

VLSI Signal Processing Class Assignment

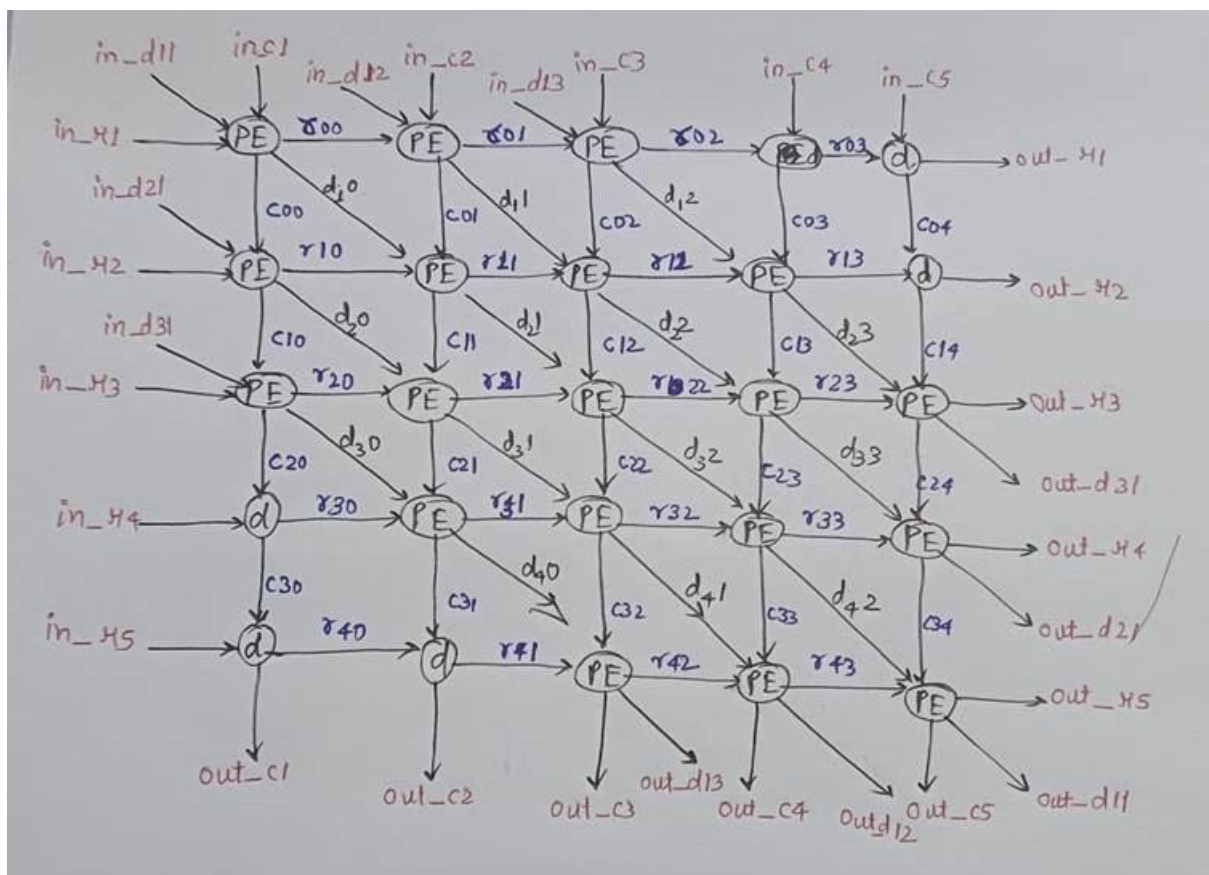
Systolic Multiplication

Submitted by:

Saurabh Kumar

SC22B146

Systolic array:



Verilog source code:

```
`timescale 1ns / 1ps
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// delay element
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```
module d(clk, in1, in2, out1, out2);
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    input clk;
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input [7:0] in1, in2;
output reg [7:0] out1, out2;

always @(posedge clk) begin
    out1 <= in1;
    out2 <= in2;
end

endmodule

// processing element
module pe(clk, in1, in2, in3, out1, out2, out3);
    input clk;
    input [7:0] in1, in2, in3;
    output reg [7:0] out1, out2, out3;

    always @(posedge clk) begin
        out1 <= in1;
        out2 <= in2;
        out3 <= (in1 * in2) + in3;
    end
endmodule

// systolic array
module array(clk, in_c1, in_c2, in_c3, in_c4, in_c5,
             in_r1, in_r2, in_r3, in_r4, in_r5,
             in_d11, in_d12, in_d13, in_d21, in_d31,
             out_c1, out_c2, out_c3, out_c4, out_c5,
             out_r1, out_r2, out_r3, out_r4, out_r5,
             out_d11, out_d12, out_d13, out_d21, out_d31);
    input clk;
    input [7:0] in_c1, in_c2, in_c3, in_c4, in_c5,
               in_r1, in_r2, in_r3, in_r4, in_r5,
               in_d11, in_d12, in_d13, in_d21, in_d31;
    output [7:0] out_c1, out_c2, out_c3, out_c4, out_c5,
               out_r1, out_r2, out_r3, out_r4, out_r5,
               out_d11, out_d12, out_d13, out_d21, out_d31;

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wire [7:0] wire_c[0:3][0:4];
wire [7:0] wire_r[0:4][0:3];
wire [7:0] wire_d1[0:2];
wire [7:0] wire_d2[0:3];
wire [7:0] wire_d3[0:3];
wire [7:0] wire_d4[0:2];

