

# ANOVA : One factor ANOVA

$\sum SC \rightarrow$  Sum of Squares b/w the sample  
 $\sum SE \rightarrow$  Sum of Squares w/in the sample.  
 $MSC \rightarrow$  Mean sum of squares  
 $MSE \rightarrow$  Mean sum of sq. within the sample

Source of variation

Source of variation	Sum of sq.	Degree of freedom	Mean sum of sq.	F
B/w the sample	$\sum SC$	$V_1 = c - 1$	$MSC = \frac{\sum SC}{V_1}$	$F = \frac{MSC}{MSE}$
w/in the sample	$\sum SE$	$V_2 = n - c$	$MSE = \frac{\sum SE}{V_2}$	

One factor ANOVA : 2D.  $\rightarrow$

$$\sum SC = \frac{A^2}{N_A} + \frac{B^2}{N_B} + \frac{C^2}{N_C} + \frac{D^2}{N_D} - \frac{T^2}{N}$$

## 2 factors

Correction factor

ex:

Days	A	B	C	D
M	3	4	4	5
T	4	5	8	7
W	6	7	8	9

$$N = 3 \times 4 = 12$$

$$\text{Mid} \Rightarrow$$

$$8.5 = 5$$

f.f. 4, 4, 5, 6, 7, 7, 8, 9

① Variance k/o the lot

	A	B	C	D	Total
M	-2	-1	-1	0	-4
T	-1	0	3	2	4
W	+1	2	3	4	10
Total	-2	1	5	6	10

①

$$\text{correction factor} = \frac{T^2}{N} \Rightarrow$$

$$\frac{(10)^2}{12} \Rightarrow$$

$$\frac{100}{12} = 8.3$$

②

$$SSC \Rightarrow \frac{(-2)^2}{3} + \frac{(+1)^2}{3} + \frac{(5)^2}{3} + \frac{(6)^2}{3} - 8.3 \Rightarrow$$

$$\Rightarrow \frac{4}{3} + \frac{1}{3} + \frac{25}{3} + \frac{36}{3} - 8.3 \Rightarrow 13.7$$

③

$$SSR \Rightarrow \frac{(-4)^2}{4} + \frac{(4)^2}{4} + \frac{(10)^2}{4} - \frac{T^2}{N} \Rightarrow$$

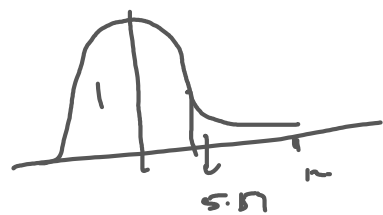
$$\Rightarrow \frac{16}{4} + \frac{16}{4} + \frac{100}{4} - 8.3 \Rightarrow 24.7$$

Source of variation	Sum of Squares	Degrees of freedom	Mean Sum of Squares	F
B/o to explain	SSC 13.7	$V_1 = C - 1 = 3$	$MSC = \frac{SSC}{V_1} = \frac{13.7}{3}$	$\frac{MSC}{MSE} = 4.5$
B/o to var	SSR 24.7	$V_2 = r - 1 = 2$	$MSR = \frac{SSR}{V_2} = \frac{24.7}{2}$	$\frac{MSR}{MSE} = 12.35$
Residual Error	SSE 8.6	$V = (C-1)(r-1) = 6$	$MSE = \frac{SSE}{V} = \frac{8.6}{6}$	
	<u>SST</u> (47)	$V = n - 1$		

$T_{0.05, 3} = 4.76$   
 $C_{0.2} = 5.14$   
 → null hypothesis rejected

$$SSE = SST - (SSC + SSR) \Rightarrow 47 - (38.4) \Rightarrow 8.6$$

$$SST \Rightarrow (-2)^2 + (-1)^2 + (-1)^2 + (0)^2 + (-1)^2 + (0)^2 + (3)^2 + (2)^2 + (1)^2 + 2^2 + 3^2 + 4^2 - \frac{T^2}{N}$$



$$\Rightarrow \underline{4} + \underline{1} + \underline{1} + \underline{0} + \underline{1} + \underline{0} + \underline{9} + \underline{4} + \underline{1} + \underline{4} + \underline{9} + \underline{16} = \underline{47}$$

SST = 47

