN / not IN.

Find details of the students from 1<sup>st</sup>, 2<sup>nd</sup> and 3<sup>rd</sup> yr.

- 1) Select \* from student where year = 1 or year = 2 or year = 3.
- 2) Select \* " " " " year in (1, 2, 3).
- 3) " " " " " " year b/w 1 and 3.
- 4) " " " " " " year ~~not in~~ 4 (x not work <sup>always</sup>)
- 5) " " " " " " year  $\leq 3$ .
- 6) " " " " " " not in (4) (x " )
- 7) " " " " " " year  $< 4$

Queries based on pattern matching: (like / unlike)

~~The~~ A% start with A

 $\frac{1}{2}A$ 

% A %

' \_ \_ ' 3 letter word.

% / % % escape %

looky for %.

Q: Find details of the students whose name starts with S and third letter is A and last letter is U.

Ans: select \* from student where name like 'S\_a % u'

Q: Find details of the students who are having letter o anywhere.

Ans

where name like '%e %'

Q: Find details of students who are having exactly 3 letter name.

Ans

where name like '— — —'

### Queries based on null value :

is null is !null.

29. Select \* from student where address is null.

where email is not null.

1. Select max(marks) from student.
2. Select max(name) from student.
3. Select avg(marks) from student.
- \* 4. Select avg(name) from student.
- \* 5. Select sum(mark<sub>1</sub>, mark<sub>2</sub>) from student.
6. Select <sup>agg</sup>avg(mark<sub>1</sub> + mark<sub>2</sub>) from student.
7. Select max(distinct marks) from student.
- \* 8. Select <sup>agg</sup>avg(mark<sub>1</sub><sup>2</sup> \*  $\sqrt{\text{mark}_2}$ ) from student.  
log marks
- \* 9. Select rollno, max(marks) from student.
- \* 10. Select \* from student where marks = max(marks).  
syntax error
11. Select sum(marks) / count(marks) from student.
12. Select count(\*) from marks.
13. Select count(~~name~~) from marks.

1/10  
Max and Min func will work both with numeric and non-numeric columns.

6-30-8-30 - Digi  
9-11 - Digi

Sum & Avg only with numeric columns.  
eg: 4)

Aggr func works on single column & produces single col. o/p.

eg. 5 X  
6 ✓

4) Aggr func will work with simple mathematical func.

5) aggr. cant be used in where clause, group by, order by clause.

It is freq. used in select, having clause.

If there is a non aggr column along with aggr col. in select stmt. It shd be associated with group by clause. and all non aggr columns in select stmt shd appear

in gp by clause.

Eg: select rollno, count(marks) from student  
group by rollno.

101	5
102	
103	
104	

↓ This is correct.

This violates 1NF principle.

There is no influence of distinct keyword in max and min func. But it will have an impact on rest of the functions.

6) count \* includes all values.

↳ null values and duplicates

count excludes null values.

in some dbs, it excludes duplicates.

Eg: 

101	}	count *	}	count
102		7		5/4
101				
103				
105				

## Group by

(24)

It is a very useful clause to get group aggr.

eg:- Find the total no. of stud. in each branch.

select brname, count (roll no) from student

group by name;

Eg:-

101	CSE
102	IT
103	CSE
104	ECE
105	CSE

o/p-

CSE	3
IT	1
ECE	1

Eg:- Total

CSE	200
IT	150
ECE	200

CSE	I	50	IT	50
CSE	II	70	IT	25
CSE	III	30	IT	25
CSE	IV	50	IT	50

Eg3: Find details of stud in each branch in each yr.

select brname, year, count (roll no) from student group by brname, year;

4: select brname, year, gender, count (roll no) from student group by brname, year, gender;

CSE	I	M	30
CSE	I	F	20
CSE	II	M	40
CSE	II	F	30

gp by  $\Rightarrow$  for analysis.

Having clause: used to filter group aggregates.

eg: Find total female students in each branch under each yr & display results if count is more than 20 in any yr in any branch.

select brname, year, gender, count(roll no) from student  
 where gender = 'F' group by brname, year  
 having count(roll no) > 20;

Diff. b/w having and where clauses:

- 1) Where is used to filter rows.  
 Having is used to filter groups.
- 2) There is no alternative for 'where'.  
 To filter groups we have options other than 'having'.
- 3) Aggr. can't be used in 'where' clause.  
 can be used in 'having' clause.

Order by

- 1) select \* from student order by roll no.
- 2) select roll<sup>1</sup>no, name<sup>2</sup> from student order by 1, 2;
- 3) select roll no, name from student order by roll no ASC,  
 name DESC;
- 4) select brname, count(roll no) from student group by  
 br name order by count(roll no);  
 aggr. can't be used here
- 5) select roll no, name from student order by roll no,  
 where br = "CSE"; ↓ should be at last

→ Aggr. func are not allowed in order by clause.

∴ we use alias for aggr. func and it is used  
 in order by clause if we want to order based on  
 aggr. values.

branch A	br A
CSE 13	IT 12
IT 12	CSE 3

4<sup>th</sup>: select brname, count(roll no) as 'A' from student  
 group by brname order by 'A';



select bname, count (roll no) as 'A' from student group by  
 bname having A > 25 order by A; (25)  
 not possible (alias not allowed)  
 → having count (roll no) > 25

### Sub Queries:

- 1) It is one of the alternatives to get data from multiple tables.
- 2) It consists of
  - outer query
  - inner query
- 3) There is no restriction on the no. of levels.
- 4) The following optrs cant be used b/w inner & outer queries
  - a) b/w and not b/w.
  - b) like and not like.
  - c) is null and is not null.
- 5) The following optrs alone must be used " "
  - a) in and not in
  - b) any, all, some, greater than any/all,
  - c) exist and not exist

### Classification of subqueries:

#### a) uncorrelated subqueries:

In these, inner query is independent of outer query and it runs only once. Then result is substituted in the outer query.

Eg:- select \* from students where marks <  
 (select avg(marks) from student)

— select \* from student where marks = (select max(marks) from student)  
(display details of stud who got max)

## 2) Correlated subqueries

In this queries inner query uses outer query variable and inner query runs as many times as the no. of values in outer query.

Eg: Find details of students who got  $n^{\text{th}}$  max.

101	550	101	550
102	600	102	600
103	500	103	500
104	400	104	400

*(Note: In the original image, lines connect the '500' values in the first table to the '500' values in the second table, and the '400' value in the first table to the '400' value in the second table, with an 'X' mark over the connection from 104 to 400 in the second table.)*

select \* from student S<sub>1</sub> where 3 = (select count(S<sub>2</sub>.marks) from student S<sub>2</sub> where S<sub>1</sub>.marks < S<sub>2</sub>.marks)

— In another classification of subqueries we classify them as

1) scalar subqueries where one col & 1 row will be displayed.

eg:- select max(marks) from (select \* from students where branch = CSE).

## 2) Row subquery

it retrieves multiple cols. but single row.

## 3) Table subquery

retrieves multiple cols & multiple rows

in and not in opns

(26)

Rno.	Name	B.rno	B.rno	B.rname.
101	a	1	1	CSE
102	b	1	2	IT
103	c	2	3	ECE
104	d	3		

select \* from student where ~~roll no~~ <sup>br.no</sup> in (select brno  
from branch where ~~branch~~ name = 'CSE')

Pg: Pg 51

list out details of all studs who have performed transactions in the library.

select \* from student where rollno in (select distinct  
roll no from library)

Pg 53

Find details of agents from hyderabad and delhi.

select \* from agents where city in ('Hyd', 'Delhi')

Q.03

Q.06.

Q: Find customer ids who have done transactions with agents  
from Delhi or Hyd.

From Table:

Query %p:

identify: Condm:

001

002

003

004

006

[select cid from order where cid in (select aid from  
agents where city in ('Hyd', 'Delhi'))]

Q: Find details of customers who performed transactions  
with agents from 'Hyd' or 'delhi'.

select \* from customer where cid in [\_\_\_\_\_]

IQ

OQ

If there is 'any' optn b/w inner and outer query then condn is considered as true if atleast one of the rows satisfies this condn from the inner query.

If 'all' optn is b/w IQ & OQ, then condn is considered true if it is satisfied by all rows from inner query.

Q: Find details of agent who is offering min<sup>percent</sup> commission

Select \* from agent where percent = 5; (not always)

Select \* from agent where percent = (select min(percent) from agent)

Q: Find details of agents who offer more than min percent commission.

Select \* from agent where percent > any(select percent from agents)

6 ✓	6	> Any	≥ any	> all
6 -	7	6	6	0 0
7 =	6	6	6	
6 =	5	7	7	
5 ✗ not	5	6	6	
5 ✗ greater than any.			5	
			5	

Note:

0 rows:

If inner query retrieves any optn treats this as false  
all optn true condn

B/w inner and outer query if there is an 'exists' operator, this condition is considered as true, if inner query returns non empty set.

If there is 'not exist' operator b/w inner and outer query, the condition is considered as true, if inner query returns empty set.

Note:

Retrieve student details who perform transaction with library

1) Select \* from student where rollno in (select rollno from library)

2) Select S.\* from student S, library L where  
 $S.Rollno = L.Rollno$

3) Select S.\* from student S where rollno exist

(Select \* from library L where  $S.rollno = L.rollno$ )

Q. Find details of customers who purchased both the pds P01, P02

Select cid from order where pid = 'p01';

∩

Select cid from order where pid = 'p02';

(or)

Select O<sub>1</sub>.cid from Order O<sub>1</sub> where O<sub>1</sub>.pid = p01 and exist

(Select \* from order O<sub>2</sub> where O<sub>1</sub>.cid = O<sub>2</sub>.cid  
and O<sub>2</sub>.pid = 'p02')

any & all

1) all queries retnd by exist  
oper may not be possible with  
any and all.

