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ADVANCED MACHINE LEARNING BTAIC602

Unit 1: Unsupervised Learning

SYLLABUS

UNIT NO 1: UNSUPERVISED LEARNING

1. **Unsupervised Learning – 1:** Introduction to Unsupervised Learning, Introduction to Clustering, Using K-means for Flat Clustering, KMeans Algorithm, Using KMeans from Sklearn, Implementing Fit & Predict Functions, Implementing K-Means Class
2. **Unsupervised Learning – 2:** How to choose Optimal K, Silhouette algorithm to choose K, Introduction to K Medoids, K Medoids Algorithm, Introduction to Hierarchical Clustering, Top down/Divisive Approach, Bottom up/Divisive Approach Principal Component Analysis
3. **PCA – 1:** Intuition behind PCA, Applying PCA to 2D data, Applying PCA on 3D data, Math behind, PCA, Finding Optimal Number of Features, Magic behind PCA, Dimensionality reduction
4. **PCA – 2:** PCA on Images, PCA on Olevitti Images, Reproducing Images, Eigenfaces, Classification of LFW Images

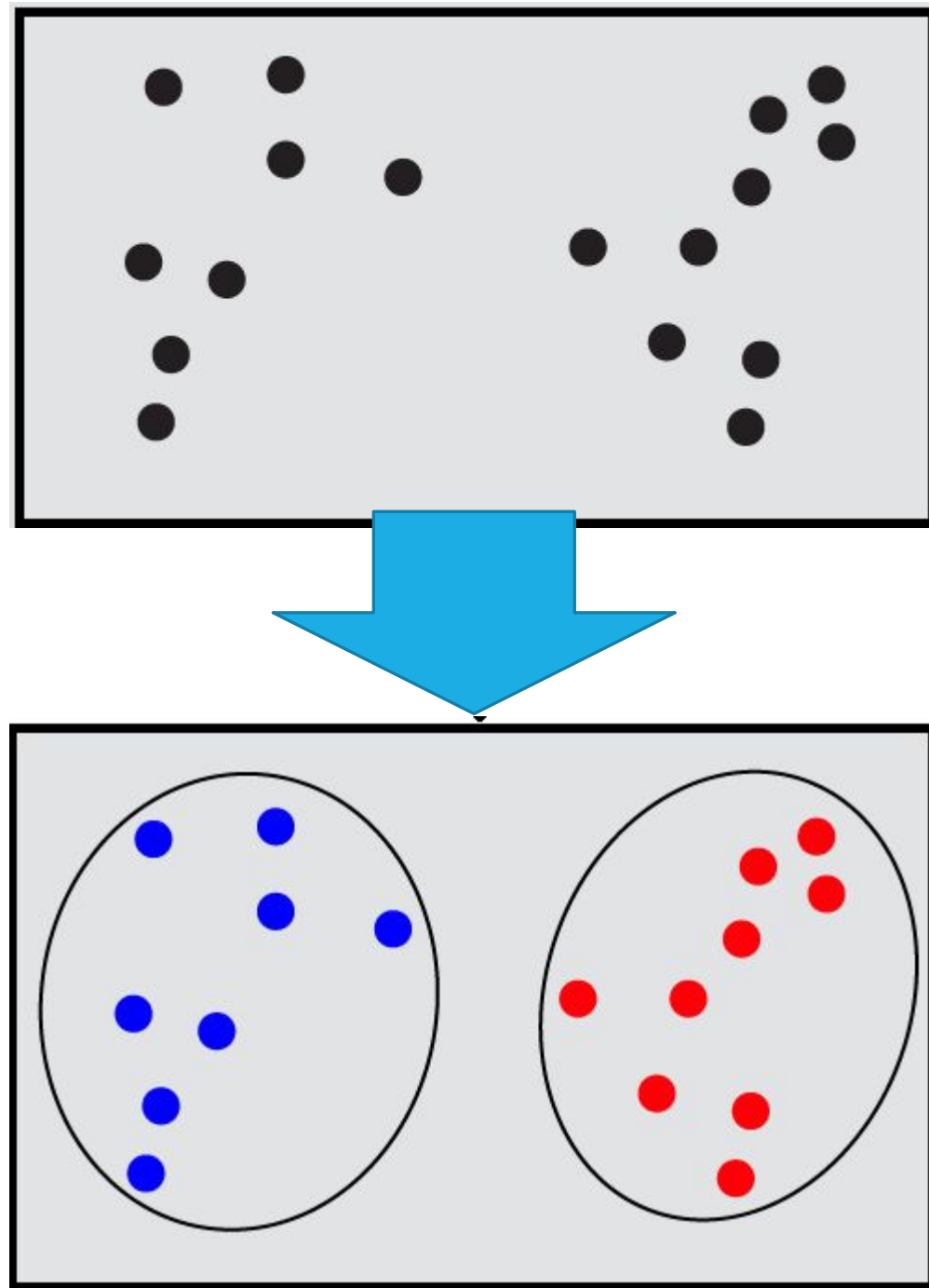
INTRODUCTION TO UNSUPERVISED LEARNING



- *Unsupervised Machine Learning* uses machine learning algorithms to analyze and cluster unlabeled datasets.
- We do not provide the machine with **labeled data**, and the machine is expected to derive structure from the data all on its own.
- Generally, it is used as a process to find meaningful structure, explanatory underlying processes, generative features, and groupings inherent in a set of examples
- There are many forms of *Unsupervised Machine Learning*, though the main form of unsupervised machine learning is '**CLUSTERING**'.

