# Homework-3 AV221-Semiconductor Devices

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Derive the expression for the built-in rollage of p-ndiode.

FC P-n junction Ev

Built-in voltage,  $V_{bi} = |\Delta V_{fp}| + |\Delta V_{fn}|$ Using  $n_o = n_i \exp\left(\frac{E_f - E_{fi}}{kT}\right)$ 

and, ▲ eav<sub>fp</sub>= E<sub>fi</sub>-E<sub>f</sub> eav<sub>fn</sub>= E<sub>f</sub>-E<sub>fi</sub>

=> no= ni exp( e Min)

⇒ DVfn = KT en (no)

Similarly,

Po= Reniemp (Fi-Ef)
= niemp (eaufp)
KT)

=> avfp= KT (n (to)

:.  $V_{bi} = \frac{KT}{e} \ln \left( \frac{n_0 p_0}{n_1 i^2} \right)$ Take  $n_0 = N_D \notin p_0 = N_A$ , e = q  $\Rightarrow V_{bi} = \frac{KT}{q} \ln \left( \frac{N_0 N_D}{n_1 i^2} \right)$ 

2 Derive the expression for the depletion widths along n-sider and p-sider of p-n junction.

3

$$\frac{d^2 \phi(x)}{dx^2} = -\frac{f(x)}{\epsilon_s} = -\frac{dE(x)}{dx}, \quad \phi(x) : \text{ Electric field }$$

f(n): volume charge density. Es: permittivity of semiconductor

$$f(x) = -eNA$$
,  $-xp < x < D$   
 $f(x) = eND$ ,  $0 < x < Xn$ 

Electric field for p-region.

Imilarly for n-Hegion,

By O and (1),

totantial in p-region,

As 
$$V_1(x) = 0$$
 at  $x = -34p \Rightarrow G = \frac{eN_1}{2G_5}x_p^2$ 

Cotential in n-region,

$$\frac{V_2(x) = \int \frac{e^{ND}}{6s} \left(x_n - x_1\right) dx}{6s} = \frac{e^{ND}}{6s} \left(x_n x - \frac{x^2}{2}\right) + c}$$

As 
$$V_2(x) = 0$$
 at  $x = 0 \Rightarrow V_1(x) = V_2(x) \Rightarrow G = C_2$ 

At 
$$x = x_n$$
,  $v_2(x_1 = v_b)$ 

$$\Rightarrow v_{bi} = \frac{e}{2\epsilon_s} \left( N_D x_n^2 + N_A x_p^2 \right) - (iii)$$

Using (ii)  $4(iii)$ ,
$$v_{bi} = \frac{e}{2\epsilon_s} \left( N_D \frac{x_p^2 N_A^2}{N_D^2} + N_A x_p^2 \right)$$

$$\Rightarrow x_p^2 = 2\epsilon_s \frac{v_b}{e} \left( \frac{N_A^2 + N_A}{N_D} + \frac{2\epsilon_s v_{bi}}{N_A} \frac{N_B}{N_A} \left( \frac{1}{N_A + N_D} \right) \right)$$

Similarly,
$$x_n = \sqrt{2\epsilon_s v_{bi}} \cdot \frac{N_A}{N_D} \left( \frac{1}{N_A + N_D} \right)$$

3 setting stating all the assumptions, derive the shockley diode equation. Som By Boltzmann's expression,

$$V_{bi} = \frac{kT}{9} \ln \left( \frac{N_A N_D}{\gamma_{i}^2} \right)$$

Assuming complete ionization, nno ND, Nn ~ Pro.

Applying fortward voltage V, Vbi - Vbi - V,  $n_p = n_n exp \left( \frac{e(Vbi-V)}{KT} \right) = n_n exp \left( \frac{eVbi}{KT} \right) exp \left( \frac{eV}{KT} \right)$ 

⇒ np=npoenp(ev), nno ≈ constant for low-level injection. Similarly for holes,

Using continuity eqn, dhe - Pr wat - up & dh + sp de Pr + Sip - Pr-Pro. At steady state din =0 1=0 for no electric field applied. Gin= o for reo generation => de Profet = Pro-mo => Pn-mo = k1 exp ( 550p ) + k2 Applying boundary conditions, At x= m, Pn (m) = Pno exp (qv) At x(-)00, Pn (00)= Pno. X=Mn => Pro exp(QN)-Pro= K1 exp (-X) => KI= Pno (exp (AV) -1 (exp (Xn) : Pn(x) = Pno + Pno (exp(av )-1) exp (xn-x). Now, Jp= -9.Dp dkn(x) = -9Dp Pno Fext (2V)-1]exp (2n-x) (-1) | x=1/n = -9 Pp. Pno exp(2V)-1]. Similarly, Jn= -9 Dn. npo [exp(qv)-1]. : Itotal = I = Ip + In = [exp {av } -1] [ QA ( Dp. Pno + Dn npo) Ln : [I = Io [exp(av)-1]].