2) It is indepen. of correlated subqueries.

3) Performance is good

exist

1) all queries retnd by any dat  
can be obtained by exist optns

2) all queries are correlated subqueries.

3) <sup>always</sup> performance problems.

## Join operations

Various ways to specify join condns.

① Select \* from student S, library L where S.roll no  
= L.roll no.

②  $n$   $n$   $n$  on g. roll no = L. roll no.

⑤ " " " using roll no.

④ Select \* from student S natural join library L

### Types of joins:

① Natural join

~~2~~ Self join

③ Equijoin

\* (A) Inner join

⑤ Outer join  $\begin{cases} \text{left} \\ \text{right} \\ \text{full outer join} \end{cases}$

Select \* from ~~emp1~~ emp1, emp2 where emp.id = mgr.id;

emp id	name	age	Q	mgr id
1				2
2				2
3				2
4				5

### Inner join

In inner join if two tables are joined, only matching rows are displayed as o/p.

### Outer join

In outer join, apart from matching rows, non-matching rows will also be displayed, but with null values.

In left outer join, everything from LHS is displayed.

If they have a matching row in RHS, that will also be displayed, else r/h side table values are displayed with nulls.

In r/h outer join - opposite of left outer join.

### Full outer join

Full outer join = (left outer)  $\cup$  (r/h outer)

City	
S No	C name
1	Hyd
2	Delhi
3	Chennai

Flight	
F No	Starts from
A01	Bhr
B02	Chennai
C03	Bombay

① select  $C.*$ ,  $f.*$  from city  $C$ , flight  $f$  where  
 $C.cname = f.start\_from$

3	Chennai	BO2	Chennai
---	---------	-----	---------

② select  $C.*$ ,  $f.*$  from city  $C$  left join flight  $f$   
 where  $C.cname = f.start\_from$

1	Hyd	x	x
2	Delhi	x	x
3	Chennai	BO2	Chennai

③ select  $C.*$ ,  $f.*$  from city  $C$  full join right join flight  $f$  where  
 $C.cname = f.start\_from$

x	x	AO1	Bhr
B	Chennai	BO2	Chennai
x	x	CO3	Bombay

1	Hyd	x	x
2	Delhi	x	x
3	Chennai	BO2	Chennai
x	x	AO1	Bhr
x	x	CO3	Bombay



Note: Select  $p.*$  from  $p, q, r$  where  $p.a = q.a$  or  $p.a = r.a$ ; (2x)

- a) returns 0 rows if  $p$  is empty
- b) returns 0 rows if  $q$  or  $r$  is empty.
- c) returns 0 rows if  $q$  and  $r$  are empty.
- d) all of the above.

1) Select rollno, <sup>avg count(marks)</sup> from student group by roll no. where roll no is a primary key.

What is not true abt this query?

- a) length of o/p table is same as original table
- b) o/p table consists duplicates.

☒ c) o/p table never contains duplicate.

d) No syntax error here.

101	500	101	1
102	100	102	1
103	200	103	1
104	300	104	1

2) select  $*$  from student where name like 'A%'.  
equivalent?

(a) select  $*$  from student where name  $\geq 'A'$  or  $\leq 'B'$ ;

(b) " " "  $\geq 'A'$  and  $\leq 'B'$ ;

☒ (c) " " "  $\geq A$  and  $< B$ ;

(d) " " "  $> A$  and  $< B$ ;

3) select  $O_1.pid$  from order  $O_1$  where  $2 \leq (\text{select count}(O_2.cid)$

from order  $O_2$  where  
 $O_1.cid = O_2.cid$ )

☒ a) It retrieves pid purchased by atleast 2 customers.

b) It retrieves pid " " " atmost 2 customers.

c) " " " ~~pid~~ who purchased atleast 2 pdk.

d) " " " ~~cid~~ who purchased atmost

2, 3, 4

## Classification of relational algebra ops.

Orafaq  
for quest

### 1) Native relational algebra ops

$\sigma$  select

$\pi$  project

$\rho$  rename

$\leftarrow$  assign

$\div$  division

$\bowtie$  join

### 2) Set theory relational operators

$\cup$

$\cap$

$-$

$\times$

### 3) Extended relational algebra ops

max, min, sum, avg, count, count(\*)

### Select

- It is unary optr.

- Degree of o/p relation is same as original relation.

- It eliminates only rows but not columns.

- Commutative in nature.

$$\sigma_{c_1}(\sigma_{c_2}(R)) = \sigma_{c_2}(\sigma_{c_1}(R))$$

$$\sigma_{\langle c_1 \rangle}(\sigma_{\langle c_2 \rangle}(\sigma_{\langle c_3 \rangle}(R))) = \sigma_{\langle c_1 \rangle \text{ and } \langle c_2 \rangle \text{ and } \langle c_3 \rangle}(R)$$

$$\pi_{\text{attr-list}}(R)$$

- degree of resultant R is equivalent to attr-list.

- It is not commutative.

$$\pi_{\text{name}}(\pi_{\text{name, rollno}}(\text{student})) \neq \pi_{\text{name, rollno}}(\pi_{\text{name}}(\text{student}))$$

- Eliminates column, but it will also eliminate duplicate rows.

$$RA: \pi_{\text{rollno, name}}(\sigma_{\text{age} > 15}(\text{student}))$$

SQL: select rollno, name from student where age > 15;

SQL: select \* from student where age > 15

$$RA: \sigma_{\text{age} > 15}(\text{student})$$

SQL: select rollno, name from student

$$RA: \pi_{\text{rollno, name}}(\text{student})$$

SQL: select \* from student;

RA: student;

$$\rho(stu - CSE) \leftarrow (\sigma_{br=CSE}(student))$$

after this we can use this new name

~~select~~ name, age (stu-CSE)

$\sigma_{age > 15}$  (stu-CSE)

If there is no rename then

$\sigma_{age > 15 \text{ and } br=CSE}(student)$

Division

R

S

CNo	PNo
1	101
2	102
3	101
4	101
1	102

PNo
101
102

$$R \div S = \frac{CNo, PNo}{PNo} = \begin{array}{|c|} \hline CNo \\ \hline 1 \\ \hline \end{array}$$

Eg ①:

A B C

a<sub>1</sub> b<sub>1</sub> c<sub>1</sub>

a<sub>2</sub> b<sub>1</sub> c<sub>2</sub>

a<sub>1</sub> b<sub>2</sub> c<sub>1</sub> ✓

a<sub>1</sub> b<sub>2</sub> c<sub>2</sub> ✓

a<sub>2</sub> b<sub>1</sub> c<sub>2</sub>

a<sub>1</sub> b<sub>2</sub> c<sub>3</sub> ✓

a<sub>1</sub> b<sub>2</sub> c<sub>3</sub> ✓

a<sub>1</sub> b<sub>1</sub> c<sub>3</sub>

$$S_1 = \frac{C}{C_1}$$

$$S_2 = \frac{C}{\begin{array}{c} C_1 \\ C_2 \\ C_3 \\ C_4 \end{array}}$$

$$S_3 = \begin{array}{|c|c|} \hline B & C \\ \hline b_1 & c_1 \\ b_2 & c_2 \\ \hline \end{array}$$

$$R \div S_1 = \frac{AB \cancel{C}}{\cancel{C}} =$$

A	B
a <sub>1</sub>	b <sub>1</sub>
a <sub>1</sub>	b <sub>2</sub>

$$R \div S_2 = \frac{ABC}{\cancel{C}} =$$

A	B
a <sub>1</sub>	b <sub>2</sub>

combination having all C<sub>1</sub> C<sub>2</sub>, C<sub>3</sub> C<sub>4</sub>

$$R \div S_3 = \frac{A \ B \ C}{B \ C} = \boxed{\begin{matrix} A \\ a_1 \end{matrix}}$$

A	B	C
$a_1$	$b_1$	$c_1$
$a_2$	$b_1$	$c_2$
$a_3$	$b_2$	$c_3$

A	B	C
$a_2$	$b_2$	$c_2$
$a_2$	$b_1$	$c_2$
$a_3$	$b_3$	$c_3$

$$R \cup S =$$

A	B	C
$a_1$	$b_1$	$c_1$
$a_2$	$b_1$	$c_2$
$a_3$	$b_2$	$c_3$
$a_2$	$b_2$	$c_2$
$a_3$	$b_3$	$c_3$

$$R \cap S =$$

A	B	C
$a_2$	$b_1$	$c_2$

$$R - S =$$

A	B	C
$a_1$	$b_1$	$c_1$
$a_3$	$b_2$	$c_3$

$$S - R =$$

A	B	C
$a_2$	$b_2$	$c_2$
$a_3$	$b_3$	$c_3$

Q: Consider 2 table  $R_1$  and  $R_2$  with  $n_1$  and  $n_2$  rows.  
where  $n_2$  is ~~very~~  $\gg n_1$

Find minimum and maxm rows for each of the  
following relational algebra expression.