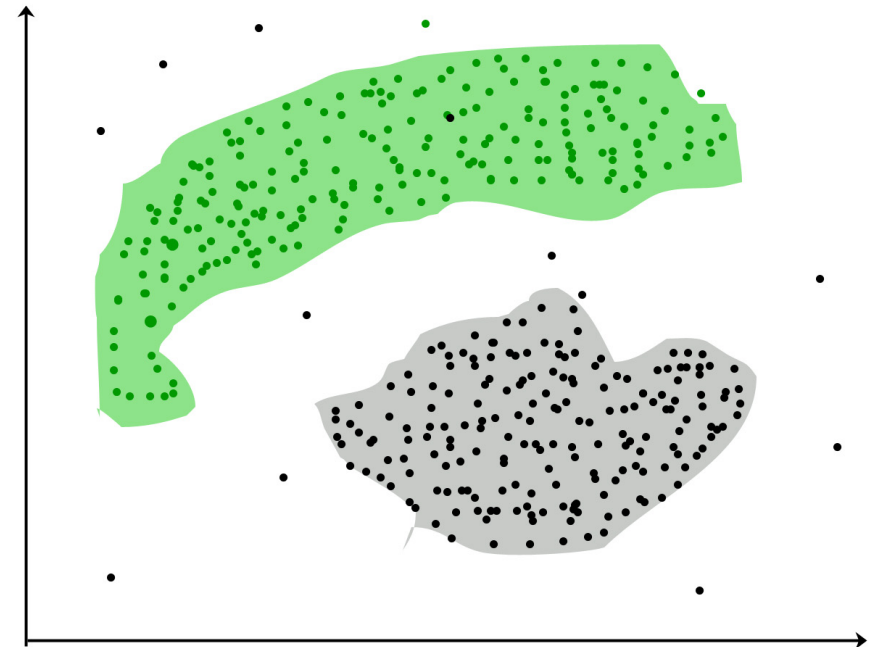
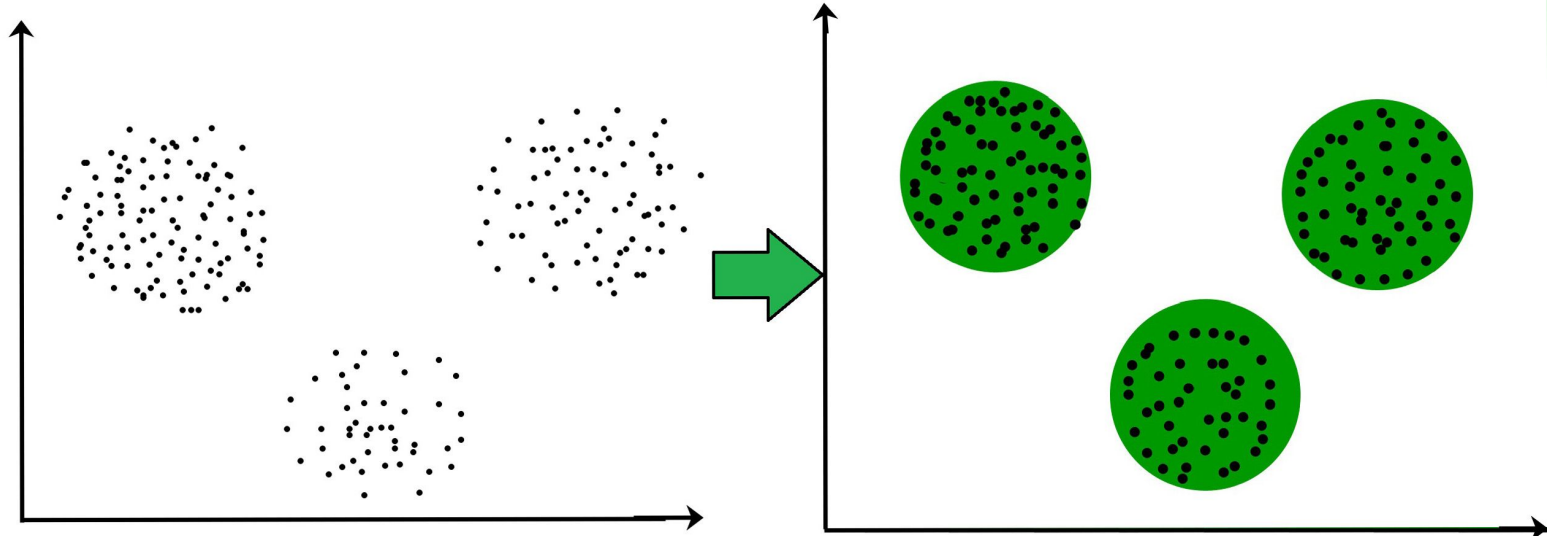
INTRODUCTION TO CLUSTERING

- ❑ Clustering or Cluster analysis is the method of grouping the entities based on similarities
- ❑ A cluster is a collection of objects which are “similar” amongst themselves and are “dissimilar” to the objects belonging to a different cluster
- ❑ It is defined as an **unsupervised learning problem** that aims to make **training data** with a given set of inputs but without any target values, or labels
- ❑ In clustering, the machine learns the attributes and trends by itself without any provided input-output mapping.
- ❑ The clustering algorithms extract patterns and inferences from the type of data objects and then make discrete classes of clustering them suitably.



EXAMPLE

- The data points in the graph, clustered together can be classified into one single group.
- We can distinguish the clusters, and we can identify that there are 3 clusters as shown in the picture
- It is not necessary for clusters to be spherical
- There are no criteria for good clustering, it depends on the user, what is the criteria they may use which satisfy their need.



