



**521150A**

# **Introduction to Internet**

**Lecture 4 – Data link layer, part II: Link Control**



# Schedule of the course

## PART I: Basics of networking and Internet, data link layer

<b>Mon 13.3.</b> 10-12 L6/Zoom	Lecture 1: Introduction & motivation
<b>Tue 14.3.</b> 10-12 L6/Zoom	Lecture 2: Architecture & design principles
<b>Wed 15.3.</b> 10-12 L5/Zoom	Lecture 3: Data link layer – basics part I
<b>Thu 16.3.</b> 10-12 L4/Zoom	Exercise session 1A
<b>Mon 20.3.</b> 10-12 L6/Zoom	Lecture 4: Data link layer – basics part II
<b>Tue 21.3.</b> 10-12 L6/Zoom	Exercise session 1B
<b>Tue 21.3.</b> 14-18 AT122/Zoom	Lab exercise 1 – group 3
<b>Wed 22.3.</b> 10-12 L5/Zoom	Lecture 5: Data link layer – Wired networks
<b>Wed 22.3.</b> 14-18 AT122/Zoom	Lab exercise 1 – group 4
<b>Thu 23.3.</b> 14-18 AT122/Zoom	Lab exercise 1 – group 2
<b>Fri 24.3.</b> 12-16 AT122/Zoom	Lab exercise 1 – group 1
<b>Mon 27.3.</b> 14-16 L5/Zoom	Exercise session 1C
<b>Tue 28.3.</b> 10-12 L6/Zoom	Lecture 6: Data link layer – Wireless networks
<b>Wed 29.3.</b> 10-12 Moodle	Theory exam 1

## PART II: Network and transport layers

<b>Thu 30.3.</b> 8-10 L5/Zoom	Lecture 7: Network layer part I
<b>Mon 3.4.</b> 14-16 L5/Zoom	Exercise session 2A
<b>Tue 4.4.</b> 10-12 L6/Zoom	Lecture 8: Network layer part II
<b>Wed 5.4.</b> 10-12 L5/Zoom	Lecture 9: Transport layer part I
	Course work intro
<b>Tue 11.4.</b> 10-12 L6/Zoom	Lecture 10: Transport layer part II
<b>Tue 11.4.</b> 14-18 AT122/Zoom	Lab exercise 2 – group 3
<b>Wed 12.4.</b> 10-12 Moodle	Theory exam 2
<b>Wed 12.4.</b> 14-18 AT122/Zoom	Lab exercise 2 – group 4
<b>Thu 13.4.</b> 8-10 L5/Zoom	Exercise session 2B
<b>Thu 13.4.</b> 14-18 AT122/Zoom	Lab exercise 2 – group 2
<b>Fri 14.4.</b> 12-16 AT122/Zoom	Lab exercise 2 – group 1
	Course work (independent work)

## PART III: Application layer, network security and multimedia

<b>Fri 14.4.</b> 10-12 L5/Zoom	Lecture 11: Networking applications
<b>Mon 17.4.</b> 14-16 L5/Zoom	Lecture 12: Network security
<b>Tue 18.4.</b> 10-12 L6/Zoom	Exercise session 3A
<b>Wed 19.4.</b> 10-12 L5/Zoom	Lecture 13: Multimedia and QoS
<b>Mon 24.4.</b> 14-16 L5/Zoom	Exercise session 3B
<b>Tue 25.4.</b> 14-18 AT122/Zoom	Lab exercise 3 – group 3
<b>Wed 26.4.</b> 10-12 L5/Zoom	Lecture 14: Challenges&Future Internet trends
<b>Wed 26.4.</b> 14-18 AT122/Zoom	Lab exercise 3 – group 4
<b>Thu 27.4.</b> 14-18 AT122 /Zoom	Lab exercise 3 – group 2
<b>Fri 28.4.</b> 12-16 AT122 /Zoom	Lab exercise 3 – group 1
<b>Wed 3.5.</b> 10-12 Moodle	Theory exam 3
<b>Thu 25.5.</b> 16-19 L1	Final exam



# Main learning objectives of this lecture

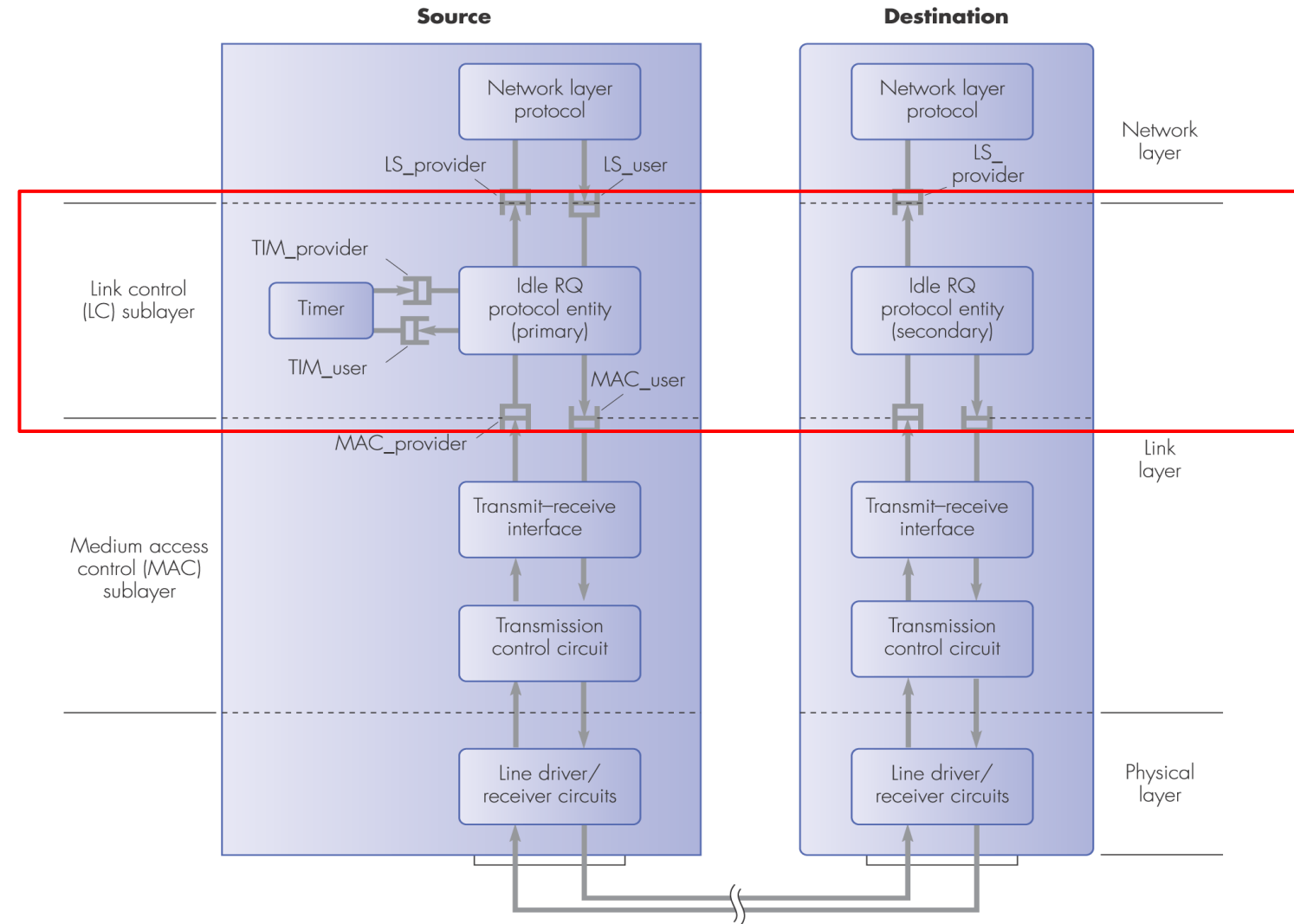
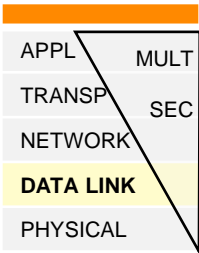
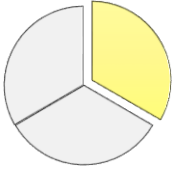
1. Know the main functions of Link Control
2. Understand the basic concept of flow control and know its basic types:
  - Stop&wait
  - Pipelining
  - Sliding window
3. Understand the concept of error control and know its basic types:
  - Stop&wait ARQ
  - Go-Back-N ARQ
  - Selective repeat



# Basics of Link Control



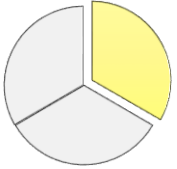
# Link Control (LC)



LS = link service



# Data link layer architecture



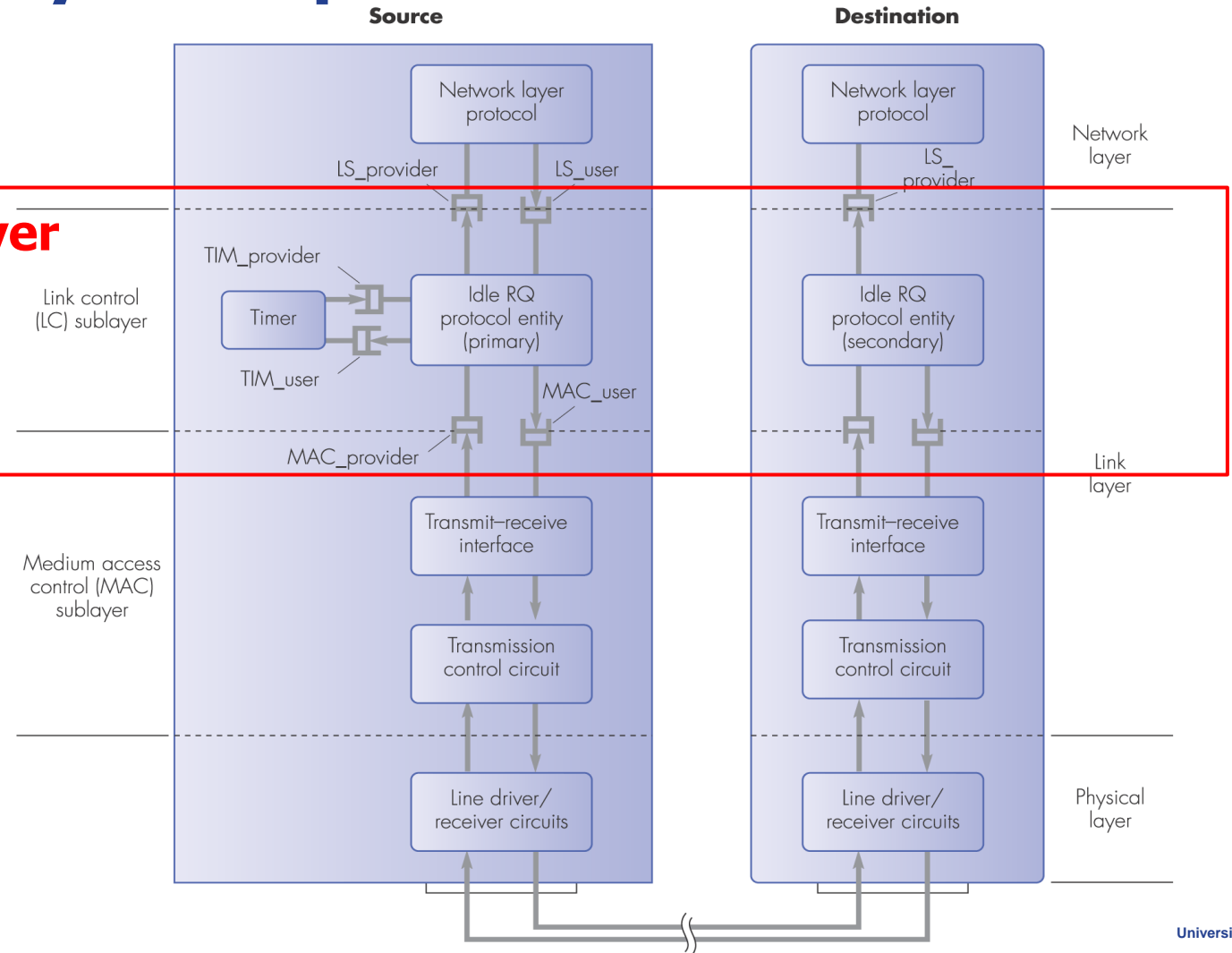
Typically data link layer comprises of two sublayers:

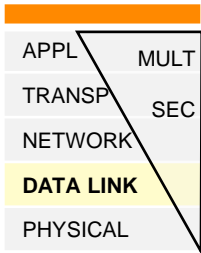
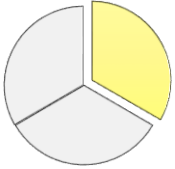
## – Link control (LC) sublayer

- Error control
- Flow control

## – Medium access control (MAC) sublayer

- Framing
- Transmission (medium access)

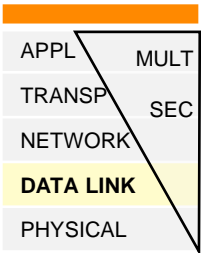
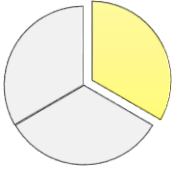




# Data link control protocols

- Requirements/objectives for effective data communication between two directly-connected transmitting-receiving stations
  - **Frame synchronization:** data are sent in frames, the beginning and end of each frame must be recognizable;
  - **Flow control:** sending station must not send frames at a rate faster than the receiving station can absorb them;
  - **Error control:** bit errors introduced by the transmission system should be corrected, or at least the upper layer should be informed;
  - **Addressing:** in a shared link (such as LAN), the identity of the two stations involved in transmission must be specified;
  - **Control and data on same link:** not desirable to have a separate physical communication path for control information, receiver must be able to distinguish control information from the data being transmitted;
  - **Link management:** procedures for coordination and cooperation among stations for the initiation, maintenance and termination of sustained data exchange;

→ **A data link control protocol is needed**



# Specification of a data link control protocol

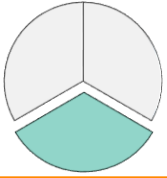
## – Building blocks

- Frames (data, acknowledgments)
- Buffers
- Timers
- Sequence numbers (frame ID's)
- Flow control
- Error control (incl. error detection)

## – Notation of following protocol examples

- P = primary (sender, source)
- S = secondary (receiver, destination)
- I(N) = information (data) with sequence number N
- ACK = positive acknowledgment frame
- NAK = negative acknowledgment frame

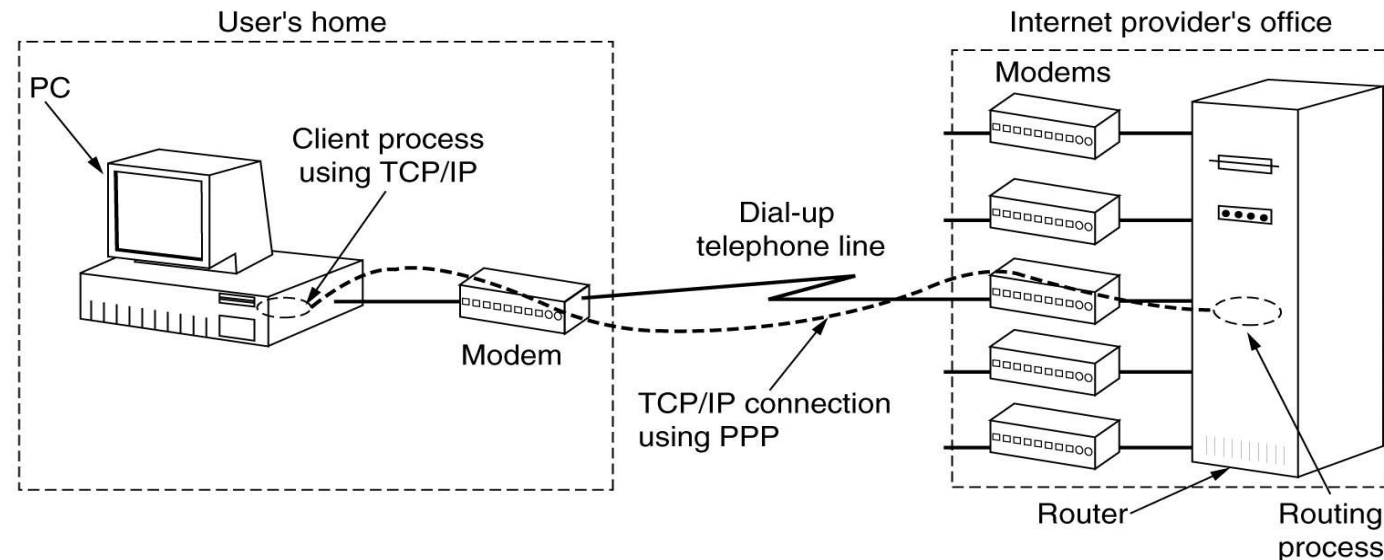


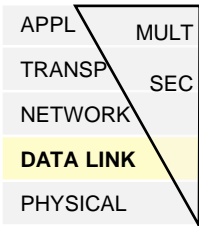
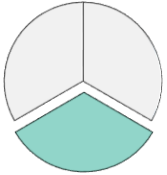