// row1
pe pe11(clk, in_c1, in_r1, in_d11, wire_c[0][0], wire_r[0][0], wire_d1[0]);
pe pe12(clk, in_c2, wire_r[0][0], in_d12, wire_c[0][1], wire_r[0][1], wire_d1[1]);
pe pe13(clk, in_c3, wire_r[0][1], in_d13, wire_c[0][2], wire_r[0][2], wire_d1[2]);
d d14(clk, in_c4, wire_r[0][2], wire_c[0][3], wire_r[0][3]);
d d15(clk, in_c5, wire_r[0][3], wire_c[0][4], out_r1);

// row2
pe pe21(clk, wire_c[0][0], in_r2, in_d21, wire_c[1][0], wire_r[1][0], wire_d2[0]);
pe pe22(clk, wire_c[0][1], wire_r[1][0], wire_d1[0], wire_c[1][1], wire_r[1][1], wire_d2[1]);
pe pe23(clk, wire_c[0][2], wire_r[1][1], wire_d1[1], wire_c[1][2], wire_r[1][2], wire_d2[2]);
pe pe24(clk, wire_c[0][3], wire_r[1][2], wire_d1[2], wire_c[1][3], wire_r[1][3], wire_d2[3]);
d d25(clk, wire_c[0][4], wire_r[1][3], wire_c[1][4], out_r2);

// row3
pe pe31(clk, wire_c[1][0], in_r3, in_d11, wire_c[2][0], wire_r[2][0], wire_d3[0]);
pe pe32(clk, wire_c[1][1], wire_r[2][0], wire_d2[0], wire_c[2][1], wire_r[2][1], wire_d3[1]);
pe pe33(clk, wire_c[1][2], wire_r[2][1], wire_d2[1], wire_c[2][2], wire_r[2][2], wire_d3[2]);
pe pe34(clk, wire_c[1][3], wire_r[2][2], wire_d2[2], wire_c[2][3], wire_r[2][3], wire_d3[3]);
pe pe35(clk, wire_c[1][4], wire_r[2][3], wire_d2[3], wire_c[2][4], out_r3, out_d31 );

// row4
d d41(clk, wire_c[2][0], in_r4, wire_c[3][0], wire_r[3][0]);
pe pe42(clk, wire_c[2][1], wire_r[3][0], wire_d3[0], wire_c[3][1], wire_r[3][1], wire_d4[0]);
pe pe43(clk, wire_c[2][2], wire_r[3][1], wire_d3[1], wire_c[3][2], wire_r[3][2], wire_d4[1]);
pe pe44(clk, wire_c[2][3], wire_r[3][2], wire_d3[2], wire_c[3][3], wire_r[3][3], wire_d4[2]);
pe pe45(clk, wire_c[2][4], wire_r[3][3], wire_d3[3], wire_c[3][4], out_r4, out_d21);

// row5

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d d51(clk, wire_c[3][0], in_r5, out_c1, wire_r[4][0]);
