

(m x n)

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 7 & 4 \end{bmatrix}$$

$$B = \begin{bmatrix} 1 & -1 \\ 0 & 1 \end{bmatrix}$$

$$C = \begin{bmatrix} 5 & -1 \\ 9 & 1 \\ 6 & 0 \end{bmatrix}$$

$$D = \begin{bmatrix} 3 & -2 & -1 \\ 1 & 2 & 3 \end{bmatrix}$$

$$U = [6 \ 2 \ -3 \ 5]$$

$$V = [3 \ 5 \ -1 \ 4]$$

$$w = \begin{bmatrix} 1 \\ 8 \\ 0 \\ 5 \end{bmatrix}$$

write dimensions

1) a)  $A = \mathbb{R}^{2 \times 3}$   $2 \times 3$

b)  $B = \mathbb{R}^{2 \times 2}$   $2 \times 2$

c)  $C = \mathbb{R}^{3 \times 2}$   $3 \times 2$

d)  $D = \mathbb{R}^{2 \times 3}$   $2 \times 3$

e)  $U = \mathbb{R}^{1 \times 4}$   $1 \times 4$

f)  $w = \mathbb{R}^{4 \times 1}$   $4 \times 1$

2.) Perform following operations  $\alpha = 6$

a)  $\vec{U} + \vec{V} = [6+3, 2+5, -3-1, 5+4] \rightarrow [9 \ 7 \ -4 \ 9]$

b)  $\vec{U} - \vec{V} = [6-3, 2-5, -3-(-1), 5-4] \rightarrow [3 \ -3 \ -2 \ 1]$

c)  $\alpha \vec{U} = [36, 12, -18, 30]$

e)  $\vec{U} \cdot \vec{V} = [6 \cdot 3 + 2 \cdot 5 + (-3) \cdot (-1) + 5 \cdot 4] = 51$

f)  $\|\vec{U}\| = \sqrt{6^2 + 2^2 + (-3)^2 + 5^2} = \sqrt{36 + 4 + 9 + 25} = \sqrt{74}$

3.) Evaluate each of the following expressions, if it is defined

a)  $A + C = \text{"not defined"}$

b)  $A - C^T = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 7 & 4 \end{bmatrix} - \begin{bmatrix} 5 & 9 & 6 \\ -1 & 1 & 0 \end{bmatrix} = \begin{bmatrix} -4 & -7 & -3 \\ 3 & 6 & 4 \end{bmatrix}$

c)  $C^T + 3D = \begin{bmatrix} 5 & 6 \\ -1 & 1 & 0 \end{bmatrix} + \begin{bmatrix} 9 & -6 & 3 \\ 3 & 6 & 9 \end{bmatrix} = \begin{bmatrix} 14 & 0 & 3 \\ 2 & 7 & 9 \end{bmatrix}$

d)  $BA = \begin{bmatrix} 1 & -1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 2 & 3 \\ 2 & 7 & 4 \end{bmatrix} = \begin{bmatrix} -1 & -5 & -1 \\ 2 & 7 & 4 \end{bmatrix}$

e)  $BA^T = \text{not defined}$

f)  $BC = \text{not defined}$