## Given the basic architecture, the probability of any word can be written in the way shown below:

Dual Language Model

$$P[w' \mid w] = \begin{cases} P_1[w' \mid \langle \mathbf{s} \rangle] & \text{if } w' \in V_1 \\ P_2[w' \mid \langle \mathbf{s} \rangle] & \text{if } w' \in V_2 \\ 0 & \text{if } w' = \langle /\mathbf{s} \rangle \end{cases}$$
 for  $w = \langle \mathbf{s} \rangle$ 

$$P[w' \mid w] = \begin{cases} P_1[w' \mid w] & \text{if } w' \in \mathcal{V}_1 \cup \{\langle / \mathbf{s} \rangle \} \\ P_1[\langle \mathbf{s} \mathbf{w} \rangle \mid w] \cdot P_2[w' \mid \langle \mathbf{s} \mathbf{w} \rangle] & \text{if } w' \in \mathcal{V}_2 \end{cases} \qquad \text{for } w \in \mathcal{V}_1$$

$$P[w' \mid w] = \begin{cases} P_2[w' \mid w] & \text{if } w' \in \mathcal{V}_2 \cup \{\langle / \mathfrak{s} \rangle \} \\ P_2[\langle \mathfrak{sw} \rangle \mid w] \cdot P_1[w' \mid \langle \mathfrak{sw} \rangle] & \text{if } w' \in \mathcal{V}_1 \end{cases} \quad \text{for } w \in \mathcal{V}_2$$

## Dual Language Model

Given the basic architecture, the probability of any word can be written in the way shown below:

$$P[w' \mid w] = \begin{cases} P_1[w' \mid \langle \mathtt{s} \rangle] & \text{if } w' \in \mathrm{V}_1 \\ P_2[w' \mid \langle \mathtt{s} \rangle] & \text{if } w' \in \mathrm{V}_2 \\ 0 & \text{if } w' = \langle /\mathtt{s} \rangle \end{cases} \qquad \text{for } w = \langle \mathtt{s} \rangle$$

$$P[w'\mid w] = \begin{cases} P_1[w'\mid w] & \text{if } w' \in \mathcal{V}_1 \cup \{\langle/\mathfrak{s}\rangle\} \\ P_1[\langle \mathfrak{sw}\rangle \mid w] \cdot P_2[w'\mid \langle \mathfrak{sw}\rangle] & \text{if } w' \in \mathcal{V}_2 \end{cases} \qquad \text{for } w \in \mathcal{V}_1$$

$$P[w' \mid w] = \begin{cases} P_2[w' \mid w] & \text{if } w' \in \mathcal{V}_2 \cup \{\langle / \mathfrak{s} \rangle\} \\ P_2[\langle \mathfrak{sw} \rangle \mid w] \cdot P_1[w' \mid \langle \mathfrak{sw} \rangle] & \text{if } w' \in \mathcal{V}_1 \end{cases} \qquad \text{for } w \in \mathcal{V}_2$$

## FST for DLM