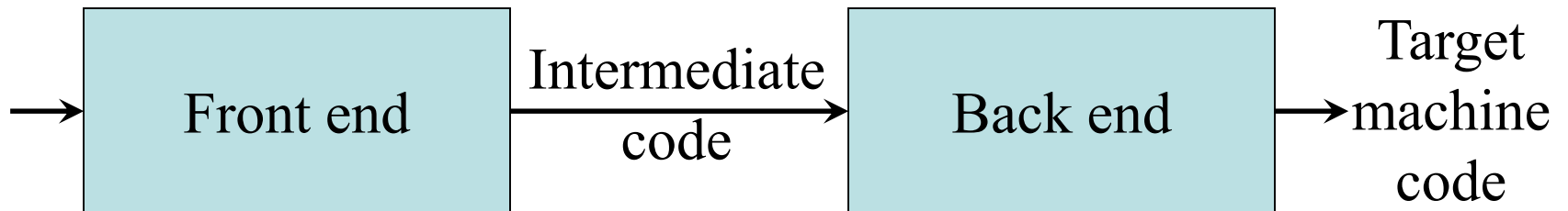


Intermediate Code Generation

Intermediate Code Generation

- Facilitates *retargeting*: enables attaching a back end for the new machine to an existing front end



- Enables machine-independent code optimization

$$T1 = x * 5$$

$$T1 = x + x + x + x + x$$

$$T1 = x + x$$

$$T2 = x + x$$

$$T3 = T1 + T2$$

$$T4 = X + t3$$

Intermediate Representations

- *Graphical representations* (e.g. AST)
- *Postfix notation*: operations on values stored on operand stack (similar to JVM bytecode)
- *Three-address code*: (e.g. *triples* and *quads*)

$x := y \text{ op } z$

- *Two-address code*:

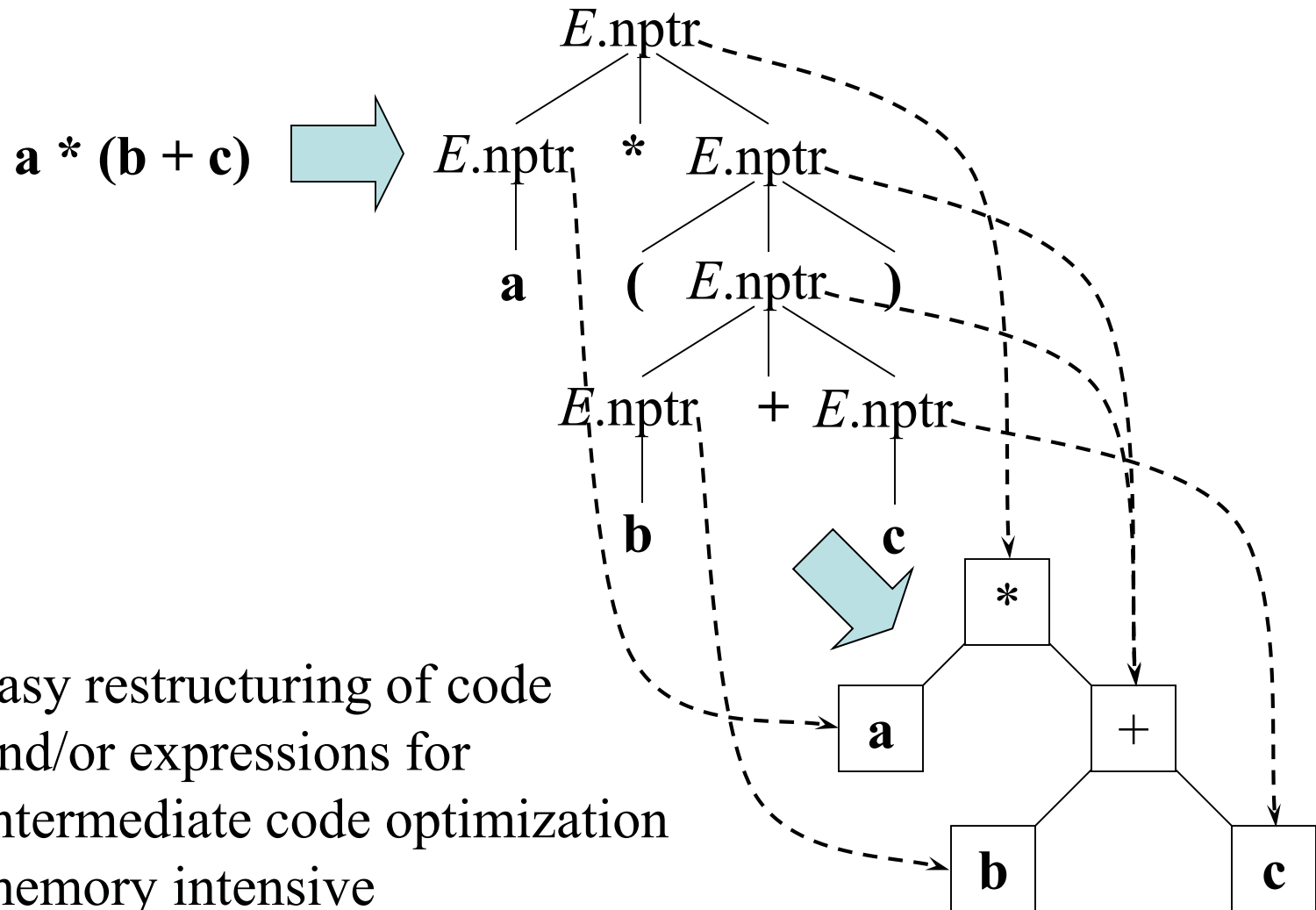
$x := \text{op } y$

which is the same as $x := x \text{ op } y$

Syntax-Directed Translation of Abstract Syntax Trees

Production	Semantic Rule
$S \rightarrow \mathbf{id} := E$	$S.\text{nptr} := \text{mknode}(':=', \text{mkleaf}(\mathbf{id}, \mathbf{id}.\text{entry}), E.\text{nptr})$
$E \rightarrow E_1 + E_2$	$E.\text{nptr} := \text{mknode}('+', E_1.\text{nptr}, E_2.\text{nptr})$
$E \rightarrow E_1 * E_2$	$E.\text{nptr} := \text{mknode}('*', E_1.\text{nptr}, E_2.\text{nptr})$
$E \rightarrow - E_1$	$E.\text{nptr} := \text{mknode}(\text{'uminus'}, E_1.\text{nptr})$
$E \rightarrow (E_1)$	$E.\text{nptr} := E_1.\text{nptr}$
$E \rightarrow \mathbf{id}$	$E.\text{nptr} := \text{mkleaf}(\mathbf{id}, \mathbf{id}.\text{entry})$