Mention assumptions if any.

expression	assumption	Min	Max
$\sigma_{\text{age} > 15}(R_1)$	age	0	$n_1$
$\pi_{\text{name, age}}(R_2)$	name, age no duplicates	$n_2$	$n_2$
$R_1 \cup R_2$	✓	$n_2$	$n_1 + n_2$
$R_1 \cap R_2$	✓	0	$n_1$
$R_1 - R_2$	✓	0	$n_1$
$R_1 \times R_2$	✓	$n_1 \times n_2$	$n_1 \times n_2$

we drop  
my count  
so  $n_1, n_2$

Complete set of relational algebra ops:

$$\sigma, \pi, \cup, -, \overset{\times}{\neq}, \cap, \div, \bowtie$$

$$\textcircled{1} R \cap S = R \cup S - ((S - R) \cup (R - S))$$

$$\textcircled{2} R \bowtie S = \sigma_{\langle C \rangle} (R \times S)$$

$$\textcircled{3} R \div S = T$$

$$T_1 \leftarrow \pi_{\text{attrlist}}(R)$$

$$T_2 \leftarrow \pi_{\text{attrlist}}(S \times T_1) - R$$

$$T = T_1 - T_2$$

Precedence of relational operators:

$\pi$   
 $\sigma$   
 $\times$   
 $\div$   
 $\cap$   
 $\cup$   
 High.  
 ↓  
 Low

## Relational calculus:

RA — How to get

RC — what to get

relational algebra is procedural lang and concerns abt how to get the result.

relational calculus is non procedural & looks for what to get.  
SQL will have more flavours of relational calculus.

RC  $\begin{cases} \rightarrow \text{tuple RC} \\ \quad (\text{no boundary}) \\ \rightarrow \text{Domain RC} \\ \quad (\text{boundary is defnd}) \\ \quad \text{gives finite result.} \end{cases}$

name	age	addr

Eg:

TRC:  $\{ t \mid S(t) \wedge t.br = cse \}$

SQL: select \* from student where br=cse

RA =  $\sigma_{br=cse}(\text{student})$

DRC =  $\{ \underset{\%p}{(Rno, name, br)} \mid \underset{attr}{S(Rno, name, br)} \wedge br = cse \}$

Eg②: SQL: select Rno from student where br=cse;

RA:  $\pi_{Rno}(\sigma_{br=cse}(\text{student}))$

TRC:  $\{ t.rno \mid S(t) \wedge t.br = cse \}$

DRC:  $\{ (Rno) \mid S(Rno, name, br) (name, br) \wedge br = cse \}$

%p

①

total var.

②

not o/p.

③

## Existential quantifier ( $\exists$ )

$(\exists d)(c)$  is considered as true if condn is true for atleast one of the tuples. else it is considered as false.

## Universal

$(\forall d)(c)$  is considered as true if condn is true for all the tuples.

SQL: select \* from student S, ~~table~~<sup>library</sup> L where S.Rno = L.Rno

RA:  $\sigma_{\text{student.rno} = \text{library.rno}}(\text{student} \times \text{library})$

TRC:  $\{ \overset{\text{all cols from } t, L}{t, L} \mid \text{student}(t) \text{ and } (\exists L) \text{ library}(L) \text{ and } t.Rno = L.Rno \}$

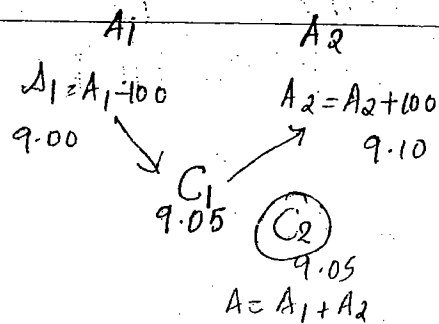
DRC:  $\{ (Rno, name, age), (Rno, S/date, E/date) \mid \text{student}(Rno, name, age) \text{ and } \exists (\text{library})$

$(Rno, S/date, E/date \text{ and } Rno = Rno) \}$



## Transaction:

### Need for transaction:



Trans.  
↓ schedule  
conc. c  
↓  
Serial  
↓

here  $C_2$  gets wrong ans. since run after that there is an updation.

- ① Inconsistent results.
- ② interference from various users in multi user environment.
- ③ ambiguity in deciding when to make changes permanent.

To solve all the probs we have a sol called transactions with 4 properties:

### ④ ACID properties.

Atomicity  
Consistency  
Isolation  
Durability

#### Atomicity:

- Either all or none of the transactions must be executed.
- no partial transactions.
- transaction mgr in dbms ensure this problem.

#### Consistency:

- Transaction opns on db shd bring db from one consistent state to another consistent state.

Eg: withdrawal of money.

maintain min. balance.

- None of the dbms component will ensure this property. Pgrmr must implement this using pgmg logic.

#### Isolation:

- Opns of 1 transaction shdn't be interfered by another transaction.

- concurrency control protocol will ensure this

## Durability

- changes made by the transaction shd be permanent.

Log mechanism will ensure this using transaction & recovery mgrs.

Name	dep	Sal
J	P	500
K	S	600
M	Q	<del>100</del> 600

### Problems:

#### ① Dirty reading

reading uncommitted data  
before committing '600' we perform sm calculation on it  
but instead of committing '600' can be aborted.  
Timing is imp. here.

#### ② Not repeatable values

each write  
imply.

10.10 Set M = 600

10.06 Read sal  $\Rightarrow$  500, 600, 100

10.25 Read sal  $\Rightarrow$  500, 600, 600

#### ③ not repeatable reads (Rows)

10 St Trans1

10.10 Insert new value (Jeff, D, 800)

10.20 Commit1

10.05 St T2

10.25 read salary 500, 600, 100, 800

#### ④ Incorrect summary problems

10. St Tx1

10.10 Set M sal = 600

10.20 C1

10.05 St Tx2

10.06 Sum(sal) 1600

10.25 Sum(sal) 1700

## ⑤ lost update or ww conflict

10.00 St Tx1

10.10 set m sal = 600

~~100 600~~ 700

10.20 C1

10.15 set Tx2

10.16 set m = sal = 700

10.17 C2

## ⑥ Unstable control

10.08 St Tx1

10.10 Drop col sal

10.15 C1

10.05 St Tx2

10.06 Read sal ✓

10.20 Read sal X

To solve transaction problems mentioned above we use schedule.

## Schedule

Order of execution of stmts from different transactions is known as schedule.

Classification of schedule:

Serial schedule

Non serial schedule

recoverable

non-recoverable.

cascading cascades

T<sub>1</sub>

T<sub>2</sub>

S<sub>1</sub>

T<sub>1</sub>

T<sub>2</sub>

S<sub>2</sub>

T<sub>2</sub>

T<sub>1</sub>

giving from T<sub>1</sub> then T<sub>2</sub>

S<sub>2</sub> " " T<sub>2</sub> then T<sub>1</sub>

ie we can have n! schedules possible

$\{T_1\}$  if one is a blk, it stays at halt

$\{T_2\}$

so we look for non ~~serializability~~ serial

$T_1$   
 $T_2$   
 $T_1$   
 $T_2$

$$\text{no. of nonserial schedule} = \frac{(n_1 + n_2 + \dots + n_m)!}{n_1! \cdot n_2! \cdot \dots \cdot n_m!}$$

where  $n_1$  = no. of stmts in transaction 1

$n_2$  = " " " " " " 2

$m$  = no. of transactions.

eg:-  $n_1 = 5$   
 $n_2 = 3$

$$\text{no. of nonserial} = \frac{(5+3)!}{5! \times 3!} = \underline{56}$$

Recoverability (in non serial)

S1:

$T_1$	$T_2$
R(x) 10	R(x)
W(x) 20	W(x)
	R(x)
	C2
a1 $\cancel{C_1}$	

$T_2$  not rolled bk.

if there is a necessity to rollback committed transaction, then schedule is called non-recoverable schedule.

S1 is non recoverable bcz instead of committing if  $T_1$  aborts the optn, then  $T_1$  is rolled bk but  $T_2$  is not rolled bk. but there is a necessity to roll bk.

S2:

$T_1$	$T_2$
R(x)	R(y)
W(x)	W(y)
	R(x)
a1 $\cancel{C_1}$	C2

S2 is recoverable but it is cascading

if  $T_1$  is rolled bk we are able to roll back  $T_2$ .

roll bk of one transaction leads to roll bk of another.

S3:

$T_1$	$T_2$
$R(X)$	
$W(X)$	
$C_1$	
	$R(Y)$
	$W(Y)$
	$R(X)$
	$C_2$

S3 is recoverable cascadeless schedule  
but it is serial schedule.  
but we are interested in non serial

S4:

$T_1$	$T_2$
$R(X)$	
	$R(Y)$
	$R(X)$
$W(X)$	
	$W(Y)$
	$C_2$
$C_1$	

S4 is recoverable cascadeless and  
non serial schedule.

1	1 x x	3
2	2 x ✓	56
	3 ✓ x	2
	x x	48
	48	48
	56 ✓ x	

A schedule S with n transactions is said to be serializable,  
if it is equivalent to a schedule S' with same n transactions.

where  $S \rightarrow$  non serial schedule

$S' \rightarrow$  serial schedule.

3 kinds of serializability

- ① result serial. or result equivalence
- ② conflict " or conflict "
- ③ view " or view "

Q.11.

① O/p result of any transaction heavily depends on initial values of data items. For some initial values o/p ~~may~~ be same, ~~the~~ result equivalence is not valid always.