APPL	MULT
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<b>DATA LINK</b>	
PHYSICAL	

# PPP: Point-to-point data link control

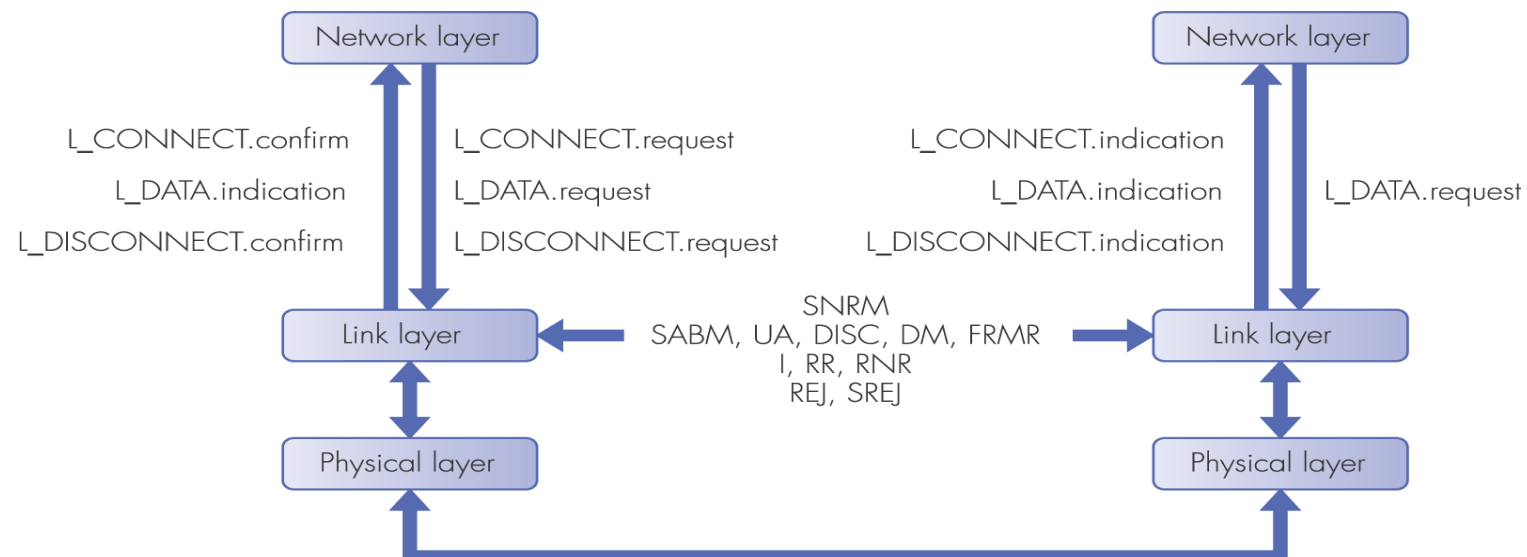
- RFC 1661 etc.
- One sender, one receiver, one link
- Easier than shared broadcast link
  - No medium access control
  - No need for explicit MAC addressing
  - E.g., dialup link, ISDN line

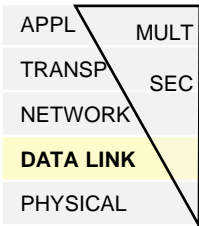
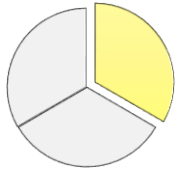




# HDLC (High-level Data Link Control)

- ISO 3009, ISO 4335
- Most important data link control protocol
- Bit-oriented
- Synchronous transmission
  - All transmission in form of frames
- Widely used for point-to-point and point-to-multipoint links
- Also basis for many other important data link protocols





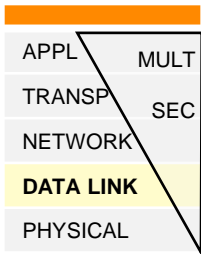
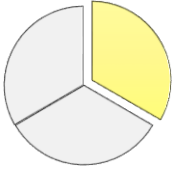
# Link performance characterization (1)

## – Assumptions

- $d$ : length of the physical link (m)
- $V$ : signal propagation speed in the link medium (m/s)
- $L$ : length of a frame (bits)
- **Data rate ( $R$ , bps) (also called bit rate or bandwidth)**
- Amount of data (bits) that can be transmitted per unit of time (s)
- Note inverse relation between data rate and bit duration

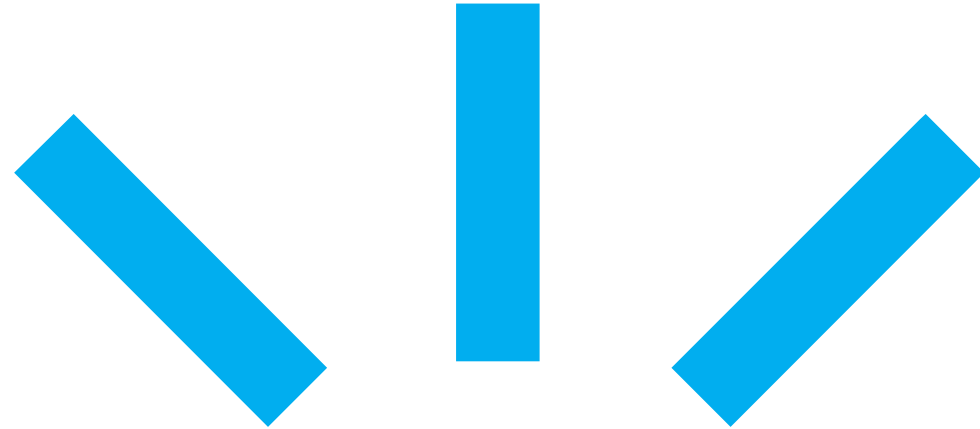
## – Delays

- **Transmission delay  $T_x$** : time taken to transmit a frame at the data rate of the link ( $L/R$ )
- **Propagation delay  $T_p$** : time for the signal to propagate (travel) from one of the link to the other end (medium specific) ( $d / V$ )
- **One-way delay**: time from the transmission of the first bit of a frame to the arrival of the last bit of the frame at receiver
- **Round-trip delay**: time from the transmission of the first bit of a frame to the arrival of the last bit of the acknowledgment sent by the receiver at sender

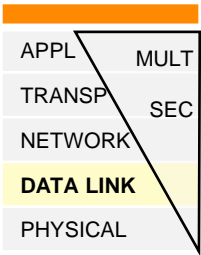
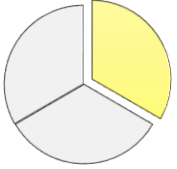


# Link performance characterization (2)

- **Bit length of a link:  $B = R \times (d / V)$** 
  - Number of bits fully occupying a link (i.e. *bandwidth x delay* product, bdp)
- **Let's define relationship  $a = B / L = (d/V) / (L/R) = T_p / T_x$** 
  - Number of frames in link of bit length B, when frame length is L
  - Ratio between propagation delay and transmission delay
- **Relationship between a and round-trip delay**
  - $a < 1 \rightarrow$  round-trip delay determined primarily by transmission delay
  - $a = 1 \rightarrow$  both delays have qual effect
  - $a > 1 \rightarrow$  round-trip delay determined primarily by propagation delay
  - This relationship has great impact on link utilization, as we will soon see
- **Bandwidth-delay product (bdp)**
  - One-way: number of bits transmitted before first bit arrives at receiver
  - Round-trip: number of bits transmitted before sender receives acknowledgment

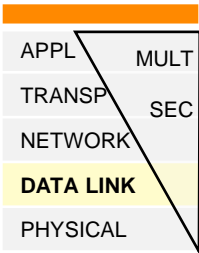
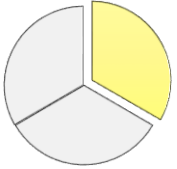


# Flow control

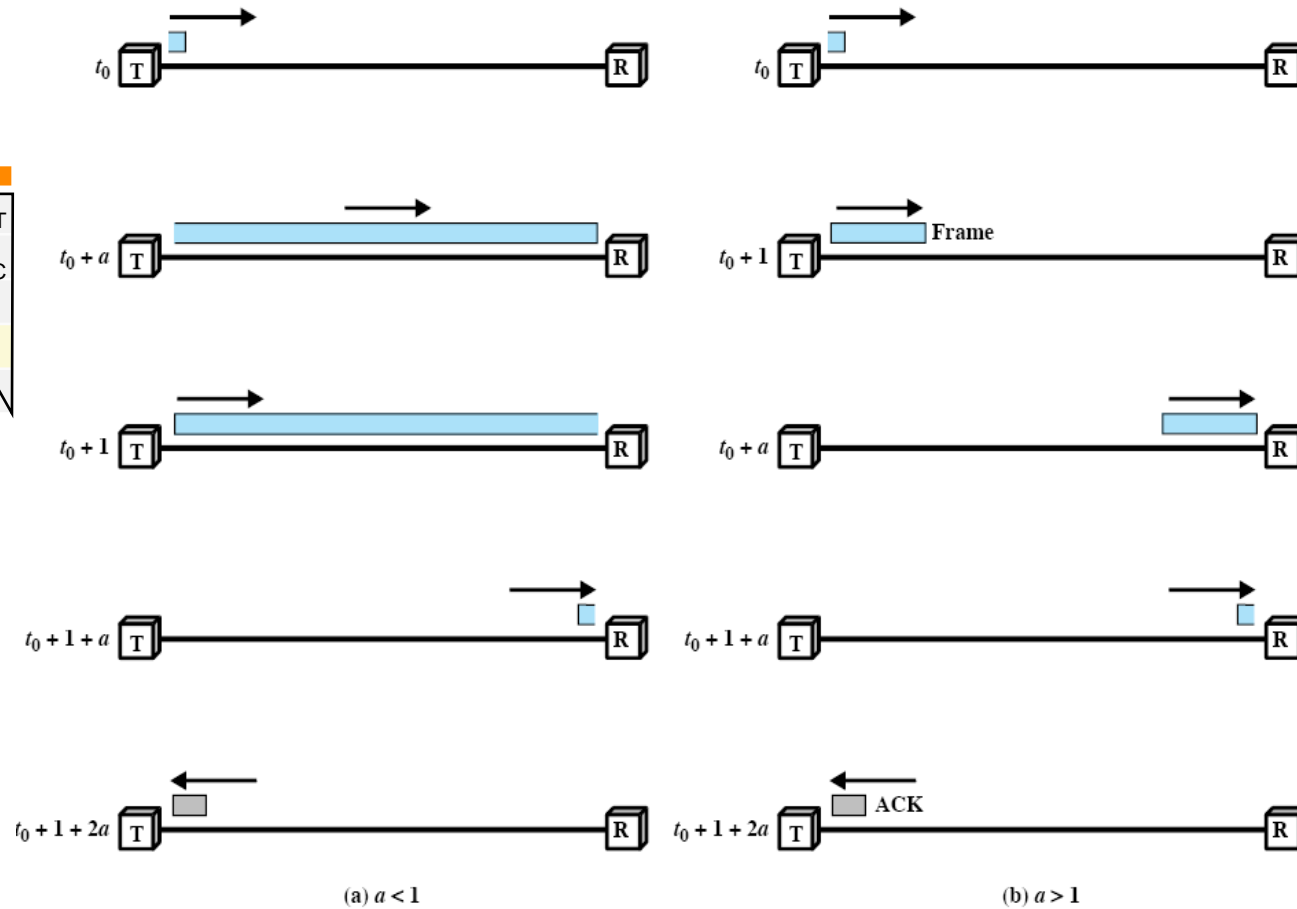


# Flow control

- Regulate the flow of data in such manner that fast senders do not swamp slow receivers
  - Receiver typically allocates data buffer of finite length for a connection
- Two basic approaches
  - **Feedback-based flow control**
    - Based on information provided by receiver to sender
    - Stop-and-wait flow control
    - Flow control with sliding windows
  - Rate-based flow control
    - Built in sender, not based on information provided by receiver
    - Not used in data link layer protocols

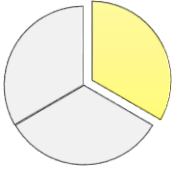


# Stop-and-wait flow control



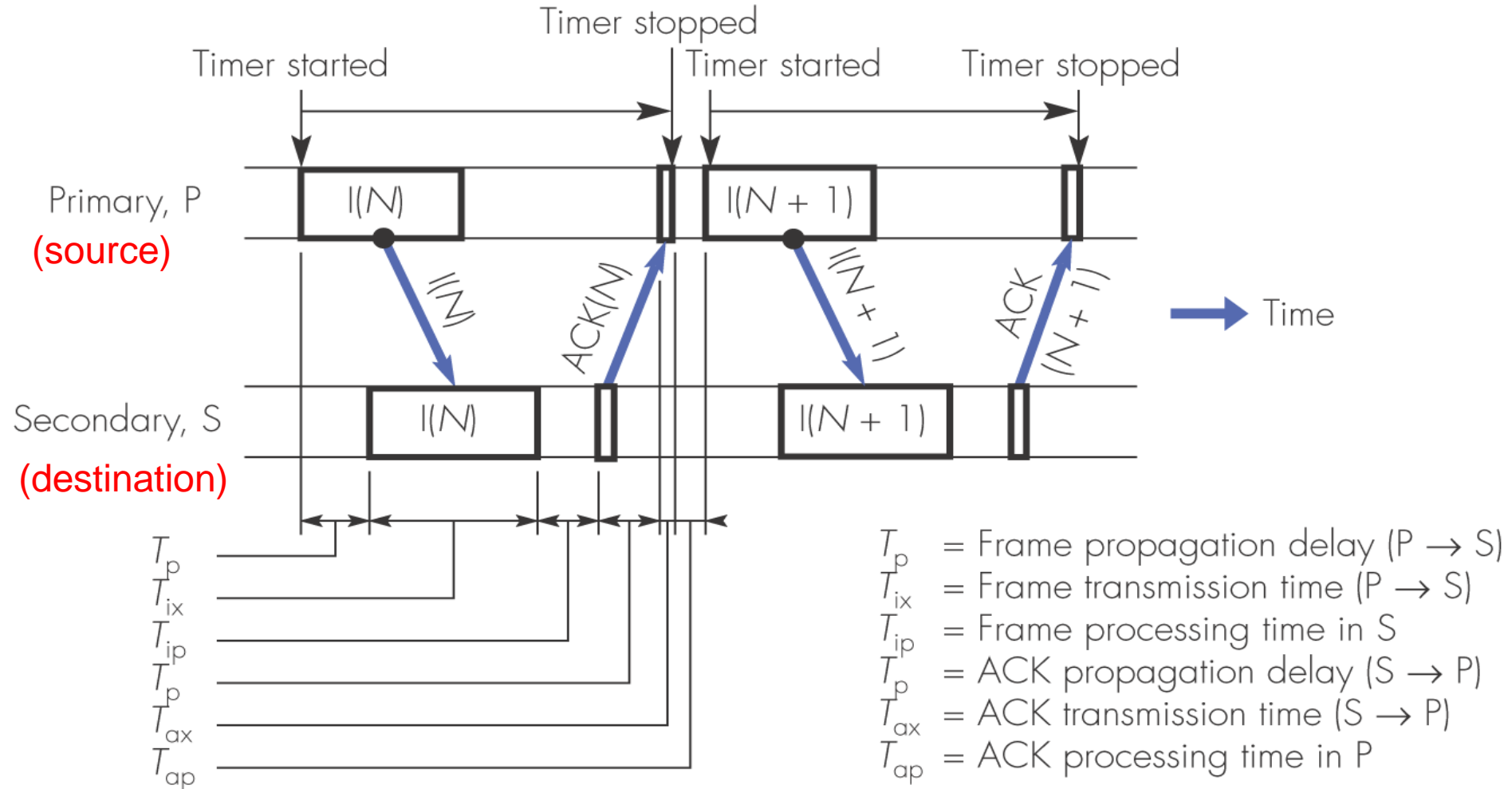
- Source transmits frame
- Destination receives frame and replies with acknowledgement (ACK)
- Source waits for ACK before sending next frame
- Destination can stop flow by not send ACK
- Only one frame in transit at any time