Abstract Syntax Trees



$\text{Prog} \rightarrow \text{if exp then st else st}$

$\text{Exp} \rightarrow E \text{ relop } E \mid E + E \mid (E) \mid E * E$

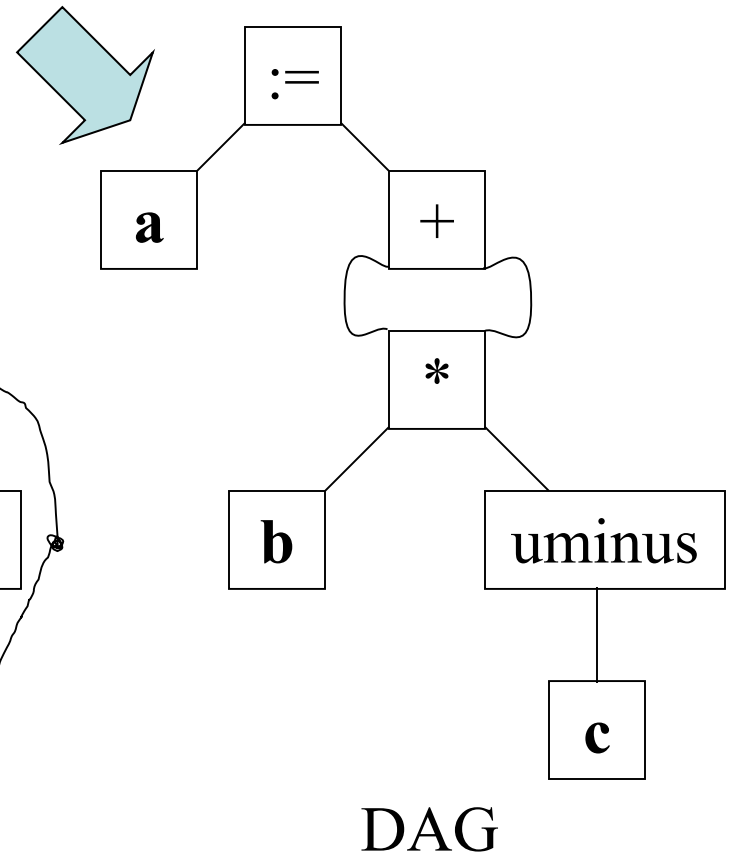
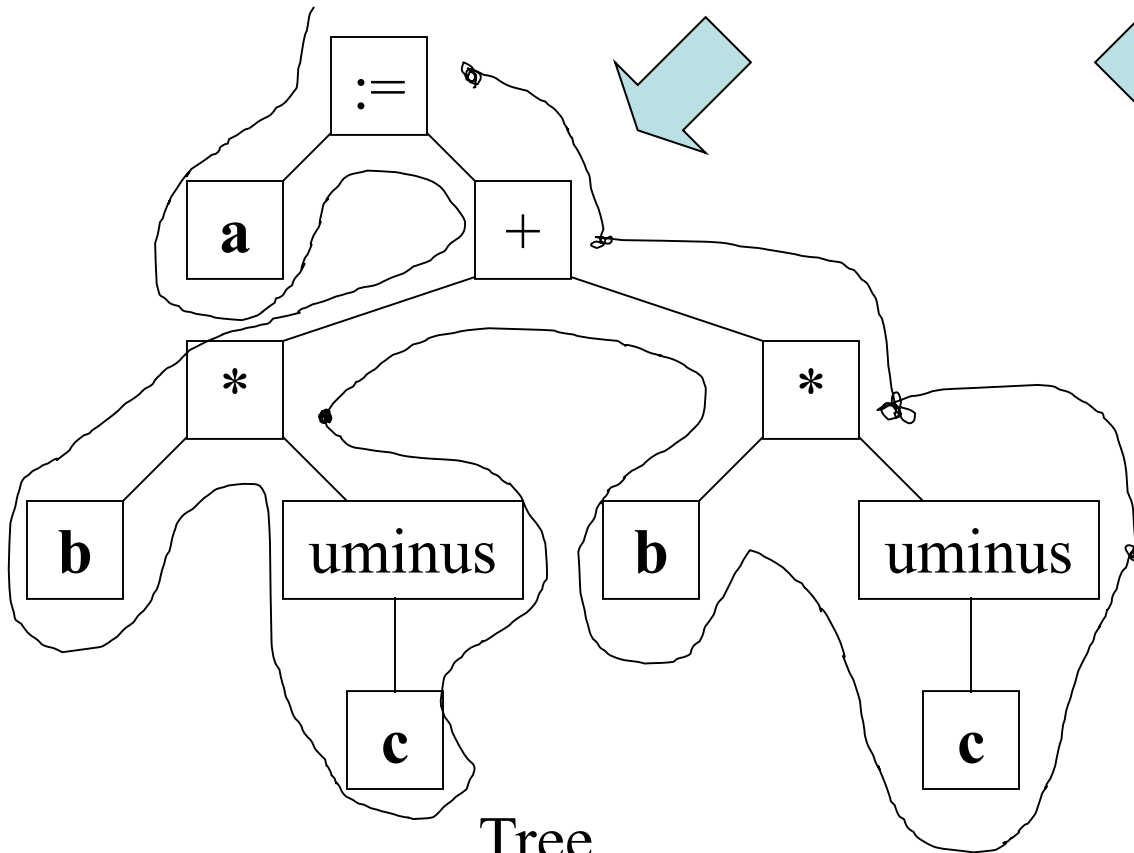
$E \rightarrow \text{id} \mid \text{number}$

$\text{St} \rightarrow \text{id} := \text{exp}$

$\text{if } x > 1 \text{ then } x = 2 * (y + 1) \text{ else } y = y + 1$

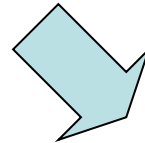
Abstract Syntax Trees versus DAGs

$a := b * -c + b * -c$



Postfix Notation

a := b * -c + b * -c



a b c uminus * b c uminus * + assign

Postfix notation represents
operations on a stack

Pro: easy to generate

Cons: stack operations are more
difficult to optimize

Bytecode (for example)

iload 2	// push b
iload 3	// push c
ineg	// uminus
imul	// *
iload 2	// push b
iload 3	// push c
ineg	// uminus
imul	// *
iadd	// +
istore 1	// store a

P-code

- Stack based virtual m/c
- Operands are always `stack[top]`
- Push operands onto STACK
- $E1 * E2$
- Code to evaluate E1 and then E2
- Mult

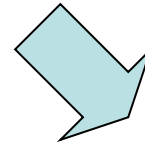
Three-Address Code

$a := b * -c + b * -c$



```
t1 := - c
t2 := b * t1
t3 := - c
t4 := b * t3
t5 := t2 + t4
a  := t5
```

Linearized representation
of a syntax tree



```
t1 := - c
t2 := b * t1
t5 := t2 + t2
a  := t5
```

Linearized representation
of a syntax DAG

Three-Address Statements

- Assignment statements: $x := y \text{ op } z$, $x := \text{op } y$
- Indexed assignments: $x := y[i]$, $x[i] := y$
- Pointer assignments: $x := \&y$, $x := *y$, $*x := y$
- Copy statements: $x := y$
- Unconditional jumps: **goto** *lab*
- Conditional jumps: **if** $x \text{ relop } y$ **goto** *lab*
- Function calls: **param** $x \dots$ **call** p, n
return y
- $A = \text{fun}(\text{para1}, \text{para2}, \dots)$ *return* x

Syntax-Directed Translation into Three-Address Code

Productions

$S \rightarrow \mathbf{id} := E$
 $\quad | \mathbf{while} \ E \ \mathbf{do} \ S$
 $E \rightarrow E + E$
 $\quad | E * E$
 $\quad | - E$
 $\quad | (E)$
 $\quad | \mathbf{id}$
 $\quad | \mathbf{num}$

Synthesized attributes:

$S.code$	three-address code for S
$S.begin$	label to start of S or nil
$S.after$	label to end of S or nil
$E.code$	three-address code for E
$E.place$	a name holding the value of E

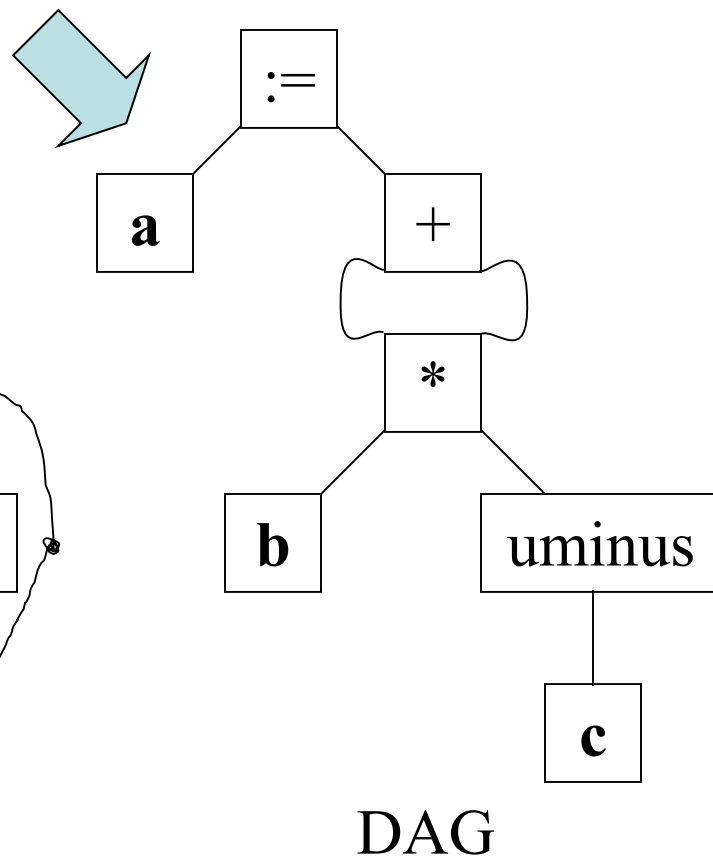
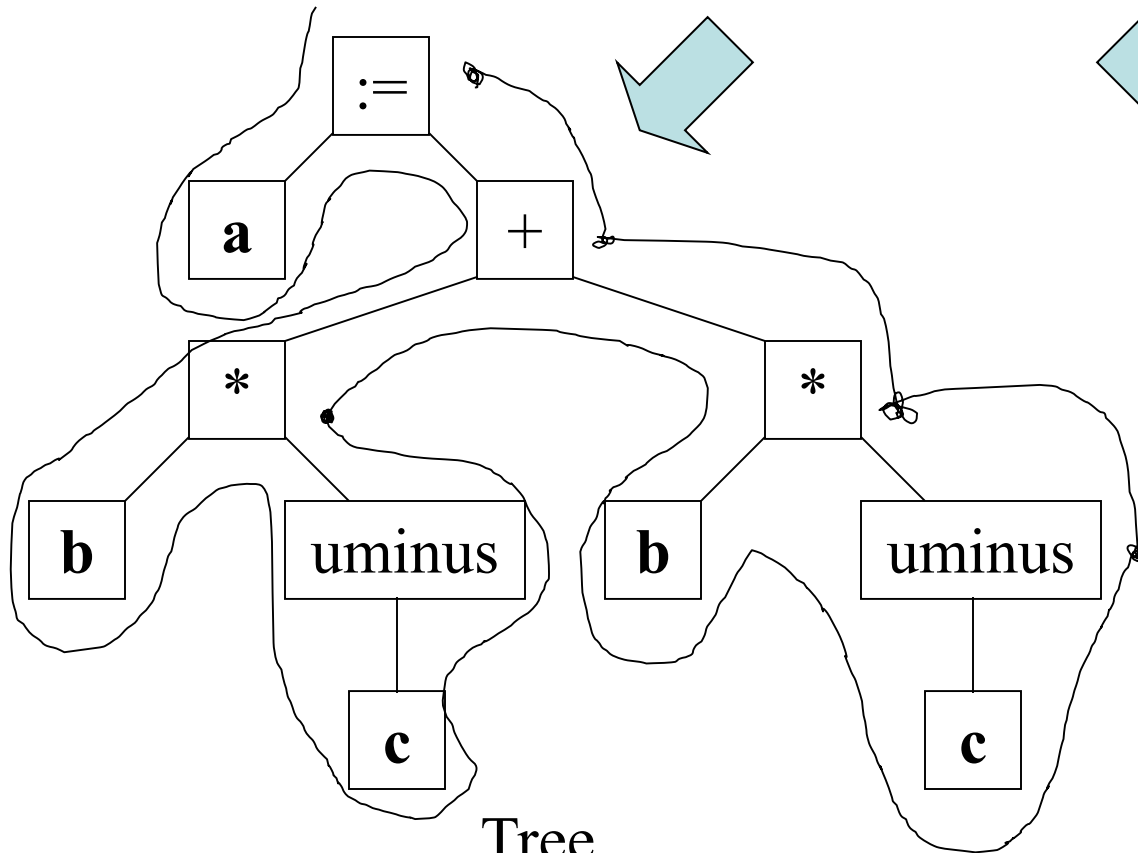
Code generation $\nearrow gen(E.place \ ':= \ E_1.place \ '+' \ E_2.place)$