Eg:-

②

10  $R_1(X)$  |  $W_2(X)$  20  
20  $W_2(X)$  |  $R_1(X)$  20  
X

$R_1(X)$  |  $R_2(X)$   
 $R_2(X)$  |  $R_1(X)$   
✓

$W_1(X)$  |  $W_2(X)$   
 $W_2(X)$  |  $W_1(X)$   
X

$R_1(X)$  |  $W_2(Y)$   
 $W_2(Y)$  |  $R_1(X)$   
✓

$R_1(X)$  |  $W_1(X)$   
 $W_1(X)$  |  $R_1(X)$   
✓

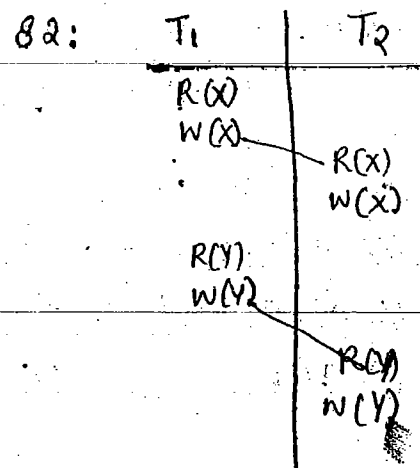
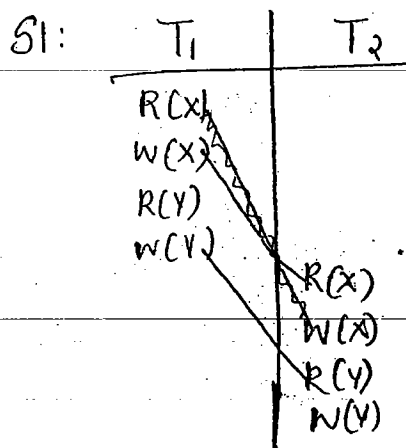
same trans, can't swap opn.  
So can't consider it as conflict opn.

$X_i(A)$ ,  $Y_i(B)$

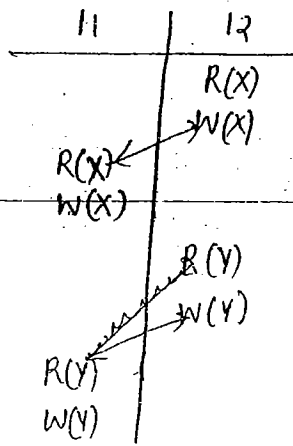
①  $A = B$

②  $i \neq j$

③  $X$  or  $Y$  must be write opn.



SS:



$S_2$  is conflict equi to  $S_1$   
(non serial) (serial)

### Rules for Serializability

a) A non serial schedule  $S^2$  and serial  $S'$  are view equivalent if they meet <sup>all</sup> the following 3 condns:

- ① if  $T_1$  reads initial value of  $X$  in  $S'$  then  $T_1$  shd also read initial value of  $X$  in  $S$
- ② If  $T_2$  performs final write opm on  $X$  in  $S'$ , then  $T_2$  shd also perform final write opm on  $X$  in  $S$ .
- ③ If  $T_2$  reads <sup>a</sup>value produced by  $T_j$  in  $S'$ , then  $T_2$  in  $S$  shd also Read value produced by  $T_j$ .

6-8 Sds.  
404.

6-8:30 CO  
311

## Desirable properties of decomposition:

① lossless join

② dependency preserving.

Note:

If a relation  $R$  is given, then the decomposition of relation into  $R_1$  and  $R_2$  shd be done such that common attribute in  $R_1$  and  $R_2$  is a candidate key of anyone of the relation (either  $R_1$  or  $R_2$ ).

eg:  $R = (A, B, C)$

Decomposition can be done as:

$$R_1 = (A, C)$$

$$R_2 = (B, C)$$

## Dependency preservation:

If a relation ' $R$ ' is given, then it shd be decomposed into relations  $R_1, R_2$  such that the FD's of relation  $R$  can be obtained from FD's of  $R_1$  and  $R_2$ .

$$(F_1 \cup F_2)^+ = F^+$$

eg:-  $R = (A, B, C, D)$

$$A \rightarrow B$$

$$A \rightarrow C$$

$$C \rightarrow D$$

$$R_1 = (A, B, C)$$

$$R_2 = (C, D)$$

$$R_1 \cap R_2 = C$$

$$R_1 \cap R_2 = R_2$$

lossless join property is preserved.

$$FD_1: F_1 = \begin{matrix} A \rightarrow B \\ A \rightarrow C \end{matrix}$$

$$F_2: C \rightarrow D$$

$$F_1 \cup F_2 = \begin{matrix} A \rightarrow B \\ A \rightarrow C \\ C \rightarrow D \end{matrix}$$

Eg 2:  $A \rightarrow B$

$$A \rightarrow C$$

$$C \rightarrow D$$

$$R = (A, B, C, D)$$

$$R_1 = (A, B, D)$$

$$R_2 = (B, C)$$

$$R_1 \cap R_2 = B$$

lossless join not satisfied

$$R_1 \neq (A, B, D) \quad R_2 \neq (B, C)$$

$$A \rightarrow B$$

✓



$S_1$		$S_2$		$S_3$	
$T_1$	$T_2$	$T_1$	$T_2$	$T_1$	$T_2$
$R(A)$		$R(A)$		$R(A)$	
$A = A + 10$		$A = A + 10$		$A = A + 10$	
$W(A)$		$W(A)$		$W(A)$	
$R(B)$		$R(B)$		$R(B)$	
$B = B + A$		$B = B + A$		$B = B + A$	
$W(B)$		$W(B)$		$W(B)$	
	$R(A)$		$R(A)$		$R(A)$
	$A = A + 20$		$A = A + 20$		$A = A + 20$
	$W(A)$		$W(A)$		$W(A)$
	$R(B)$		$R(B)$		$R(B)$
	$B = B + 1$		$B = B + 1$		$B = B + 1$
	$W(B)$		$W(B)$		$W(B)$

$S_2$  is view equivalent to  $S_1$  but  $S_3$  is not view equivalent.

equivalent.

Differences b/w conflict serializability and view serializability

1) All conflict serializable schedules are view serializable but converse not true.

2) It is easy to test and achieve conflict serializ. but it's difficult to test and achieve view serializ.

3) Majority of concurrency control protocols are based on conflict serializ. except Thomas <sup>wait</sup> right rule.

$S_1$		$S_3$	
$T_1$	$T_2$	$T_1$	$T_2$
$W_1(X)$		$W_1(X)$	
	$W_2(X)$		$W_2(X)$
$W_1(X)$		$W_1(X)$	
	$W_2(X)$		$W_2(X)$

$S_3$  is view equivalent to  $S_1$ .

but  $S_3$  is not conflict equiv- to  $S_1$ .

$S_1$		$S_2$		$S_3$	
$T_1$	$T_2$	$T_1$	$T_2$	$T_1$	$T_2$
$R(A)$		$R(A)$		$R(A)$	
$A = A + 10$		$A = A + 10$		$A = A + 10$	
$W(A)$		$W(A)$		$W(A)$	
$R(B)$		$R(B)$		$R(B)$	
$B = B + A$		$B = B + A$		$B = B + A$	
$W(B)$		$W(B)$		$W(B)$	
	$R(A)$		$R(A)$		$R(A)$
	$A = A + 20$		$A = A + 20$		$A = A + 20$
	$W(A)$		$W(A)$		$W(A)$
	$R(B)$		$R(B)$		$R(B)$
	$B = B * 1.1$		$B = B * 1.1$		$B = B * 1.1$
	$W(B)$		$W(B)$		$W(B)$

$S_2$  is view equivalent to  $S_1$  but  $S_3$  is not view equivalent.

equivalent.

Differences b/w conflict serializability and view serializability

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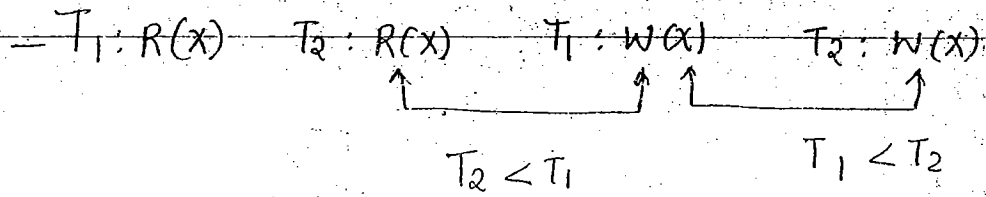
3) Majority of concurrency control protocols are based on conflict serializ. except Thomas <sup>wait</sup> right rule.

$S_1$		$S_3$	
$T_1$	$T_2$	$T_1$	$T_2$
$W_1(X)$		$W_1(X)$	
	$W_2(X)$		$W_2(X)$
$W_1(X)$		$W_1(X)$	
	$W_2(X)$		$W_2(X)$
$W_1(X)$		$W_1(X)$	
	$W_2(X)$		$W_2(X)$

$S_3$  is view equivalent to  $S_1$ .

but  $S_3$  is not conflict equiv. to  $S_1$ .

99/3. a) strict schedules — view, recoverable and cascades  
 serial schedule is strict.  
 first test conflict ser.



not conflict serializable.

$T_1$	$T_2$
$R(x)$	$R(x)$
$W(x)$	$W(x)$

$T_1$	$T_2$
$R_1(x)$	$R_2(x)$
$W_1(x)$	$W_2(x)$
$R_2(x)$	$R_1(x)$
$W_2(x)$	$W_1(x)$

not view serializable.

$R_2$  reads  
value written  
by  $R_1$

— there is no dirty read, therefore it is cascades  
 cascades schedules are recoverable as there is no  
 dirty read.

3(b)  $T_1: W(x), T_2: R(y), T_1: R(y), T_2: R(x)$   
 $\uparrow \quad \quad \quad \uparrow$   
 $T_1 < T_2$

it is conflict equivalent & conflict equivalent  
 to  $T_1$  and  $T_2$  serial schedule  $T_1$  and  $T_2$ .  
 Since conflict equivalent, it is also view equivalent.