d d52(clk, wire_c[3][1], wire_r[4][0], out_c2, wire_r[4][1]);
pe pe53(clk, wire_c[3][2], wire_r[4][1], wire_d4[0], out_c3, wire_r[4][2], out_d13);
pe pe54(clk, wire_c[3][3], wire_r[4][2], wire_d4[1], out_c4, wire_r[4][3], out_d12);
pe pe55(clk, wire_c[3][4], wire_r[4][3], wire_d4[2], out_c5, out_r5, out_d11);
endmodule

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Verilog TestBench:

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`timescale 1ns / 1ps

module dut;
    reg clk;

    reg [7:0] in_c1, in_c2, in_c3, in_c4, in_c5,
              in_r1, in_r2, in_r3, in_r4, in_r5,
              in_d11, in_d12, in_d13, in_d21, in_d31;
    wire [7:0] out_c1, out_c2, out_c3, out_c4, out_c5,
              out_r1, out_r2, out_r3, out_r4, out_r5,
              out_d11, out_d12, out_d13, out_d21, out_d31;

    array array1(clk, in_c1, in_c2, in_c3, in_c4, in_c5,
                 in_r1, in_r2, in_r3, in_r4, in_r5,
                 in_d11, in_d12, in_d13, in_d21, in_d31,
                 out_c1, out_c2, out_c3, out_c4, out_c5,
                 out_r1, out_r2, out_r3, out_r4, out_r5,
                 out_d11, out_d12, out_d13, out_d21, out_d31);

    initial begin
        clk <= 0;

        in_c1 <= 8'h2;
        in_c2 <= 8'h3;
        in_c3 <= 8'h4;
        in_c4 <= 8'h0;
        in_c5 <= 8'h0;

        in_r1 <= 8'h1;

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in_r2 <= 8'h2;
in_r3 <= 8'h3;
in_r4 <= 8'h0;
in_r5 <= 8'h0;

in_d11 <= 8'h0;
in_d12 <= 8'h0;
in_d13 <= 8'h0;
in_d21 <= 8'h0;
in_d31 <= 8'h0;
end

always begin
    #5 clk <= ~clk;
end

always @(posedge clk) begin

    #5    in_c1 <= 8'h0;           #20    in_c1 <= 8'h0;           #35    in_c1 <= 8'h0;
        in_c2 <= 8'h4;           in_c2 <= 8'h0;           in_c2 <= 8'h0;
