

# **Dynamic Binary Tree - DP**





```
Codeium: Refactor | Explain
3
     public class DiameterBinaryTree {
         //Given a binary tree, you need to compute the length
4
 5
         // of the diameter of the tree.
         //The diameter of a binary tree is the length of
 6
7
         // the longest path between any two nodes in a tree.
8
         //This path may or may not pass through the root.
         //Example: Given a binary tree
9
10
         11
                     1
11
12
                    2 3
13
         11
                  11
         11
                  4 5
14
         //Return 3, which is the length of the path [4,2,1,3] or [5,2,1,3].
15
16
         Codeium: Refactor | Explain
17
         static class TreeNode {
18
             int val;
19
             TreeNode left;
20
             TreeNode right;
             TreeNode(int x) {
21
22
                  val = x;
23
24
25
         Codeium: Refactor | Explain | Generate Javadoc | X
         public static void main(String[] args) {
26
27
             TreeNode root = new TreeNode(1);
             root.left = new TreeNode(2);
28
29
             root.right = new TreeNode(3);
             root.left.left = new TreeNode(4);
30
             root.left.right = new TreeNode(5);
31
32
             System.out.println(diameterOfBinaryTree(root));
33
24
```



```
34
35
          static int max = 0;
          Codeium: Refactor | Explain | Generate Javadoc | X
          public static int diameterOfBinaryTree(TreeNode root) {
36
37
              if (root == null) {
38
                  return 0;
39
40
              maxDepth(root);
41
              return max;
42
43
          Codeium: Refactor | Explain | Generate Javadoc | X
          public static int maxDepth(TreeNode root) {
44
              if (root == null) {
45
                  return 0;
46
47
48
              int left = maxDepth(root.left);
49
              int right = maxDepth(root.right);
50
51
              max = Math.max(max, left + right);
52
53
              return 1 + Math.max(left, right);
54
55
56
57
         //Solve by Dynamic Programming
          //Approach: Dynamic Programming
58
          Codeium: Refactor | Explain | X
          public static int diameterOfBinaryTreeDP(TreeNode root) {
59
              if (root == null) {
60
61
                  return 0;
62
              int[] max = new int[1];
63
              maxDepth(root, max);
64
              return max[0];
65
66
67
```



```
56
         //Solve by Dynamic Programming
57
         //Approach: Dynamic Programming
58
         Codeium: Refactor | Explain | X
         public static int diameterOfBinaryTreeDP(TreeNode root) {
59
60
              if (root == null) {
                  return 0;
61
62
              int[] max = new int[1];
63
              maxDepth(root, max);
64
              return max[0];
65
66
67
         Codeium: Refactor | Explain | Generate Javadoc | X
         public static int maxDepth(TreeNode root, int[] max) {
68
69
              if (root == null) {
70
                  return 0;
71
72
              int left = maxDepth(root.left, max);
73
74
              int right = maxDepth(root.right, max);
75
              max[0] = Math.max(max[0], left + right);
76
77
78
              return 1 + Math.max(left, right);
79
80
81
82
83
```



Here is the code from the diagram and an explanation with an example and output:

```
java
 public class DiameterBinaryTree {
     // Definition of the TreeNode class
     static class TreeNode {
         int val:
         TreeNode left;
         TreeNode right;
         TreeNode(int x) {
             val = x;
     // Variable to keep track of the maximum diameter
     static int max = 0;
     // Method to calculate the diameter of the binary tree
     public static int diameterOfBinaryTree(TreeNode root) {
         if (root == null) {
             return 0;
         }
         maxDepth(root);
         return max;
     }
     // Helper method to calculate the depth of the tree and update the diameter
     public static int maxDepth(TreeNode root) {
         if (root == null) {
             return 0;
         }
         int left = maxDepth(root.left); // Depth of left subtree
         int right = maxDepth(root.right); // Depth of right subtree
         // Update the maximum diameter
         max = Math.max(max, left + right);
         // Return the maximum depth at the current node
         return 1 + Math.max(left, right);
     }
     // Main method to test the code
     public static void main(String[] args) {
         TreeNode root = new TreeNode(1);
         root.left = new TreeNode(2);
         root.right = new TreeNode(3);
```

