### Growth Mechanisms Analysis

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#### 1 Growth Mechanisms Analysis

This analysis examines how firm growth moderates the remote work productivity effect. Define:

- $var3 = Remote_i \times Post_t$
- $var4 = Post_t \times Startup_i$
- $var5 = Remote_i \times Post_t \times Startup_i$

We estimate three specifications:

Baseline: The standard remote work effect without growth interactions:

$$y_{it} = \beta_1 \text{var} 3_{it} + \beta_2 \text{var} 4_{it} + \beta_3 \text{var} 5_{it} + \alpha_{i,j} + \delta_t + \varepsilon_{it}$$
(1)

**Endogenous Growth:** Adds controls for high-growth firms (above median growth):

$$y_{it} = \beta_1 \text{var} 3_{it} + \beta_2 \text{var} 4_{it} + \beta_3 \text{var} 5_{it}$$

$$+ \beta_4 \text{Post}_t \times \text{HighGrowth}_j + \beta_5 \text{Post}_t \times \text{HighGrowth}_j \times \text{Startup}_i$$

$$+ \alpha_{i,j} + \delta_t + \varepsilon_{it}$$

$$(2)$$

**Exogenous Growth:** Uses growth residualized on industry/MSA trends, rent, and market concentration:

$$Growth_{j} = \pi_{1}IndGrowth_{-j} + \pi_{2}MSAGrowth_{-j} + \pi_{3}Rent_{j} + \pi_{4}HHI_{j} + \nu_{j}$$
(3)

Then adds controls for high residualized growth ( $\hat{\nu}_j > \text{median}$ ) in the same form as endogenous growth.

The analysis compares two fixed effects specifications: (1) worker-firm interacted fixed effects  $(\alpha_{i,j})$  that absorb time-invariant match quality, and (2) separate worker  $(\alpha_i)$  and firm  $(\alpha_j)$  fixed effects that allow estimation of firm-level heterogeneity.

# 2 First-Stage: Growth Residualization

Table 1: First-Stage Regression: Firm Growth Residualization

	Dep Var:
	Firm Growth Rate
Industry growth (leave-one-out)	0.635***
	(0.057)
MSA growth (leave-one-out)	0.314***
	(0.064)
High rent (above median)	0.045***
	(0.005)
High HHI (above median)	0.034***
	(0.004)
Constant	-0.143***
	(0.011)
Observations	3,189
R-squared	0.124

Notes: Growth rate is average post-COVID employment growth.

<sup>\*\*\*</sup> p<0.01, \*\* p<0.05, \* p<0.10

### 3 Worker-Firm Fixed Effects

Table 2: Worker-Firm Fixed Effects

	Dep Var: Total Productivity		
	(1)	(2)	(3)
Panel A: OLS			
Remote $\times$ Post	-1.23** (0.50)	-1.21** (0.50)	-0.64 $(0.52)$
Remote $\times$ Post $\times$ Startup	6.21*** (1.27)	6.24*** (1.29)	3.58*** (1.27)
N	224,708	224,708	214,151
Panel B: IV			
Remote $\times$ Post	-9.26** (4.01)	-3.68 (3.88)	-9.64* (5.02)
Remote $\times$ Post $\times$ Startup	12.45** (5.39)	6.88 $(5.65)$	10.87* (6.46)
N	224,708	224,708	214,151
KP rk Wald F	123.43	134.89	78.08
Endogenous growth Exogenous growth		$\checkmark$	$\checkmark$

Notes: Worker-firm interacted fixed effects with time FE. Raw firm growth is the average post-COVID employment growth rate (above/below median). Residualized growth is predicted by industry/MSA trends, rent, and HHI. Standard errors clustered by user in parentheses. \* p<0.10, \*\*\* p<0.05, \*\*\*\* p<0.01.

## 4 Separate Fixed Effects

Table 3: Separate Fixed Effects

	Dep Var: Total Productivity		
	(1)	(2)	(3)
Panel A: OLS			
Remote $\times$ Post	-1.03** (0.48)	-1.01** (0.48)	-0.50 $(0.51)$
Remote $\times$ Post $\times$ Startup	5.18*** (1.24)		2.51** (1.24)
N	229,862	229,862	218,909
Panel B: IV			
Remote $\times$ Post	-7.15* (3.90)	-2.08 (3.79)	-6.92 (4.80)
Remote $\times$ Post $\times$ Startup	9.94* (5.37)	4.63 (5.67)	7.42 (6.39)
N	229,862	229,862	218,909
KP rk Wald F	140.60	153.28	91.62
Endogenous growth Exogenous growth		✓	$\checkmark$

Notes: Separate user, firm, and time fixed effects. Raw firm growth is the average post-COVID employment growth rate (above/below median). Residualized growth is predicted by industry/MSA trends, rent, and HHI. Standard errors clustered by user in parentheses. \* p<0.10, \*\* p<0.05, \*\*\* p<0.01.