\Downarrow

$t3 := t1 + t2$

Abstract Syntax Trees versus DAGs

$a := b * -c + b * -c$



Syntax-Directed Translation into Three-Address Code (cont' d)

Productions	Semantic rules
$S \rightarrow \mathbf{id} := E$	$S.code := E.code \parallel gen(\mathbf{id}.place \text{ ':=' } E.place); S.begin := S.after := \mathbf{nil}$
$S \rightarrow \mathbf{while} E$ $\mathbf{do} S_1$	(see next slide)
$E \rightarrow E_1 + E_2$	$E.place := newtemp();$ $E.code := E_1.code \parallel E_2.code \parallel gen(E.place \text{ ':=' } E_1.place \text{ '+' } E_2.place)$
$E \rightarrow E_1 * E_2$	$E.place := newtemp();$ $E.code := E_1.code \parallel E_2.code \parallel gen(E.place \text{ ':=' } E_1.place \text{ '*' } E_2.place)$
$E \rightarrow - E_1$	$E.place := newtemp();$ $E.code := E_1.code \parallel gen(E.place \text{ ':=' 'uminus' } E_1.place)$
$E \rightarrow (E_1)$	$E.place := E_1.place$ $E.code := E_1.code$
$E \rightarrow \mathbf{id}$	$E.place := \mathbf{id}.name$ $E.code := \text{''}$
$E \rightarrow \mathbf{num}$	$E.place := newtemp();$ $E.code := gen(E.place \text{ ':=' } \mathbf{num}.value)$

Syntax-Directed Translation into Three-Address Code (cont' d)

Production

$S \rightarrow \mathbf{while} \ E \ \mathbf{do} \ S_1$

Semantic rule

$S.\mathbf{begin} := \mathit{newlabel}()$

$S.\mathbf{after} := \mathit{newlabel}()$

$S.\mathbf{code} := \mathit{gen}(S.\mathbf{begin} \ ':\') \parallel$

$E.\mathbf{code} \parallel$

$\mathit{gen}(\text{'if' } E.\mathbf{place} \text{'=' '0' 'goto' } S.\mathbf{after}) \parallel$

$S_1.\mathbf{code} \parallel$

$\mathit{gen}(\text{'goto' } S.\mathbf{begin}) \parallel$

$\mathit{gen}(S.\mathbf{after} \ ':\')$

$S.\mathbf{begin}:$

$E.\mathbf{code}$

$\mathbf{if} \ E.\mathbf{place} = 0 \ \mathbf{goto} \ S.\mathbf{after}$

$S.\mathbf{code}$

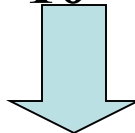
$\mathbf{goto} \ S.\mathbf{begin}$

$S.\mathbf{after}:$

...

Example

.begin:	<i>E.code</i>	<i>i</i> := 2 * <i>n</i> + <i>k</i> while <i>i</i> do <i>i</i> := <i>i</i> - <i>k</i> <i>a</i> := 10
	if <i>E.place</i> = 0 goto <i>S.after</i>	
	<i>S.code</i>	
	goto <i>S.begin</i>	
<i>S.after:</i>	...	



	t1 := 2	
	t2 := t1 * n	E.code
	t3 := t2 + k	
	i := t3	
L1:	if i = 0 goto L2	if code
	t4 := i - k	
	i := t4	S.code
	goto L1	goto S.begin
L2:	t5 := 10	S.after

Implementation of Three-Address Statements: Quads

#	<i>Op</i>	<i>Arg1</i>	<i>Arg2</i>	<i>Res</i>
(0)	uminus	c		t1
(1)	*	b	t1	t2
(2)	uminus	c		t3
(3)	*	b	t3	t4
(4)	+	t2	t4	t5
(5)	:=	t5		a

t1 := - c

t2 := b * t1

t3 := - c

t4 := b * t3

t5 := t2 + t4

a := t5

Quads (quadruples)

Pro: easy to rearrange code for global optimization

Cons: lots of temporaries

Implementation of Three-Address Statements: Triples

#	<i>Op</i>	<i>Arg1</i>	<i>Arg2</i>
(0)	uminus	c	
(1)	*	b	(0)
(2)	uminus	c	
(3)	*	b	(2)
(4)	+	(1)	(3)
(5)	:=	a	(4)

t1 := - c

t2 := b * t1

t3 := - c

t4 := b * t3

t5 := t2 + t4

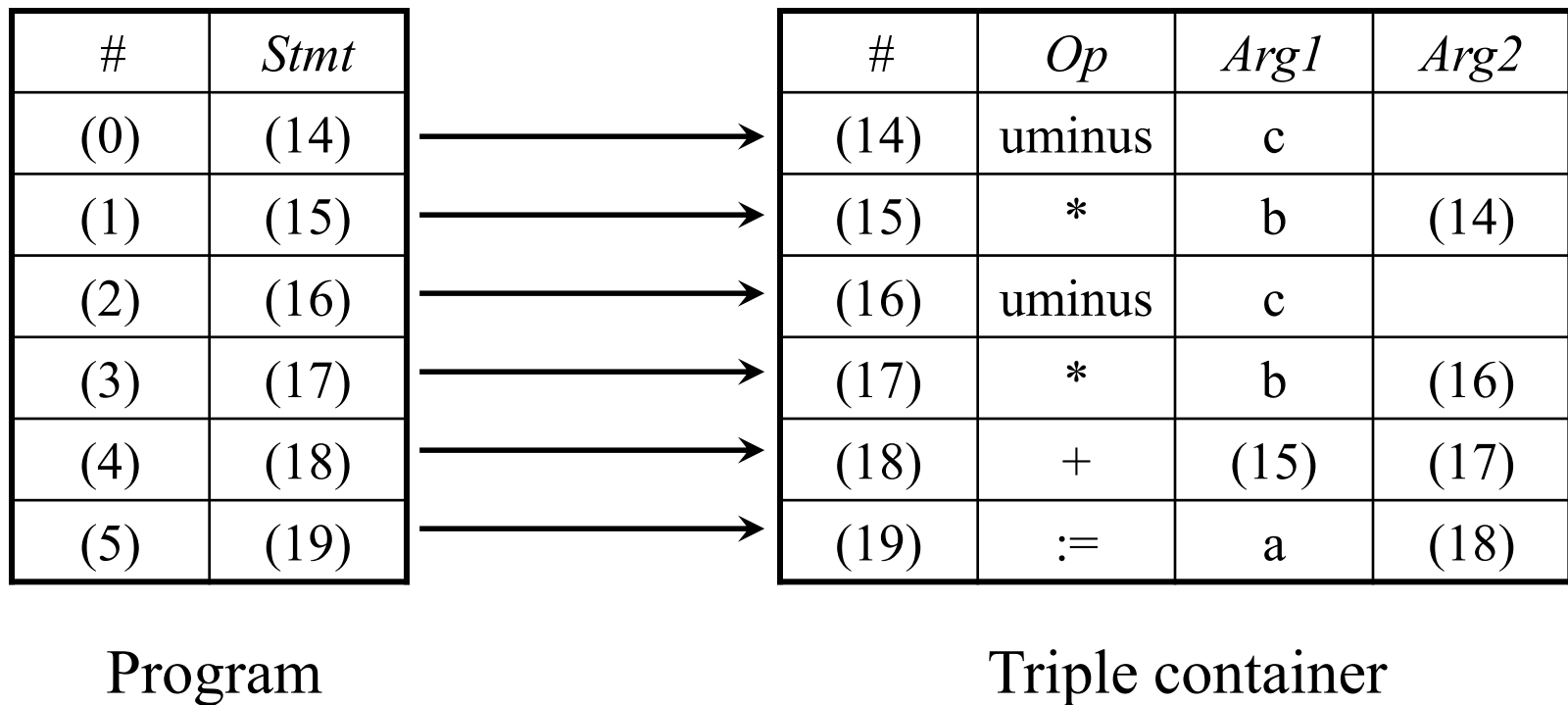
a := t5

Triples

Pro: temporaries are implicit

Cons: difficult to rearrange code

Implementation of Three-Address Stmts: Indirect Triples



Pro: temporaries are implicit & easier to rearrange code

$E \rightarrow E + E \mid (E) \mid -E \mid \text{id}$

$a + -(b + c)$

Quad?

