

Assignment -1: MOSFET DC Circuits

Av211: Analog Electronics Circuits

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SC22B146

- ① A particular n-channel MOSFET is measured to have a drain current of 0.4 mA at $V_{GS} = V_{DS} = 1 \text{ V}$ and of 0.1 mA at $V_{GS} = V_{DS} = 0.8 \text{ V}$. What are the values of K_n and V_{th} for this device?

Soln: For n-channel MOSFET,

$$I_D = K_n \left[(V_{GS} - V_{th}) V_{DS} - \frac{1}{2} V_{DS}^2 \right]$$

From given values,

$$0.4 \times 10^{-3} = K_n \left[(1 - V_{th}) \cdot 1 - \frac{1}{2} \right] \quad \text{--- (i)}$$

and,

$$0.1 \times 10^{-3} = K_n \left[(0.8 - V_{th}) \cdot 0.8 - \frac{1}{2} (0.8)^2 \right] \quad \text{--- (ii)}$$

Dividing (i)/(ii),

$$\Rightarrow 4 = \frac{(1 - V_{th}) - \frac{1}{2}}{(0.8 - V_{th}) \cdot 0.8 - 0.32} = \frac{0.5 - V_{th}}{0.32 - 0.8 V_{th}}$$

$$\Rightarrow 1.28 - 3.2 V_{th} = 0.5 - V_{th}$$

$$\Rightarrow 0.78 = 2.2 V_{th}$$

$$\Rightarrow V_{th} = \frac{0.78}{2.2} \approx \underline{0.35 \text{ V}}$$

$$\text{①} \Rightarrow 0.4 \times 10^{-3} = K_n [0.5 - 0.35]$$

$$\Rightarrow K_n = \underline{2.67 \text{ mA/V}^2}$$

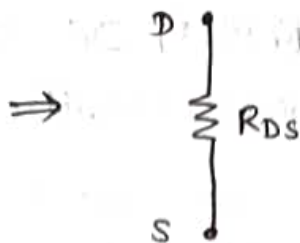
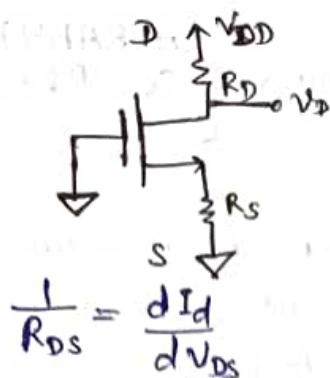
$$\therefore K_n = 2.67 \text{ mA/V}^2, V_{th} \approx 0.35 \text{ V.}$$

- ② An NMOS transistor, fabricated with $W = 20 \mu\text{m}$ and $L = 1 \mu\text{m}$ in a technology for which $K_n = 100 \mu\text{A/V}^2$ and $V_{th} = 0.8 \text{ V}$, is to be operated at very low values of V_{DS} as a linear resistor. For V_{GS} varying from 1.0 V to 4.8 V , what range of transistor resistor values can be obtained? What is the available range if (a) the device width is halved?

(b) the device length is halved?

(c) both the width and length are halved?

Soln:



$$\frac{1}{R_{DS}} = \frac{dI_D}{dV_{DS}}$$

$$= \frac{\mu_n C_{ox} (W/L) \left[(V_{GS} - V_{TH}) V_{DS} - \frac{1}{2} V_{DS}^2 \right]}{V_{DS}} \quad (\text{As } V_{DS} \text{ is very small})$$

$$= \mu_n C_{ox} \left(\frac{W}{L} \right) (V_{GS} - V_{TH})$$

$$\text{For } V_{GS} = 1V, \quad \frac{1}{R_{DS}} = 100 \times 10^{-6} (1 - 0.8) = 2 \times 10^{-5} \Omega^{-1} \Rightarrow R_{DS} = 50 k\Omega$$

$$\text{For } V_{GS} = 4.8V, \quad \frac{1}{R_{DS}} = 100 \times 10^{-6} (4.8 - 0.8) = 4 \times 10^{-4} \Omega^{-1} \Rightarrow R_{DS} = 2.5 k\Omega$$

\therefore Range of resistor $R_{DS} \rightarrow 2.5 k\Omega$ to $50 k\Omega$.

$$\textcircled{a} \quad R_{DS} = \frac{L}{\mu_n C_{ox} W} \cdot \frac{1}{(V_{GS} - V_{TH})}$$

$$\Rightarrow R_{DS} \propto \frac{1}{W}$$

If the device width is halved, R_{DS} will be doubled.

\therefore Range of $R_{DS} \rightarrow 5 k\Omega$ to $100 k\Omega$.

$$\textcircled{b} \quad R_{DS} \propto L$$

If the length is halved, R_{DS} will become half.

