Miles per gallon in different transmission types

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Executive summary of effect of transmission type on miles per gallon of road vehicles

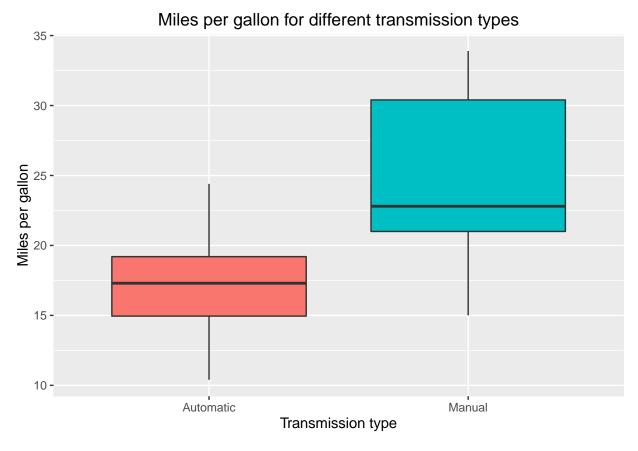
This study will analyze mtcars dataset in an attempt to provide information of automatic and manual transmission types on petrol efficiency measured in miles per gallon. The findings of this study are following:

- According to simple t-test analysis, manual transmission is more efficient by 7.24 miles per galon
- Improved multivariate model lowers this prediction to 2.45 miles per galon due to inclusion of confounding variables

In both cases the manual transmission is better for the miles per galon.

Exploratory data analysis

A boxplot of both transmission types will be produced to visually inspect if there is a difference between the two transmission types.



```
options(scipen = 999)
```

Above graph strongly hints to a better fuel efficiency of manual transmission. T-test will be performed to check if this is the case.

Table 1: t-test of mpg between manual and automatic transmission

| Automatic | Manual | t-statistic | p | CI low | CI high |
|-----------|---------|-------------|--------|----------|---------|
| 17.1474 | 24.3923 | -3.7671 | 0.0014 | -11.2802 | -3.2097 |

P-value of 0.0014 lets us reject the null hypothesis of no difference between transmission types and allows for the claim of difference in the mean MPG between manual and automatic transmission.

Regression analysis

Firstly a simple linear regression of miles per gallon by transmission type is performed

```
model_1 <- lm(mpg~am,data=mtcars)
model_1_ar2 <- summary(model_1)$adj.r.squared
model_1 %>% tidy %>% mutate(term=c('Intercept','Manual')) %>%
kable(digits=4,caption='Linear model between mpg and transmission')
```

Table 2: Linear model between mpg and transmission

| term | estimate | std.error | statistic | p.value |
|---------------------|---------------------|--------------------|---------------------|--------------------|
| Intercept Manual | $17.1474 \\ 7.2449$ | $1.1246 \\ 1.7644$ | $15.2475 \\ 4.1061$ | $0.0000 \\ 0.0003$ |

This simple model is essentially the same as the one in t-test. However with adjusted R^2 of only 0.3385 we explain only 33.85% of variability in mpg by transmission type.

To improve on this model a stepwise regression is run to find a better model, 1/4 mile times and displacement variables are removed as the first one is not a raw predictive variable and second one isi highly correlated with weight

```
mtcarslight <- mtcars %% select(-disp,-qsec)
model_2 <- step(lm(mpg~.,data=mtcarslight),direction='both',trace=0)
model_2_ar2 <- summary(model_2)$adj.r.squared
model_2 %>% tidy %>% mutate(term=c('Intercept','Horsepower','Weight','Engine type','Manual')) %>%
kable(digits=4,caption='Multivariate linear model')
```

Table 3: Multivariate linear model

| term | estimate | std.error | statistic | p.value |
|-------------|----------|-----------|-----------|---------|
| Intercept | 31.0788 | 3.3928 | 9.1603 | 0.0000 |
| Horsepower | -0.0301 | 0.0109 | -2.7508 | 0.0105 |
| Weight | -2.5910 | 0.9174 | -2.8243 | 0.0088 |
| Engine type | 1.7855 | 1.3271 | 1.3454 | 0.1897 |
| Manual | 2.4171 | 1.3794 | 1.7523 | 0.0911 |

anova(model_1,model_2) %>% tidy %>% cbind(model=c('mpg~am','mpg~am+hp+wt+vs'),.) %>% kable(digits=2,cap

Table 4: Analysis of variance between models

| model | res.df | rss | df | sumsq | statistic | p.value |
|--|--------|--------|----|--------|-----------|---------|
| mpg~am | 30 | 720.90 | NA | NA | NA | NA |
| ${\rm mpg}{\sim}{\rm am}{+}{\rm hp}{+}{\rm wt}{+}{\rm vs}$ | 27 | 168.96 | 3 | 551.93 | 29.4 | 0 |

Second model is significantly different from the simple one. It improves adjusted R^2 to 0.8277, increasing explanatory power of the model to 82.77% of variability in mpg. According to this improved model manual transmission type results in 2.42 increase in miles per gallon of the car.

Visual inspection of residual plots in the appendix provides no signs of violation of heteroskedasticity.

It is to be noted that there is significant corelation between horsepower and weight, as well as engine type and also transmission and weight. Those correlations may invalidate the findings of this study, but the author

lacks the skills to further analyze the data.

Appendix

```
par(mfrow=c(2,2))
plot(model_2)
```