**$a < 1$ :** first bit of frame arrives at receiver before last bit has been transmitted



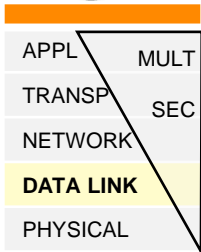
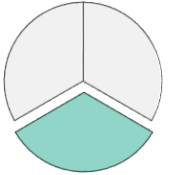
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DATA LINK	
PHYSICAL	

# Stop-and-wait flow control (2)



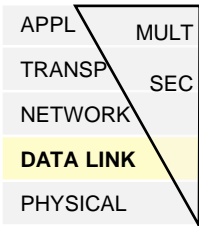
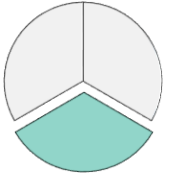
**Link utilization:**  $U = T_{ix} / T_t \sim T_{ix} / (T_{ix} + 2T_p) = 1 / (1 + 2T_p / T_{ix}) = \mathbf{1 / (1 + 2a)}$ ,  
where  $a = T_p / T_{ix}$





# Stop-and-wait flow control: Example (1)

- A series of **1000-bit frames** is to be **transmitted using stop-and-wait protocol**.
- Determine the link utilization for the following types of data links assuming a transmission bit rate of:
  - 1 **k**bps
  - 1 **M**bps
  - 1 **G**bps
    - 1 km long twisted-pair cable. Signal propagation speed is  $2 \times 10^8$  m/s.
    - 200 km long leased line. Signal propagation speed is  $2 \times 10^8$  m/s.
    - 50000 km long satellite link. Signal propagation speed is  $3 \times 10^8$  m/s.
  - Bit error rate is negligible (can be ignored).



# Stop-and-wait flow control: Example (2)

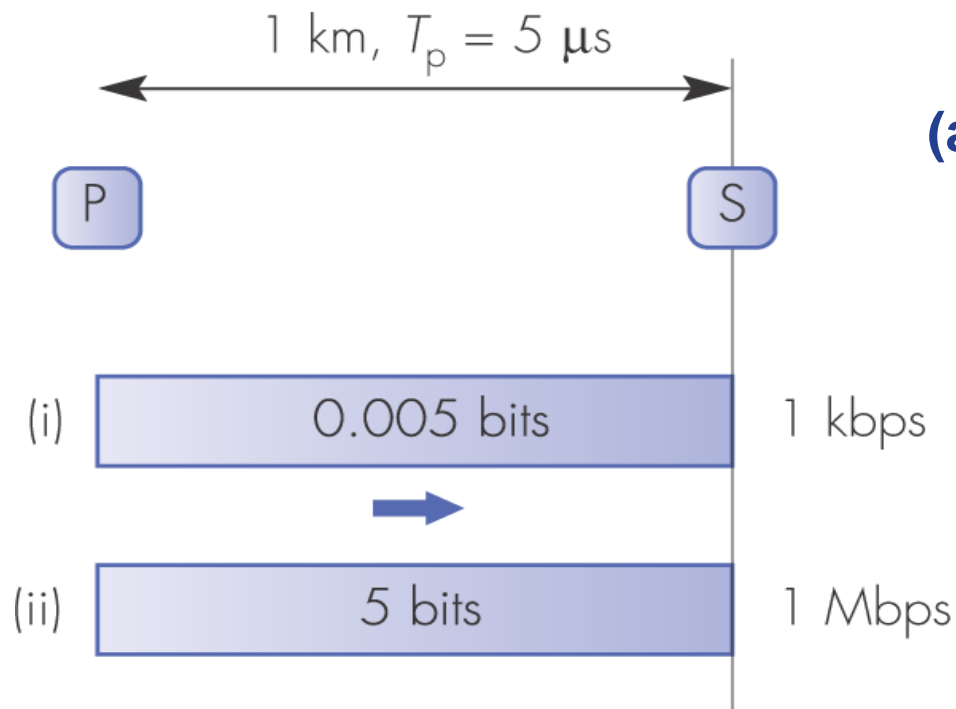
Frame transmission time  $T_{ix}$  = Number of bits in frame / Bit rate

(i) 1 kbps:  $T_{ix} = 1000 \text{ b} / 10^3 \text{ b/s} = 1 \text{ s}$

(ii) 1 Mbps:  $T_{ix} = 1000 \text{ b} / 10^6 \text{ b/s} = 10^{-3} \text{ s} = 1 \text{ ms}$

(iii) 1 Gbps:  $T_{ix} = 1000 \text{ b} / 10^9 \text{ b/s} = 10^{-6} \text{ s} = 1 \mu\text{s}$

Twisted pair



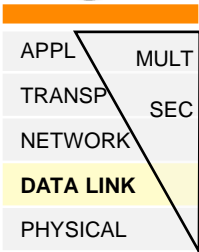
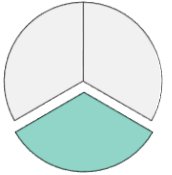
(a) 1 km long twisted-pair cable. Signal propagation speed is  $2 \times 10^8 \text{ m/s}$ .

Frame propagation delay  $T_p = 10^3 \text{ m} / 2 \times 10^8 \text{ m/s} = 5 \times 10^{-6} \text{ s}$

(i)  $a = T_p / T_{ix} = 5 \times 10^{-6} \text{ s} / 1 \text{ s} = 5 \times 10^{-6} \rightarrow (1 + 2a) \approx 1, U = 1$

(ii)  $a = 5 \times 10^{-6} \text{ s} / 10^{-3} \text{ s} = 5 \times 10^{-3} \rightarrow (1 + 2a) \approx 1, U = 1$

(iii)  $a = 5 \times 10^{-6} \text{ s} / 10^{-6} \text{ s} = 5 \rightarrow (1 + 2a) = 11, U = 0.09$



# Stop-and-wait flow control: Example (3)

## Leased line

Frame transmission time  $T_{ix}$  = Number of bits in frame / Bit rate

(i) 1 kbps:  $T_{ix} = 1000 \text{ b} / 10^3 \text{ b/s} = 1 \text{ s}$

(ii) 1 Mbps:  $T_{ix} = 1000 \text{ b} / 10^6 \text{ b/s} = 10^{-3} \text{ s} = 1 \text{ ms}$

(iii) 1 Gbps:  $T_{ix} = 1000 \text{ b} / 10^9 \text{ b/s} = 10^{-6} \text{ s} = 1 \mu\text{s}$

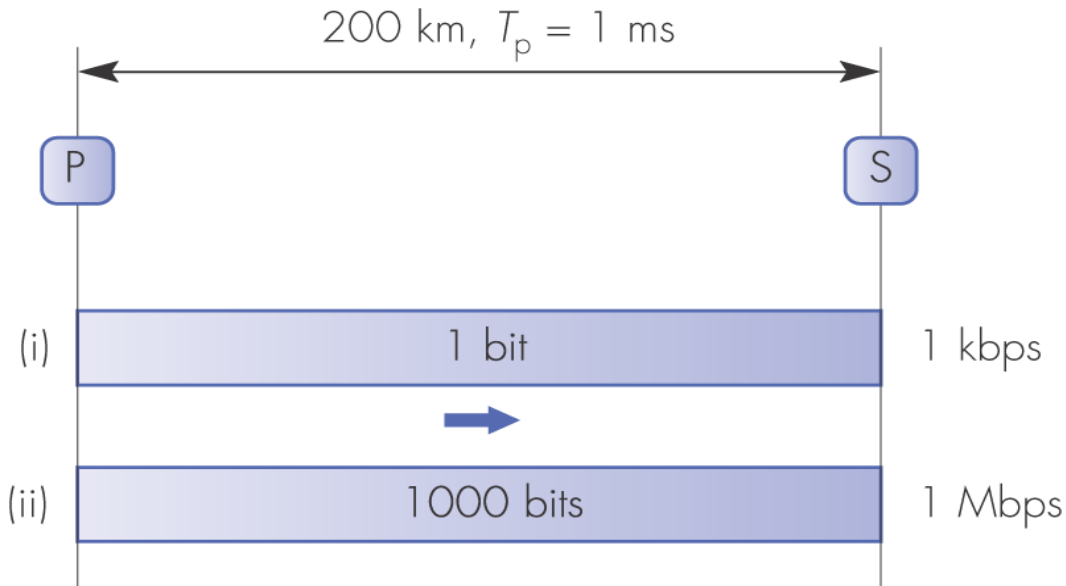
(b) 200 km long leased line. Signal propagation speed is  $2 \times 10^8 \text{ m/s}$ .

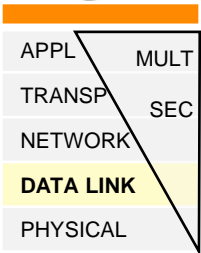
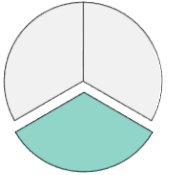
Frame propagation delay  $T_p = 200 \times 10^3 \text{ m} / 2 \times 10^8 \text{ m/s} = 10^{-3} \text{ s}$

(i)  $a = T_p / T_{ix} = 10^{-3} \text{ s} / 1 \text{ s} = 1 \times 10^{-3} \rightarrow (1 + 2a) \approx 1, U = 1$

(ii)  $a = 10^{-3} \text{ s} / 10^{-3} \text{ s} = 1 \rightarrow (1 + 2a) > 1, U = 1/(1+2) = 0.33$

(iii)  $a = 10^{-3} \text{ s} / 10^{-6} \text{ s} = 1000 \rightarrow U = 0.0005$





# Stop-and-wait flow control: Example (4)

## Satellite link

Frame transmission time  $T_{ix}$  = Number of bits in frame / Bit rate

(i) 1 kbps:  $T_{ix} = 1000 \text{ b} / 10^3 \text{ b/s} = 1 \text{ s}$

(ii) 1 Mbps:  $T_{ix} = 1000 \text{ b} / 10^6 \text{ b/s} = 10^{-3} \text{ s} = 1 \text{ ms}$

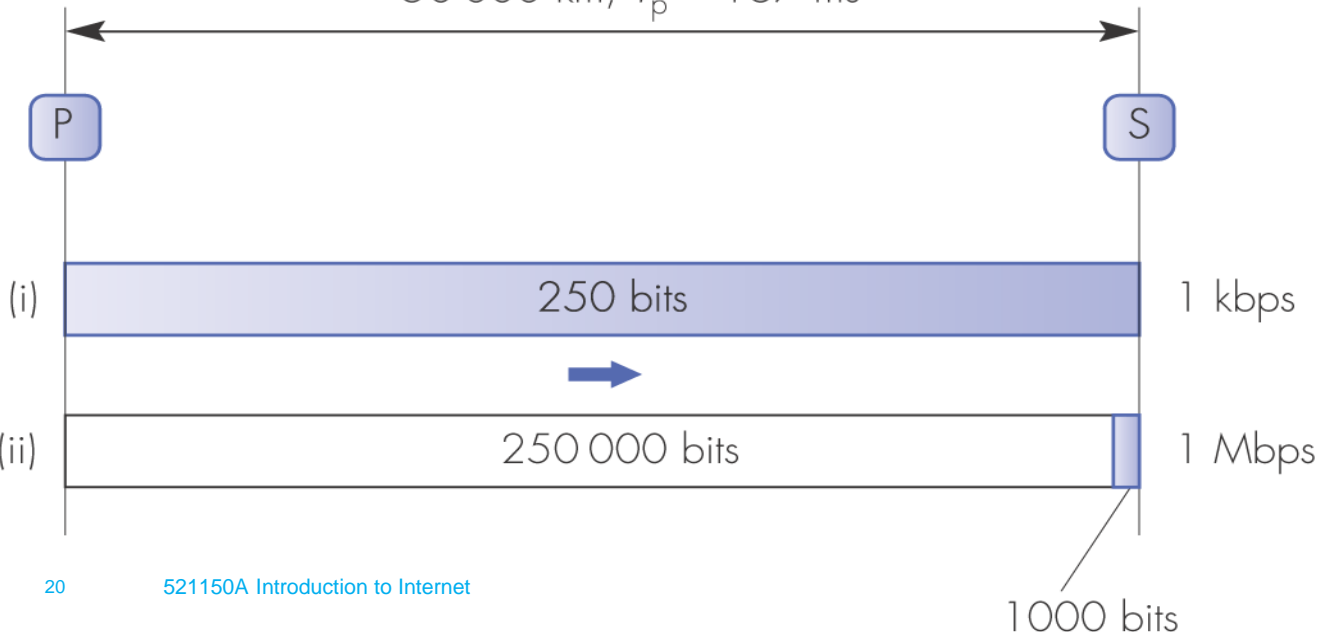
(c) A 50000 km long satellite link. Signal propagation speed is  $3 \times 10^8 \text{ m/s}$ .

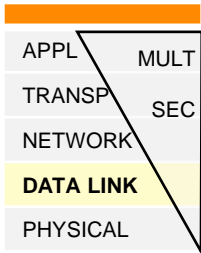
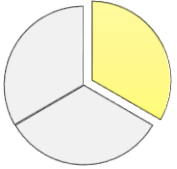
Frame propagation delay  $T_p = 50 \times 10^6 \text{ m} / 3 \times 10^8 \text{ m/s} = 0.167 \text{ s}$

(i)  $a = T_p / T_{ix} = 0.167 \text{ s} / 1 \text{ s} = 0.167 \rightarrow (1 + 2a) > 1$ ,  
 $U = 1 / (1 + 0.334) = 0.75$

(ii)  $a = 0.167 \text{ s} / 10^{-3} \text{ s} = 167 \rightarrow (1 + 2a) > 1$ ,  $U = 1 / (1 + 334) = 0.003$

50 000 km,  $T_p = 167 \text{ ms}$





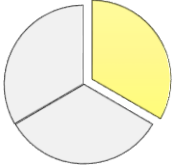
# Stop-and-wait flow control: Example (5)

## – Observations

- Relatively short links
  - Link utilization is 100% for lower bit rates
- Longer terrestrial links
  - Link utilization is high for low bit rates
  - Link utilization falls off significantly as bit rate increases
- Long satellite links
  - Link utilization is poor (due to high propagation delay)

→ **Stop-and-wait flow-control suitable for short and low bit rate links**

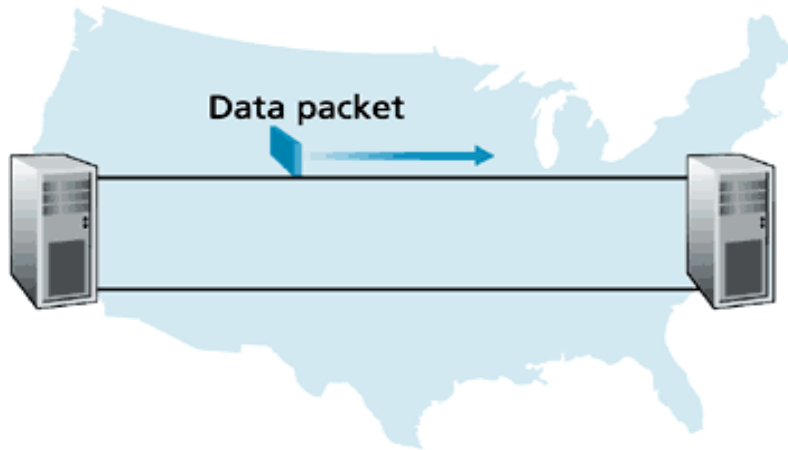
- E.g. links based on modems and analog PSTN