\therefore Range of $R_{DS} \rightarrow 1.25 k\Omega$ to $25 k\Omega$.

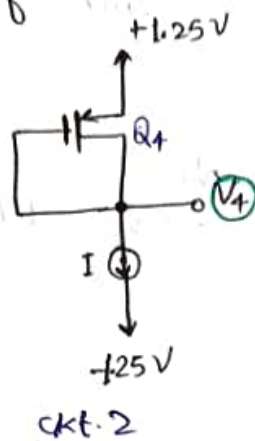
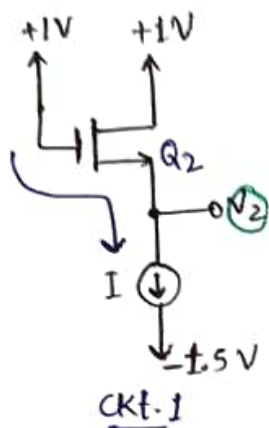
$$\textcircled{c} \quad R_{DS} \propto \frac{L}{W} \Rightarrow R_{DS_0} = \frac{L_0}{W_0} \cdot K_0$$

$$R'_{DS} = \frac{L'}{W'} \cdot K_0 \Rightarrow R'_{DS} = \frac{L_0/2}{W_0/2} \cdot K_0 = \frac{L_0}{W_0} \cdot K_0 = R_{DS_0}$$

If both length and R_{DS} are halved, there will be no change in R_{DS} .

\therefore Range of $R_{DS} \rightarrow 2.5 k\Omega$ to $50 k\Omega$.

③ Find the indicated voltages of the circuits if $|V_t| = 0.5 \text{ V}$ and $I = 0.1 \text{ mA}$. How large a resistor can be inserted in series with each drain while maintaining saturation? If the current source I requires at least 0.5 V between its terminal to operate properly, what is the largest resistor that can be placed in series with each MOSFET source while ensuring saturated-mode of operation of each transistor at $I_D = I$?

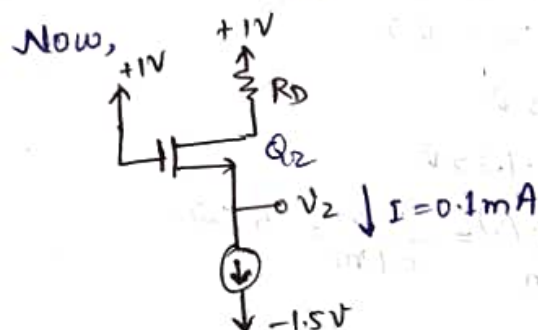


Soln: For ckt. 1, for no resistor inserted

~~$V_2 = -1.5 \text{ V}$~~

Similarly for ckt. 2,

$V_4 = -1.25 \text{ V}$



As $V_t = 0.5 \text{ V}$

$V_2 = -1.5 - 0.5 = -2 \text{ V}$

and,

$1 - I_D R_D - V_{DS} = V_2$

$\Rightarrow V_{DS} = 3 - I_D R_D$

For saturation,

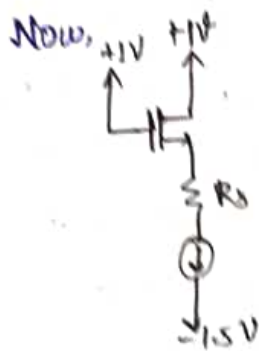
$V_{DS} = V_{GS} - V_{th}$

$= 1 - (-2) - 0.5$

$= 2.5 \text{ V}$

$\therefore 3 - I_D R_D = 2.5$

$\Rightarrow I_D R_D = 3 - 2.5 = 0.5 \text{ V} \Rightarrow R_D = \frac{0.5 \text{ V}}{0.1 \text{ mA}} = 5 \text{ k}\Omega$



$$V_{GS} \geq V_{TH}$$

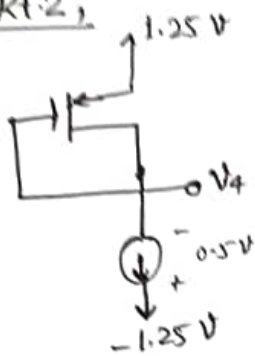
$$\Rightarrow 1 - V_{GS} - I_D R_D + 0.5 = -1.5$$

$$\Rightarrow 1 - 0.5 - I_D R_D + 0.5 = -1.5$$

$$\Rightarrow I_D R_D = 2.5 \text{ V}$$

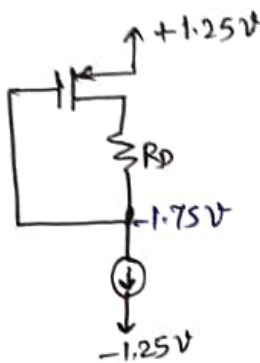
$$\Rightarrow R_D = \frac{2.5 \text{ V}}{0.1 \text{ mA}} = 25 \text{ k}\Omega$$