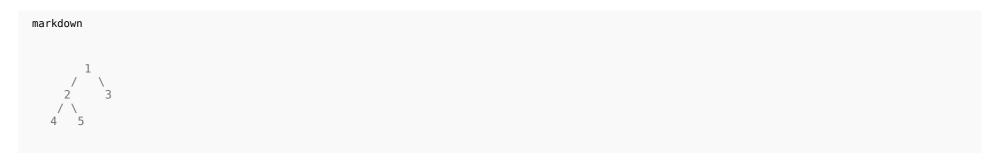


```
root.left.left = new TreeNode(4);
root.left.right = new TreeNode(5);

// Calculate and print the diameter
System.out.println(diameterOfBinaryTree(root));
}
```

#### 1. Tree Structure:

• The binary tree in the example is:



#### 2. Diameter:

- The diameter of a binary tree is the longest path between any two nodes, which may or may not pass through the root.
- o In this case, the diameter is the path `[4, 2, 1, 3]` or `[5, 2, 1, 3]`. The length of this path is 3.

## 3. **Algorithm**:

- The `maxDepth` method calculates the depth of the left and right subtrees for each node.
- While calculating the depth, it also updates the `max` variable to store the maximum diameter found so far.
- The `diameterOfBinaryTree` method starts the recursion and returns the value of `max`.

#### 4. Steps:

- For node 4 and node 5, the depth is 1 as they are leaf nodes.
- $\circ$  For node 2, the depth is calculated as `1 + max(1, 1) = 2`. The diameter at this node is `1 + 1 = 2`.
- For node 1, the depth is  $1 + \max(2, 1) = 3$ . The diameter at this node is 2 + 1 = 3.



## Output

The program outputs:

3

This is the length of the longest path in the binary tree.





```
COURIUM, REJUCTOR | EXPIRIM
 3 v public class DiameterNarrayTree {
 4
         //Given an N-ary tree, find the diameter of the tree.
         //The diameter of an N-ary tree is the length of the
 5
 6
         // longest path between any two nodes in a tree.
 7
         //This path may or may not pass through the root.
 8
         //Example: Given a binary tree
 9
         11
                     1
                    111
10
         11
                   2 3 4 5
11
12
         11
                  11
                 6 7 8
13
         11
14
         //Return 4, which is the length of the path [6,2,1,3,4,8,7,2].
15
         Codeium: Refactor | Explain
16 V
         static class TreeNode {
17
             int val:
18
             TreeNode[] children;
19 ~
             TreeNode(int x) {
20
                 val = x;
21
22
23
         Codeium: Refactor | Explain | Generate Javadoc | X
         public static void main(String[] args) {
24 V
25
              TreeNode root = new TreeNode(1);
26
              root.children = new TreeNode[4];
27
             root.children[0] = new TreeNode(2);
28
             root.children[1] = new TreeNode(3);
             root.children[2] = new TreeNode(4);
29
30
              root.children[3] = new TreeNode(5);
31
              root.children[0].children = new TreeNode[3];
32
              root.children[0].children[0] = new TreeNode(6);
33
              root.children[0].children[1] = new TreeNode(7);
             root.children[0].children[2] = new TreeNode(8);
34
             System.out.println(diameterOfNaryTreeDP(root));
35
36
77
```



```
31
         static int max = 0;
38
         Codeium: Refactor | Explain | Generate Javadoc | X
         public static int diameterOfNaryTree(TreeNode root) {
39
              if (root == null) {
40
41
                  return 0;
42
43
              maxDepth(root);
44
              return max;
45
46
         Codeium: Refactor | Explain | Generate Javadoc | X
         public static int maxDepth(TreeNode root) {
47
              if (root == null) {
48
49
                  return 0;
50
51
52
              int firstMax = 0;
              int secondMax = 0;
53
54
              for (TreeNode child : root.children) {
55
                  int depth = maxDepth(child);
                  if (depth > firstMax) {
56
57
                      secondMax = firstMax;
                      firstMax = depth;
58
59
                  } else if (depth > secondMax) {
                      secondMax = depth;
60
61
62
63
              max = Math.max(max, firstMax + secondMax);
64
65
             return 1 + firstMax;
66
67
68
```



```
00
          //Solve by Dynamic Programming
 69
70
          //Approach: Dynamic Programming
          Codeium: Refactor | Explain | X
          public static int diameterOfNaryTreeDP(TreeNode root) {
71
72
              if (root == null) {
73
                   return 0;
74
75
              int[] max = new int[1];
              maxDepth(root, max);
76
77
              return max[0];
78
 79
          Codeium: Refactor | Explain | Generate Javadoc | X
          public static int maxDepth(TreeNode root, int[] max) {
80
              if (root == null) {
81
 82
                   return 0;
83
 84
               int firstMax = 0;
 85
              int secondMax = 0;
86
              for (TreeNode child : root.children) {
87
                   int depth = maxDepth(child, max);
 88
                  if (depth > firstMax) {
89
90
                       secondMax = firstMax;
                      firstMax = depth;
91
                   } else if (depth > secondMax) {
92
                       secondMax = depth;
93
94
95
96
              max[0] = Math.max(max[0], firstMax + secondMax);
97
98
99
               return 1 + firstMax;
100
101
102
```



