

# Leveraging multi-harvest data for simultaneously selecting high-yield and witches' broom-resistant *Theobroma grandiflorum* hybrids

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## Required packages

```
require(asreml)
require(tidyverse)
require(patchwork)
```

## Loading the data

```
data = read.csv("data.csv", header = T, sep=';')
```

## Setting the factors

```
data = transform(data,  
  Harvests = factor(Harvests),  
  Plots = factor(Plots),  
  Replicates = factor(Replicates),  
  Hybrids = factor(Hybrids))
```

## Linear Mixed Models

### Homoscedastic model for Fruit Yield

```
fy1 = asreml(fixed = yd ~ Harvests + Replicates:Harvests,  
  random = ~ Hybrids + Hybrids:Harvests + Plots,  
  data = data)  
  
sum.fy1 = summary(fy1)$varcomp[,1:2]  
  
sum.fy1$CI = sum.fy1$std.error * 1.96  
  
aic.fy1 = summary(fy1)$aic  
  
predfy1_vcov = predict(fy1, classify = "Hybrids", vcov = T)  
predfy1_sed = predict(fy1, classify = "Hybrids", sed = T)  
  
PEV = mean(diag(predfy1_vcov$vcov))  
MVdelta = mean((predfy1_sed$sed^2)[upper.tri(predfy1_sed$sed^2, diag = F)])  
  
acc1 = sqrt(1-(PEV/sum.fy1[1,1]))  
her1 = 1-(MVdelta/(2*sum.fy1[1,1]))
```

	Value	Std. Error	Conf. Int.
$\sigma_g^2$	14.45	5.56	10.90
$\sigma_p^2$	35.08	4.24	8.31
$\sigma_{gh}^2$	12.02	1.99	3.90
$\sigma_e^2$	71.08	2.47	4.84
$r$	0.82	NA	NA
$H_g^2$	0.68	NA	NA

### Heteroscedastic model for Fruit Yield

```

fy2 = asreml(fixed = yd ~ Harvests + Replicates:Harvests,
             random = ~ Hybrids + Hybrids:Harvests + Plots,
             residual = ~dsum(~id(units)|Harvests),
             data = data)

sum.fy2 = summary(fy2)$varcomp[,1:2]

sum.fy2$CI = sum.fy2$std.error * 1.96

aic.fy2 = summary(fy2)$aic

predfy2_vcov = predict(fy2, classify = "Hybrids", vcov = T)
predfy2_sed = predict(fy2, classify = "Hybrids", sed = T)

PEV = mean(diag(predfy2_vcov$vcov))
MVdelta = mean((predfy2_sed$sed^2)[upper.tri(predfy2_sed$sed^2, diag = F)])

acc2 = sqrt(1-(PEV/sum.fy2[1,1]))
her2 = 1-(MVdelta/(2*sum.fy2[1,1]))

# Harvest-wise heritability

her2j = NULL
for(i in 1:nlevels(data$Harvests)){
  predfy2_sed = predict(fy2, classify = "Hybrids:Harvests",
                       level=list(Harvests = i), sed = T)

  MVdelta = mean((predfy2_sed$sed^2)[upper.tri(predfy2_sed$sed^2, diag = F)])

  her2j[i] = 1-(MVdelta/(2*sum.fy2[1,1]))
}

blups.fy = coef(fy2)$random[grep("Hybrids", rownames(coef(fy2)$random))]