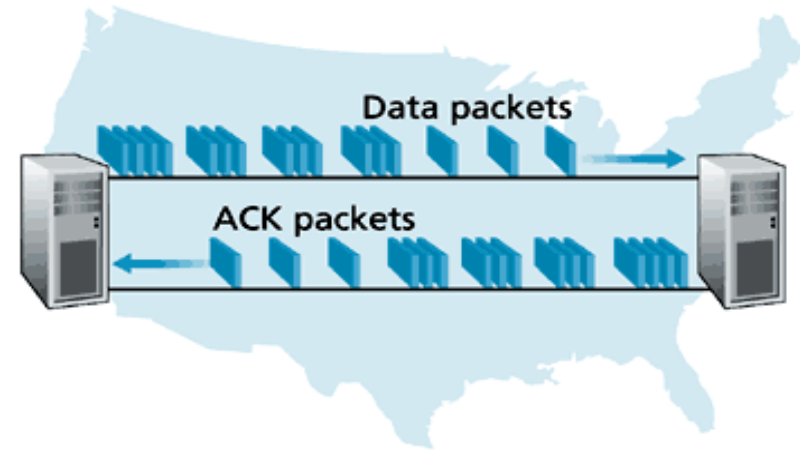
APPL	MULT
TRANSP	SEC
NETWORK	
DATA LINK	
PHYSICAL	

# Pipelining (1)

- Primary (sender, source) is allowed to **send multiple packets without waiting for acknowledgements**

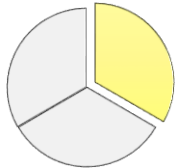


a. A stop-and-wait protocol in operation



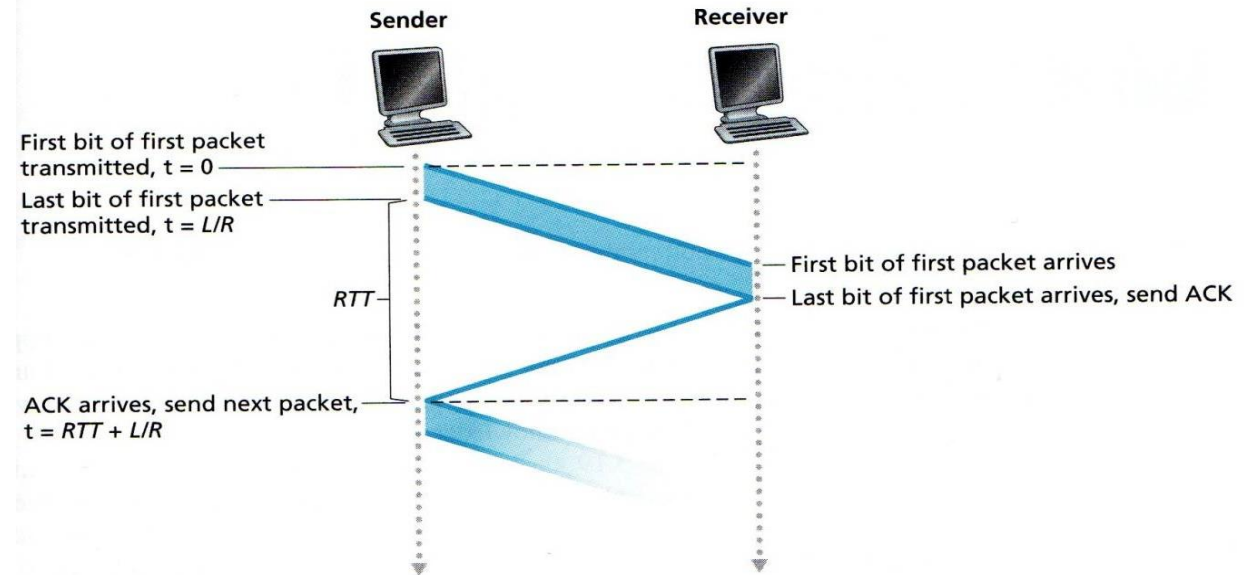
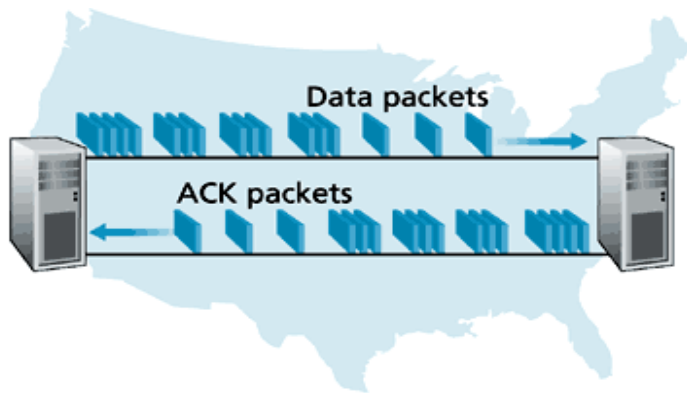
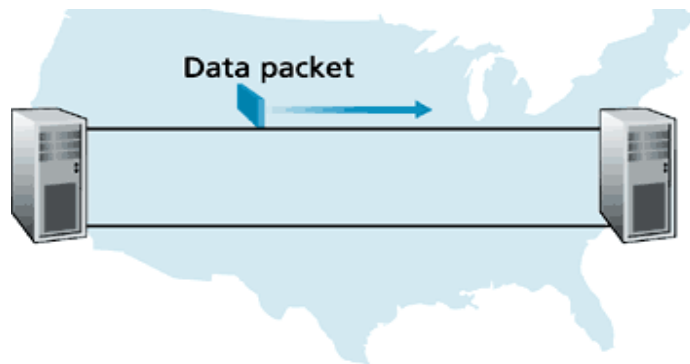
b. A pipelined protocol in operation

- Much **better utilization of link capacity**, with **increased buffer requirements** and **larger ranges of sequence numbers**
- Bi-directional, requires full-duplex link
- Requires flow control with sliding windows

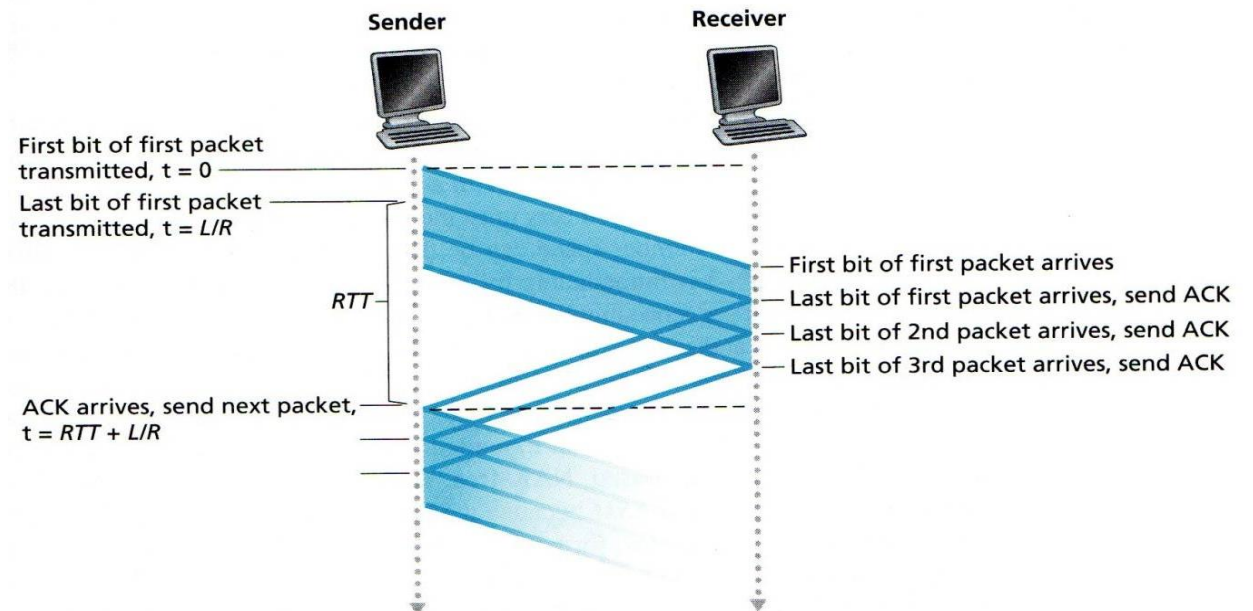


APPL	MULT
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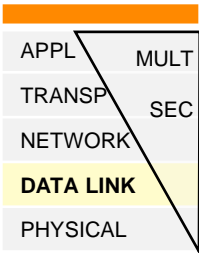
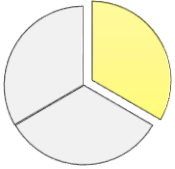
# Pipelining (2)



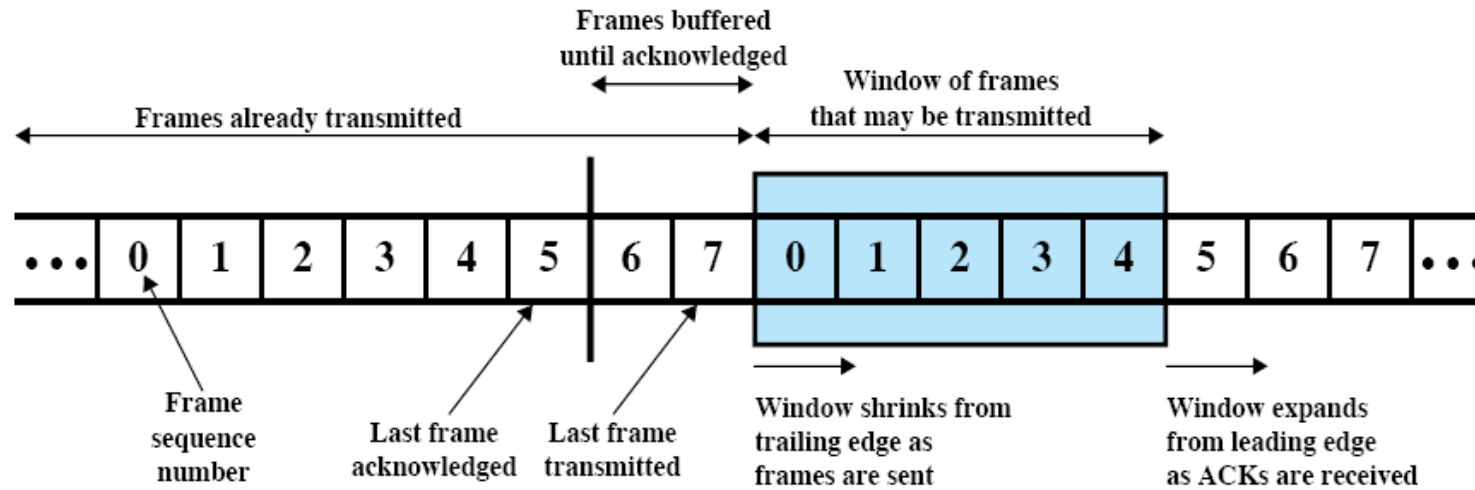
a. Stop-and-wait operation



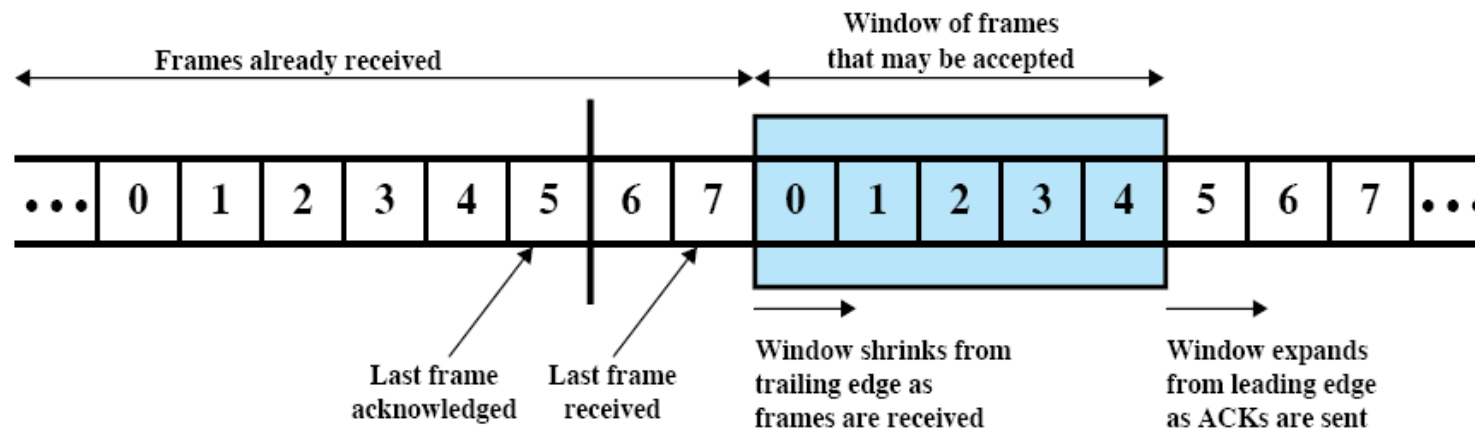
b. Pipelined operation



# -Flow control: Sliding windows (1)



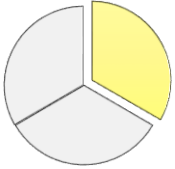
(a) Sender's perspective



(b) Receiver's perspective

- Receiver has buffer  $W$  long
- Transmitter can send up to  $W$  frames without ACK
- Each frame is numbered
- ACK includes number of next frame expected

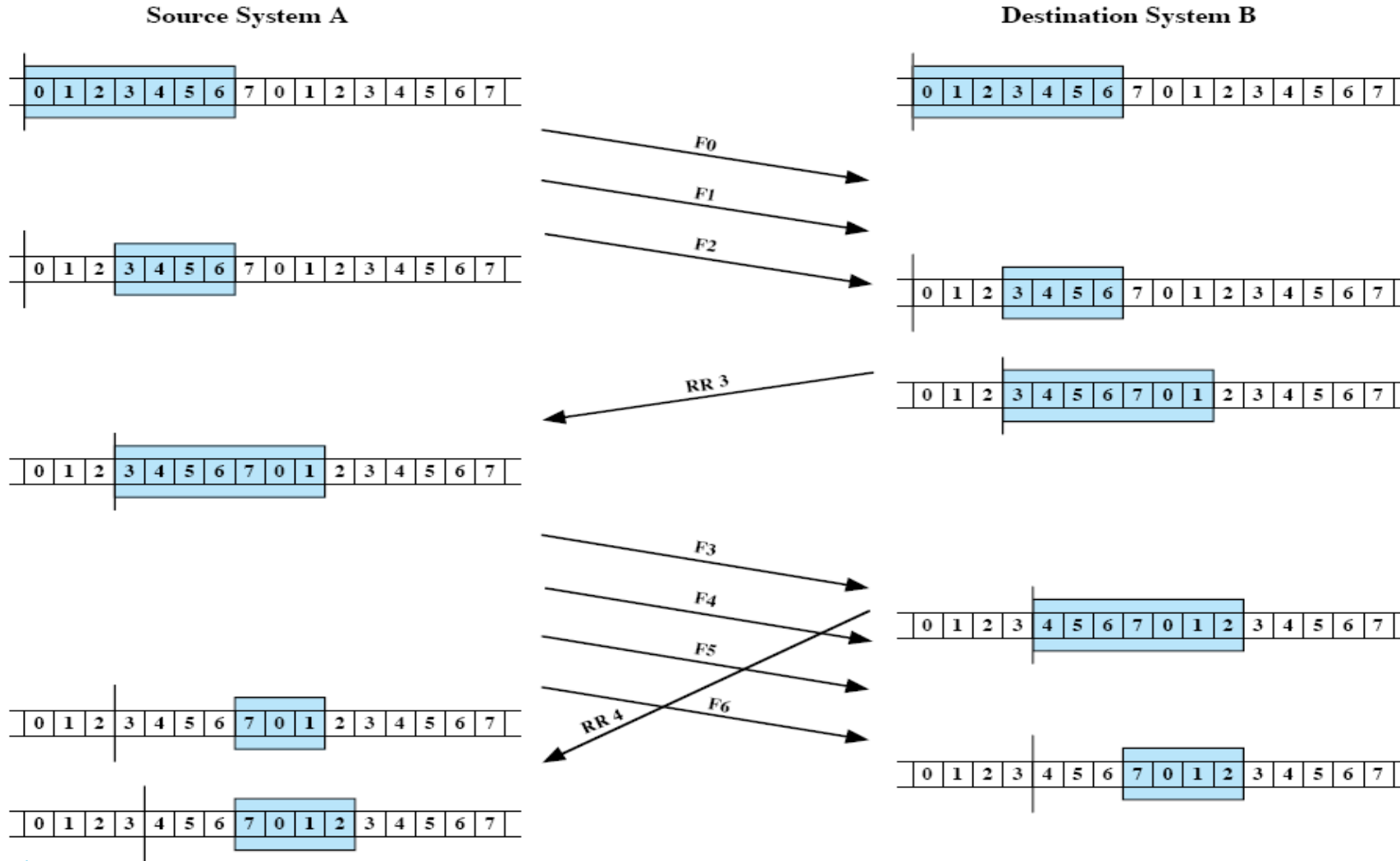


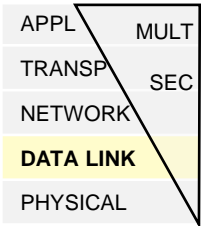
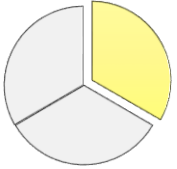


