

## DECISION VARIABLES

1.  $x_{ik}$  : Truck serves customer from warehouse  $i$  to  $k$  (1 if true, 0 if false)
2.  $d_{kj}$  : Drone dispatched from truck at node  $k$  to serve customer  $j$  (1 if true, 0 if false)
3.  $y_{ik}$  : Truck visits node  $k$  when serving customers from warehouse  $i$
4.  $z_{kj}$  : Drone visits node  $k$  when serving customer  $j$
5.  $T_{\text{Truck}_{ik}}$  : Time by truck from  $i$  to  $k$  to serve  $j$
6.  $T_{\text{Drone}_{kj}}$  : Time by drone from  $k$  to serve customer  $j$
7.  $u_{ijk}$  : Binary variable to mark nodes visited by truck between  $i$  and  $k$

## OBJECTIVE FUNCTION

$$\text{Minimize: } Z = \alpha_T \sum_{i,k} x_{ik} \cdot C_{\text{Truck}_{ik}} + \alpha_D \sum_{k,j} d_{kj} \cdot C_{\text{Drone}_{kj}} + \lambda \cdot (T_{\text{Truck}_{ik}} + T_{\text{Drone}_{kj}})$$

## CONSTRAINTS

1.  $\sum_k x_{ik} + \sum_j d_{kj} = 1$  (Serve by truck or drone)
2.  $T_{\text{Truck}_{ik}} = \frac{\text{Dist}_{\text{Truck}_{ik}}}{\text{Speed}_{\text{Truck}}}$  (Truck Time Constraint)
3.  $T_{\text{Drone}_{kj}} = \frac{\text{Dist}_{\text{Drone}_{kj}}}{\text{Speed}_{\text{Drone}}}$  (Drone Time Constraint)
4.  $x_{ik} \geq d_{kj}$  (Drone Dispatch Constraint)
5.  $\sum_j x_{ik} = y_{ik}$  (Mark nodes visited by truck)
6.  $\sum_j d_{kj} = z_{kj}$  (Mark nodes visited by drone)
7.  $u_{ijk} \geq y_{ik} - z_{kj}$  (Mark nodes visited by truck between  $i$  and  $k$ )

### Where:

- $x_{ik}$  is binary, indicating truck serves from warehouse  $i$  to  $k$ .
- $d_{kj}$  is binary, indicating drone dispatched from truck at  $k$  to serve  $j$ .
- $y_{ik}$  is binary, indicating truck visits  $k$  when serving from  $i$ .
- $z_{kj}$  is binary, indicating drone visits  $k$  when serving  $j$ .
- $T_{\text{Truck}_{ik}}$  is time by truck from  $i$  to  $k$  to serve  $j$ .
- $T_{\text{Drone}_{kj}}$  is time by drone from  $k$  to serve  $j$ .
- $C_{\text{Truck}_{ik}}$  is cost for truck serving from  $i$  to  $k$ .
- $C_{\text{Drone}_{kj}}$  is cost for drone serving from  $k$  to  $j$ .
- $\alpha_T$  is unit variable cost for truck.
- $\alpha_D$  is unit variable cost for drone.
- $\lambda$  is weight parameter for time in the objective function.