



GRIFFITH COLLEGE DUBLIN
Assignment Cover Sheet

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Lecturer Name: Paddhy Fahy

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Signed: _____

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Question 1

A survey of 350 randomly selected Irish households shows that only 62% have a broadband connection. Infer a 95% confidence interval for the proportion of all Irish households that have broadband connection.

Answer:

Given,

No of people surveyed (N) = 350

62% People with broadband connection (p) = 0.62

38% People without broadband connection (q) = 0.38

Two steps for finding confidence interval

Step 1: Standard Error

$$\begin{aligned} S_{\text{error}} &= \sqrt{pq/n} \\ &= \sqrt{0.62 * 0.38/350} \\ &= \sqrt{0.2356/350} \\ &= 0.0259 \end{aligned}$$

Hence Standard error = 0.0259

Step 2: Confidence Interval at 95%

$$\begin{aligned} &= p \pm (\text{Standard Error} * 1.96) \\ &= 0.62 \pm (0.0259 * 1.96) \\ &= 0.62 \pm 0.05076 \\ &= 62\% \pm 5.08\% \end{aligned}$$

Question 2

At a vehicle testing centre, 30 out of 200 randomly selected vehicles are found to have defective tyres. Infer a 95% confidence interval for the proportion of all vehicles presenting for testing that have defective tyres.

Answer:

30 out of 200 randomly selected vehicles are found to have defective tyres

i.e. $30/200 * 100$

$$= 15\%$$

So 85% are not found with defective tyres

$$N = 200$$

$$p = 15\% \quad (0.15)$$

$$q = 85\% \quad (0.85)$$

Two steps for finding confidence interval

Step 1: Standard Error

$$S_{\text{error}} = \sqrt{pq/n}$$

error

$$= \sqrt{0.15 * 0.85/200}$$

$$= 0.025$$

Hence Standard error = 0.025

Step 2: Confidence Interval at 95%

$$= p \pm (\text{Standard Error} * 1.96)$$

1.96 in this case as $0.95/2 = 0.4750$ i.e. 1.96 from the normal distribution table

$$= 0.15 \pm (0.025 * 1.96)$$

$$= 0.15 \pm 0.049$$

$$= 15\% \pm 4.9\%$$

Question 3

A survey of mortgage holders at the current time shows that 14% are in arrears with their mortgage repayments. Out of the 300 people surveyed, 48% report that they are currently able to manage, while some in the sample also report that although they are not in arrears, they fear for the future. Infer a 99% confidence interval for the proportion of all mortgage holders who are currently in arrears with their mortgage repayments.

Answer:

We need to infer 99% confidence interval for the proportion of all mortgage holders who are currently in arrears with mortgage repayment. According to question 14% are in arrears with mortgage repayments.

14% are in arrears (p) = 0.14

86% are not in arrears currently (q) = 0.86

No of people surveyed (N) = 300

Two steps for finding confidence interval

Step 1: Standard Error

$$\begin{aligned} S_{\text{error}} &= \sqrt{pq/n} \\ &= \sqrt{0.14 * 0.86/300} \\ &= 0.020 \end{aligned}$$

Hence Standard error = 0.020

Step 2: Confidence Interval at 99%

$$\begin{aligned} &= p \pm (\text{Standard Error} * 2.58) \\ &\quad 2.58 \text{ in this case as } 0.99/2 = 0.495 \text{ i.e. 2.58 from the normal distribution table} \\ &= 0.14 \pm (0.02 * 2.58) \\ &= 0.14 \pm 0.516 \\ &= 14\% \pm 5.16\% \end{aligned}$$

Question 4

In a low-temperature performance test (CCA test) of 190 vehicle batteries, an average current reading of 160A is observed, with a standard deviation of 14A. Infer a 95% confidence interval for the current output of a battery selected at random.

Answer:

Total no batteries tested (N) = 190
 Average Current Reading (Mean) = 160A
 Standard Deviation (S) = 14A

Two steps for confidence interval

Step 1: Standard Error

$$\begin{aligned}\text{Standard Error} &= S/\sqrt{N} \\ &= 14/\sqrt{190} \\ &= 1.0159\text{A}\end{aligned}$$

Step 2: Confidence Interval @ 95%

$$\begin{aligned}&= \text{Mean} \pm (\text{Standard Error} * 1.96) \\ &\text{1.96 in this case as } 0.95/2 = 0.4750 \text{ i.e. 1.96 from the normal distribution table}\end{aligned}$$

$$\begin{aligned}&= 160 \pm (1.0159 * 1.96) \\ &= 160 \pm 1.99\end{aligned}$$

Question 5

A television programme is watched by 35% of a representative test audience consisting of 350 people. Infer a 95% confidence interval for the proportion of all viewers who watched the programme.

Answer:

Total No of audience (N) = 350
 35 % watch the programme (p) = 0.35
 65% don't watch the programme (q) = 0.65

Two steps for finding confidence interval

Step 1: Standard Error

$$\begin{aligned} S_{\text{error}} &= \sqrt{pq/n} \\ &= \sqrt{0.35 * 0.65/350} \\ &= 0.0254 \end{aligned}$$

Hence Standard error = 0.0254

Step 2: Confidence Interval at 95%

$$\begin{aligned} &= p \pm (\text{Standard Error} * 1.96) \\ &1.96 \text{ in this case as } 0.95/2 = 0.4750 \text{ i.e. } 1.96 \text{ from the normal distribution table} \\ &= 0.35 \pm (0.0254 * 1.96) \\ &= 0.35 \pm 0.0499 \\ &= 35\% \pm 5\% \end{aligned}$$