$I_1$	$I_2$
$W(x)$	$R(y)$
$R(y)$	$R(x)^*$

since it has dirty read, it is cascading schedule.

$C_2 < C_1$  recoverable

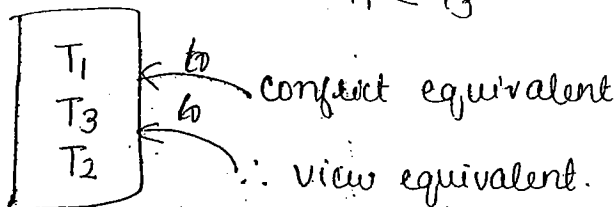
$C_1 < C_2$  recoverable.

Depending on commit recoverability is decided.

3(c)  $T_1: R(x), T_2: R(y), T_3: W(x), T_2: R(x)$

$T_1 < T_3$

$T_3 < T_2$



$T_1$	$T_2$	$T_3$
$R(x)$	$R(y)$	
<del><math>W(x)</math></del>	$R(x)$	$W(x)$

dirty read ( $\therefore$  cascading schedule)

$C_3 < C_2 \rightarrow$  recoverable

$C_2 < C_3 \rightarrow$  not recoverable.

3(d)  $T_1: R(x), T_2: W(x), T_1: W(x), T_2: A, T_1: C$

$T_1 < T_2, T_2 < T_1$

based on rules it's not conflict equivalent

but  $T_2$  is aborted:  $\therefore$  s/m is left with only 1 transaction.

$T_1$	$T_2$
$R(x)$	$W(x)$
$W(x)$	$A_2$
$C_2$	

Cascadeless and recoverable.

all cascadeless are recoverable.

d)  $T_1: R(x), T_1: R(y), T_1: W(x), T_2: R(y), T_3: W(y), T_1: W(x),$   
 $T_2: R(y)$   $T_3 < T_2$   $T_2 < T_3$

$T_1$	$T_2$	$T_3$
$R(x)$		
$R(y)$		
$W(x)$	$R(y)$	
		$W(y)$
$W(x)$	$R(y)$	

it is not conflict equivalent

$T_2$	$T_3$
$T_3$	$T_2$
$R(y)$	$W(y)$
$R(y)$	$R(y)$
$W(y)$	$R(y)$

j)  $T_2: R(x), T_3: W(x), T_3: C, T_1: W(y), T_1: C, T_2: R(y),$   
 $T_2: W(z)$   $T_2 < T_3$   $T_2: C$   $T_1: C$   $T_2: R(y)$   
 since  $T_1$  already C

$T_1$	$T_2$
$T_2$	$T_1$
$T_3$	$T_3$

conflict equivalent

hence

view equivalent too.

$T_1$	$T_2$	$T_3$
	$R(x)$	
		$W(x)$
$W(y)$		$C$
$C$		
	$R(y)$	
	$W(z)$	
	$C$	

no dirty read

so cascadeless & recoverable.

1.)  $T_1: R(x) \quad T_2: w(x) \quad T_1: w(x) \quad T_3: R(x) \quad T_1: C_1 \quad T_2: C \quad T_3: C$   
 $T_1 < T_2 \quad T_2 < T_1$

not conflict equivalent.

$T_1$	$T_2$	$T_3$
$R(x)$		
	$w(x)$	
$w(x)$		
$C$	$C$	$C$

cascading schedule  
 $R(x)$   
 $T_1 \quad T_1 \quad T_2 \quad T_1 \quad T_3 \quad T_3$   
 $T_2 \quad T_3 \quad T_1 \quad T_3 \quad T_1 \quad T_2$   
 $T_3 \quad T_2 \quad T_3 \quad T_2 \quad T_2 \quad T_1$

$T_1 < T_2$  not view equivalent  
 $T_2 < T_1$  "

not view equivalent. too.

cascading schedule but its recoverable since we commit  $T_3$  after  $T_1$ .

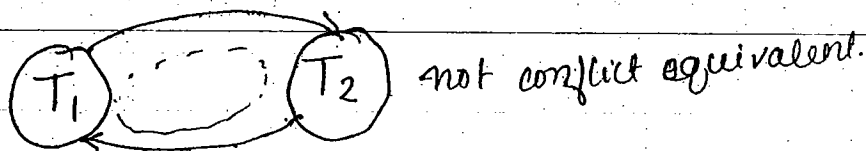
Shortcut to identify conflict serializability  
 by using directed graph.

No. of nodes in the graph is exactly equivalent to no. of transactions in the schedule.

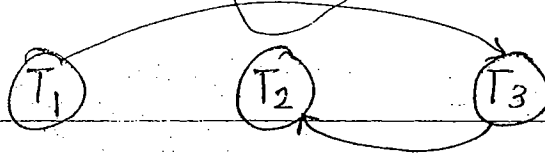
No. of edges in gph = no. of conflict ops in the schedule.

Once gph is drawn, verify for cycles, if graph contains cycles, then it is not conflict serializable.

19/4.  $R_1(x) : R_2(x) : w_1(x) : w_2(x), C_1, C_2$   
 $T_2 < T_1 \quad T_1 < T_2$  not conflict equivalent.



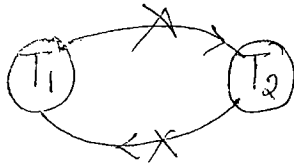
b)  $R_1(X), R_2(Y), W_3(X), R_2(X), R_2(Y), C_1, C_2$



not conflict equivalent.

conflict equivalent to  $T_1 T_3 T_2$

d)  $W_1(X), R_2(X), W_1(X), C_2, C_1$



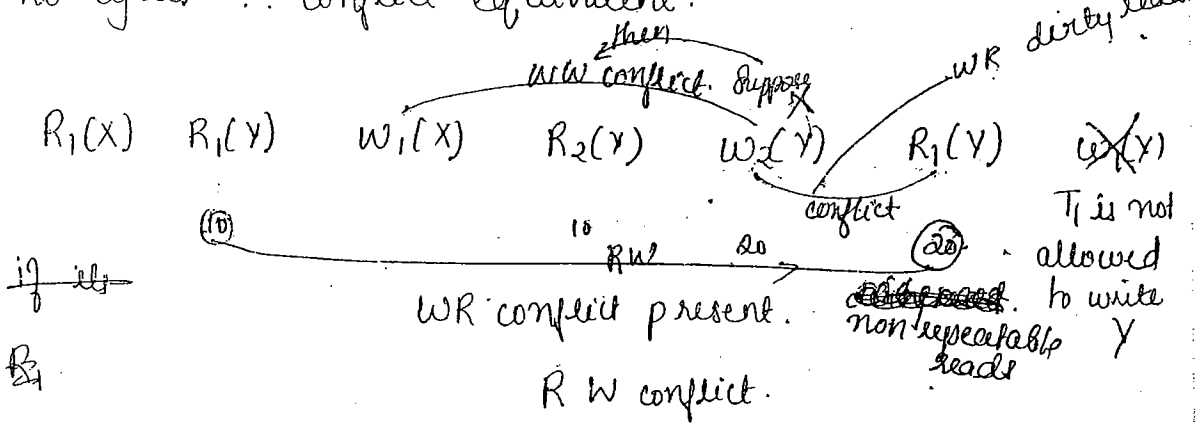
but  $T_1$  is aborted.

so all edges cancelled

$\therefore$  conflict serializable.

(i) no cycles  $\therefore$  conflict equivalent.

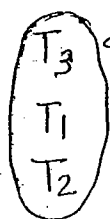
19/2



If there is W b/w R-R then R-W conflict.

99/1

(i)  $r_1(x), r_3(x), w_1(x), r_2(x), w_2(x)$   
 $T_3 < T_1 \quad T_1 < T_2$



conflict equivalent

# Classification of concurrency control protocol

## 1) log-based protocol.

### a) 2 phase log<sup>ckg</sup>

(i) B2PL

(ii) C2PL conservative

(iii) S2PL

(iv) R2PL rigorous

### b) Graph based

## 2) Time stamp based protocol

### a) Timestamp ordering protocol

a) Fitz Thomas Wright.

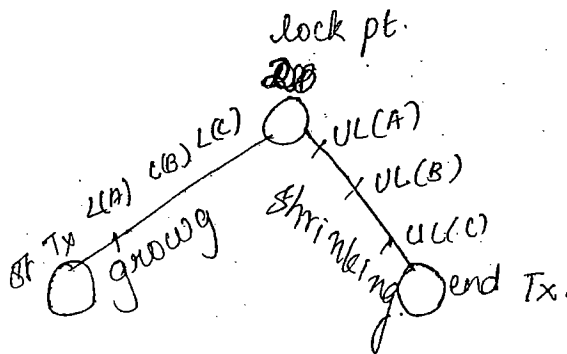
## 3) Multiple granularity protocol.

### a) multiple versional protocol.

a) MV two phase proto.

b) MV timestamp ordering protocol.

locks  
Shared - R.  
Exclusive - W.



all locks in one phase  
after unlock no lockg.  
ie all unlocks  
together.

growing - lockg  
shrinking - unlockg.

RL(A)

WL(A)

RL(B)

RL(C)

✓  
UL(B)  
UL(A)  
UL(C)



2) C2PL

L(A)  
L(B)  
L(C)

St. Tx

UL(A)

UL(B)

UL(C)

end Tx

here no growing phase.