        in_c3 <= 8'h5;           in_c3 <= 8'h0;           in_c3 <= 8'h0;
        in_c4 <= 8'h6;           in_c4 <= 8'h0;           in_c4 <= 8'h0;
        in_c5 <= 8'h0;           in_c5 <= 8'h0;           in_c5 <= 8'h0;

        in_r1 <= 8'h0;           in_r1 <= 8'h0;           in_r1 <= 8'h0;
        in_r2 <= 8'h2;           in_r2 <= 8'h0;           in_r2 <= 8'h0;
        in_r3 <= 8'h3;           in_r3 <= 8'h0;           in_r3 <= 8'h0;
        in_r4 <= 8'h4;           in_r4 <= 8'h0;           in_r4 <= 8'h0;
        in_r5 <= 8'h0;           in_r5 <= 8'h0;           in_r5 <= 8'h0;

        in_d11 <= 8'h0;           in_d11 <= 8'h0;           in_d11 <= 8'h0;
        in_d12 <= 8'h0;           in_d12 <= 8'h0;           in_d12 <= 8'h0;
        in_d13 <= 8'h0;           in_d13 <= 8'h0;           in_d13 <= 8'h0;
        in_d21 <= 8'h0;           in_d21 <= 8'h0;           in_d21 <= 8'h0;
        in_d31 <= 8'h0;           in_d31 <= 8'h0;           in_d31 <= 8'h0;

    #10    in_c1 <= 8'h0;           #25    in_c1 <= 8'h0;           #40    in_c1 <= 8'h0;
        in_c2 <= 8'h0;           in_c2 <= 8'h0;           in_c2 <= 8'h0;

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	in_c3 <= 8'h5;		in_c3 <= 8'h0;		in_c3 <= 8'h0;
	in_c4 <= 8'h6;		in_c4 <= 8'h0;		in_c4 <= 8'h0;
	in_c5 <= 8'h7;		in_c5 <= 8'h0;		in_c5 <= 8'h0;
	in_r1 <= 8'h0;		in_r1 <= 8'h0;		in_r1 <= 8'h0;
	in_r2 <= 8'h0;		in_r2 <= 8'h0;		in_r2 <= 8'h0;
	in_r3 <= 8'h3;		in_r3 <= 8'h0;		in_r3 <= 8'h0;
	in_r4 <= 8'h4;		in_r4 <= 8'h0;		in_r4 <= 8'h0;
	in_r5 <= 8'h5;		in_r5 <= 8'h0;		in_r5 <= 8'h0;
	in_d11 <= 8'h0;		in_d11 <= 8'h0;		in_d11 <= 8'h0;
	in_d12 <= 8'h0;		in_d12 <= 8'h0;		in_d12 <= 8'h0;
	in_d13 <= 8'h0;		in_d13 <= 8'h0;		in_d13 <= 8'h0;
	in_d21 <= 8'h0;		in_d21 <= 8'h0;		in_d21 <= 8'h0;
	in_d31 <= 8'h0;		in_d31 <= 8'h0;		in_d31 <= 8'h0;