CLUSTERING VS CLASSIFICATION

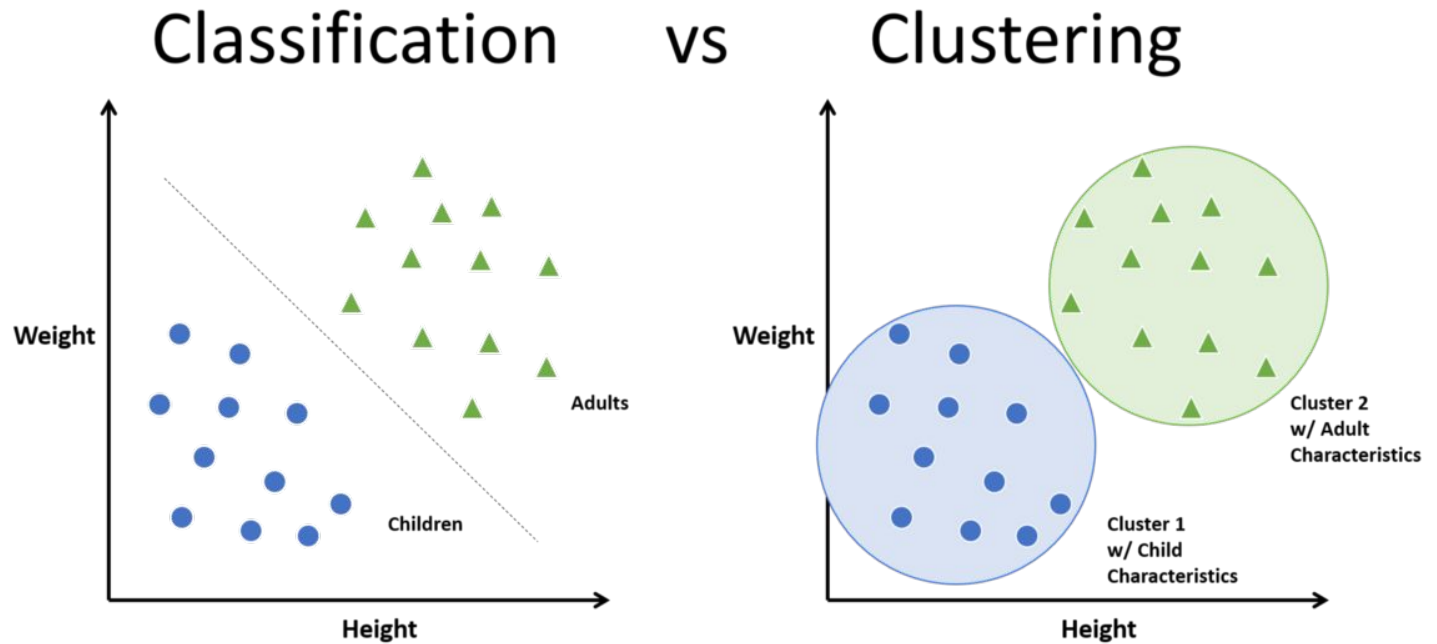
The difference between clustering and classification may not seem great at first.

As, in both cases we have a partition of a set of documents into groups.

But as we will see the two problems are fundamentally different.

Classification is a form of supervised learning our goal is to replicate a categorical distinction that a human supervisor imposes on the data.

In unsupervised learning, of which clustering is the most important example, we have no such teacher to guide us.



CLUSTERING VS CLASSIFICATION

| Parameter | CLASSIFICATION | CLUSTERING |
|--------------------|--|--|
| Type | used for supervised learning | used for unsupervised learning |
| Basic | process of classifying the input instances based on their corresponding class labels | grouping the instances based on their similarity without the help of class labels |
| Need | it has labels so there is need of training and testing dataset for verifying the model created | there is no need of training and testing dataset |
| Complexity | more complex as compared to clustering | less complex as compared to classification |
| Example Algorithms | Logistic regression, Naive Bayes classifier, Support vector machines, etc. | k-means clustering algorithm, Fuzzy c-means clustering algorithm, Gaussian (EM) clustering algorithm, etc. |

TYPES OF CLUSTERING METHODS

The major fundamental clustering methods are:

1. Partitioning Methods
2. Hierarchical Methods
3. Density-based Methods
4. Grid Based Methods

1. PARTITIONING METHODS

Given a set of n objects, a partitioning method constructs k partitions of the data

Where each partition represents a cluster and $k \leq n$

That is, it divides the data into k groups such that each group must contain at least one object

The basic partitioning methods typically adopt exclusive cluster separation

That is the object must belong to exactly one group

Most popular partitioning methods are:

1. K-Means Clustering
2. K-Medoids algorithm

2. HIERARCHICAL METHODS

A hierarchical method creates a hierarchical decomposition of the given set of data objects