Triples?

Indirect triples?

$(0) = b + c$

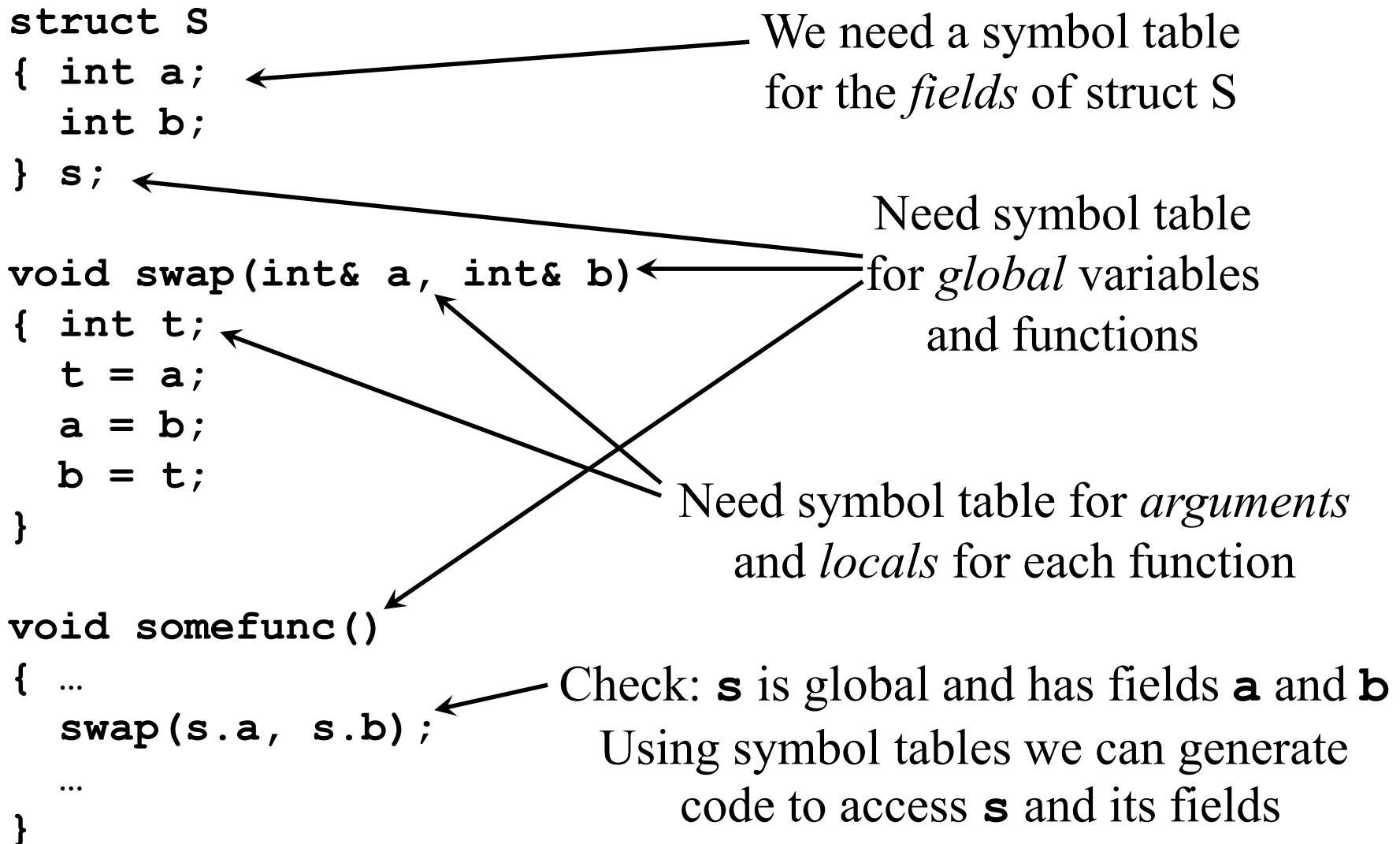
$(1) = -(0)$

$(2) = a + (1)$

Names and Scopes

- The three-address code generated by the syntax-directed definitions shown on the previous slides is somewhat simplistic, because it assumes that the names of variables can be easily resolved by the back end in global or local variables
- We need local symbol tables to record global declarations as well as local declarations in procedures, blocks, and structs to resolve names

Symbol Tables for Scoping



Offset and Width for Runtime Allocation

```
struct S
{ int a;
  int b;
} s;
```

The fields **a** and **b** of struct **S** are located at *offsets* 0 and 4 from the start of **S**

```
void swap(int& a, int& b)
{ int t;
  t = a;
  a = b;
  b = t;
}
```

The *width* of **S** is 8

a	(0)
b	(4)

Subroutine frame holds arguments **a** and **b** and local **t** at *offsets* 0, 4, and 8

```
void somefunc()
{ ...
  swap(s.a, s.b);
  ...
}
```

Subroutine frame

fp[0]=	a	(0)
fp[4]=	b	(4)
fp[8]=	t	(8)

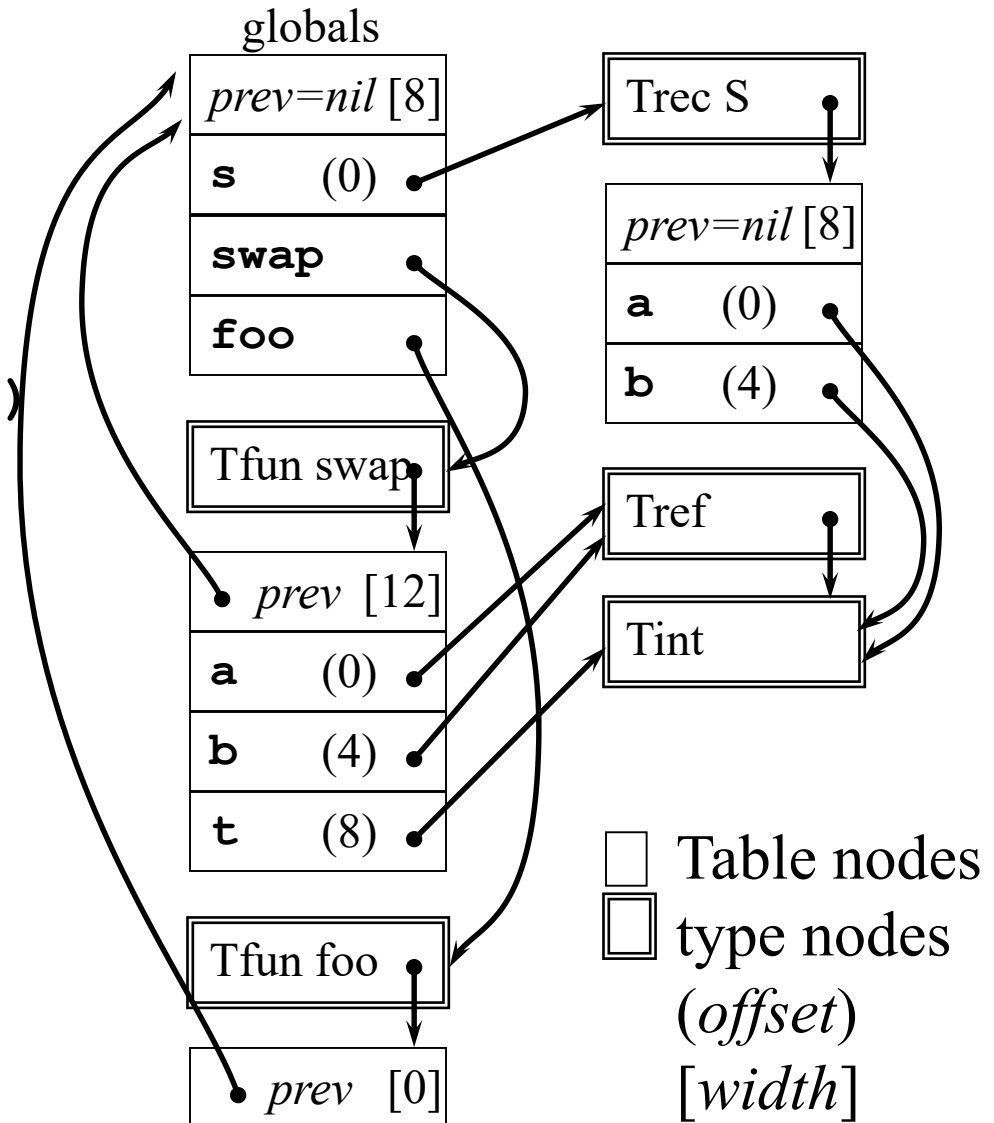
The *width* of the frame is 12

Symbol Tables for Scoping

```
struct S
{ int a;
  int b;
} s;
```

```
void swap(int& a, int& b)
{ int t;
  t = a;
  a = b;
  b = t;
}
```

```
void foo()
{ ...
  swap(s.a, s.b);
  ...
}
```