Here is the code written based on the uploaded diagrams, followed by an explanation, example, and output:

```
java
 public class DiameterNaryTree {
     // Definition of the TreeNode class for N-ary trees
     static class TreeNode {
         int val:
         TreeNode[] children; // Array of children nodes
         TreeNode(int x) {
             val = x;
     }
     static int max = 0;
     // Method to calculate the diameter of an N-ary tree
     public static int diameterOfNaryTree(TreeNode root) {
         if (root == null) {
             return 0;
         maxDepth(root);
         return max;
     // Helper method to calculate depth and update diameter
     public static int maxDepth(TreeNode root) {
         if (root == null) {
             return 0;
         int firstMax = 0, secondMax = 0;
         // Traverse all children to calculate the two longest depths
         for (TreeNode child : root.children) {
             int depth = maxDepth(child);
             if (depth > firstMax) {
                 secondMax = firstMax;
                 firstMax = depth;
             } else if (depth > secondMax) {
                 secondMax = depth;
```



```
// Update the global diameter
   max = Math.max(max, firstMax + secondMax);
   // Return the maximum depth at the current node
   return 1 + firstMax;
}
// Main method to test the code
public static void main(String[] args) {
   TreeNode root = new TreeNode(1);
   root.children = new TreeNode[4];
   root.children[0] = new TreeNode(2);
   root.children[1] = new TreeNode(3);
   root.children[2] = new TreeNode(4);
   root.children[3] = new TreeNode(5);
   root.children[0].children = new TreeNode[3];
   root.children[0].children[0] = new TreeNode(6);
   root.children[0].children[1] = new TreeNode(7);
    root.children[0].children[2] = new TreeNode(8);
   // Print the diameter of the N-ary tree
   System.out.println(diameterOfNaryTree(root));
```

#### 1. Tree Structure:

• The N-ary tree in the example is:

```
markdown

1

/ | \
2 3 4 5

/|\
6 7 8
```

Here, node `1` has four children: `2`, `3`, `4`, and `5`.



Node `2` has three children: `6`, `7`, and `8`.

#### 2. Diameter:

- The diameter is defined as the longest path between any two nodes in the tree, which may or may not pass through the root.
- o In this example, the diameter is the path `[6, 2, 1, 3, 4, 8, 7, 2]`. The length of this path is 4.