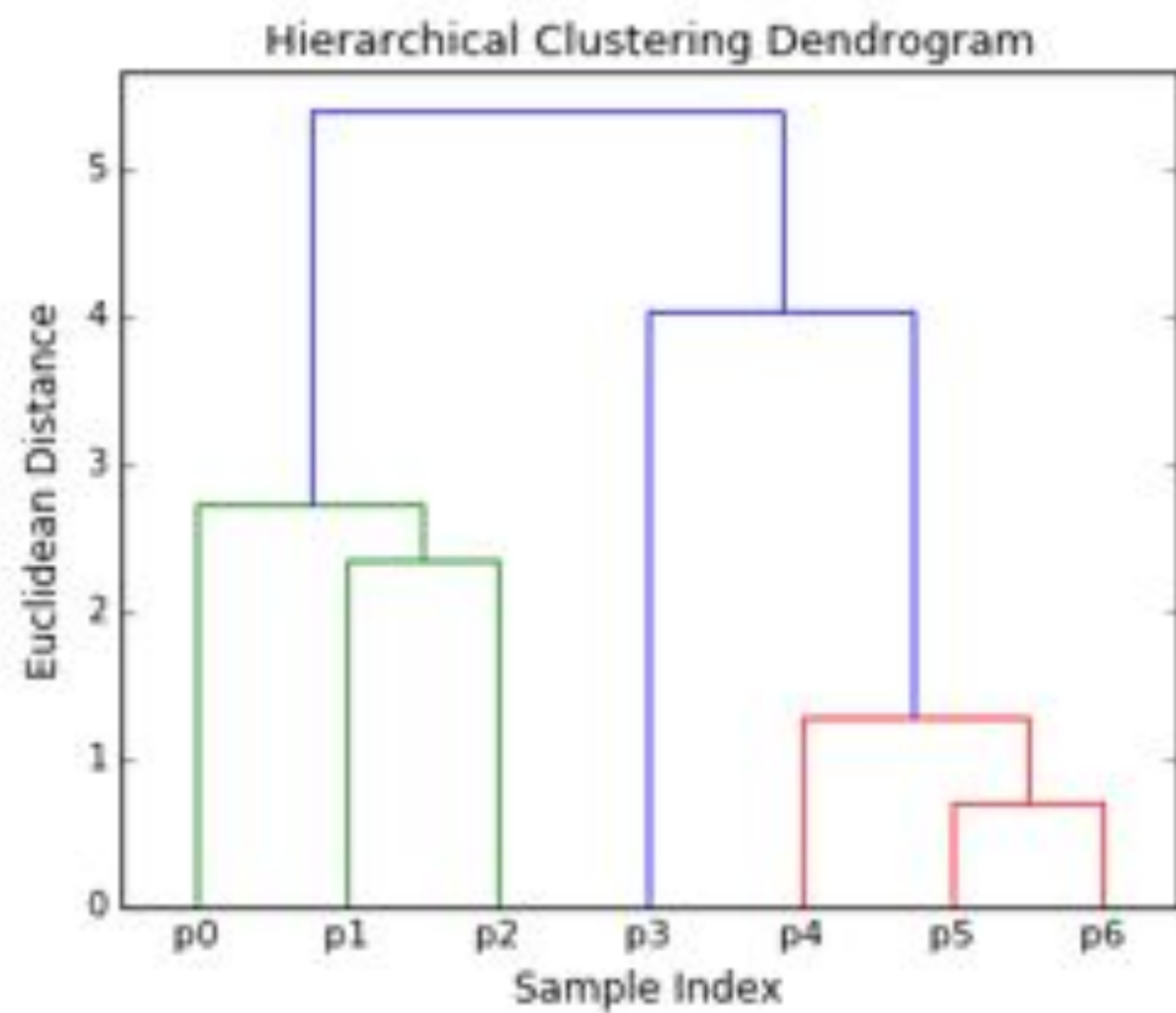
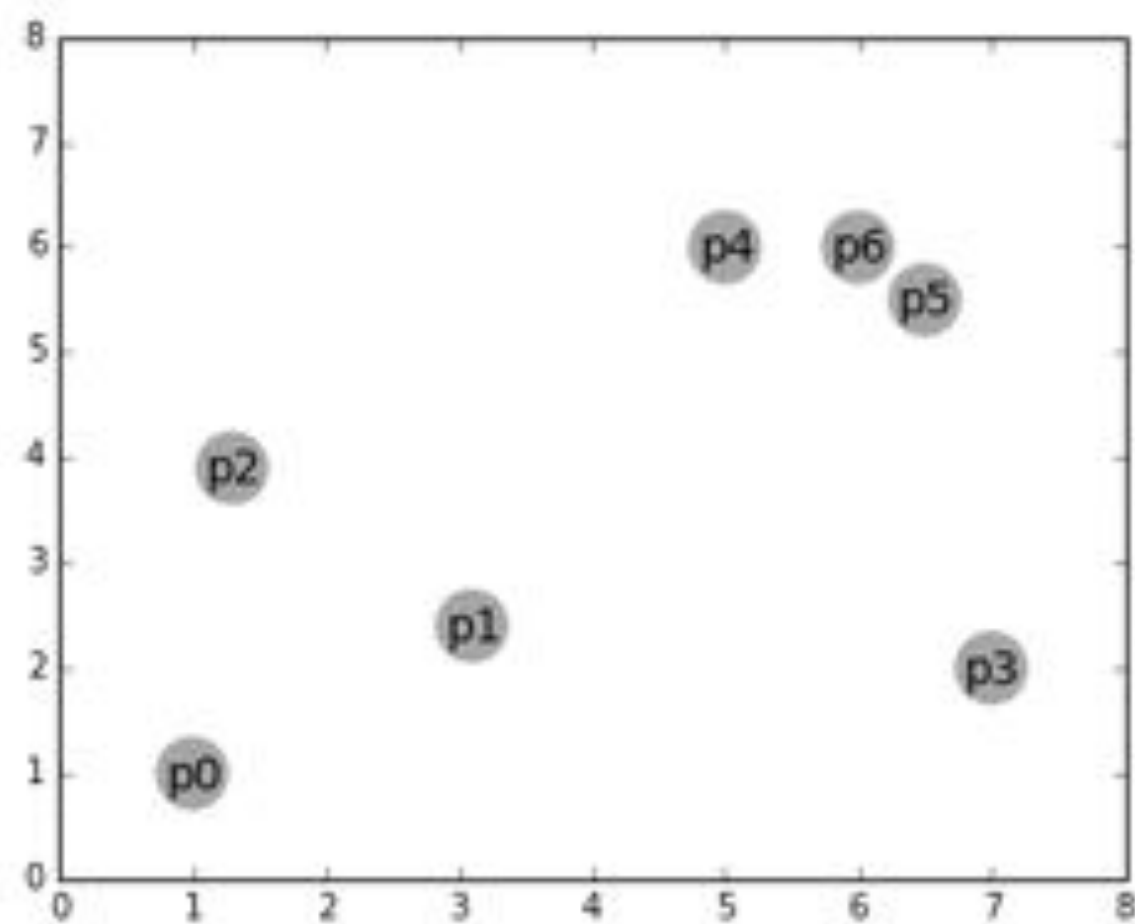
A hierarchical method can be classified into *agglomerative* or *divisive* approach

The *agglomerative* approach also called *bottom up* approach, starts with each object forming a separate group

It then successively merges the objects or groups close to one another, until all groups are merged into one .