APPL	MULT
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# Flow control: Sliding windows (2)

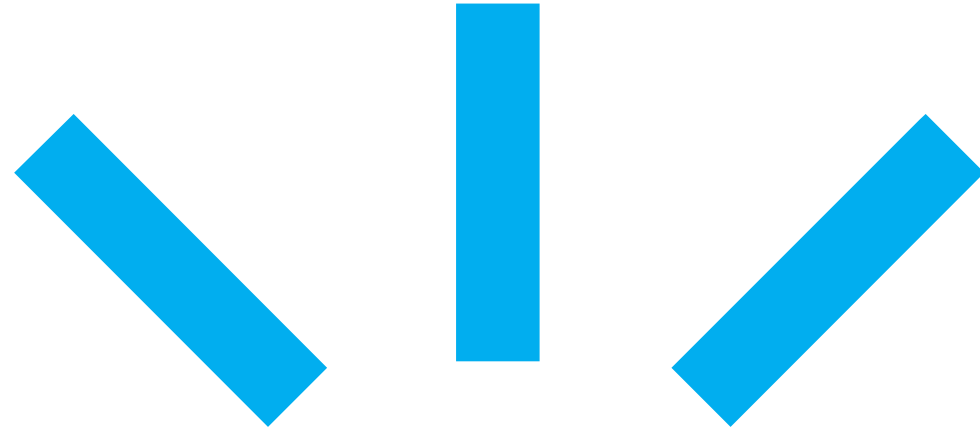
Example with sliding window of 7 frames



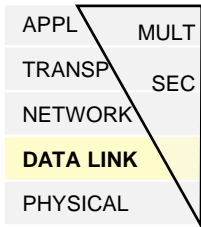
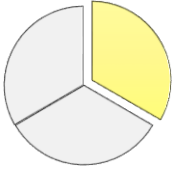


# Flow control: Performance enhancements

- **Receiver acknowledges multiple I frames with one ACK**
- **Piggybacking**
  - Acknowledgements are attached to I frames (ACK field), instead of being transmitted as separate ACK frames



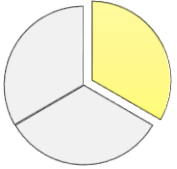
# Error control



# Error control

- **Two types of errors**
  - Lost frame
  - Damaged frame
- **Mechanisms used for error control**
  - Error detection
  - Positive acknowledgments
  - Retransmission after timeout (retransmission timer)
  - Negative acknowledgment and retransmission
- **Three types of ARQ (automatic repeat request)**
  - Stop-and-wait ARQ
  - Go-back-N ARQ
  - Selective repeat ARQ

**Continuous RQ**  
(uses sliding window flow control)



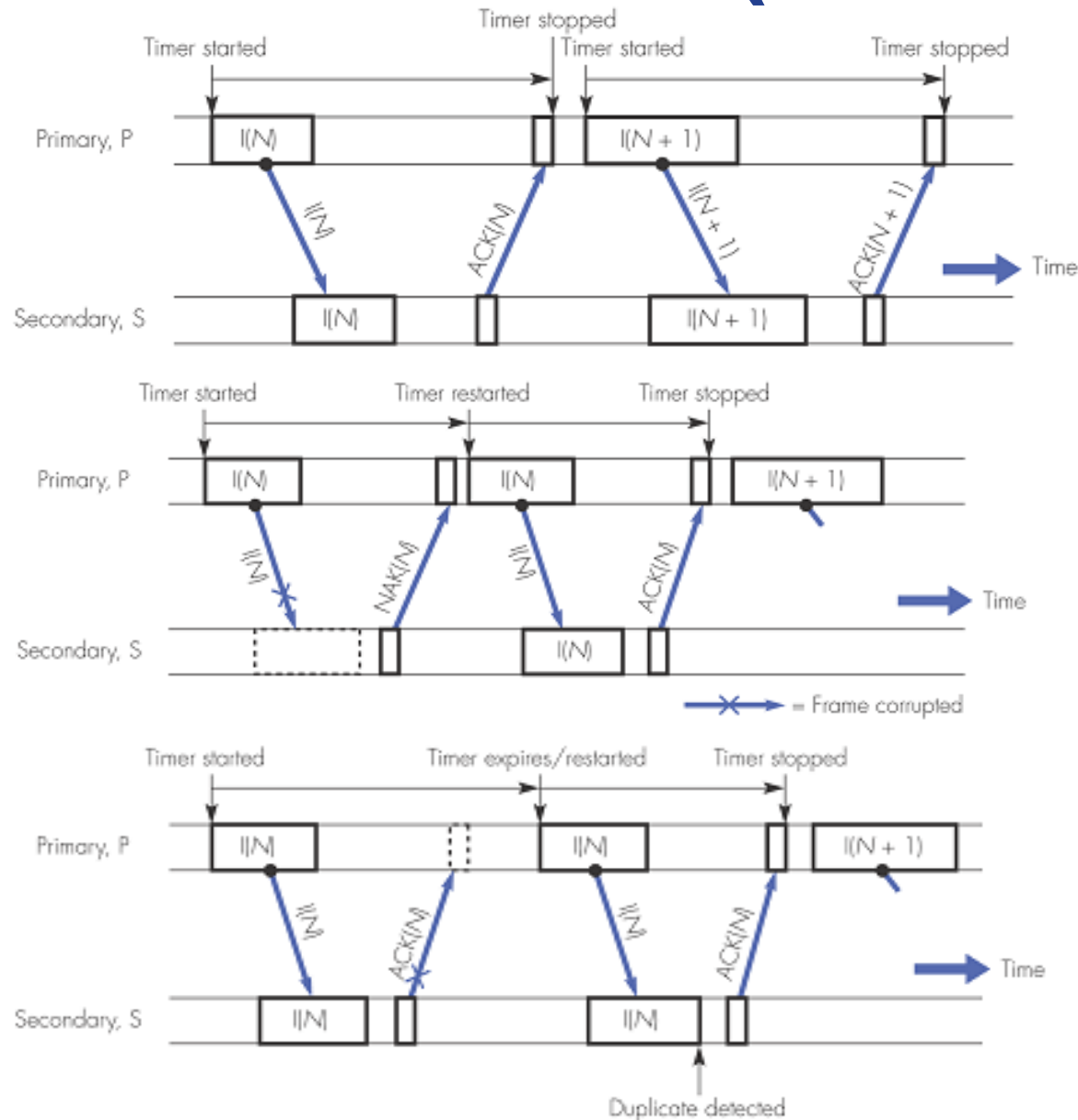
APPL	MULT
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NETWORK	
DATA LINK	
PHYSICAL	

# Stop-and-wait ARQ (aka idle RQ)

error free

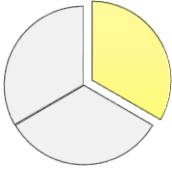
corrupted  
I frame

corrupted  
ACK frame



## Building blocks

- Retransmission timer
- Error detection
- Receiver feedback (ACK, NAK)
- Retransmission

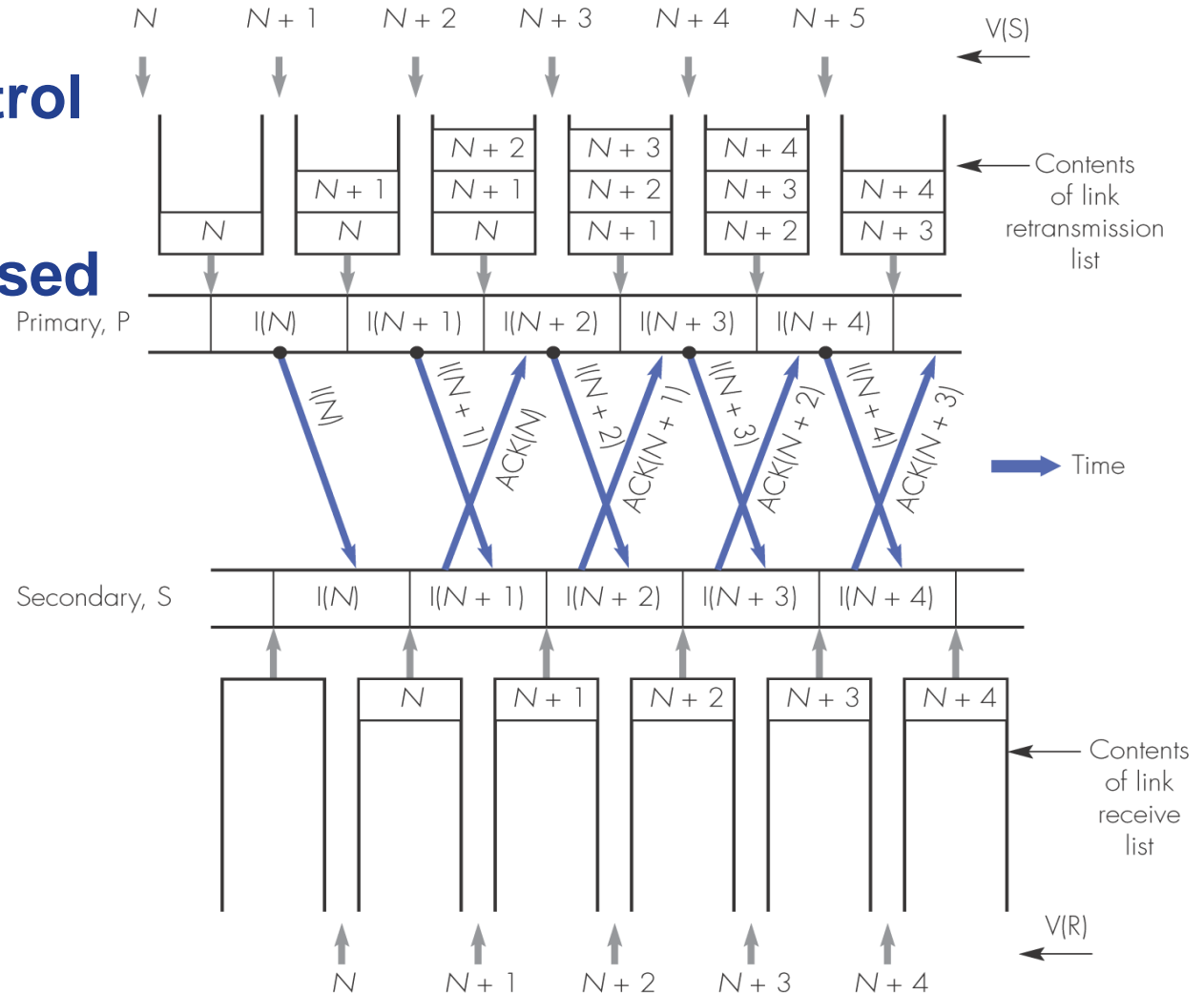


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PHYSICAL	

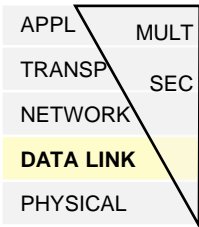
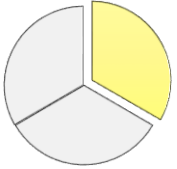
# Continuous RQ

- Incorporate flow control
- Link utilization much improved with increased buffer storage requirements
- Bidirectional
  - Requires duplex link
- Two basic types
  - Go-back-N ARQ
  - Selective repeat ARQ

Continuous RQ frame sequence without transmission errors:

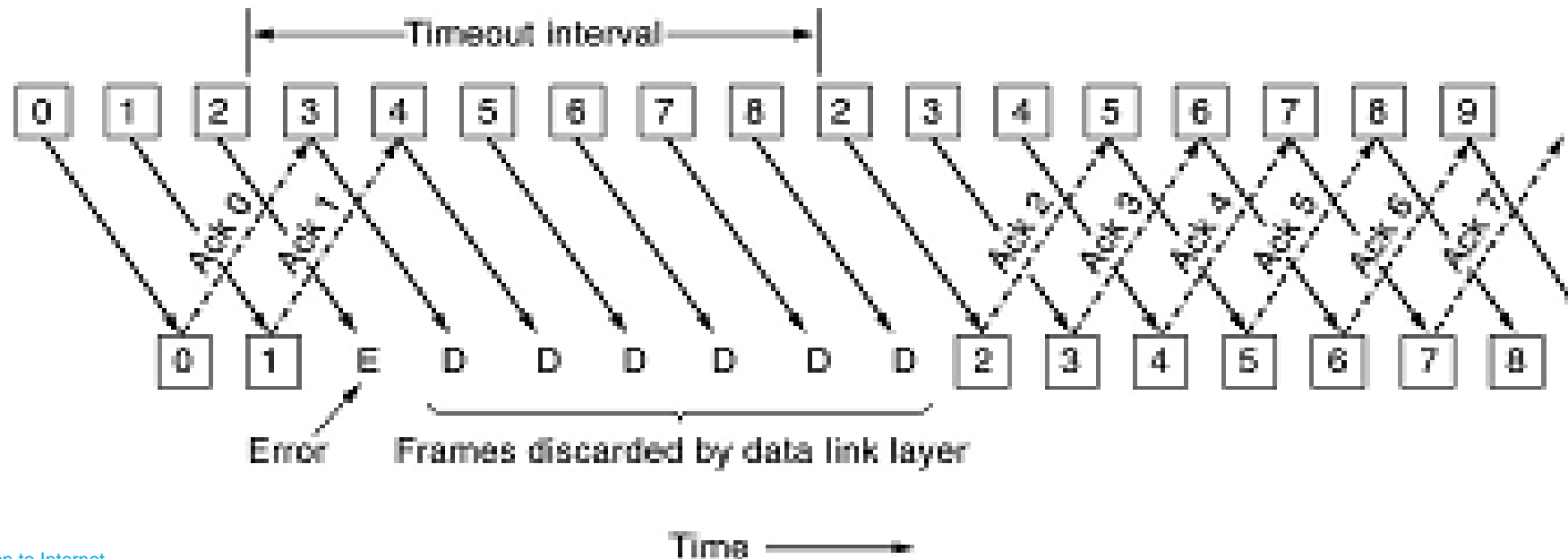


$V(S)$  = send sequence variable  
 $V(R)$  = receive sequence variable



# Go-back-N ARQ (1)

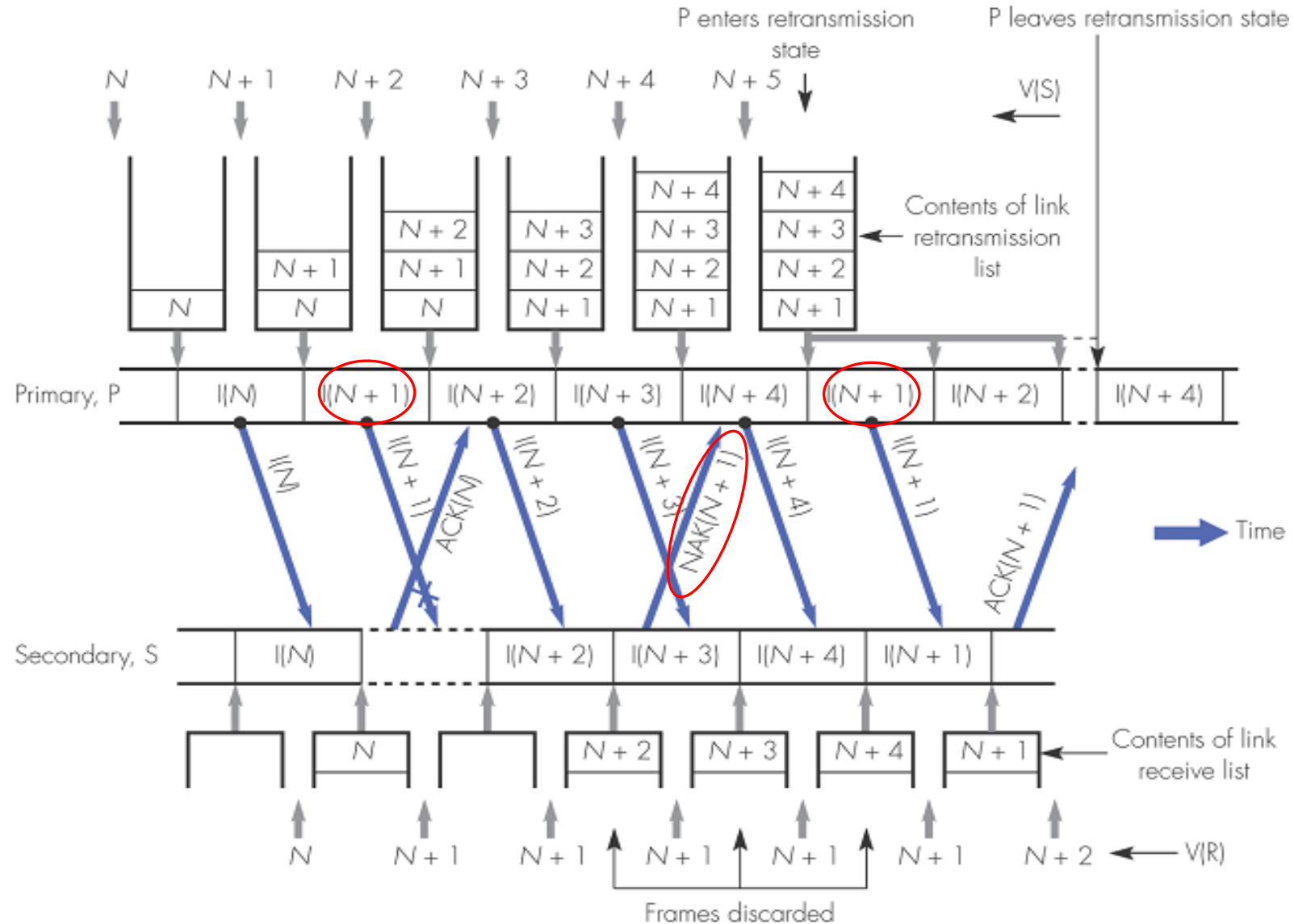
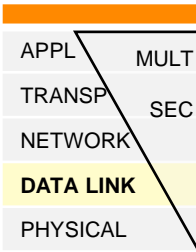
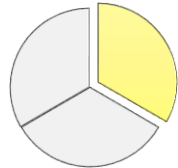
- Receiver discards all frames after an erroneous frame
- Sender resends all discarded frames
  - Sender has to buffer unacknowledged frames



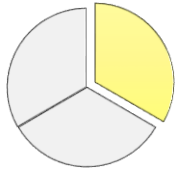


# Go-back-N ARQ (2)

Corrupted I frame:



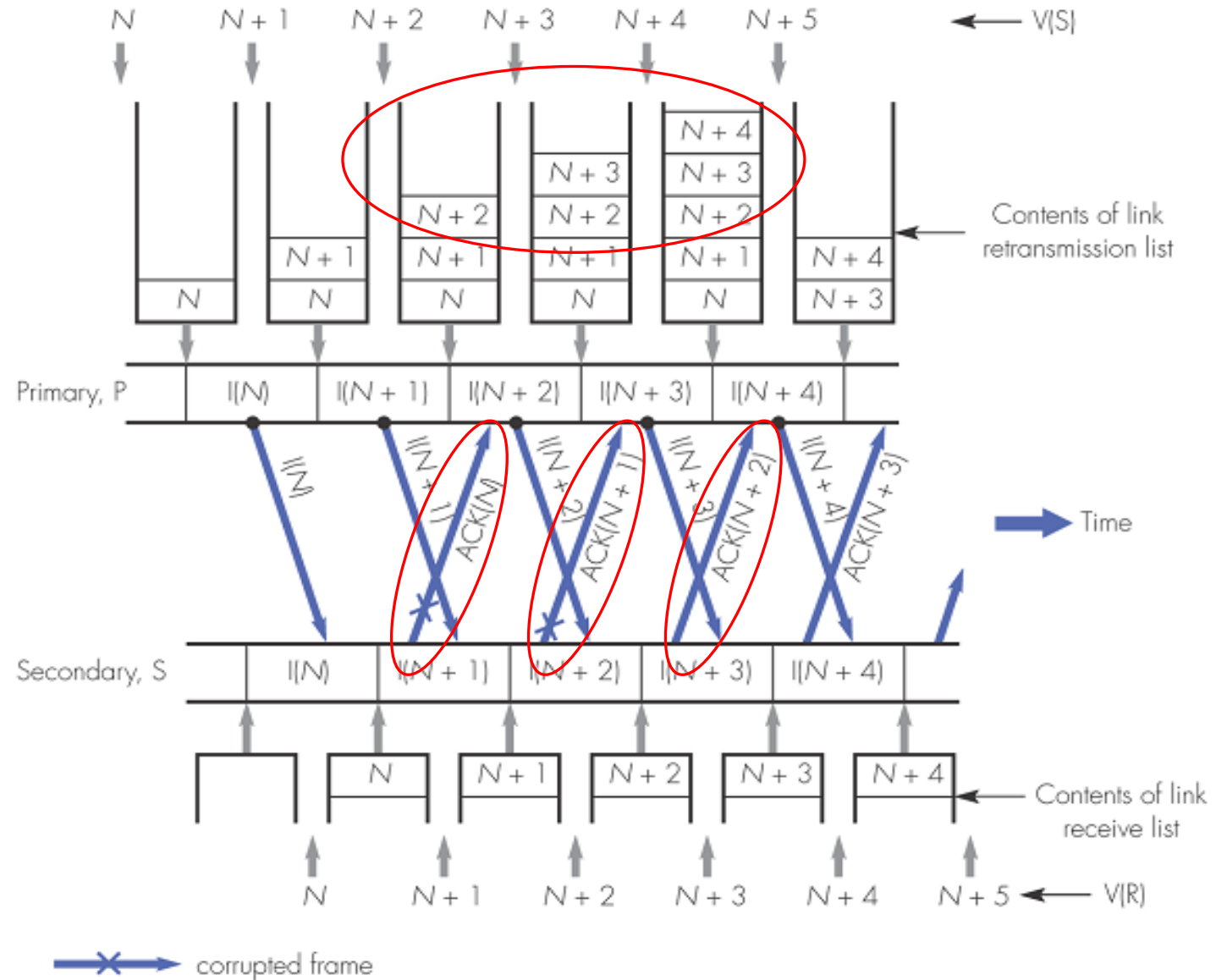


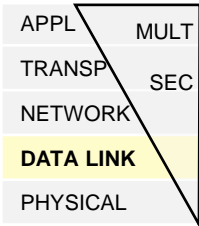


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# Go-back-N ARQ (3)

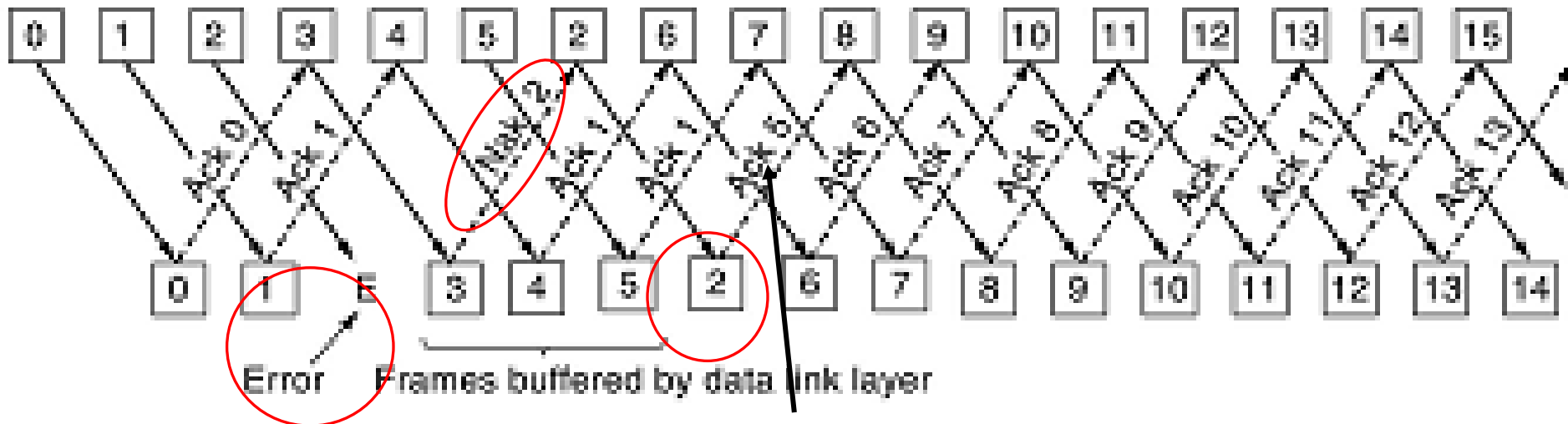
Corrupted ACK frame:

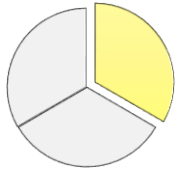




# Selective repeat ARQ (1)

- **Receiver buffers frames received after an erroneous frame**
- **Sender retransmits only the erroneous frame**
  - Sender has to buffer unacknowledged frames

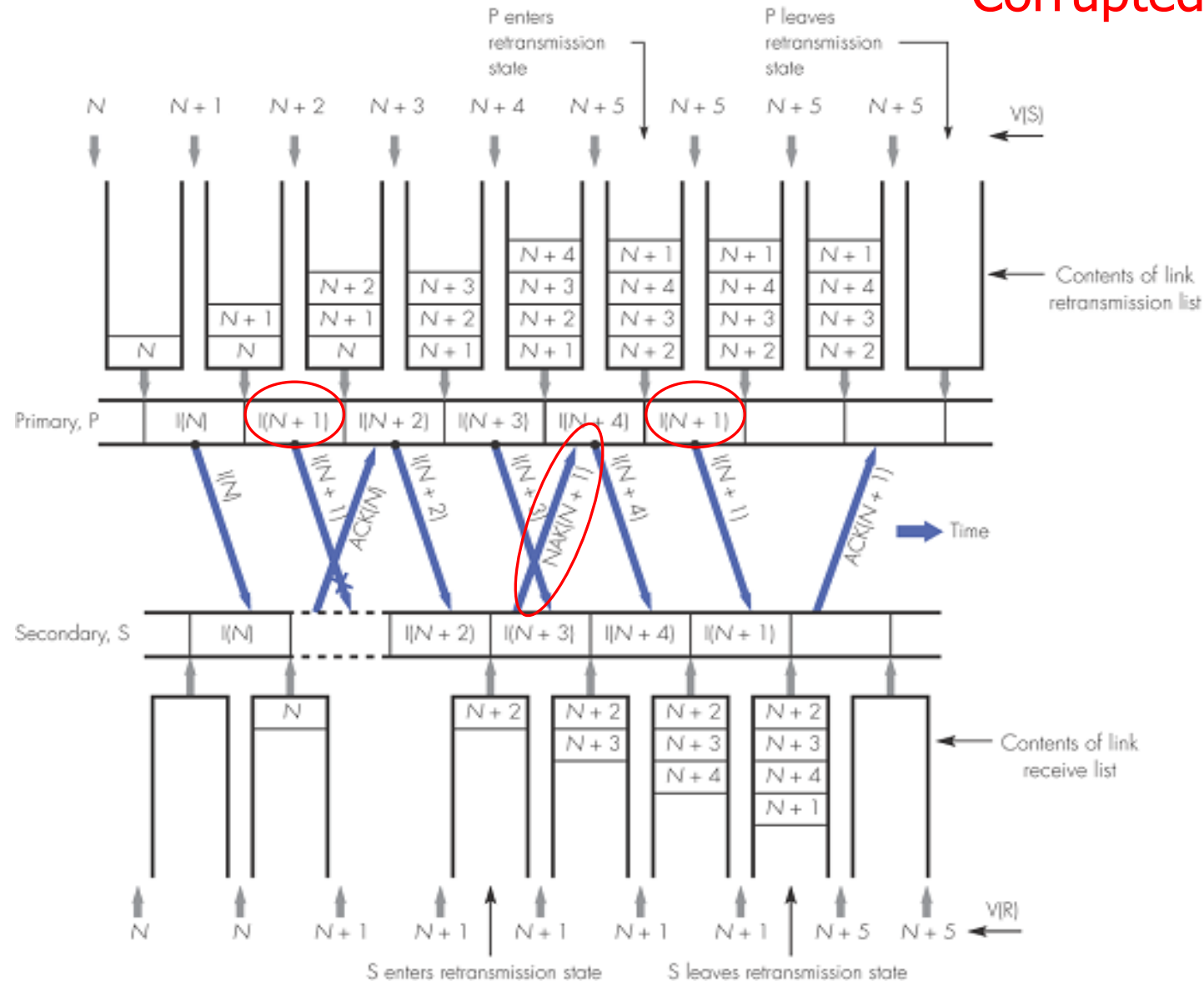


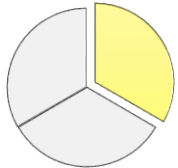


APPL	MULT
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PHYSICAL	

# Selective repeat ARQ (2)

Corrupted I frame:

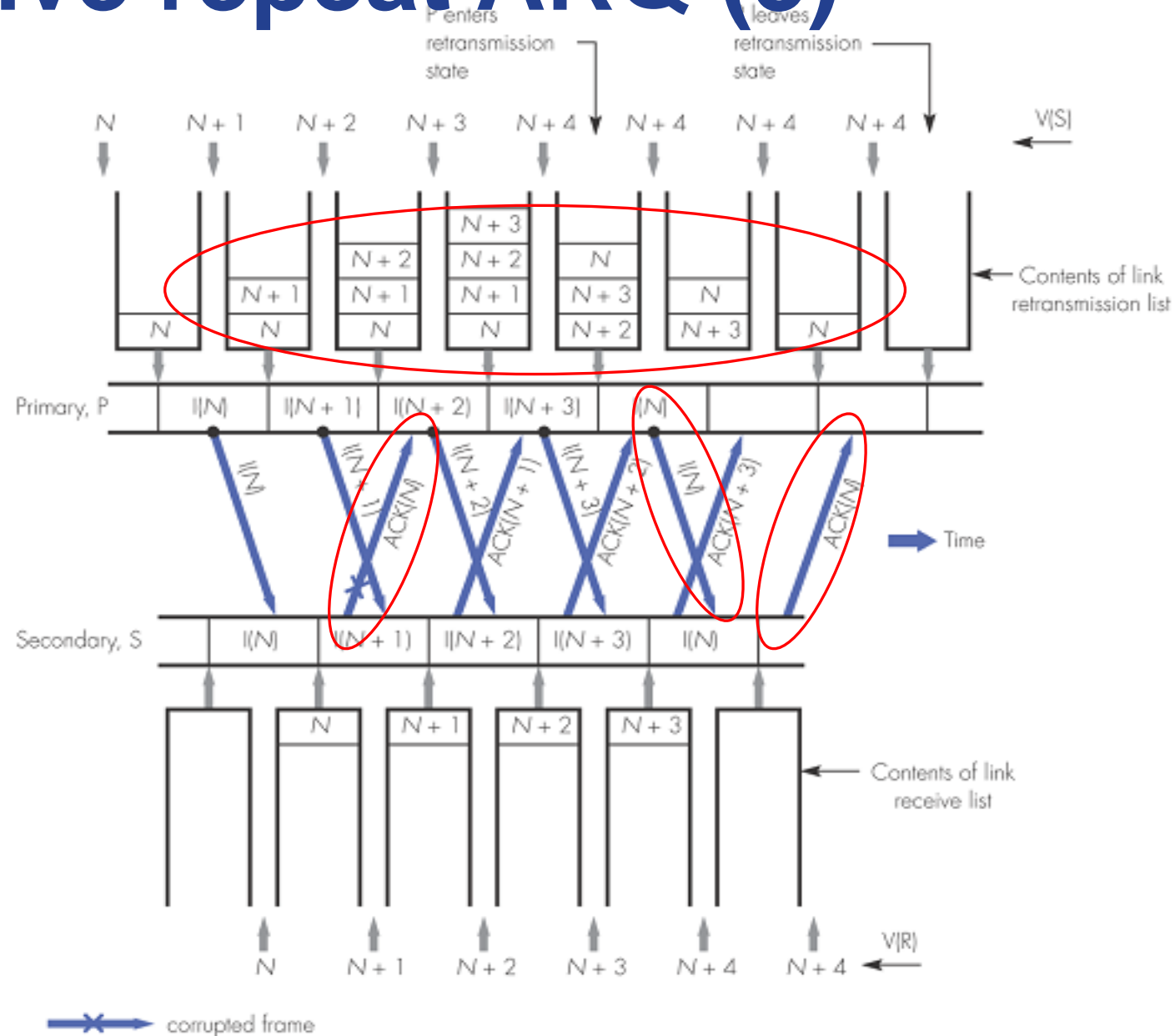


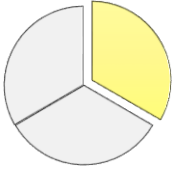


APPL	MULT
TRANSP	SEC
NETWORK	
DATA LINK	
PHYSICAL	

# Selective repeat ARQ (3)

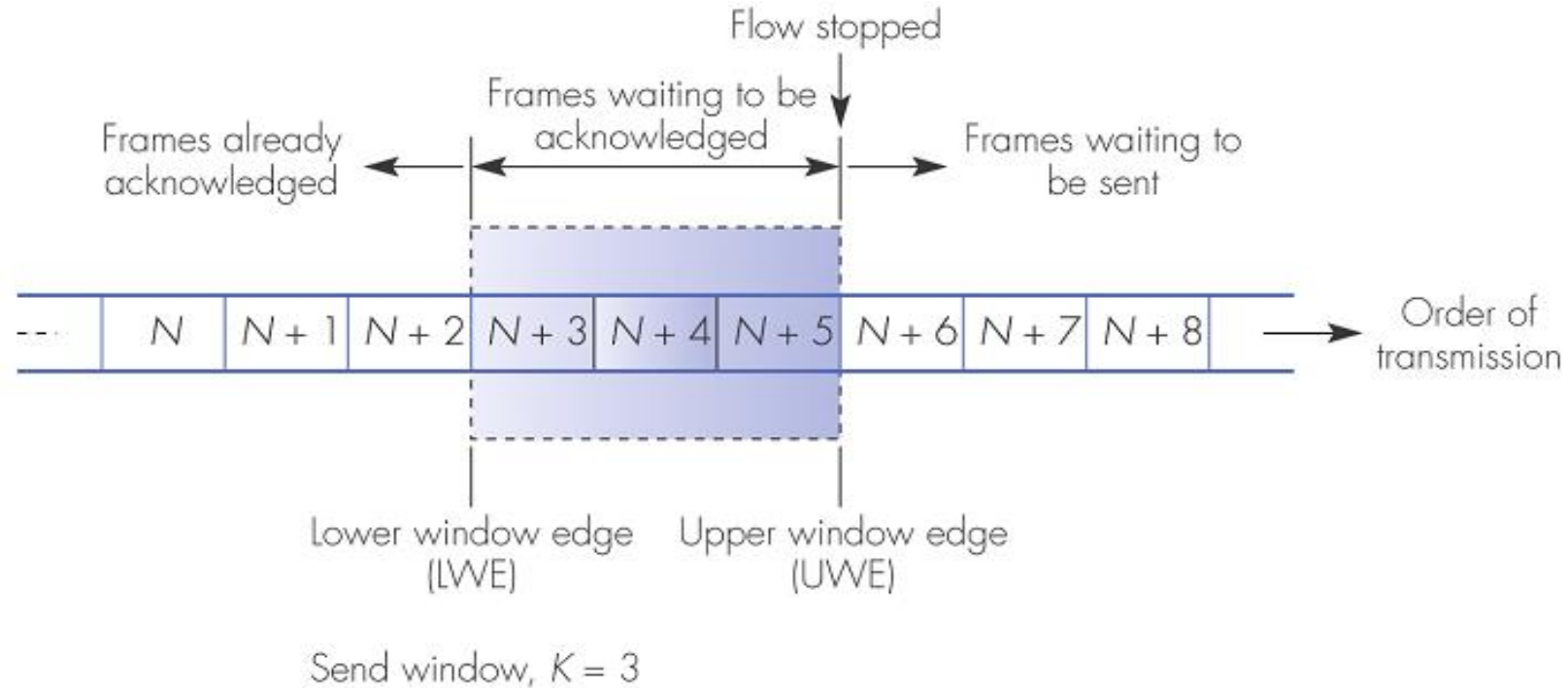
Corrupted ACK frame:



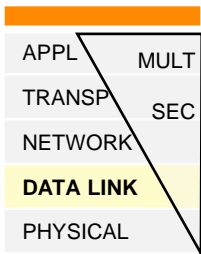
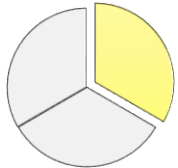


APPL	MULT
TRANSP	SEC
NETWORK	
DATA LINK	
PHYSICAL	

# ARQ: Send/receive window sizes



Protocol	Send window	Receive window
Idle RQ	1	1
Selective repeat	$K$	$K$
Go-back-N	$K$	1



# ARQ: Sequence numbers (frame ID's)

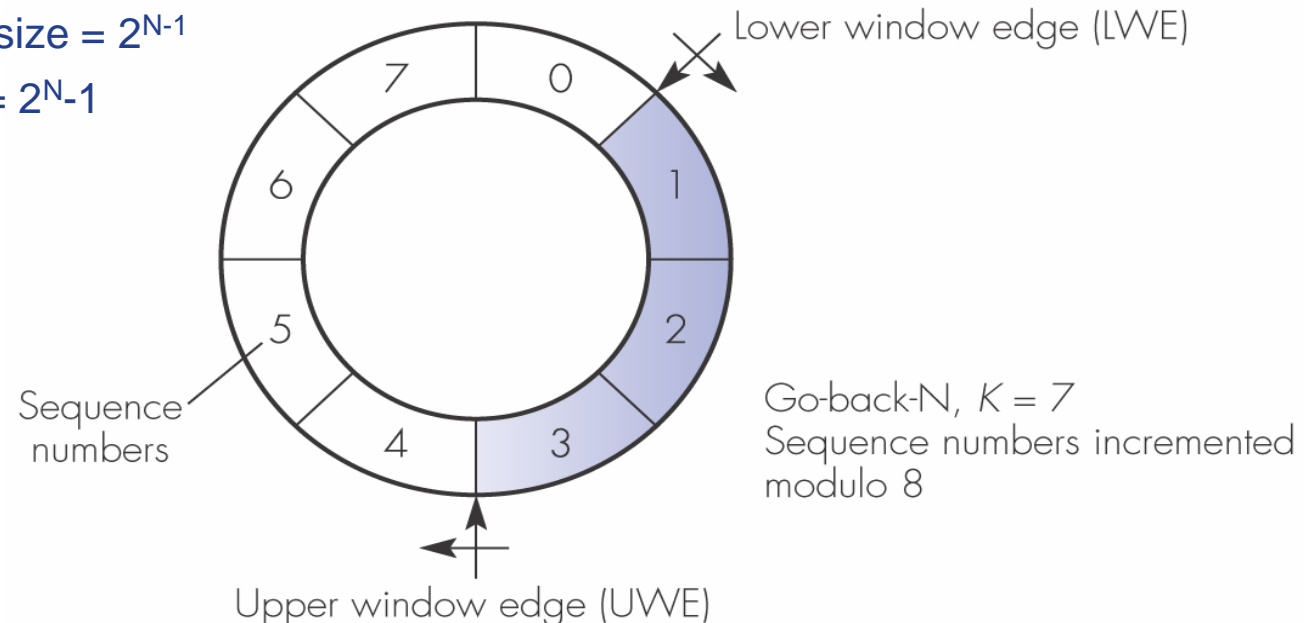
- Number of sequence numbers required for *window size K*

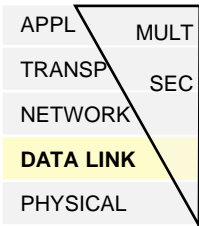
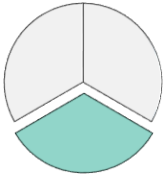
Protocol	Maximum number of frame identifiers
Idle RQ	2
Selective repeat	$2K$
Go-back-N	$K + 1$

- In practice, *N bits* reserved for sequence numbers

- Selective repeat: max window size =  $2^{N-1}$
- Go-back-N: max window size =  $2^{N-1}$

- Example:  
Go-back-N with  
window size  $K=7$   
(need 8 sequence numbers,  
i.e. 3-bit field,  $2^3=8$ )





# Performance: Error-free stop-and-wait flow control

**Link utilization:  $U = 1/(1+2a)$**

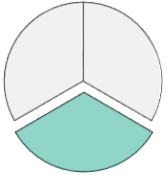
$$a = T_{\text{prop}} / T_{\text{trans}}$$

- $a \sim$  Number of frames in link of bit length  $B$ , when frame length is  $L$
- $a \sim$  Ratio between propagation delay and transmission delay

$$a = (d/V)/(L/R) = [Rd/V] / L$$

$Rd/V$  = length of medium in bits (bit length)

$L$  = length of frame in bits



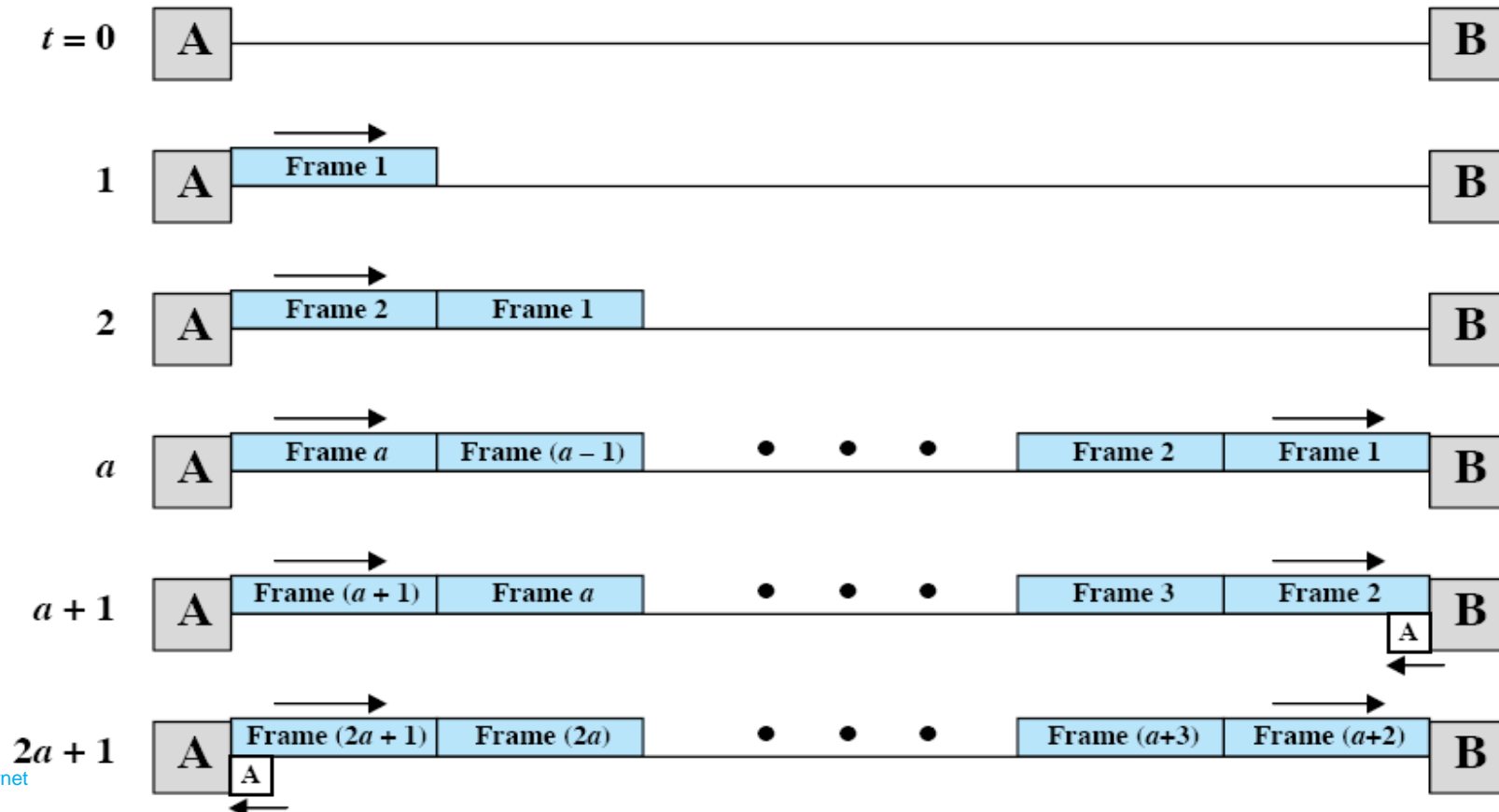
APPL	MULT
TRANSP	SEC
NETWORK	
DATA LINK	
PHYSICAL	

# Performance: Error-free sliding window flow control (1)

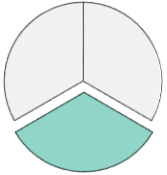
Case 1:  $W$  (window size)  $\geq 2a+1$