Hierarchical Symbol Table Operations

- *mktable(previous)* returns a pointer to a new table that is linked to a previous table in the outer scope
- *enter(table, name, type, offset)* creates a new entry in *table*
- *addwidth(table, width)* accumulates the total width of all entries in *table*
- *enterproc(table, name, newtable)* creates a new entry in *table* for procedure with local scope *newtable*
- *lookup(table, name)* returns a pointer to the entry in the table for *name* by following linked tables

Syntax-Directed Translation of Declarations in Scope

Productions

$$P \rightarrow D ; S$$

$$D \rightarrow D ; D$$

$$| \text{ id } : T$$

$$| \text{ proc id } ; D ; S$$

$$T \rightarrow \text{ integer}$$

$$| \text{ real}$$

$$| \text{ array [num] of } T$$

$$| ^ T$$

$$| \text{ record } D \text{ end}$$

$$S \rightarrow S ; S$$

$$| \text{ id } := E$$

$$| \text{ call id } (A)$$

Productions (*cont'd*)

$$E \rightarrow E + E$$

$$| E * E$$

$$| - E$$

$$| (E)$$

$$| \text{ id}$$

$$| E ^$$

$$| \& E$$

$$| E . \text{ id}$$

$$A \rightarrow A , E$$

$$| E$$

Synthesized attributes:

$T.\text{type}$ pointer to type

$T.\text{width}$ storage width of type (bytes)

$E.\text{place}$ name of temp holding value of E

Global data to implement scoping:

tblptr stack of pointers to tables

offset stack of offset values

Syntax-Directed Translation of Declarations in Scope (cont' d)

$$P \rightarrow \{ t := mktable(\text{nil}); \text{push}(t, \text{tblptr}); \text{push}(0, \text{offset}) \}$$

$$D ; S$$

$$D \rightarrow \mathbf{id} : T$$

$$\{ \text{enter}(\text{top}(\text{tblptr}), \mathbf{id}.\text{name}, T.\text{type}, \text{top}(\text{offset}));$$

$$\text{top}(\text{offset}) := \text{top}(\text{offset}) + T.\text{width} \}$$

$$D \rightarrow \mathbf{proc id} ;$$

$$\{ t := mktable(\text{top}(\text{tblptr})); \text{push}(t, \text{tblptr}); \text{push}(0, \text{offset}) \}$$

$$D_1 ; S$$

$$\{ t := \text{top}(\text{tblptr}); \text{addwidth}(t, \text{top}(\text{offset}));$$

$$\text{pop}(\text{tblptr}); \text{pop}(\text{offset});$$

$$\text{enterproc}(\text{top}(\text{tblptr}), \mathbf{id}.\text{name}, t) \}$$

$$D \rightarrow D_1 ; D_2$$

Syntax-Directed Translation of Declarations in Scope (cont' d)

$T \rightarrow \mathbf{integer} \quad \{ T.type := 'integer'; T.width := 4 \}$

$T \rightarrow \mathbf{real} \quad \{ T.type := 'real'; T.width := 8 \}$

$T \rightarrow \mathbf{array} [\mathbf{num}] \mathbf{of} T_1$
 $\quad \{ T.type := array(\mathbf{num.val}, T_1.type);$
 $\quad \quad T.width := \mathbf{num.val} * T_1.width \}$

$T \rightarrow \wedge T_1$
 $\quad \{ T.type := pointer(T_1.type); T.width := 4 \}$

$T \rightarrow \mathbf{record}$
 $\quad \{ t := mktable(\mathbf{nil}); push(t, tblptr); push(0, offset) \}$

$D \mathbf{end}$

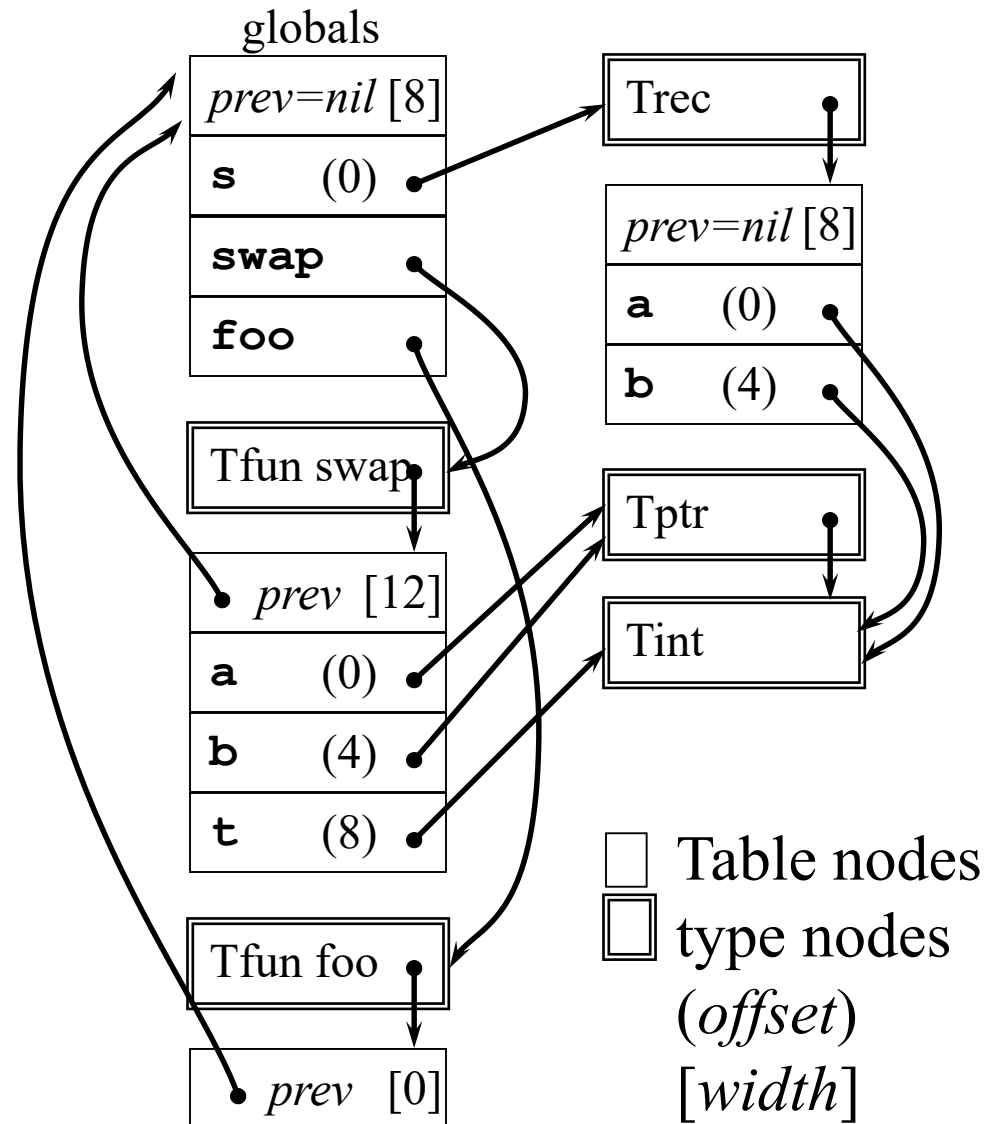
$\quad \{ T.type := record(top(tblptr)); T.width := top(offset);$
 $\quad \quad addwidth(top(tblptr), top(offset)); pop(tblptr); pop(offset) \}$

Example

```
s: record
  a: integer;
  b: integer;
end;
```

```
proc swap;
  a: ^integer;
  b: ^integer;
  t: integer;
  t := a^;
  a^ := b^;
  b^ := t;
```

```
proc foo;
  call swap(&s.a, &s.b);
```



Syntax-Directed Translation of Statements in Scope

$S \rightarrow S ; S$

$S \rightarrow \mathbf{id} := E$

$\{ p := \text{lookup}(\text{top}(\text{tblptr}), \mathbf{id.name});$

$\mathbf{if} \ p = \text{nil} \ \mathbf{then}$

$\text{error}()$

$\mathbf{else if} \ p.\text{level} = 0 \ \mathbf{then} \ // \ \text{global variable}$

$\text{emit}(\mathbf{id.place} \ ' := ' \ E.\text{place})$

$\mathbf{else} \ // \ \text{local variable in subroutine frame}$

$\text{emit}(\text{fp}[p.\text{offset}] \ ' := ' \ E.\text{place}) \}$

Globals

s	(0)
x	(8)
y	(12)

Subroutine
frame

fp[0]=	a	(0)
fp[4]=	b	(4)
fp[8]=	t	(8)

...