```

	Value	Std. Error	Conf. Int.
$\sigma_g^2$	13.88	4.93	9.67
$\sigma_p^2$	26.62	3.23	6.33
$\sigma_{gh}^2$	7.92	1.56	3.05
$\sigma_{e_1}^2$	28.98	3.43	6.72
$\sigma_{e_2}^2$	28.41	3.36	6.59
$\sigma_{e_3}^2$	40.46	4.43	8.69
$\sigma_{e_4}^2$	49.32	5.27	10.33
$\sigma_{e_5}^2$	72.59	7.46	14.62
$\sigma_{e_6}^2$	98.50	10.09	19.79
$\sigma_{e_7}^2$	167.26	16.52	32.38
$\sigma_{e_8}^2$	101.13	10.43	20.44
$\sigma_{e_9}^2$	100.17	10.05	19.69
$r$	0.85	0.85	0.85
$H_{g_1}^2$	0.57	0.57	0.57
$H_{g_2}^2$	0.57	0.57	0.57
$H_{g_3}^2$	0.52	0.52	0.52
$H_{g_4}^2$	0.49	0.49	0.49
$H_{g_5}^2$	0.43	0.43	0.43
$H_{g_6}^2$	0.39	0.39	0.39
$H_{g_7}^2$	0.31	0.31	0.31
$H_{g_8}^2$	0.38	0.38	0.38
$H_{g_9}^2$	0.38	0.38	0.38

### Coefficients of determination

```

sig2f = NULL
cgh = NULL
cp = NULL
ce = NULL

for (i in 1:nlevels(data$Harvests)) {
  sig2f[i] = sum(sum.fy2[1:3,1]) + sum.fy2[i+3,1]
  cgh[i] = sum.fy2["Hybrids:Harvests", "component"] / sig2f[i]
  cp[i] = sum.fy2["Plots", "component"] / sig2f[i]
  ce[i] = sum.fy2[i+3,1] / sig2f[i]
}

coef.det = data.frame(
  "Harvests" = levels(data$Harvests),
  "sig2f" = sig2f,
  "chg" = cgh,
  "cp" = cp,

```

```
"ce" = ce
)
```

Harvests	$\sigma_f^2$	$c_{gh}^2$	$c_p^2$	$c_e^2$
Yr1	77.40	0.10	0.34	0.37
Yr2	76.83	0.10	0.35	0.37
Yr3	88.88	0.09	0.30	0.46
Yr4	97.74	0.08	0.27	0.50
Yr5	121.01	0.07	0.22	0.60
Yr6	146.92	0.05	0.18	0.67
Yr7	215.68	0.04	0.12	0.78
Yr8	149.56	0.05	0.18	0.68
Yr9	148.59	0.05	0.18	0.67

## Generalized linear mixed model for witches' broom resistance

```
wb = asreml(fixed = wb ~ Harvests + Replicates:Harvests,
            random = ~ Hybrids + Hybrids:Harvests + Plots,
            family=asr_binomial(link="logit"),
            data = data, maxit = 100)

sum.wb = summary(wb)$varcomp[,1:2]

sum.wb$CI = sum.wb$std.error * 1.96

predwb = predict(wb, classify = "Hybrids", sed = T)

MVdelta = mean((predwb$sed^2)[upper.tri(predwb$sed^2, diag = F)])

herwb = 1-(MVdelta/(2*sum.wb[1,1]))

blups.wb = coef(wb)$random[1:nlevels(data$Hybrids)]
```