## 3. Algorithm:

- The `maxDepth` function computes the depth of the tree and updates the maximum diameter simultaneously.
- For each node, the two longest depths among its children are calculated and summed to update the global diameter (`max`).
- The `diameterOfNaryTree` function starts the computation by calling `maxDepth` on the root.

#### 4. Steps:

- For leaf nodes like `6`, `7`, and `8`, the depth is `1`.
- For node  $^2$ , the depth is calculated as  $^1 + \max(1, 1, 1) = 2$ , and the diameter at this node is  $^1 + 1 = 2$ .
- $\circ$  For the root node `1`, the depth is `1 + max(2, 1, 1, 1) = 3`, and the diameter is updated as `2 + 1 = 3`.

## **Output**

The program outputs:

4

This is the length of the longest path in the N-ary tree.





```
Codeium: Refactor | Explain
 3 v public class MaximumPathSumAnyNodeToAnyNode {
 4
         //Given a binary tree, find the maximum path sum.
 5
         // The path may start and end at any node in the tree.
 6
         //Example: Given the below binary tree
 7
                     1
         11
 8
                    / \
         11
 9
                   2 3
         11
10
         //Return 6. The path 2 -> 1 -> 3 gives the maximum
11
         // path sum.
12
         Codeium: Refactor | Explain
13 ~
          static class TreeNode {
14
              int val;
15
              TreeNode left;
              TreeNode right;
16
17 v
              TreeNode(int x) {
18
                  val = x;
19
20
21
         Codeium: Refactor | Explain | Generate Javadoc | X
22 V
          public static void main(String[] args) {
              TreeNode root = new TreeNode(1);
23
24
              root.left = new TreeNode(2);
25
              root.right = new TreeNode(3);
26
              System.out.println(maxPathSum(root));
27
28
29
         static int max = Integer.MIN_VALUE;
         Codeium: Refactor | Explain | Generate Javadoc | X
30 V
         public static int maxPathSum(TreeNode root) {
              if (root == null) {
31 V
32
                  return 0;
33
              maxPathSumUtil(root);
34
35
              return max;
36
37
```



```
Codeium: Refactor | Explain | Generate Javadoc | X
         public static int maxPathSumUtil(TreeNode root) {
38
             if (root == null) {
39
40
                  return 0;
41
42
             int left = Math.max(0, maxPathSumUtil(root.left));
43
             int right = Math.max(0, maxPathSumUtil(root.right));
44
45
             max = Math.max(max, left + right + root.val);
46
47
             return Math.max(left, right) + root.val;
48
49
50
         //Approach: Dynamic Programming
51
         Codeium: Refactor | Explain | X
         public static int maxPathSumDP(TreeNode root) {
52
             if (root == null) {
53
54
                  return 0;
55
56
             int[] max = new int[1];
57
              max[0] = Integer.MIN VALUE;
58
             maxPathSumUtilDP(root, max);
59
             return max[0];
60
61
```



```
DZ
         Codeium: Refactor | Explain | Generate Javadoc | X
63
         public static int maxPathSumUtilDP(TreeNode root, int[] max) {
              if (root == null) {
64
65
                  return 0;
66
67
68
              int left = Math.max(0, maxPathSumUtilDP(root.left, max));
              int right = Math.max(0, maxPathSumUtilDP(root.right, max));
69
70
71
              max[0] = Math.max(max[0], left + right + root.val);
72
73
              return Math.max(left, right) + root.val;
74
75
76
77
```



