

Rule for derivatives of a scalar by a vector

1. A is not a function of x:

- Row layout: $\frac{\partial x^T A x}{\partial x} = x^T (A^T + A)$
- Column layout: $\frac{\partial x^T A x}{\partial x} = (A + A^T)x$

2. A is not a function of x and A is symmetric:

- Row layout: $\frac{\partial x^T A x}{\partial x} = 2x^T A$
- Column layout: $\frac{\partial x^T A x}{\partial x} = 2Ax$

3. A is not a function of x:

- Row layout: $\frac{\partial Ax}{\partial x} = A$
- Column layout: $\frac{\partial Ax}{\partial x} = A^T$

4. A is not a function of x:

- Row layout: $\frac{\partial x^T A}{\partial x} = A^T$
- Column layout: $\frac{\partial x^T A}{\partial x} = A^T$