## Optimum number of harvests

```
rho_fy = NULL
for (i in 1:nlevels(data$Harvests)) {
  rho_fy[i] = sum(sum.fy2["Hybrids", "component"], sum.fy2["Plots", "component"])/
  sig2f[i]
}

rho_fy = mean(rho_fy) #Fruit yield repeatability
```

```

rho_wb = sum(sum.wb["Hybrids", "component"], sum.wb["Plots", "component"])/
  sum(c(sum.wb[1:3,1], 3.29)) #WB resistance repeatability

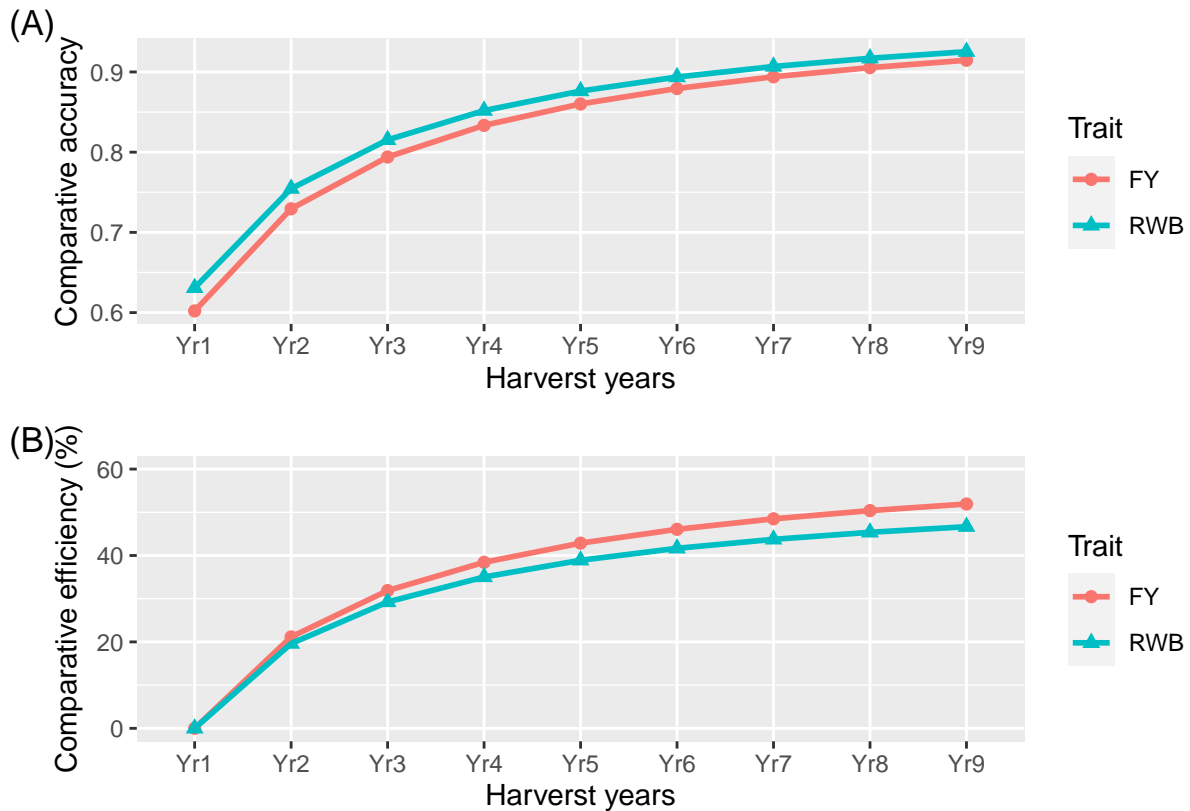
effh_fy = NULL
acch_fy = NULL
effh_wb = NULL
acch_wb = NULL
for (i in 1:nlevels(data$Harvests)) {
  effh_fy[i] = sqrt(i/(1+(i-1)*rho_fy))
  effh_wb[i] = sqrt(i/(1+(i-1)*rho_wb))
  acch_fy[i] = sqrt((i*rho_fy)/(i*rho_fy+1-rho_fy))
  acch_wb[i] = sqrt((i*rho_wb)/(i*rho_wb+1-rho_wb))
}

a = data.frame(
  "Harvests" = rep(levels(data$Harvests), 2),
  "Trait" = rep(c("FY", "RWB"), each = nlevels(data$Harvests)),
  "Accuracy" = c(acch_fy, acch_wb)
) %>% ggplot()+
  geom_point(aes(x = Harvests, y = Accuracy, color = Trait, shape = Trait),
    size=2)+
  geom_line(aes(x = Harvests, y = Accuracy, color = Trait, group = Trait),
    size=1)+
  labs(y = "Comparative accuracy", x = "Harvest years", tag = "(A)")

b = data.frame(
  "Harvests" = rep(levels(data$Harvests), 2),
  "Trait" = rep(c("FY", "RWB"), each = nlevels(data$Harvests)),
  "Efficiency" = c((effh_fy-1)*100, (effh_wb-1)*100)
) %>% ggplot()+
  geom_point(aes(x = Harvests, y = Efficiency, color = Trait, shape = Trait),
    size=2)+
  geom_line(aes(x = Harvests, y = Efficiency, color = Trait, group = Trait),
    size=1)+ ylim(0, 60)+
  labs(y = "Comparative efficiency (%)", x = "Harvest years", tag = "(B)")

a/b