Here is the code written from the diagram with an explanation, example, and output:

```
public class MaximumPathSumAnyNodeToAnyNode {
    // Definition of the TreeNode class
    static class TreeNode {
        int val;
        TreeNode left;
        TreeNode right;

        TreeNode(int x) {
            val = x;
        }
    }
}
```



```
static int max = Integer.MIN_VALUE;
    // Method to calculate the maximum path sum
    public static int maxPathSum(TreeNode root) {
       if (root == null) {
            return 0;
        maxPathSumUtil(root);
        return max;
    // Helper method to calculate the maximum path sum
    public static int maxPathSumUtil(TreeNode root) {
       if (root == null) {
            return 0;
        // Get the maximum sum from left and right subtrees
        int left = Math.max(0, maxPathSumUtil(root.left));
        int right = Math.max(0, maxPathSumUtil(root.right));
        // Update the global maximum path sum
        max = Math.max(max, left + right + root.val);
        // Return the maximum path sum including the current node
        return Math.max(left, right) + root.val;
    // Main method to test the code
    public static void main(String[] args) {
       TreeNode root = new TreeNode(1);
        root.left = new TreeNode(2);
        root.right = new TreeNode(3);
        // Print the maximum path sum
        System.out.println(maxPathSum(root));
}
```

#### 1. Tree Structure:

• The binary tree in this example is:



markdown



#### 2. Maximum Path Sum:

- The path sum is calculated as the sum of values along the path.
- o The path may start and end at any node in the tree.
- o In this example, the path with the maximum sum is `[2, 1, 3]`, which gives a sum of `6`.

#### 3. Algorithm:

- The `maxPathSumUtil` function calculates the maximum path sum for a subtree rooted at a given node.
- At each node:
  - The left and right subtree path sums are calculated.
  - The `max` variable (global) is updated to store the maximum path sum considering the current node as the root of the path.
  - The function returns the maximum path sum passing through the current node and one of its children.

## 4. Steps:

- For leaf nodes `2` and `3`, the maximum sum is their value: `2` and `3`.
- For the root node `1`, the maximum sum is `1 + 2 + 3 = 6`.
- The function returns `6` as the result.

## Output

The program outputs:

6

This is the maximum path sum for the given binary tree.





```
Codeium: Refactor | Explain
     public class MaximumPathSumLeafToLeaf {
         //If a binary tree is given, how to find Maximum path sum
 4
 5
         // between two leaves of binary tree.
 6
         11
         //All should be numbers
         //The maximum sum path may or may not go through root.
 8
 9
         //For example, in the following binary tree, the maximum sum
         // is 27(3 + 6 + 9 + 0 - 1 + 10). Expected time complexity is O(n)
10
11
         // where n is the number of nodes in the given Binary Tree.
12
         11
                   -15
13
14
         11
15
                 / \ / \
16
               -8 1 3 9
17
18
         // 2 6 0 6 4
19
                / \
20
               0 10
         //Approach: Dynamic Programming
21
22
         Codeium: Refactor | Explain
         static class TreeNode {
23
24
             int val;
25
             TreeNode left;
26
             TreeNode right;
             TreeNode(int x) {
27
28
                 val = x;
29
30
31
          Cadaium Defector | Euplain | Concepts Isuadae | V
```



```
Codeium: Refactor | Explain | Generate Javadoc | X
         public static void main(String[] args) {
32
33
             TreeNode root = new TreeNode(-15);
34
             root.left = new TreeNode(5);
35
             root.right = new TreeNode(6);
36
             root.left.left = new TreeNode(-8);
37
             root.left.right = new TreeNode(1);
             root.right.left = new TreeNode(3);
38
39
             root.right.right = new TreeNode(9);
40
             root.left.left.left = new TreeNode(2);
             root.left.right.left = new TreeNode(6);
41
             root.left.right.right = new TreeNode(0);
42
             root.right.right.left = new TreeNode(6);
43
44
             root.right.right = new TreeNode(4);
45
             root.left.right.left.left = new TreeNode(0);
             root.left.right.left.right = new TreeNode(10);
46
             System.out.println(maxPathSum(root));
47
48
49
50
         static int max = Integer.MIN VALUE;
         Codeium: Refactor | Explain | Generate Javadoc | X
51
         public static int maxPathSum(TreeNode root) {
             if (root == null) {
52
53
                  return 0;
54
55
             maxPathSumUtil(root);
56
             return max;
57
58
```



```
Codeium: Refactor | Explain | Generate Javadoc | X
59
         public static int maxPathSumUtil(TreeNode root) {
60
             if (root == null) {
61
                  return 0;
62
63
             int left = Math.max(0, maxPathSumUtil(root.left));
64
             int right = Math.max(0, maxPathSumUtil(root.right));
65
66
             max = Math.max(max, left + right + root.val);
67
68
             return Math.max(left, right) + root.val;
69
70
71
72
         //Approach: Dynamic Programming
         Codeium: Refactor | Explain | X
         public static int maxPathSumDP(TreeNode root) {
73
74
             if (root == null) {
75
                 return 0;
76
77
             int[] max = new int[1];
78
79
             max[0] = Integer.MIN_VALUE;
             maxPathSumUtilDP(root, max);
80
             return max[0];
81
82
83
```



```
Codeium: Refactor | Explain | Generate Javadoc | X
84
         public static int maxPathSumUtilDP(TreeNode root, int[] max) {
85
              if (root == null) {
86
                  return 0;
87
88
              int left = Math.max(0, maxPathSumUtilDP(root.left, max));
89
90
              int right = Math.max(0, maxPathSumUtilDP(root.right, max));
91
92
              max[0] = Math.max(max[0], left + right + root.val);
93
94
              return Math.max(left, right) + root.val;
95
96
97
```