Syntax-Directed Translation of Expressions in Scope

$$\begin{array}{ll}
 E \rightarrow E_1 + E_2 & \{ E.\text{place} := \text{newtemp}(); \\
 & \quad \text{emit}(E.\text{place} \text{ ':=' } E_1.\text{place} \text{ '+' } E_2.\text{place}) \} \\
 E \rightarrow E_1 * E_2 & \{ E.\text{place} := \text{newtemp}(); \\
 & \quad \text{emit}(E.\text{place} \text{ ':=' } E_1.\text{place} \text{ '*' } E_2.\text{place}) \} \\
 E \rightarrow - E_1 & \{ E.\text{place} := \text{newtemp}(); \\
 & \quad \text{emit}(E.\text{place} \text{ ':=' 'uminus' } E_1.\text{place}) \} \\
 E \rightarrow (E_1) & \{ E.\text{place} := E_1.\text{place} \} \\
 E \rightarrow \mathbf{id} & \{ p := \text{lookup}(\text{top}(\text{tblptr}), \mathbf{id}.\text{name}); \\
 & \quad \mathbf{if } p = \text{nil} \mathbf{ then error}() \\
 & \quad \mathbf{else if } p.\text{level} = 0 \mathbf{ then // global variable} \\
 & \quad \quad E.\text{place} := \mathbf{id}.\text{place} \\
 & \quad \mathbf{else // local variable in frame} \\
 & \quad \quad E.\text{place} := \text{fp}[p.\text{offset}] \}
 \end{array}$$

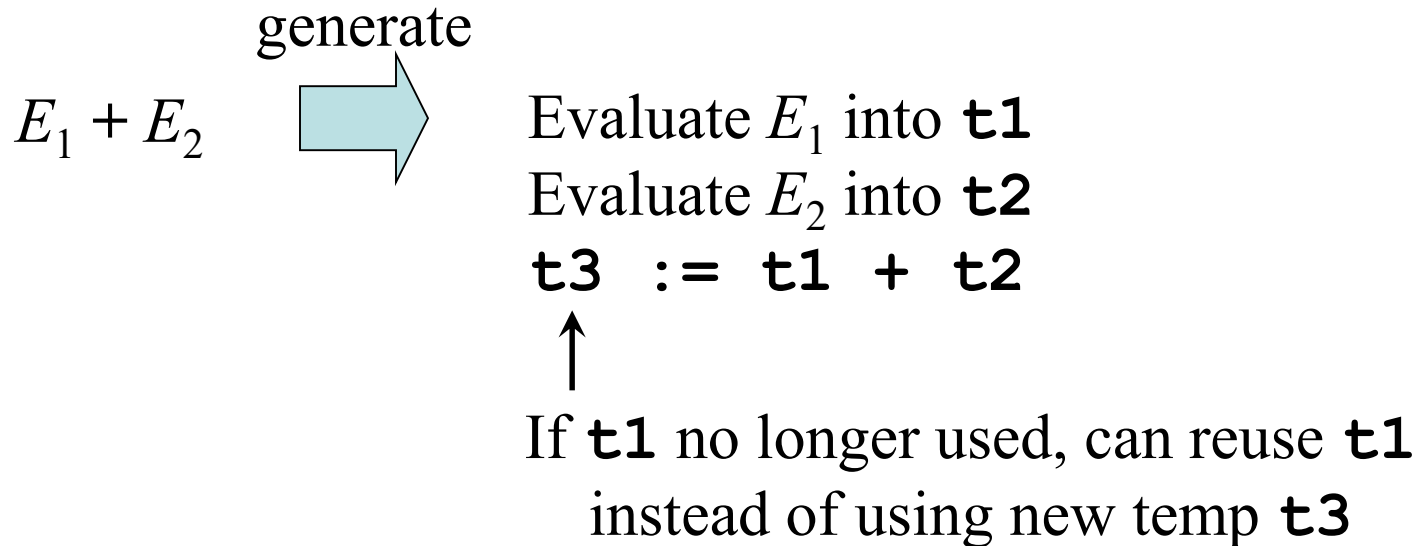
Syntax-Directed Translation of Expressions in Scope (cont' d)

$$\begin{array}{ll}
 E \rightarrow E_1 \wedge & \{ E.place := newtemp(); \\
 & \quad emit(E.place \text{ ':=' } * E_1.place) \} \\
 E \rightarrow \& E_1 & \{ E.place := newtemp(); \\
 & \quad emit(E.place \text{ ':=' } \& E_1.place) \} \\
 E \rightarrow \mathbf{id}_1 . \mathbf{id}_2 & \{ p := lookup(top(tblptr), \mathbf{id}_1.name); \\
 & \quad \mathbf{if } p = \mathbf{nil} \text{ or } p.type \neq \mathbf{Trec} \text{ then } error() \\
 & \quad \mathbf{else} \\
 & \quad \quad q := lookup(p.type.table, \mathbf{id}_2.name); \\
 & \quad \quad \mathbf{if } q = \mathbf{nil} \text{ then } error() \\
 & \quad \quad \mathbf{else if } p.level = 0 \text{ then } // \textit{global variable} \\
 & \quad \quad \quad E.place := \mathbf{id}_1.place[q.offset] \\
 & \quad \quad \mathbf{else } // \textit{local variable in frame} \\
 & \quad \quad \quad E.place := fp[p.offset+q.offset] \}
 \end{array}$$

Advanced Intermediate Code Generation Techniques

- Reusing temporary names
- Addressing array elements
- Translating logical and relational expressions
- Translating short-circuit Boolean expressions and flow-of-control statements with backpatching lists
- Translating procedure calls

Reusing Temporary Names



Modify *newtemp()* to use a “stack”:

Keep a counter c , initialized to 0

Decrement counter on each use of a $\$i$ in a three-address statement

newtemp() returns temporary $\$c++$ (that is, c is post incremented)

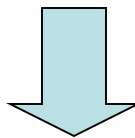
Syntax-Directed Translation into Three-Address Code (cont' d)

Productions	Semantic rules
$S \rightarrow \mathbf{id} := E$	$S.code := E.code \parallel gen(\mathbf{id}.place \text{ ':=' } E.place); S.begin := S.after := \mathbf{nil}$
$S \rightarrow \mathbf{while} E$ $\mathbf{do} S_1$	(see next slide)
$E \rightarrow E_1 + E_2$	$E.place := newtemp();$ $E.code := E_1.code \parallel E_2.code \parallel gen(E.place \text{ ':=' } E_1.place \text{ '+' } E_2.place)$
$E \rightarrow E_1 * E_2$	$E.place := newtemp();$ $E.code := E_1.code \parallel E_2.code \parallel gen(E.place \text{ ':=' } E_1.place \text{ '*' } E_2.place)$
$E \rightarrow - E_1$	$E.place := newtemp();$ $E.code := E_1.code \parallel gen(E.place \text{ ':=' } \text{'uminus'} E_1.place)$
$E \rightarrow (E_1)$	$E.place := E_1.place$ $E.code := E_1.code$
$E \rightarrow \mathbf{id}$	$E.place := \mathbf{id}.name$ $E.code := \text{''}$
$E \rightarrow \mathbf{num}$	$E.place := newtemp();$ $E.code := gen(E.place \text{ ':=' } \mathbf{num}.value)$

Reusing Temporary Names (cont' d)

$x := a * b + c * d - e * f$

$a := b * c + (-1 + 2) * 3$



$\$0 = b * c$ 0-0-1

$\$1 = 1$ 1-1-2

$\$1 = - \1 2-1-2

$\$2 = 2$ 2-2-3

$\$1 = \$1 + \$2$ 3-1-2

$\$2 = 3$ 2-2-3

$\$1 = \$1 * \$2$ 3-1-2

$\$0 = \$0 + \$1$ 2-0-1

$a := \$0$ 1-0-0

Statement

$c \rightarrow c_{decr} \rightarrow c_{incr}$

$\$0 := a * b$

$\$1 := c * d$

$\$0 := \$0 + \$1$

$\$1 := e * f$

$\$0 := \$0 - \$1$

$x := \$0$

0

$0 \rightarrow 0 \rightarrow 1$

$1 \rightarrow 1 \rightarrow 2$

$2 \rightarrow 0 \rightarrow 1$

$1 \rightarrow 1 \rightarrow 2$

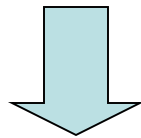
$2 \rightarrow 0 \rightarrow 1$

$1 \rightarrow 0 \rightarrow 0$

Addressing Array Elements: One-Dimensional Arrays

A : array [10..20] of integer;

$$\begin{aligned} \dots := \mathbf{A}[\mathbf{i}] &= base_{\mathbf{A}} + (i - low) * w \\ &= i * w + c \end{aligned}$$



where $c = base_{\mathbf{A}} - low * w$

with $low = 10; w = 4$ (= type width)

```
t1 := c      // c = baseA - 10 * 4
t2 := i * 4
t3 := t1[t2]
... := t3
```