LP.  
L(A)  
L(B)  
L(C)  
St. Tx

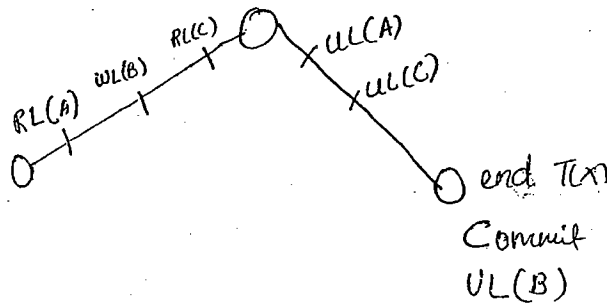
end

If 49 items  
all locked  
1 waiting  
then all  
cant start.  
if items more  
go for B2PL

3) Strict 2PL

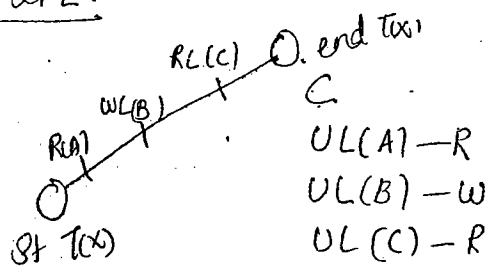
St. Tx

GO'10.



unlock write locks only after committing.

4) Rigorous 2PL:



③ & ④  
are used  
nowadays

eg: St Tx<sub>1</sub>  
R<sub>1</sub>L(A)  
St Tx<sub>2</sub>

W<sub>2</sub>L(B)  
UL(A)  
C<sub>1</sub>  
end Tx<sub>2</sub>

it is strict 2PL.  
C<sub>2</sub>  
UL(B) after committing

assum: of query.

① deadlocks

② starvation

St  $TX_1 - 9.00$

$T_1$   $\boxed{A}$  RTS  $\boxed{9.00}$   
WTS  $\boxed{9.00}$

$R(A) - 9.30$

$W(A) - 10.00$

End  $TX - 10.30$

Read and write timestamp values for a data item is not, actual equal to read and write of a transaction. But its transaction timestamp. Starting time of transaction.

Pg. 88.

8.50 $T_1$	9.00 $T_2$
$W_1(x)$	$W_2(x)$

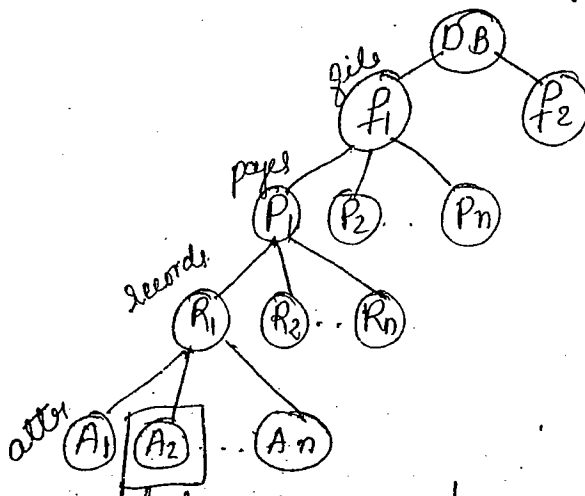
is also  $\leftarrow W_1(x)$   
allowed.

TS  $\rightarrow$  conflict serializ.

Two wright - view serializ.

Multiple Granularity protocol

deals with size of db.



lock on roll no. only. [select \* from student then lock on file. F1. for particular roll no]

SIX condition that  $T_2$  shd vacate when  $T_1$  makes it X

9.00 R	SIX S	9.05 R
9.30 W	X	9.30
10.0		$T_2$

X/S is meaningless

Consider a db with 2 files  $F_1$  and  $F_2$  and  $F_1$  consists pg  $P_1$  to  $P_{1000}$  and  $F_2$  consists  $P_{1001}$  to  $P_{2000}$ . Each pg consists 100 records  $R_1 - R_{100}$ . Each rec is read as  $(P_i, R_j)$

$P \rightarrow$  page no.  $R \rightarrow$  record no. For each of the following ops specify the sequence of blk request

① Read records from  $P_1.98$  to  $P_2.2$

IS on DB  
IS on  $F_1$   
S on  $P_2$   
S on  $P_1$

But if  $P_1.50$  is to be accessed it can't be accessed since it is also locked. 100 recs are locked. reduces concurrency.

②  
IS on DB  
IS on  $F_1$   
IS on  $P_2$   
S on  $P_2.2$   
S on  $P_2.1$   
IS on  $P_1$   
S on  $P_1.100$   
S on  $P_1.99$   
S on  $P_1.98$

good method.

③ Read rec from  $P_{50.1}$  to  $P_{100.1}$

IS on DB  
IS on  $F_1$   
S on  $P_{100}$   
S on  $P_{51}$   
S on  $P_{50}$

lengthy. we need almost 50 locks.

IS on DB  
S on  $F_1$

all thousand under control

concurrency is low.

3) Read ~~record~~  $P_{50}$  to  $P_{500}$ .

locks

IS on DB

IS on  $P_1$

S on  $P_{500}$

...

S on  $P_2$

S on  $P_1$

IS on DB

~~S on  $P_1$~~

4) Delete just record in each page.

IX on DB

IX on  $P_2$

X on  $P_{2000}$

X on  $P_{1001}$

IX on  $P_1$

X on  $P_{1000}$

...

X on  $P_2$

X on  $P_1$

①

IX on DB

X on  $P_2$

X on  $P_1$

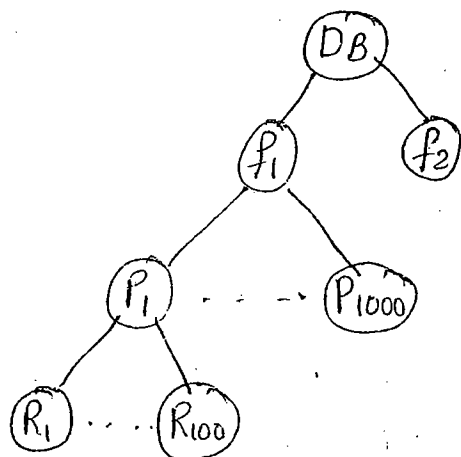
②

X on DB

③

to delete - exclusive lock needed.

Q: Select \* from student. Assume <sup>all</sup> student recs are in  $P_1$ .



no need to hold  $P_2$ .

IS on DB

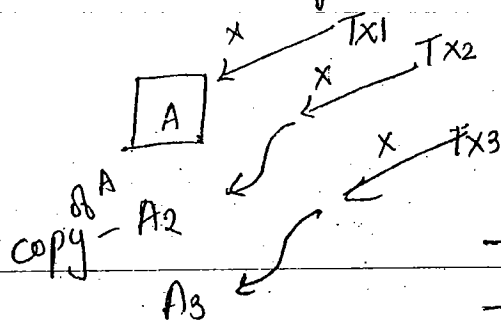
S on  $P_1$

can be read.

S on DB.

since  $P_2$  will also be affected

Multiversion Locking protocol



we create separate version of datattem A. for each Tx

- improves concurrency. but granularity be small as poss
- migrate  $A_3$  to  $A_2$  to  $A_1$
- if  $A_2$  has not completed  $A_3$  can be migrated directly to  $A_1$ .

if we ask lock a file and make copy takes longer time than getting actual lock on that file, then its disadvantages.

From files on disks to DB, multiversion is not advan. because it is time consuming.

In multiversion, we created new Q<sub>1</sub> and give to old timestamp. Before,  $T_s(T_i) < WTS(Q)$  means it has to be rolled back.

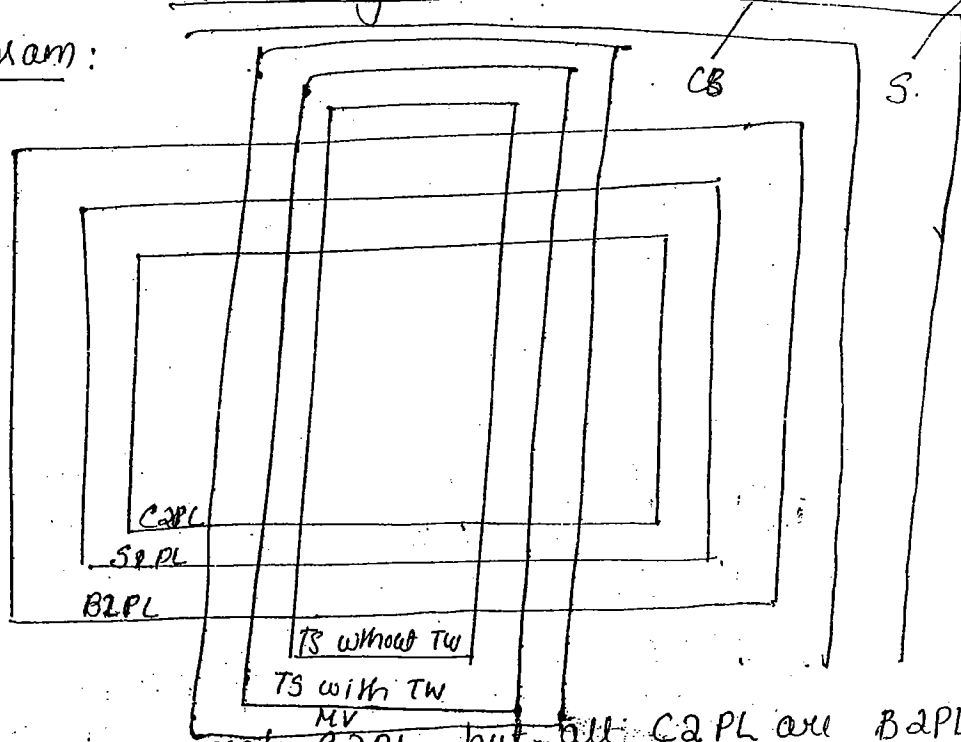
Ques asked

1) strict 2PL (which represents?)  
identity 2PL, BPL.