The *divisive* approach, also called top-down approach, starts with all the objects in the same cluster

It then split the cluster into smaller clusters, until each object is one cluster



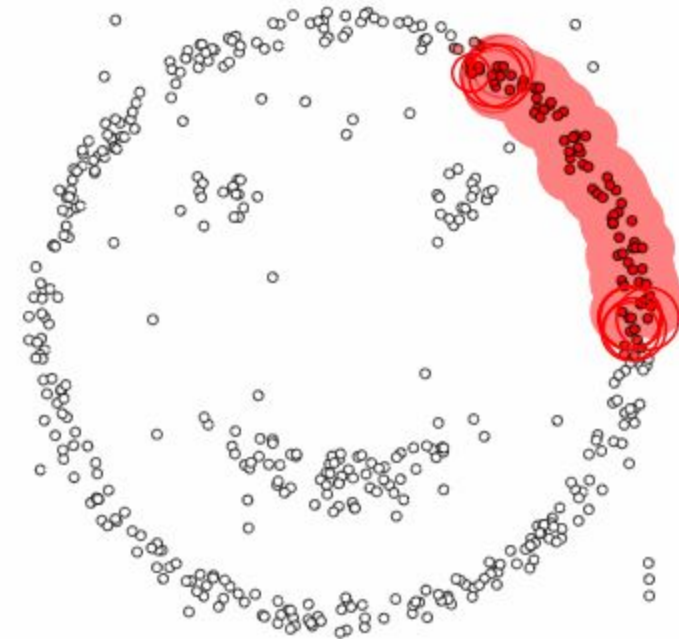
3. DENSITY-BASED METHODS

Most partitioning methods cluster objects based on distance between objects

Such methods can find only *spherical shaped* clusters

Such methods encounter difficulty in discovering clusters of *arbitrary shapes*

The general idea of density based clustering is to continue growing a given cluster as long as the density (number of objects or data points) in the neighborhood exceeds some threshold



epsilon = 1.00
minPoints = 4

Restart



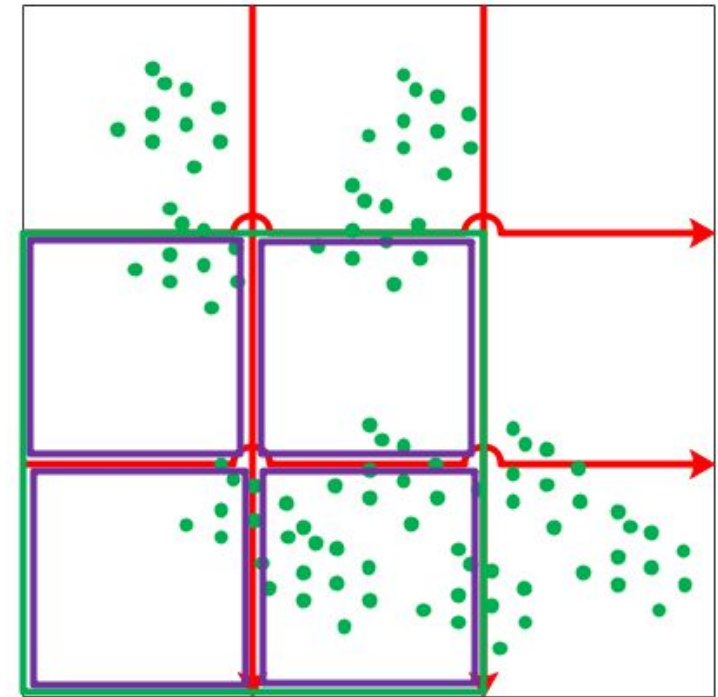
Pause

4. GRID BASED METHODS

Grid based methods quantize the object space into a finite number of cells that form a grid structure

All the clustering operations are performed on the grid structure

These are seen as Faster Clustering Methods



CLUSTERING METHODS- COMPARISON

| Method | General Characteristics |
|-----------------------|--|
| Partitioning Methods | <ul style="list-style-type: none">- Find Mutually Exclusive clusters of spherical shape- Distance based- May use Mean or Medoid to represent cluster center- Effective for small or medium sized data sets |
| Hierarchical Methods | <ul style="list-style-type: none">- Clustering is a hierarchical decomposition- Cannot correct erroneous merges or splits |
| Density-based Methods | <ul style="list-style-type: none">- Can find arbitrarily shaped clusters- Clusters are dense regions of objects in space that are separated by low density regions- Cluster Density: each point must have a minimum number of points within its neighborhood- May filter out outliers |
| Grid- based Methods | <ul style="list-style-type: none">- Use multiresolution grid data structure- Fast processing time |



PARTITIONING METHODS: USING K-MEANS FOR FLAT CLUSTERING

K-MEANS CLUSTERING

Suppose a Data set D , contains n objects in Euclidean space

Partitioning methods distribute the objects in D into k clusters, C_1, \dots, C_k , that is $C_i \subset D$, and $C_i \cap C_j = \emptyset$ for $(1 \leq i, j \leq k)$

An objective function is used to assess the partitioning quality so that objects within a cluster are similar to one another but dissimilar to objects in other clusters

That is objective function aims for high intra-cluster similarity and low inter-cluster similarity

K-MEANS CLUSTERING

A centroid based partitioning technique uses the centroid of a cluster C_i to represent that cluster

Conceptually the centroid of a cluster is its center point

The centroid can be defined in various ways such as by the *mean* or *medoid* of the objects assigned to the cluster

The difference between an object $p \in C_i$ and c_i the representation of cluster is measured by $\text{dist}(p, c_i)$,

Where $\text{dist}(x, y)$ is the Euclidean distance between two points x and y

K-MEANS CLUSTERING - *WITHIN-CLUSTER VARIATION*

The quality of cluster C_i can be measured by the *within-cluster variation*:

$$E = \sum_{i=1}^k \sum_{p \in C_i} \text{dist}(p, c_i)^2$$

For Each object in each cluster, the distance from the object to its cluster centre is squared, and distances are summed up

This objective function tries to make the resulting k clusters as compact and as separate as possible

Where, E is sum of all squared error for all objects in the data set

p is the point in space representing a given object

c_i is the centroid of cluster C_i

K-MEANS ALGORITHM

The background is a solid dark blue. On the left side, there are several 3D cubes of varying sizes, some of which are connected by thin, light blue lines. On the right side, there is a network graph consisting of numerous small dots (nodes) connected by thin, light blue lines, forming a complex web-like structure.