# Homework-3

4. For a Silicon p–n junction, the p-side has a doping density of 10^(16)/cm3, and the n-side has a doping density of 10^(17)/cm3. Plot the charge density, electric field, electric potential and depletion regions on both p and n side. You can use Matlab, Mathematica or any programming language of your choice to generate the plots. For any missing parameters, refer your text book.

Given values:

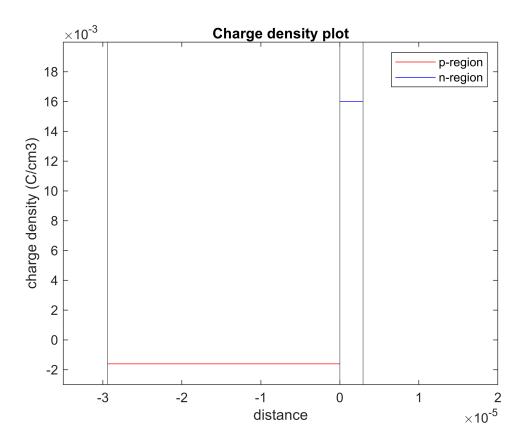
```
Na = power(10,16); % acceptor atom concentration (in /cm3)
Nd = power(10,17); % donor atom concentration (in /cm3)
Ni = 1.5 * power(10,10); % intrinsic carrier concentration (in /cm3)
Vt = 0.0253; % thermal voltage in volts
e = 1.6 * power(10,-19); % charge of electron in coulomb
epsilonNot = 8.85 * power(10,-14); % permittivity of free space
epsilon = 11.68 * epsilonNot; % permittivity of siliconlegend("Position",
[0.6,0.8,0.1,0.1]);
```

## Calculating variables

```
% built-in voltage
Vbi = Vt * log( (Na*Nd)/(Ni*Ni) );
% depletion region dimensions
Xp = power( ( (2*epsilon*Vbi*Nd)/(e*Na*(Na + Nd)) ), 0.5); % p-side
Xn = power( ( (2*epsilon*Vbi*Na)/(e*Nd*(Na + Nd)) ), 0.5); % n-side
% range of regions of depletion region
x1 = linspace(-Xp,0,1000);
x2 = linspace(0,Xn,1000);
```

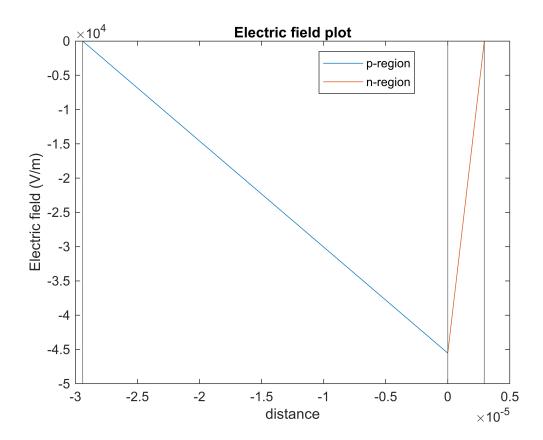
#### Charge density calculation

```
% charge density of depletion region
rhoP = ones(1,1000)* (-1*e*Na); % n-side charge density
rhoN = ones(1,1000)* (e*Nd); % p-side charge density
plot(x1,rhoP,"r");
hold on
plot(x2,rhoN,"b");
xline(0); xline(-Xp); xline(Xn);
hold off
title("Charge density plot"); xlabel("distance"); ylabel("charge density (C/cm3)");
legend("p-region","n-region");
xlim([-3.5*0.00001 2*0.00001]); ylim([-3*0.001 20*0.001]);
```



## Electric field calculation

```
% Electric field of depletion region
Ep = -e*Na*(x1+ Xp)/epsilon;
En = -e*Nd*(Xn - x2)/epsilon;
plot(x1,Ep);
hold on
plot(x2,En);
hold off
xline(0); xline(-Xp); xline(Xn);
title("Electric field plot"); xlabel("distance"); ylabel("Electric field (V/m)");
legend("p-region", "n-region"); legend("Position", [0.6,0.8,0.1,0.1]);
```



## **Electric Potential Calculation**

```
% Electric potential of depletion region
Vp = 10000*e*Na*power( (x1+Xp),2)/(2*epsilon);
Vn = 10000*(e/epsilon)*( (Nd*((Xn*x2) - (x2.*x2)/2) ) + (Na*Xp*Xp/2));
plot(x1,Vp);
hold on
plot(x2,Vn);
hold off
xline(0); xline(-Xp); xline(Xn);
title("Electric Potential plot"); xlabel("distance"); ylabel("electric potential (V)");
legend("p-region", "n-region"); legend("Position", [0.6,0.8,0.1,0.1]);
```

