

Understanding and Implementing Image Denoising with DnCNN

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Introduction

Image denoising is the process of removing noise from images while preserving important structures like edges and textures. The Deep CNN-based Denoising (DnCNN) model has shown excellent performance for this task.

Mathematical Formulation

Let:

- x be the clean image
- n be the noise
- y be the noisy image

Then, $y = x + n$

The goal is to recover x given y .

DnCNN Model

DnCNN learns the residual noise $R(y)$, and recovers the image as:

$$x = y - R(y)$$

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Training minimizes the MSE loss:

$$L = (1/N) * \sum || R(y_i) - (y_i - x_i) ||^2$$

Network Architecture

- First layer: Conv + ReLU
- Middle layers: Conv + BatchNorm + ReLU
- Final layer: Conv

Example Convolution

Given a 3x3 patch and a 3x3 kernel:

Patch:

[0.2, 0.3, 0.4]

[0.1, 0.5, 0.6]

[0.0, 0.2, 0.3]

Kernel:

[-1, 0, 1]

[-2, 0, 2]

[-1, 0, 1]

Output = Sum(Patch * Kernel) = 1.5

After ReLU: max(0, 1.5) = 1.5

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Final Prediction

The model predicts noise for each pixel and subtracts it from the input image to get the clean image.

Citations

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[3] Buades, A., Coll, B., & Morel, J. M. (2005). A Non-Local Algorithm for Image Denoising. In 2005 IEEE Computer Society Conference on Computer Vision and Pattern Recognition (CVPR'05), Vol. 2, pp. 6065.

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