WORKING

The k means algorithm defines the centroid of a cluster as the mean value of the points within the cluster

1. it randomly selects k of the objects in D , each of which initially represents a cluster mean or center
2. For each remaining objects, an object is assigned to the cluster to which it is most similar, based on Euclidean Distance between object and cluster mean
3. The k-mean algorithm then iteratively improves the within cluster variation
4. For each cluster, it computes the new mean the objects assigned to the cluster in the previous iteration
5. All the objects are then reassigned using the updated means as the new cluster centers
6. The iterations continue until the assignment is stable, that is, the cluster formed in the current round are the same as those formed in the previous round

K-MEANS ALGORITHM

Algorithm

- The K-means algorithm for partitioning, where each cluster's center is represented by the mean value of the objects in the cluster

Input

- K: the number of clusters
- D: a Data set consisting of n Objects

Output:

- A set of k Clusters

Method:

1. Arbitrarily choose k objects from D as the initial cluster centers
2. **Repeat:**
3. Calculate the distance from each data point to each centroid.
4. Assign the data points to the closest centroid.
5. Recalculate the centroids as the mean of the points in their cluster.
6. **Until** no change

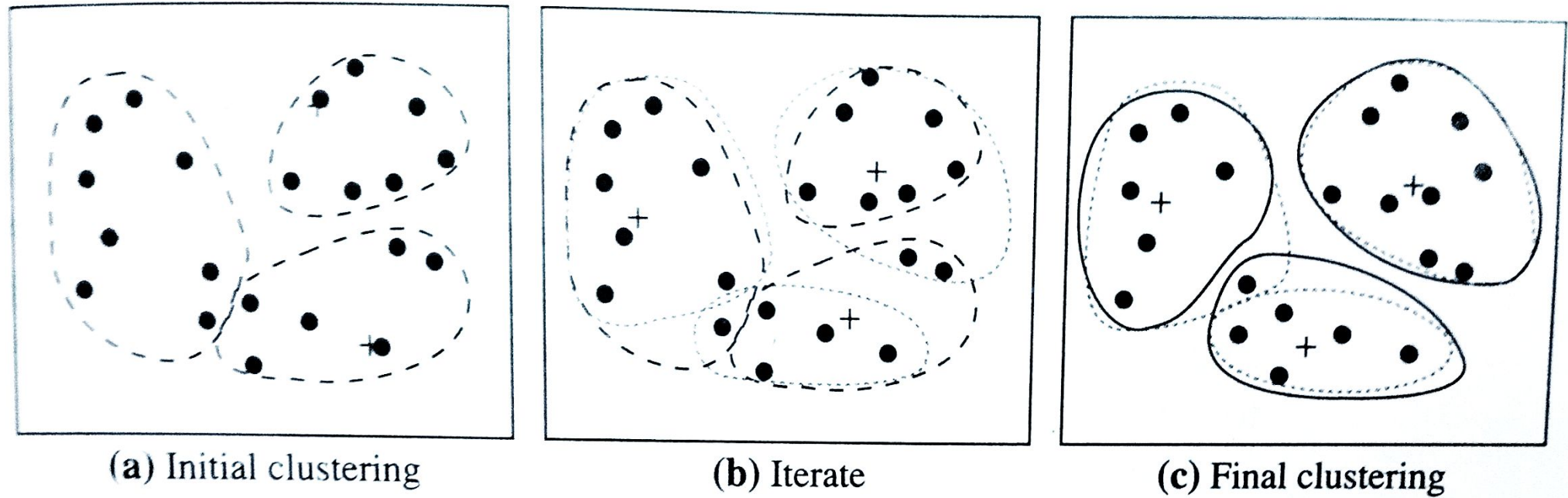


Figure 10.3 Clustering of a set of objects using the k -means method; for (b) update cluster centers and reassign objects accordingly (the mean of each cluster is marked by a +).

EXAMPLE

Suppose that we have following items to cluster: $\{2,4,10,12,3,20,30,11,25\}$

And suppose that $k = 2$

We Assign means to the first two values $m1=2$, $m2=4$

Using Euclidean distance we find that initially $K1=\{2,3\}$, $K2=\{4,10,12,20,30,11,25\}$

The value 3 is equally closed to both means, so arbitrarily choose $K1$

We then re-calculate the means to get $m1=2.5$ and $m2=16$

We again make assignments to cluster to get $K1=\{2,3,4\}$ and $K2=\{10,12,20,30,11,25\}$

EXAMPLE

| m_1 | m_2 | K_1 | K_2 |
|-------|-------|---------------------------|--------------------------|
| 3 | 18 | $\{2, 3, 4, 10\}$ | $\{12, 20, 30, 11, 25\}$ |
| 4.75 | 19.6 | $\{2, 3, 4, 10, 11, 12\}$ | $\{20, 30, 25\}$ |
| 7 | 25 | $\{2, 3, 4, 10, 11, 12\}$ | $\{20, 30, 25\}$ |



scikit-learn

Machine Learning in Python

- Simple and efficient tools for predictive data analysis
- Accessible to everybody, and reusable in various contexts
- Built on NumPy, SciPy, and matplotlib
- Open source, commercially usable - BSD license

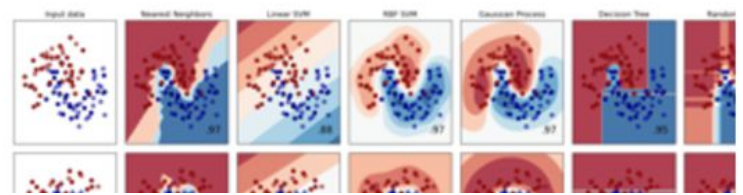
[Getting Started](#) [Release Highlights for 1.2](#) [GitHub](#)

Classification

Identifying which category an object belongs to.

Applications: Spam detection, image recognition.

Algorithms: SVM, nearest neighbors, random forest, and more...



Regression

Predicting a continuous-valued attribute associated with an object.