Addressing Array Elements: Multi-Dimensional Arrays

A : array [1..2, 1..3] of integer;

$low_1 = 1, low_2 = 1, n_1 = 2, n_2 = 3, w = 4$

$base_A$

A[1, 1]
A[1, 2]
A[1, 3]
A[2, 1]
A[2, 2]
A[2, 3]

Row-major

$base_A$

A[1, 1]
A[2, 1]
A[1, 2]
A[2, 2]
A[1, 3]
A[2, 3]

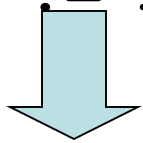
Column-major

Addressing Array Elements: Multi-Dimensional Arrays

A : array [1..2, 1..3] of integer; (Row-major)
 base 11 n1 12 n2 w=4

$$= base_A + ((i_1 - low_1) * n_2 + i_2 - low_2) * w$$

... **:= A[i, j]** = $((i_1 * n_2) + i_2) * w + c$



where $c = base_A - ((low_1 * n_2) + low_2) * w$

with $low_1 = 1; low_2 = 1; n_2 = 3; w = 4$

t1 := i * 3

t1 := t1 + j

t2 := c // c = $base_A - (1 * 3 + 1) * 4$

t3 := t1 * 4

t4 := t2[t3] // t4 := mem[$((i * 3) + j) * 4 + c$]

... := t4

Addressing Array Elements: Grammar

$$S \rightarrow L := E$$

$$E \rightarrow E + E$$

$$| (E)$$

$$| L$$

$$| \mathbf{num}$$

$$L \rightarrow Elist \]$$

$$| \mathbf{id}$$

$$Elist \rightarrow Elist \ , \ E$$

$$| \mathbf{id} \ [\ E$$

Synthesized attributes:

$E.place$

name of temp holding value of E

$Elist.array$

array name

$Elist.place$

name of temp holding index value

$Elist.ndim$

number of array dimensions

$L.place$

lvalue (=name of temp)

$L.offset$

index into array (=name of temp)

null indicates non-array simple **id**

a:=b

a:=b[2]

a:=b[3,4]

c[2,4]:=a[3,4]

Addressing Array Elements

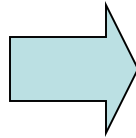
$$\begin{aligned}
 S \rightarrow L := E & \quad \{ \text{if } L.\text{offset} = \mathbf{null} \text{ then} \\
 & \quad \text{emit}(L.\text{place} \text{ '}' := \text{' } E.\text{place}) \\
 & \quad \mathbf{else} \\
 & \quad \text{emit}(L.\text{place}[L.\text{offset}] \text{ '}' := \text{' } E.\text{place}) \} \\
 E \rightarrow E_1 + E_2 & \quad \{ E.\text{place} := \text{newtemp}(); \\
 & \quad \text{emit}(E.\text{place} \text{ '}' := \text{' } E_1.\text{place} \text{ '}' + \text{' } E_2.\text{place}) \} \\
 E \rightarrow (E_1) & \quad \{ E.\text{place} := E_1.\text{place} \} \\
 E \rightarrow L & \quad \{ \text{if } L.\text{offset} = \mathbf{null} \text{ then} \\
 & \quad E.\text{place} := L.\text{place} \\
 & \quad \mathbf{else} \\
 & \quad E.\text{place} := \text{newtemp}(); \\
 & \quad \text{emit}(E.\text{place} \text{ '}' := \text{' } L.\text{place}[L.\text{offset}] \}
 \end{aligned}$$

Addressing Array Elements

$$\begin{aligned}
L \rightarrow Elist \] \quad & \{ L.place := newtemp(); \\
& L.offset := newtemp(); \\
& emit(L.place \text{ ':=' } c(Elist.array)); \\
& emit(L.offset \text{ ':=' } Elist.place \text{ '*' } width(Elist.array)) \} \\
L \rightarrow \mathbf{id} \quad & \{ L.place := \mathbf{id}.place; \\
& L.offset := \mathbf{null} \} \\
Elist \rightarrow Elist_1, E \quad & \{ t := newtemp(); m := Elist_1.ndim + 1; \\
& emit(t \text{ ':=' } Elist_1.place \text{ '*' } limit(Elist_1.array, m)); \\
& emit(t \text{ ':=' } t \text{ '+' } E.place); \\
& Elist.array := Elist_1.array; Elist.place := t; \\
& Elist.ndim := m \} \\
Elist \rightarrow \mathbf{id} \ [\ E \quad & \{ Elist.array := \mathbf{id}.place; Elist.place := E.place; \\
& Elist.ndim := 1 \}
\end{aligned}$$

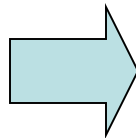
Translating Logical and Relational Expressions

a or b and not c



```
t1 := not c  
t2 := b and t1  
t3 := a or t2
```

a < b



```
if a < b goto L1  
t1 := 0  
goto L2  
L1: t1 := 1  
L2:
```

Translating Short-Circuit Expressions Using Backpatching

$E \rightarrow E \text{ or } ME$
 | $E \text{ and } ME$
 | **not** E
 | (E)
 | **id relop id**
 | **true**
 | **false**

$M \rightarrow \varepsilon$

Synthesized attributes:

$E.\text{truelist}$

backpatch list for jumps on true

$E.\text{falselist}$

backpatch list for jumps on false

$M.\text{quad}$

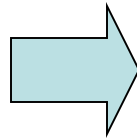
location of current three-address quad

Backpatch Operations with Lists

- *makelist*(i) creates a new list containing three-address location i , returns a pointer to the list
- *merge*(p_1, p_2) concatenates lists pointed to by p_1 and p_2 , returns a pointer to the concatenated list
- *backpatch*(p, i) inserts i as the target label for each of the statements in the list pointed to by p

Backpatching with Lists: Example

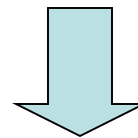
$a < b$ or $c < d$ and $e < f$



```

100: if a < b goto _
101: goto _
102: if c < d goto _
103: goto _
104: if e < f goto _
105: goto _

```



backpatch

```

100: if a < b goto TRUE →
101: goto 102
102: if c < d goto 104
103: goto FALSE →
104: if e < f goto TRUE →
105: goto FALSE →

```

Backpatching with Lists: Translation Scheme

$M \rightarrow \varepsilon$	{ $M.\text{quad} := \text{nextquad}()$ }
$E \rightarrow E_1 \text{ or } M E_2$	{ $\text{backpatch}(E_1.\text{falselist}, M.\text{quad});$ $E.\text{truelist} := \text{merge}(E_1.\text{truelist}, E_2.\text{truelist});$ $E.\text{falselist} := E_2.\text{falselist}$ }
$E \rightarrow E_1 \text{ and } M E_2$	{ $\text{backpatch}(E_1.\text{truelist}, M.\text{quad});$ $E.\text{truelist} := E_2.\text{truelist};$ $E.\text{falselist} := \text{merge}(E_1.\text{falselist}, E_2.\text{falselist});$ }
$E \rightarrow \text{not } E_1$	{ $E.\text{truelist} := E_1.\text{falselist};$ $E.\text{falselist} := E_1.\text{truelist}$ }
$E \rightarrow (E_1)$	{ $E.\text{truelist} := E_1.\text{truelist};$ $E.\text{falselist} := E_1.\text{falselist}$ }