2) which repres. timestamp ordering?

3) relationship betwn protocols.  
(Venn diagram)

Venn Diagram:



all B2PL are not C2PL but all C2PL are B2PL

## Types of Indexes

- 1<sup>o</sup> index
- clustered index
- 2<sup>o</sup> index

another classification:

- Sparse index
- Dense index

### 1<sup>o</sup> index

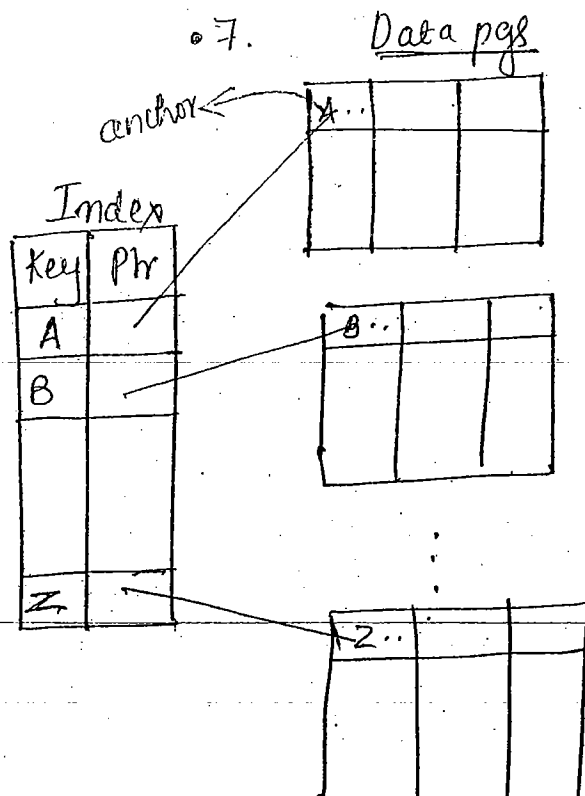
① It is created on primary key of a table hence there shd be only 1 primary index per table.

② It is an eg of sparse index.

③ Both data pgs & indx pgs are ordered.

④ It consists 2 attr — ① ~~set~~ search key value  
② blk pointer.

⑤ Fill factor of data and indx pgs shd be from 0.5 to 1 and mostly it is around



P. key: name.

1<sup>st</sup> rec in each pg is called anchor rec.

Searching

- first in index then to data pgs.

(6) Index pages are developed using anchor rec.

Assume that no. of total records = 30,000,

Length of each record = 100 B, OS

OS page size = 1024 B

$$\text{no. of rec / pg} = \frac{1024}{100} = 10$$

$$\text{no. of pgs reqd.} = \frac{30,000}{10} = 3000$$

no. of index records = 3000

Key = 9 bytes

Ptr = 6 bytes

Length of each record = ~~9~~ 9 + 6 = 15 B

$$\text{no. of index rec / pg} = \frac{1024}{15} = 68 \quad \text{OS pg size.}$$

$$\text{no. of index records} = \frac{3000}{68} = 45$$

(indx pgs)

Case @ Search operation reqd without index

$$\text{No. of searches reqd} = \log_2 3000$$

(Binary)

$$= 12$$

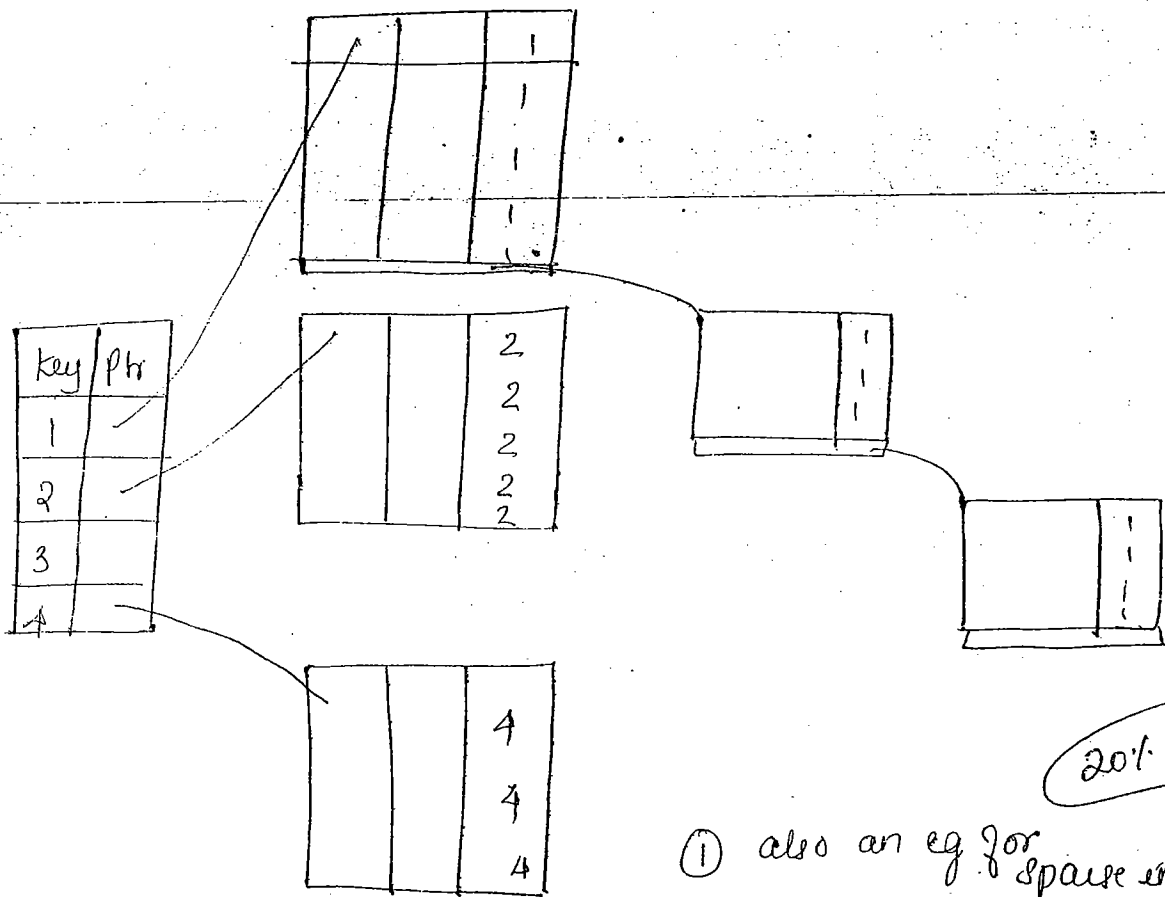
$$\text{No. of searches with indx pgs} = \log_2 45 = 6$$

Search From index to data pg = 1

Total = 7 search.

60% queries  
run on 1<sup>st</sup> keys

of Primary Index is created on a column with unique values.  
But clustered index is created on a gp of values.



- ② Only one cluster index per table
- ③ Both datapgs and index pgs are ordered.

### Secondary index

- ① It is created on other than 1<sup>o</sup> key & clustered col.
- ② It is an example for dense index.
- ③ Each index consists 2 attr.

① Search key values

② Record ptr

Ques ④ Here indx pgs are ordered but not datapgs.

⑤ We can have more than 1 secondary index per table.



		5
		7
		4

for duplicates

		6
		3
		8

key	ptr
1	
2	
3	
4	
5	
6	
7	
8	
9	
10	

		10
		1
		2
		9

$$\text{no. of rec} = 30,000$$

$$\text{length of each rec} = 100 \text{ B}$$

$$\text{OS pg size} = 1024 \text{ B}$$

$$\text{no. of rec/pg} = \frac{1024}{100} = 10$$

$$\text{no. of pgs reqd} = \frac{30000}{10} = 3000$$

$$\therefore \text{No. of indx rec} = 30,000$$

$$\text{key} = 9 \text{ B}$$

$$\text{ptr} = 6 \text{ B}$$

$$\text{len of each record} = 9 + 6 = 15 \text{ B}$$

$$\text{no. of index records/pg} = \frac{1024}{15} = 68$$

$$\text{no. of indx rec} = \frac{30000}{68} = 450$$

Here linear search,

$$\text{we need} = \frac{3000}{2} = 1500$$

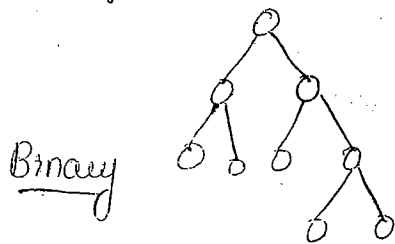
b) with  $\text{index} = \log_2 450 = \underline{9}$

B and B+ trees are multilevel indexes.