Applications: Drug response, Stock prices.

Algorithms: SVR, nearest neighbors, random forest, and more...



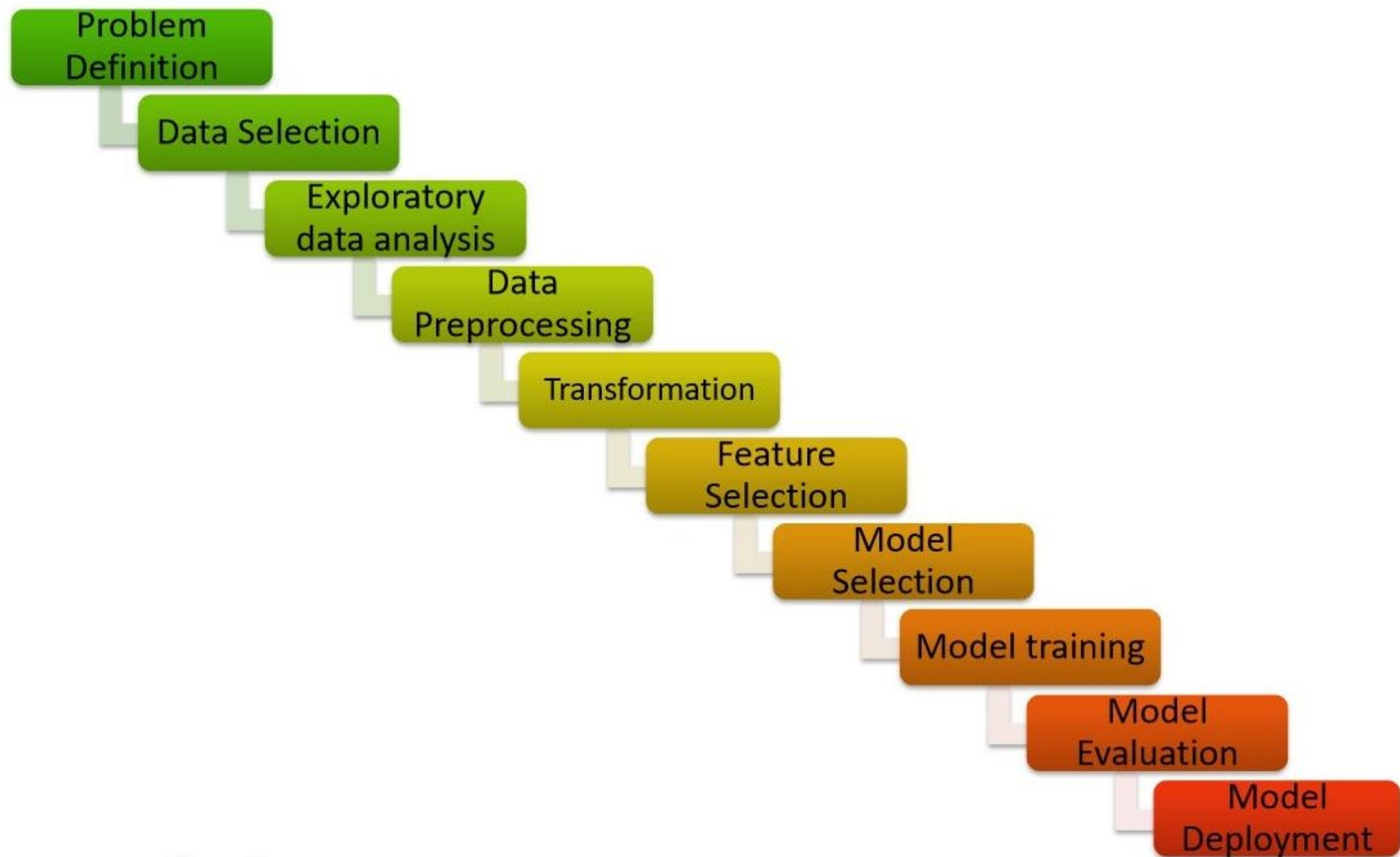
Clustering

Automatic grouping of similar objects into sets.

Applications: Customer segmentation, Grouping experiment outcomes

Algorithms: k-Means, spectral clustering, mean-shift, and more...





USING KMEANS FROM SKLEARN

Clustering of unlabeled data can be performed with the module `sklearn.cluster`

K-Means algorithm can be implemented using the class `KMeans`

The Kmeans class has many important methods, constructors and attributes, which are used to implement K-Means Algorithm

| Method | Description |
|--|--|
| <code>fit(X[, y, sample_weight])</code> | Compute k-means clustering. |
| <code>fit_predict(X[, y, sample_weight])</code> | Compute cluster centers and predict cluster index for each sample. |
| <code>fit_transform(X[, y, sample_weight])</code> | Compute clustering and transform X to cluster-distance space. |
| <code>get_feature_names_out([input_features])</code> | Get output feature names for transformation. |
| <code>get_params([deep])</code> | Get parameters for this estimator. |
| <code>predict(X[, sample_weight])</code> | Predict the closest cluster each sample in X belongs to. |
| <code>score(X[, y, sample_weight])</code> | Opposite of the value of X on the K-means objective. |
| <code>set_output(*[, transform])</code> | Set output container. |
| <code>set_params(**params)</code> | Set the parameters of this estimator. |
| <code>transform(X)</code> | Transform X to a cluster-distance space. |

IMPLEMENTING FIT & PREDICT FUNCTIONS

```
fit(X, y=None, sample_weight=None)
```

Compute k-means clustering

Parameters:

X : {array-like, sparse matrix} of shape (n_samples, n_features)

Training instances to cluster. It must be noted that the data will be converted to C ordering, which will cause a memory copy if the given data is not C-contiguous. If a sparse matrix is passed, a copy will be made if it's not in CSR format.

y : Ignored

Not used, present here for API consistency by convention.

sample_weight : array-like of shape (n_samples,), default=None

The weights for each observation in X. If None, all observations are assigned equal weight.