#15	in_c1 <= 8'h0;	#30	in_c1 <= 8'h0;	#45	in_c1 <= 8'h0;
	in_c2 <= 8'h0;		in_c2 <= 8'h0;		in_c2 <= 8'h0;
	in_c3 <= 8'h0;		in_c3 <= 8'h0;		in_c3 <= 8'h0;
	in_c4 <= 8'h0;		in_c4 <= 8'h0;		in_c4 <= 8'h0;
	in_c5 <= 8'h0;		in_c5 <= 8'h0;		in_c5 <= 8'h0;
	in_r1 <= 8'h0;		in_r1 <= 8'h0;		in_r1 <= 8'h0;
	in_r2 <= 8'h0;		in_r2 <= 8'h0;		in_r2 <= 8'h0;
	in_r3 <= 8'h0;		in_r3 <= 8'h0;		in_r3 <= 8'h0;
	in_r4 <= 8'h0;		in_r4 <= 8'h0;		in_r4 <= 8'h0;
	in_r5 <= 8'h0;		in_r5 <= 8'h0;		in_r5 <= 8'h0;
	in_d11 <= 8'h0;		in_d11 <= 8'h0;		in_d11 <= 8'h0;
	in_d12 <= 8'h0;		in_d12 <= 8'h0;		in_d12 <= 8'h0;
	in_d13 <= 8'h0;		in_d13 <= 8'h0;		in_d13 <= 8'h0;
	in_d21 <= 8'h0;		in_d21 <= 8'h0;		in_d21 <= 8'h0;
	in_d31 <= 8'h0;		in_d31 <= 8'h0;		in_d31 <= 8'h0;

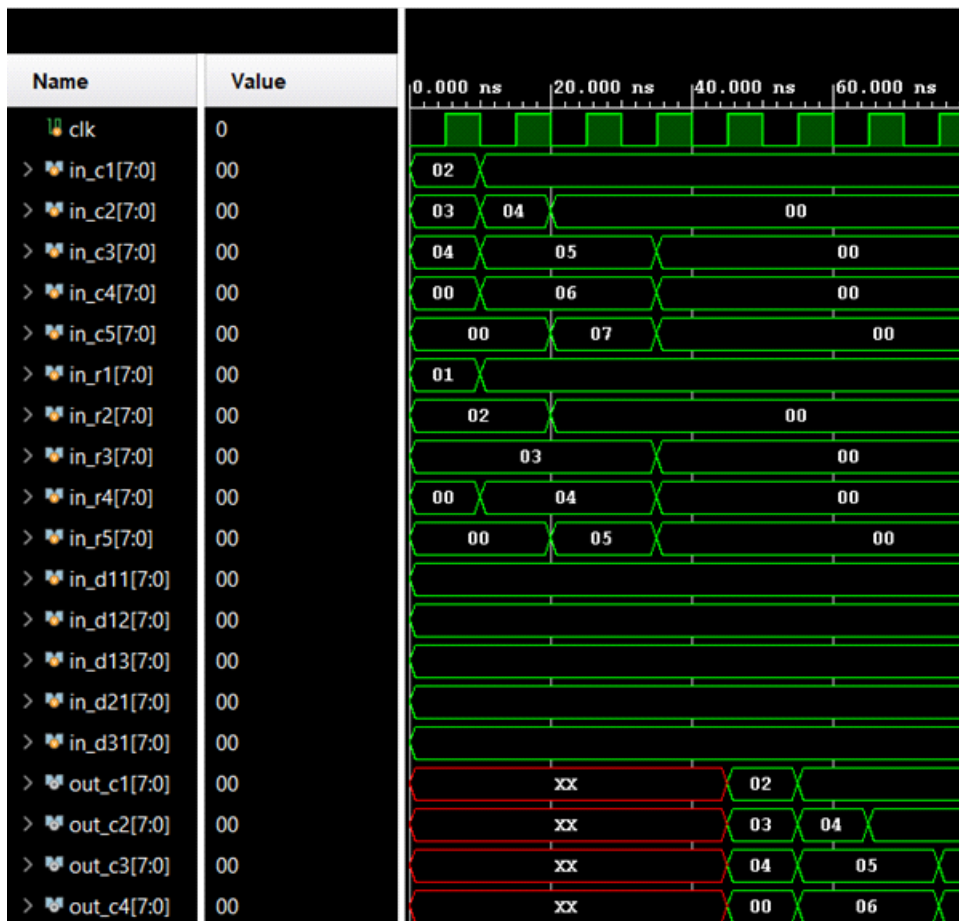
end

endmodule

$$\begin{pmatrix} 1 & 2 & 3 \\ 2 & 3 & 4 \\ 3 & 4 & 5 \end{pmatrix} \begin{pmatrix} 2 & 4 & 5 \\ 3 & 5 & 6 \\ 4 & 6 & 7 \end{pmatrix} = \begin{pmatrix} 20 & 32 & 38 \\ 29 & 47 & 56 \\ 38 & 62 & 74 \end{pmatrix}_{10} = \begin{pmatrix} 14 & 20 & 26 \\ 1d & 2f & 38 \\ 26 & 3e & 4a \end{pmatrix}_{16}$$

Handwritten annotations show the calculation of the second matrix element (47) as $2 \times 3 + 3 \times 4 + 4 \times 5 = 6 + 12 + 20 = 38$ (labeled 20, 32, 38). The final result is shown in hexadecimal: $\begin{pmatrix} 14 & 20 & 26 \\ 1d & 2f & 38 \\ 26 & 3e & 4a \end{pmatrix}_{16}$. Red arrows point from the hexadecimal values to labels d_{31} , d_{2f} , d_{13} , d_{12} , and d_{11} .

Simulation:



> out_c5[7:0]	00	xx	00	07
> out_r1[7:0]	00	xx	01	
> out_r2[7:0]	00	xx	02	
> out_r3[7:0]	00	xx	03	
> out_r4[7:0]	00	xx	00	04
> out_r5[7:0]	00	xx	00	05
> out_d11[7:0]	00	xx	14	2f 4a
> out_d12[7:0]	00	xx	1d	3e
> out_d13[7:0]	00	xx	26	
> out_d21[7:0]	00	xx	20	38
> out_d31[7:0]	00	xx	26	