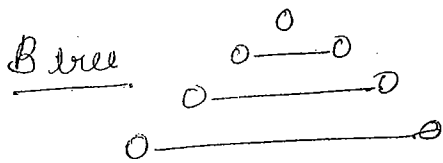
most effective index  
- 2° index

Q Why are we use B & B+ in db?

most useful index  
- 1° index

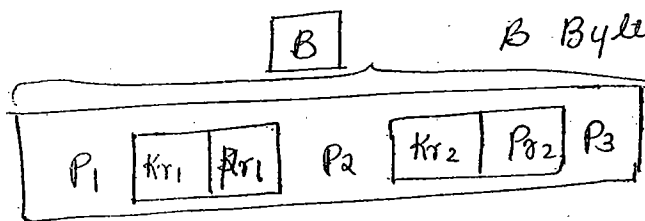


levels are more.  
grows vertically



grows horizontally.  
with less no of levels.

data items placed at equidistance  
from root.



B Bytes.

$P \rightarrow \text{blk ptr}$

$K_v \rightarrow \text{key value}$

$P_n \rightarrow \text{data ptr}$

$B \rightarrow \text{size of pg}$

$n \rightarrow \text{order of pg}$

$$nP + (n-1)K_v + (n-1)P_n \leq B$$

eg:-  $P = 6B$

$K_v = 9B$

$P_n = 7B$

$B = 512B$

$$n \times 6 + (n-1)9 + (n-1)7 \leq 512$$

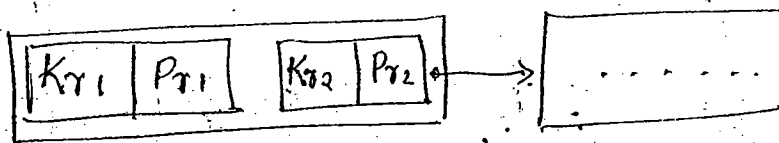
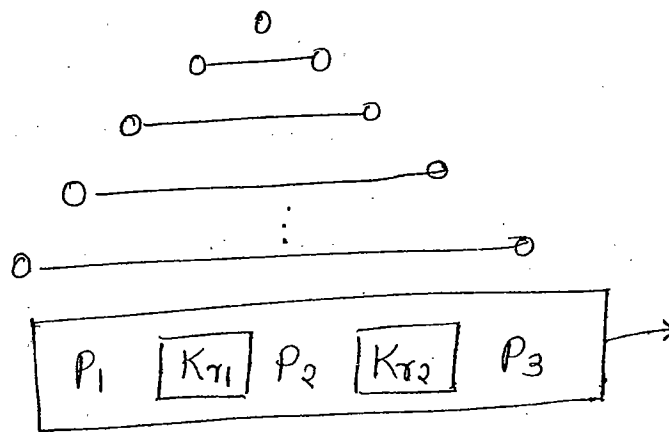
$$n = 23$$

$$\text{fill factor} = 0.65$$

$$n = 16$$

	Nodes	ptr	Data
R	1	16	15
L <sub>1</sub>	16	$16 \times 16$ 256	$16 \times 15$ 240
L <sub>2</sub>	256	4096	3840
L <sub>3</sub>	4096	65,536	61,440

○ In B tree, each node has K value & ptr, to minimize this we have B+ trees.



$$nP + (n-1)K_p \leq B$$

$$P=6, K=9$$

$$n \times 6 + (n-1) \times 9 \leq 512$$

$$n = 32$$

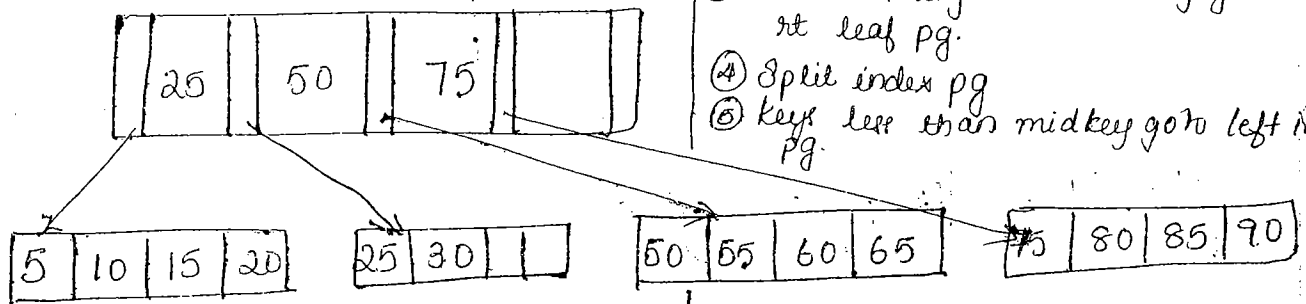
$$\text{fill factor} = 0.65$$

$$n = 23$$

	nodes	ptr	Data
R	23	23	22
L <sub>1</sub>	23	529	506
L <sub>2</sub>	529	12, 167	11638
L <sub>3</sub>	12, 167	2, 79, 841	2, 67, 674

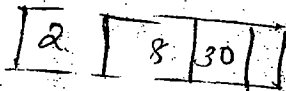
Inserting data item:

Leaf page full	Index Page full	Action
NO	NO	Place the record in the sorted position in the appr. leaf pg.
YES	NO	<ol style="list-style-type: none"> <li>Split the leaf pg.</li> <li>Place the middle key in index pg in sorted order</li> <li>Left leaf pg contains records with keys below the middle key.</li> <li>rt leaf pg contains rec with equal or greater than middle.</li> </ol>
<del>YES</del>	<del>YES</del>	
YES	YES	<ol style="list-style-type: none"> <li>Split the leaf pg.</li> <li>Rec with keys less than middle key go to left leaf pg.</li> <li>Rec with key <math>\geq</math> middle key go to rt leaf pg.</li> <li>Split index pg</li> <li>Keys less than midkey go to left pg.</li> </ol>

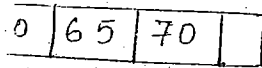
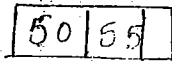
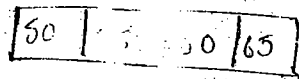


- Keys greater than midkey go to rt index pg.
- Midkey goes to next higher level of index.

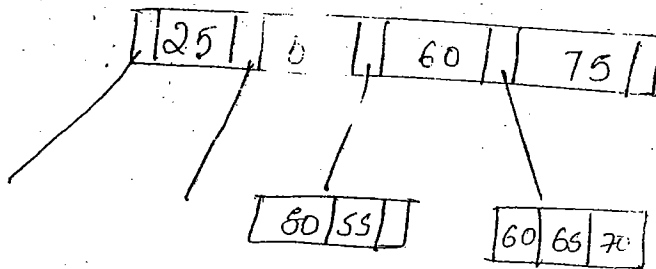
Case 2: new node



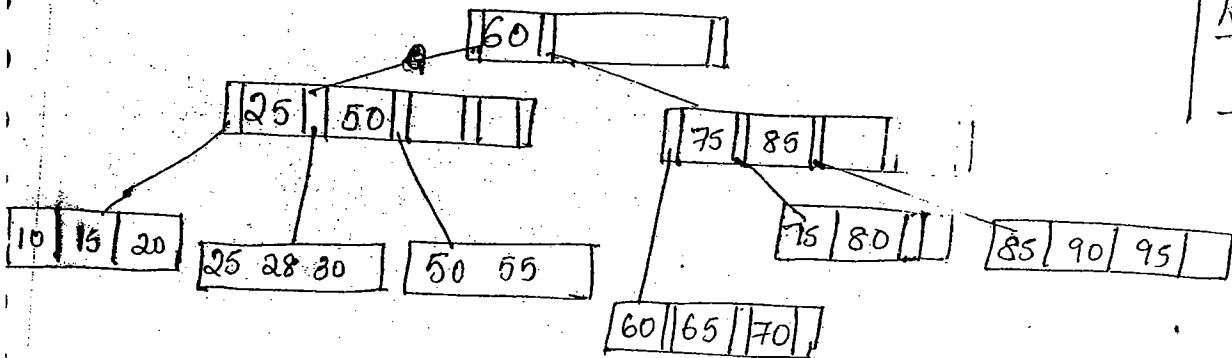
2: add new node with key value 70.



push 60 to root



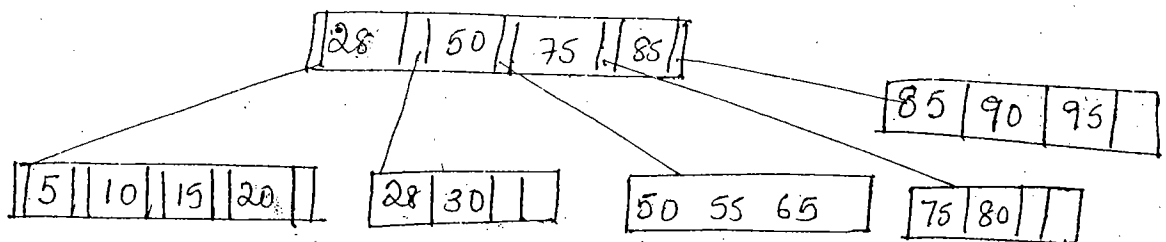
3: add 95.



\*  
Root  
> only  
  
>=  
only  
in  
leaf

leaf pg below fill factor	Index Page below fill factor	Action
Delete B+ NO	NO	① Delete rec from leaf page and arrange keys in ascending order to fill the gap. ② If the key of the deleted rec appears in index pg, use the next key to replace it
YES	NO	① Combine leaf pg and its sibling ② Change index pg to reflect this change
YES	YES	① Combine leaf pg and its sibling ② adjust the index pg to reflect the change ③ combine the index pg and its sibling ④ Continue combining index pgs until u reach a pg with correct fill factor (or u reach root pg)

- (a) Delete 70  
 (b) " 25  
 (c) 60



50 - SQL  
 30 - Transact  
 10-15 - Normal  
 - Files & ER diagrams