New in version 0.20.

Returns:

self : object

Fitted estimator.

IMPLEMENTING FIT & PREDICT FUNCTIONS

predict(*X*, *sample_weight=None*) (Predict the closest cluster each sample in *X* belongs to)

Parameters:

***X* : {array-like, sparse matrix} of shape (n_samples, n_features)**

New data to predict.

***sample_weight* : array-like of shape (n_samples,), default=None**

The weights for each observation in *X*. If None, all observations are assigned equal weight.

Returns:

***labels* : ndarray of shape (n_samples,)**

Index of the cluster each sample belongs to.

IMPLEMENTING FIT & PREDICT FUNCTIONS

```
fit_predict(X, y=None, sample_weight=None)
```

Compute cluster centers and predict cluster index for each sample.

Parameters:

X : {array-like, sparse matrix} of shape (n_samples, n_features)

New data to transform.

y : Ignored

Not used, present here for API consistency by convention.

sample_weight : array-like of shape (n_samples,), default=None

The weights for each observation in X. If None, all observations are assigned equal weight.

Returns:

labels : ndarray of shape (n_samples,)

Index of the cluster each sample belongs to.

IMPLEMENTING FIT & PREDICT FUNCTIONS

`get_params(deep=True)`

Get parameters for this estimator.

| | |
|--------------------|---|
| Parameters: | <code>deep : <i>bool</i>, <i>default=True</i></code> If True, will return the parameters for this estimator and contained subobjects that are estimators. |
| Returns: | <code>params : <i>dict</i></code> Parameter names mapped to their values. |

IMPLEMENTING K-MEANS CLASS

```
class sklearn.cluster.KMeans(n_clusters=8, *, init='k-means++', n_init='warn', max_iter=300,
```

```
tol=0.0
```

Parameters:

n_clusters : int, default=8

The number of clusters to form as well as the number of centroids to generate.

init : {'k-means++', 'random'}, callable or array-like of shape (n_clusters, n_features), default='k-means++'

Method for initialization:

'k-means++': selects initial cluster centroids using sampling based on an empirical probability distribution of the points' contribution to the overall inertia. This technique speeds up convergence. The algorithm implemented is "greedy k-means++". It differs from the vanilla k-means++ by making several trials at each sampling step and choosing the best centroid among them.

'random': choose `n_clusters` observations (rows) at random from data for the initial centroids.

If an array is passed, it should be of shape (n_clusters, n_features) and gives the initial centers.

If a callable is passed, it should take arguments X, n_clusters and a random state and return an initialization.

IMPLEMENTING K-MEANS CLASS

```
class sklearn.cluster.KMeans(n_clusters=8, *, init='k-means++', n_init='warn', max_iter=300,
```

```
tol=0.0001, verbose=0, random_state=None, copy_x=True, algorithm='lloyd')
```

n_init : 'auto' or int, default=10

Number of times the k-means algorithm is run with different centroid seeds. The final results is the best output of `n_init` consecutive runs in terms of inertia. Several runs are recommended for sparse high-dimensional problems

When `n_init='auto'`, the number of runs depends on the value of `init`: 10 if using `init='random'`, 1 if using `init='k-means++'`.

New in version 1.2: Added 'auto' option for `n_init`.

IMPLEMENTING K-MEANS CLASS

```
class sklearn.cluster.KMeans(n_clusters=8, *, init='k-means++', n_init='warn', max_iter=300,
```

```
tol=0.0001, verbose=0, random_state=None, copy_x=True, algorithm='lloyd')  
    max_iter : int, default=300
```

Maximum number of iterations of the k-means algorithm for a single run.

tol : float, default=1e-4

Relative tolerance with regards to Frobenius norm of the difference in the cluster centers of two consecutive iterations to declare convergence.

verbose : int, default=0

Verbosity mode.

random_state : int, RandomState instance or None, default=None

Determines random number generation for centroid initialization. Use an int to make the randomness deterministic.

IMPLEMENTING K-MEANS CLASS

```
class sklearn.cluster.KMeans(n_clusters=8, *, init='k-means++', n_init='warn', max_iter=300,
```

```
tol=0.0001, verbose=0, random_state=None, copy_x=True, algorithm='lloyd',  
copy_x : bool, default=True
```

When pre-computing distances it is more numerically accurate to center the data first. If `copy_x` is `True` (default), then the original data is not modified. If `False`, the original data is modified, and put back before the function returns, but small numerical differences may be introduced by subtracting and then adding the data mean. Note that if the original data is not C-contiguous, a copy will be made even if `copy_x` is `False`. If the original data is sparse, but not in CSR format, a copy will be made even if `copy_x` is `False`.

algorithm : {"lloyd", "elkan", "auto", "full"}, default="lloyd"

K-means algorithm to use. The classical EM-style algorithm is `"lloyd"`. The `"elkan"` variation can be more efficient on some datasets with well-defined clusters, by using the triangle inequality. However it's more memory intensive due to the allocation of an extra array of shape `(n_samples, n_clusters)`.

`"auto"` and `"full"` are deprecated and they will be removed in Scikit-Learn 1.3. They are both aliases for `"lloyd"`.

USING KMEANS FROM SKLEARN

SKLearn

We usually follow following 4 steps:

1. import the library:

```
from sklearn.cluster import KMeans
```

2. initialize the model

```
model = KMeans(2)
```

3. Train the model with model.fit(...)

```
model = model.fit(df[ ["Label1", "Label2", "Label3"] ] )
```

4. predict the outcome

```
df["cluster"] = model.predict(df[ ["Label1", "Label2", "Label3"] ] )
```

EXAMPLE

<https://www.kaggle.com/code/funxexcel/p1-sklearn-k-means-example/notebook>



QUESTIONS?

Thank you!

REFERENCES

[1] Han Kamber Pie, “Data Mining Concepts and Techniques”, Morgan Kaufman, Elsevier 2012

[2] <https://www.analytixlabs.co.in/blog/types-of-clustering-algorithms/>

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