```



## Selection index

### Obtaining the yield persistence

```
blups.fy = left_join(data.frame(
  'Hybrids' = rep(levels(data$Hybrids), each = nlevels(data$Harvests)),
  'Harvests' = rep(levels(data$Harvests), nlevels(data$Hybrids)),
  'blup' = blups.fy[(nlevels(data$Hybrids)+1):length(blups.fy)]
), data.frame(
  'Hybrids' = levels(data$Hybrids),
  'blup' = blups.fy[1:nlevels(data$Hybrids)]
), by='Hybrids') %>% mutate(
  BLUP = blup.x + blup.y
) %>% select(Hybrids, Harvests, BLUP)

max.fy = blups.fy %>% group_by(Harvests) %>%
  summarise(max = max(BLUP))

num = NULL
```

```

for (i in levels(data$Hybrids)) {

  dttes = blups.fy %>% filter(Hybrids == i) %>%
    select(Hybrids,Harvests,BLUP)

  num[i] = 1/sum((dttes$BLUP - max.fy$max)^2)

}

den = sum(num)^2

Per.fy = num/den
Per.fy = rownames_to_column(as.data.frame(Per.fy), 'Hybrids')

```

### Additive index

```

blups.fy = blups.fy %>% group_by(Hybrids) %>%
  summarise(BLUP = mean(BLUP))

AI = cbind(Per.fy,blups.fy$BLUP,blups.wb)

colnames(AI)[2:4] = c("PERS.FY", "BLUP.FY", "BLUP.RWB")

AI = AI %>% mutate(
  AI = (BLUP.FY/sqrt(sum.fy2["Hybrids", "component"])) -
    (BLUP.RWB/sqrt(sum.wb["Hybrids", "component"]))
)

```



Hybrids	PERS.FY	BLUP.FY	BLUP.RWB	AI
H125	2.55	6.94	-0.64	2.39
H165	0.51	5.54	-0.68	2.05
H143	0.09	1.72	-1.17	1.43
H117	0.26	4.50	-0.09	1.28
H137	0.04	-0.76	-1.73	1.23
H140	0.26	4.48	0.05	1.16
H167	0.08	1.68	-0.85	1.15
H124	0.05	-0.37	-1.30	0.98
H129	0.11	2.55	-0.17	0.83
H127	0.08	1.43	-0.43	0.74
H149	0.05	-0.19	-0.89	0.69
H135	0.04	-1.60	-1.31	0.65
H157	0.04	-0.50	-0.89	0.60
H131	0.05	-0.05	-0.50	0.40
H166	0.04	-0.71	-0.65	0.35
H118	0.03	-2.09	-0.94	0.22
H130	0.06	0.39	-0.08	0.17
H132	0.03	-2.18	-0.65	-0.05
H162	0.15	3.46	1.46	-0.28
H169	0.28	4.57	1.86	-0.32
H120	0.12	2.53	1.23	-0.34
H134	0.03	-3.36	-0.65	-0.36
H133	0.03	-3.39	-0.52	-0.48
H136	0.02	-4.03	-0.68	-0.51
H144	0.08	1.39	1.10	-0.54
H163	0.08	1.44	1.38	-0.76
H138	0.05	-0.33	1.10	-1.00
H152	0.04	-1.71	0.91	-1.21
H150	0.04	-1.16	1.30	-1.39
H121	0.04	-1.60	1.29	-1.50
H161	0.06	0.40	1.96	-1.51
H128	0.02	-6.38	-0.20	-1.54
H123	0.01	-7.96	-0.07	-2.08
H126	0.02	-4.67	1.45	-2.46