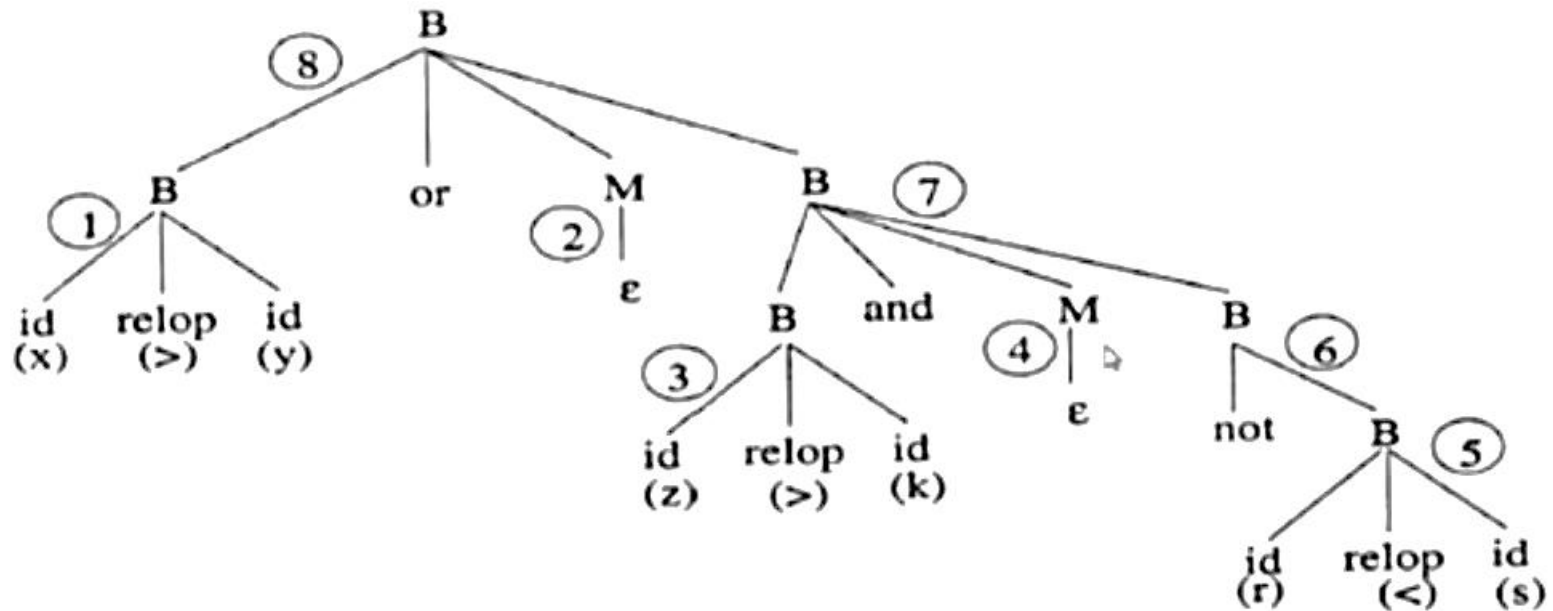
Backpatching with Lists: Translation Scheme (cont' d)

$E \rightarrow \mathbf{id}_1 \text{ relop } \mathbf{id}_2$	$\{$ $E.\text{truelist} := \text{makelist}(\text{nextquad}());$ $E.\text{falselist} := \text{makelist}(\text{nextquad}());$ $\text{emit}(\text{'if' id}_1.\text{place relop.op id}_2.\text{place 'goto '});$ $\text{emit}(\text{'goto '});$ $\}$
$E \rightarrow \mathbf{true}$	$\{ E.\text{truelist} := \text{makelist}(\text{nextquad}());$ $E.\text{falselist} := \text{nil};$ $\text{emit}(\text{'goto '});$ $\}$
$E \rightarrow \mathbf{false}$	$\{ E.\text{falselist} := \text{makelist}(\text{nextquad}());$ $E.\text{truelist} := \text{nil};$ $\text{emit}(\text{'goto '});$ $\}$

x and y or z > k

T F

a and (b or c and not d)



Reduction	Action	Code generated
1	B.truelist = {1} B.falselist = {2}	1: if x > y goto ... 2: goto ...
2	M.quad = 3	
3	B.truelist = {3}, B.falselist = {4}	3: if z > k goto ... 4: goto ...
4	M.quad = 5	
5	B.truelist = {5} B.falselist = {6}	5: if r > s goto ... 6: goto ...
6	B.truelist = {6}, B.falselist = {5}	
7	Backpatches list {3} with 5 $\{3, 6\}, \{5\}$	3: if z > k goto 5
8	Backpatches list {2} with 3 B.truelist = {1, 6}, B.falselist = {4, 5}	2: goto 3

x and M y or M z > k

T

F

E1.truelist{1}

1: goto _3_

E1.falselist{2}

2: goto _5_

M.quad{3}

E2.truelist{3}

3: goto _TRUE_

E2.falselist{4}

4: goto _5_

Backpatch {1} with 3

E1.tl{3} E1.fl{2,4}

M.quad{5}

E2.tl{5}

5: if z > k goto _TRUE_

E2.fl{6}

6: Goto _FALSE_

Backpatch {2,4} with 5

TRUE{3,5} FALSE{6}

FALSE{4}

Flow-of-Control Statements and Backpatching: Grammar

$S \rightarrow$ **if** E **then** S
 | **if** E **then** S **else** S
 | **while** E **do** S
 | **begin** L **end**
 | A
 $L \rightarrow L ; S$
 | S

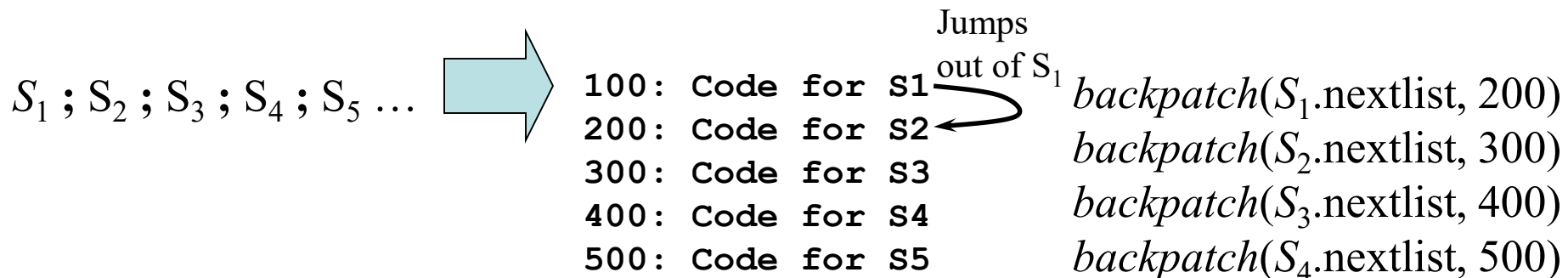
Synthesized attributes:

$S.nextlist$

backpatch list for jumps to the next statement after S (or nil)

$L.nextlist$

backpatch list for jumps to the next statement after L (or nil)



Flow-of-Control Statements and Backpatching

$S \rightarrow A$	$\{ S.\text{nextlist} := \text{nil} \}$
$S \rightarrow \mathbf{begin} \ L \ \mathbf{end}$	$\{ S.\text{nextlist} := L.\text{nextlist} \}$
$S \rightarrow \mathbf{if} \ E \ \mathbf{then} \ M \ S_1$	$\{ \text{backpatch}(E.\text{truelist}, M.\text{quad});$ $S.\text{nextlist} := \text{merge}(E.\text{falselist}, S_1.\text{nextlist}) \}$
$L \rightarrow L_1 ; M \ S$	$\{ \text{backpatch}(L_1.\text{nextlist}, M.\text{quad});$ $L.\text{nextlist} := S.\text{nextlist}; \}$
$L \rightarrow S$	$\{ L.\text{nextlist} := S.\text{nextlist}; \}$
$M \rightarrow \varepsilon$	$\{ M.\text{quad} := \text{nextquad}() \}$
$A \rightarrow \dots$	<i>Non-compound statements, e.g. assignment, function call</i>

Flow-of-Control Statements and Backpatching (cont' d)

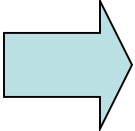
$S \rightarrow \text{if } E \text{ then } M_1 S_1 N \text{ else } M_2 S_2$
 $\quad \{ \text{backpatch}(E.\text{truelist}, M_1.\text{quad});$
 $\quad \text{backpatch}(E.\text{falselist}, M_2.\text{quad});$
 $\quad S.\text{nextlist} := \text{merge}(S_1.\text{nextlist},$
 $\quad \text{merge}(N.\text{nextlist}, S_2.\text{nextlist})) \}$

$S \rightarrow \text{while } M_1 E \text{ do } M_2 S_1$
 $\quad \{ \text{backpatch}(S_1.\text{nextlist}, M_1.\text{quad});$
 $\quad \text{backpatch}(E.\text{truelist}, M_2.\text{quad});$
 $\quad S.\text{nextlist} := E.\text{falselist};$
 $\quad \text{emit}(\text{'goto } M_1.\text{quad'}) \}$

$N \rightarrow \varepsilon$
 $\quad \{ N.\text{nextlist} := \text{makelist}(\text{nextquad}());$
 $\quad \text{emit}(\text{'goto } _') \}$

Translating Procedure Calls

$$S \rightarrow \text{call id } (\textit{Elist})$$
$$\textit{Elist} \rightarrow \textit{Elist} , E$$
$$| E$$

call foo(a+1, b, 7) 

```
t1 := 1
t1 := a + t1
t2 := 7
param t1
param b
param t2
call foo 3
```


Translating Procedure Calls

$S \rightarrow \text{call id} (Elist)$	{ for each item p on $queue$ do $emit(\text{'param'} p);$ $emit(\text{'call'} id.place queue)$ }
$Elist \rightarrow Elist , E$	{ append $E.place$ to the end of $queue$ }
$Elist \rightarrow E$	{ initialize $queue$ to contain only $E.place$ }