ACK reaches A at  $t = 2a+1$

→ A can transmit without pause → utilization = 1







APPL	MULT
TRANSP	SEC
NETWORK	
DATA LINK	
PHYSICAL	

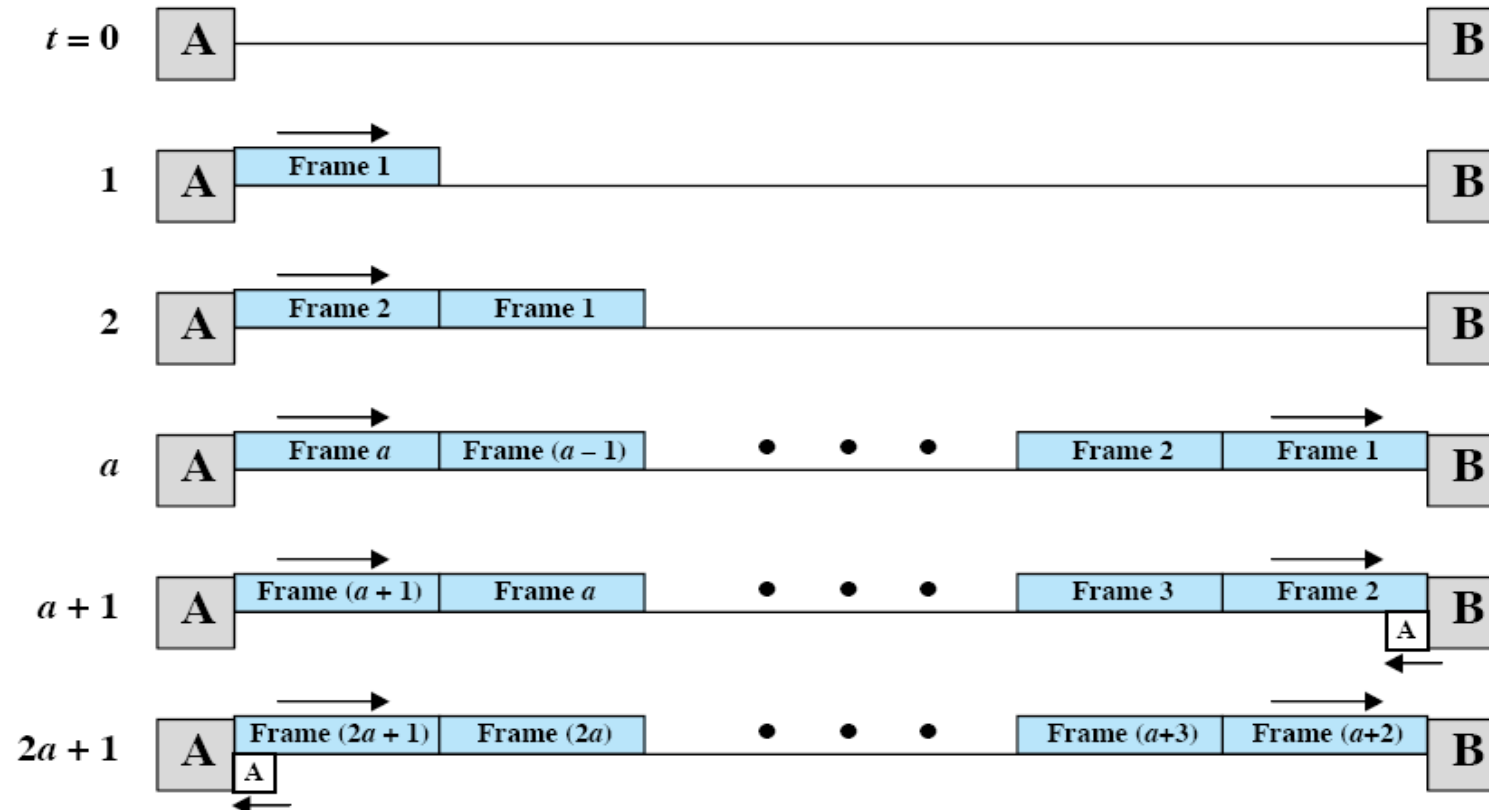
# Performance: Error-free sliding window flow control (2)

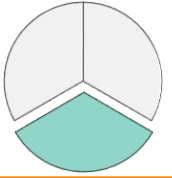
## Case 2: $W$ (window size) $< 2a+1$

A exhausts its send window at  $t = W$  frames

→ A cannot send additional frames until  $t = 2a+1$

→ utilization =  $W/(2a + 1)$



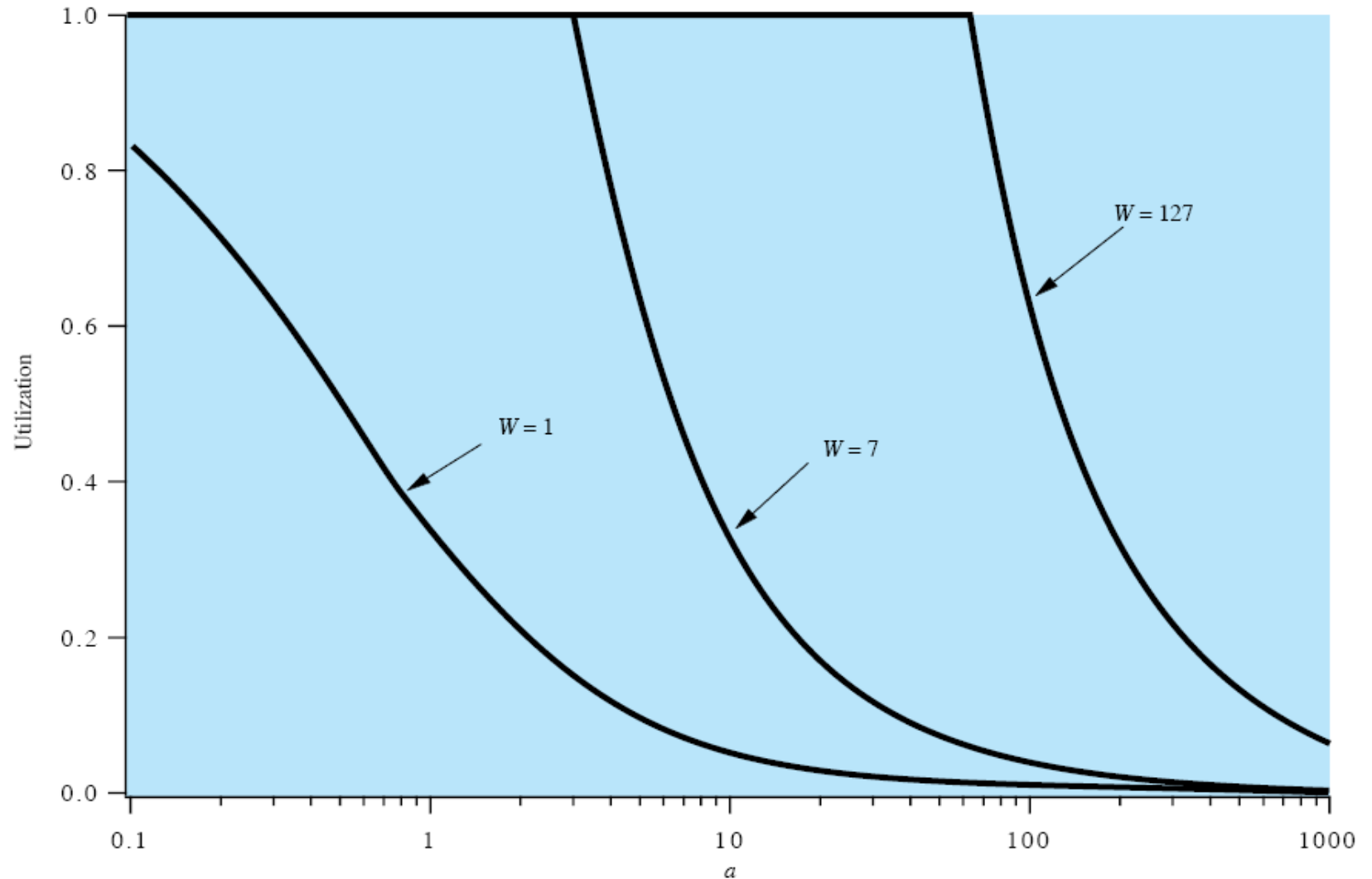


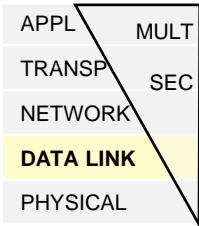
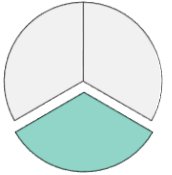
APPL	MULT
TRANSP	SEC
NETWORK	
DATA LINK	
PHYSICAL	

# Performance: Error-free sliding window flow control (3)

**Utilization:**

$$U = \begin{cases} 1 & W \geq 2a + 1 \\ \frac{W}{2a + 1} & W < 2a + 1 \end{cases}$$





# Performance: Stop-and-wait ARQ (1)

- Utilization of error-free transmission:

$$U = \frac{T_f}{T_t} \approx \frac{T_f}{T_f + 2T_p} = \frac{1}{1 + 2a}$$

where  $T_f$  = time for emitting single frame

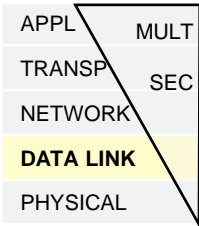
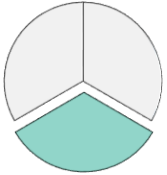
$T_t$  = total time of line being engaged in transmission of single frame

$T_p$  = propagation time

- If errors occur, then utilization

$$U = \frac{T_f}{N_r T_t} = \frac{1}{N_r (1 + 2a)}$$

where  $N_r$  is the expected number of transmissions of a frame



# Performance: Stop-and-wait ARQ (2)

- $N_r$  derived assuming

- A single data frame is in error with probability  $P$
- ACK and NAK are never in error

- **Propability it takes exactly  $k$  attempts to transmit a frame successfully is  $P^{k-1}(1-P)$**

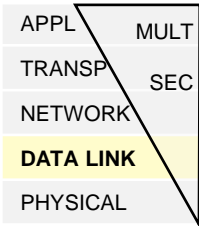
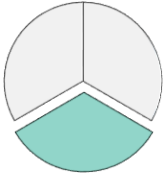
- **Then expected number of transmissions of a frame**

$$N_r = E[\text{transmission}] = \sum_{i=1}^{\infty} (i \times \Pr[i \text{ transmissions}]) = \sum_{i=1}^{\infty} (i P^{i-1} (1 - P)) = \frac{1}{1 - P}$$

Derivation uses equality  $\sum_{i=1}^{\infty} (i X^{i-1}) = \frac{1}{(1 - X)^2}$  for  $(-1 < X < 1)$

- **Hence utilization**

$$U = \left\{ \frac{1 - P}{1 + 2a} \right.$$



# Performance: Selective repeat ARQ

- Utilization without errors was

$$U = \begin{cases} 1 & W \geq 2a + 1 \\ \frac{W}{2a + 1} & W < 2a + 1 \end{cases}$$

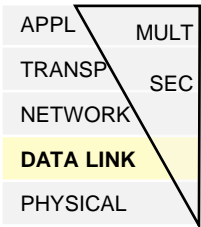
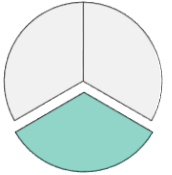
- Again utilization is divided by

$$N_r = \frac{1}{1 - P}$$

- Thus utilization for selective repeat ARQ

$$U = \begin{cases} 1 - P & W \geq 2a + 1 \\ \frac{W(1 - P)}{2a + 1} & W < 2a + 1 \end{cases}$$

- Note:  $W=1 \rightarrow$  reduces to stop-and-wait ARQ utilization



# Performance: Go-back-N ARQ (1)

- Error in single frame generates requirement to retransmit K frames

$$N_r = E[\text{number of transmitted frames to successfully transmit one frame}] = \sum_{i=1}^{\infty} f(i)P^{i-1}(1-P)$$

where  $f(i)$  is the total number of frames transmitted if the original frame must be transmitted  $i$  times:

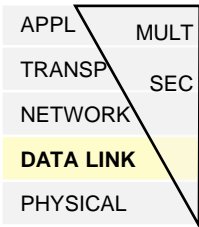
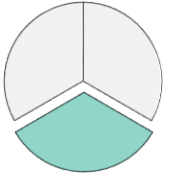
$$f(i) = 1 + (i-1)K = (1-K) + Ki$$

- Substituting yields

$$\begin{aligned} N_r &= (1-K) \sum_{i=1}^{\infty} P^{i-1}(1-P) + K \sum_{i=1}^{\infty} iP^{i-1}(1-P) \\ &= 1-K + \frac{K}{1-P} = \frac{1-P+KP}{1-P} \end{aligned}$$

derivation uses equality

$$\sum_{i=1}^{\infty} X^{i-1} = \frac{1}{1-X} \text{ for } (-1 < X < 1)$$



# Performance: Go-back-N ARQ (2)

- It can be approximated that

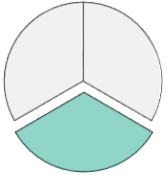
$$K = (2a+1) \text{ for } W \geq (2a+1)$$

$$K = W \quad \text{for } W < (2a+1)$$

- Thus utilization for Go-back-N ARQ

$$U = \begin{cases} \frac{1-P}{1+2aP} & W \geq 2a+1 \\ \frac{W(1-P)}{(2a+1)(1-P+WP)} & W < 2a+1 \end{cases}$$

- Note:  $W=1 \rightarrow$  reduces to stop-and-wait ARQ utilization

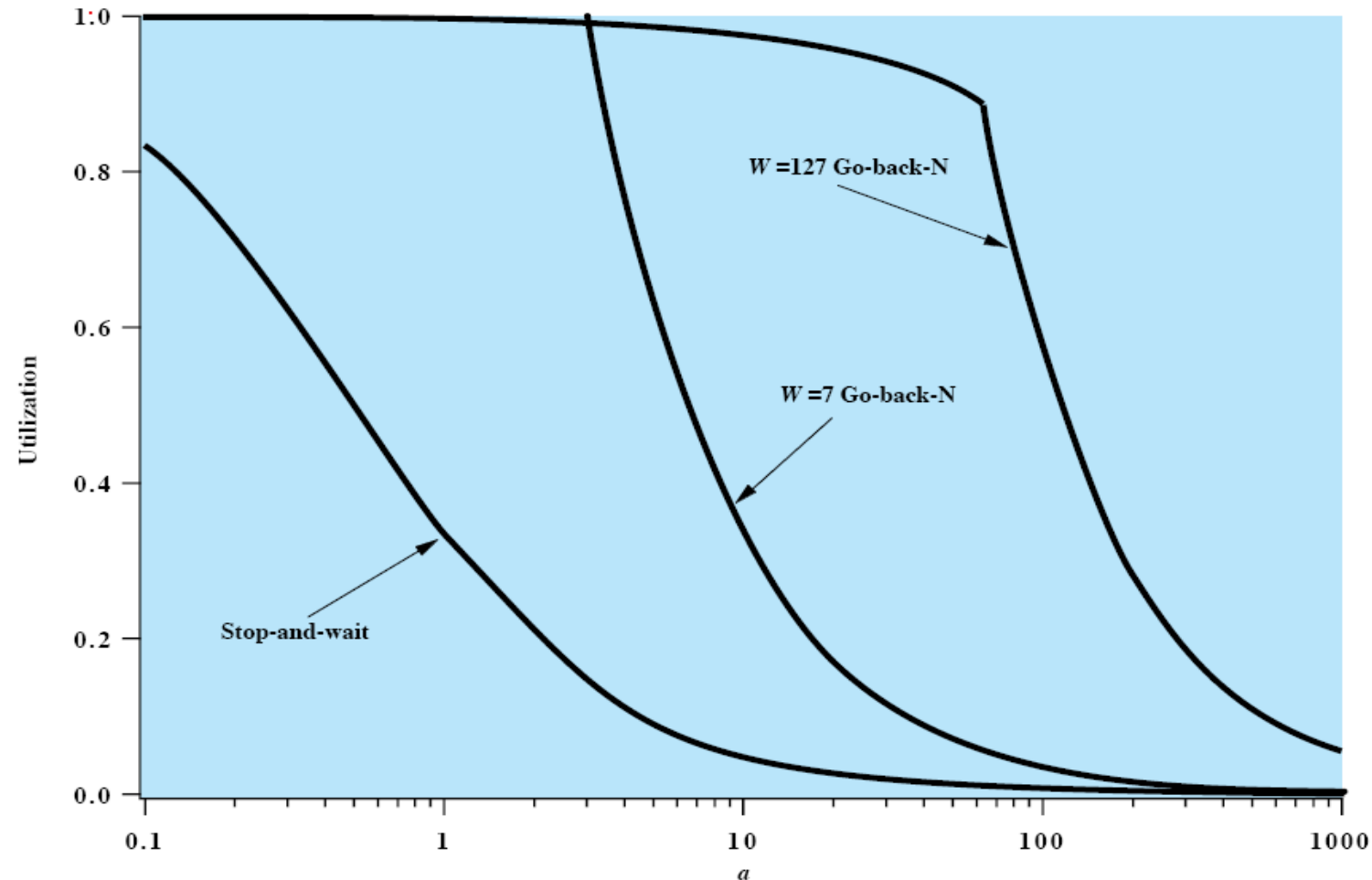


APPL	MULT
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PHYSICAL	

# Performance: ARQ comparison

ARQ utilization as a function of  $a$  ( $P=10^{-3}$ )

Selective repeat ARQ is effectively equal to Go-back-N ARQ







# Key points to remember

1. Main functions of Link Control
2. Flow control and its basic types:
  - Stop&wait
  - Pipelining
  - Sliding window
3. Error control and its basic types:
  - Stop&wait ARQ
  - Go-Back-N ARQ
  - Selective repeat



**Thank you!**