Here is the code written from the diagram along with an explanation, example, and output:

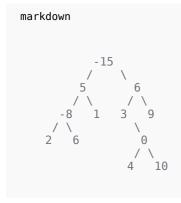
```
public class MaximumPathSumLeafToLeaf {
    // Definition of the TreeNode class
    static class TreeNode {
        int val;
        TreeNode left;
        TreeNode right;

        TreeNode(int x) {
            val = x;
        }
    }
    static int max = Integer.MIN_VALUE;
```



```
// Method to calculate the maximum path sum between two leaves
public static int maxPathSum(TreeNode root) {
   if (root == null) {
        return 0;
   maxPathSumUtil(root);
   return max;
// Helper method to calculate the maximum path sum
public static int maxPathSumUtil(TreeNode root) {
   if (root == null) {
       return 0;
   }
   int left = maxPathSumUtil(root.left); // Calculate left subtree sum
   int right = maxPathSumUtil(root.right); // Calculate right subtree sum
   // If both left and right children exist, update max
   if (root.left != null && root.right != null) {
       max = Math.max(max, left + right + root.val);
        return Math.max(left, right) + root.val;
   }
   // If one child is null, return sum including the non-null child
    return (root.left == null ? right : left) + root.val;
}
public static void main(String[] args) {
   TreeNode root = new TreeNode(-15):
   root.left = new TreeNode(5);
   root.right = new TreeNode(6);
    root.left.left = new TreeNode(-8);
    root.left.right = new TreeNode(1);
    root.right.left = new TreeNode(3);
   root.right.right = new TreeNode(9);
    root.left.left.left = new TreeNode(2);
    root.left.left.right = new TreeNode(6);
    root.right.right = new TreeNode(0);
    root.right.right.left = new TreeNode(4);
    root.right.right.right = new TreeNode(10);
   System.out.println(maxPathSum(root));
}
```

#### 1. Tree Structure:



#### 2. Maximum Path Sum:

- The maximum path sum is the highest sum of values between two leaves in the binary tree.
- In this case, the maximum path sum is obtained from the path `[3 -> 6 -> 9 -> 0 -> 10]` which gives `27`.

#### 3. **Algorithm**:

- The `maxPathSumUtil` function calculates the maximum path sum passing through each node.
- If the current node has both left and right children, the sum of the left and right subtree plus the node's value is compared to the global maximum (`max`).
- o If one child is null, only the path through the non-null child is considered.

#### 4. Steps:

- Calculate the path sums for each subtree recursively.
- Update the `max` variable whenever a higher path sum is found between two leaves.

## Output

The program outputs:

27



This is the maximum path sum between two leaves in the given binary tree.