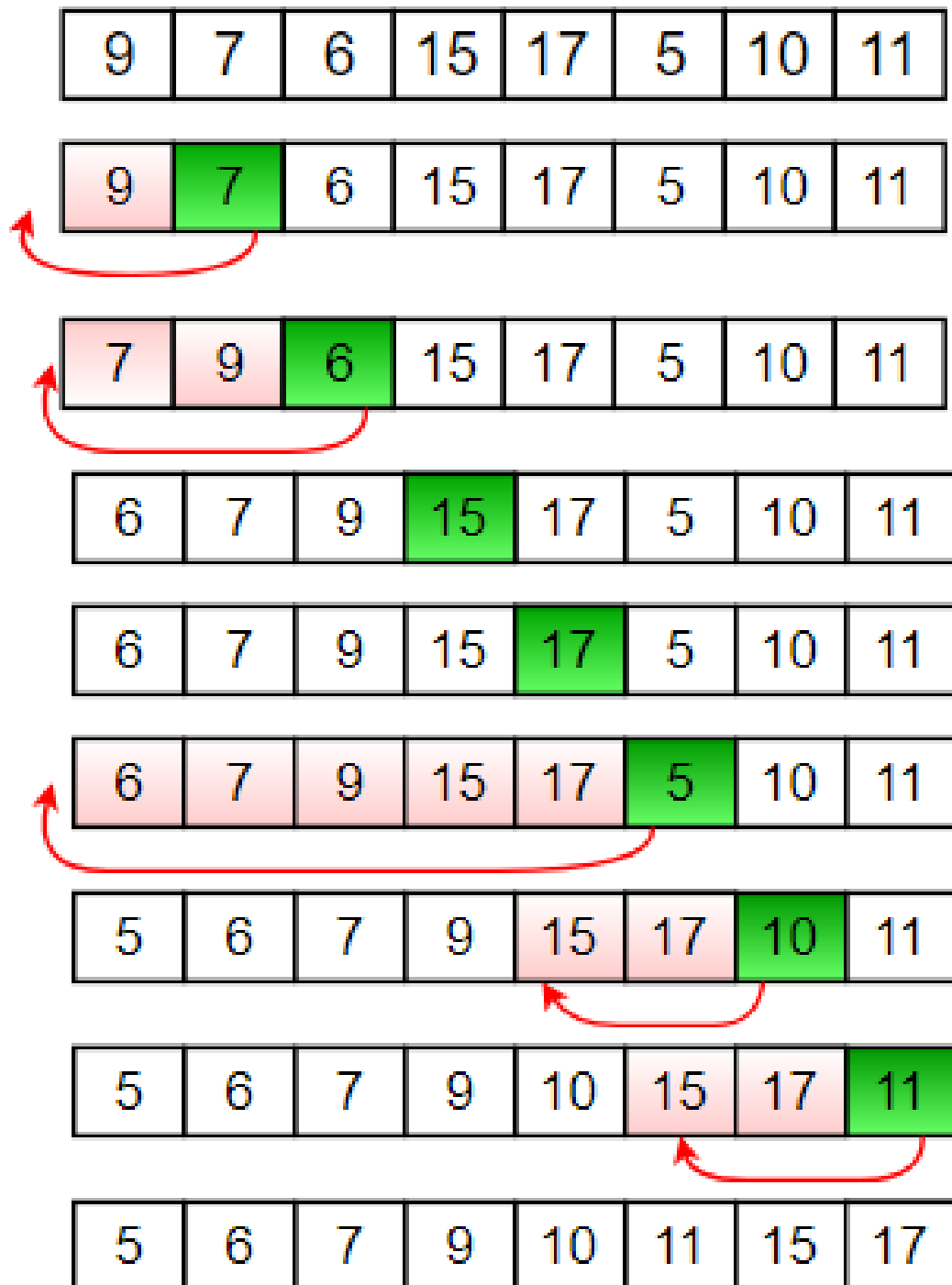


# INSERTION SORT



# INSERTION SORT

INSERTION-SORT( <i>A</i> )		<i>cost</i>	<i>times</i>
1	<b>for</b> <i>j</i> = 2 to <i>A.length</i>	$c_1$	$n$
2	$key = A[j]$	$c_2$	$n - 1$
3	// Insert $A[j]$ into the sorted sequence $A[1 \dots j - 1]$ .	0	$n - 1$
4	$i = j - 1$	$c_4$	$n - 1$
5	<b>while</b> $i > 0$ and $A[i] > key$	$c_5$	$\sum_{j=2}^n t_j$
6	$A[i + 1] = A[i]$	$c_6$	$\sum_{j=2}^n (t_j - 1)$
7	$i = i - 1$	$c_7$	$\sum_{j=2}^n (t_j - 1)$
8	$A[i + 1] = key$	$c_8$	$n - 1$

## Example Recurrences for Algorithms

- Insertion sort

$$T(n) = \begin{cases} 1 & \text{for } n \leq 1 \\ T(n-1) + n & \text{otherwise} \end{cases}$$

- Linear search of a list

$$T(n) = \begin{cases} 1 & \text{for } n \leq 1 \\ T(n-1) + 1 & \text{otherwise} \end{cases}$$

# INSERTION SORT

HOMEWORK

## Common Recurrence Relations

Recurrence Relation	Result	Example
$T(n) = T(n/2) + O(1)$	$T(n) = O(\log n)$	Binary search, Euclid's GCD
$T(n) = T(n-1) + O(1)$	$T(n) = O(n)$	Linear search
$T(n) = 2T(n/2) + O(1)$	$T(n) = O(n)$	
$T(n) = 2T(n/2) + O(n)$	$T(n) = O(n \log n)$	Merge sort (Chapter 24)
$T(n) = 2T(n/2) + O(n \log n)$	$T(n) = O(n \log^2 n)$	
$T(n) = T(n-1) + O(n)$	$T(n) = O(n^2)$	Selection sort, insertion sort
$T(n) = 2T(n-1) + O(1)$	$T(n) = O(2^n)$	Towers of Hanoi
$T(n) = T(n-1) + T(n-2) + O(1)$	$T(n) = O(2^n)$	Recursive Fibonacci algorithm