For ckt. 2,



$$V_G + 0.5 = -1.25 \text{ V}$$

$$\Rightarrow V_G = -1.75 \text{ V}$$



$$V_{GS} = -1.75 \text{ V}$$

$$\therefore V_{SG} = 1.25 + 1.75 = 3 \text{ V}$$

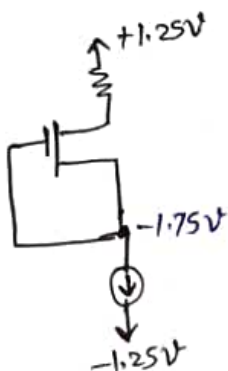
For saturation,

$$V_{SD} \geq V_{SG} - |V_{TH}|$$

$$\Rightarrow 1.25 - V_D \geq 3 - 0.5$$

$$\Rightarrow V_D \leq -1.25 \text{ V}$$

$$\therefore V_{Dmax} = -1.25 \text{ V}$$



$$\Rightarrow R_{Dmax} = \frac{-1.25 - (-1.75)}{0.1 \text{ mA}} = \frac{0.5}{0.1 \text{ mA}} = 5 \text{ k}\Omega$$

$$V_{GS} = -1.75 \text{ V}$$

For $V_{SG} \geq |V_{TH}|$

$$\Rightarrow V_S + 1.75 \geq 0.5$$

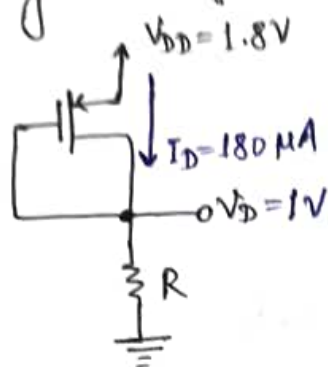
$$\Rightarrow V_S \geq -1.25 \text{ V}$$

$$\Rightarrow V_S = -1.25 \text{ V}$$

$$\therefore R_S = \frac{1.25 + 1.25 \text{ V}}{0.1 \text{ mA}} = 25 \text{ k}\Omega$$

⑤

- ④ The PMOS transistor in the circuit shown below has $V_t = -0.5\text{ V}$, $\mu_p C_{ox} = 100\text{ }\mu\text{A/V}^2$, $L = 0.18\text{ }\mu\text{m}$ and $\lambda = 0$. Find the values required for W and R in order to establish a drain current of $180\text{ }\mu\text{A}$ and a voltage V_D of 1 V .



Soln: $R = \frac{V_D - 0}{I_D}$

$$= \frac{1 - 0}{180\text{ }\mu\text{A}} = 5.55 \times 10^3 \Omega$$

$$= \underline{5.55\text{ k}\Omega}$$

As $V_{SD} (= 0.8\text{ V}) \geq V_{SG} - |V_{tp}|$
 $(= 0.8 - 0.5 = 0.3\text{ V})$,
 the device is in saturation region.

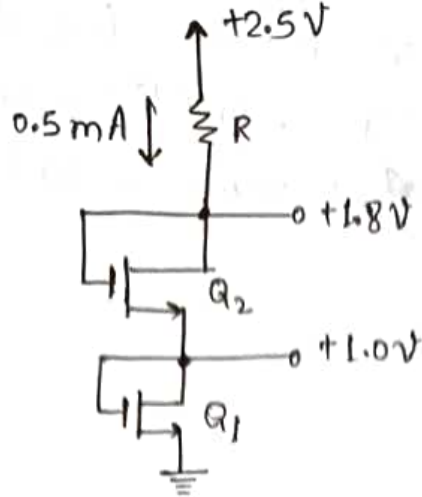
$$\therefore I_D = \frac{K_p}{2} \left(\frac{W}{L}\right) (V_{SG} - |V_{tp}|)^2$$

$$\Rightarrow 180 \times 10^{-6} = \frac{100 \times 10^{-6}}{2} \times \left(\frac{W}{0.18 \times 10^{-6}}\right) (0.8 - 0.5)^2$$

$$\Rightarrow W = \frac{180 \times 0.36}{100 \times 0.09} \mu\text{m}$$

$$\Rightarrow W = \underline{7.2\text{ }\mu\text{m}}$$

- ⑤ The NMOS transistors in the circuit shown below have $V_t = 0.5\text{ V}$, $\mu_n C_{ox} = 250\text{ }\mu\text{A/V}^2$, $\lambda = 0$ and $L_1 = L_2 = 0.25\text{ }\mu\text{m}$. Find the required values of gate width for each Q_1 and Q_2 , and the value of R , to obtain the voltage and current values indicated.



Soln: $R = \frac{2.5V - 1.8V}{0.5mA} = 1.4k\Omega$

For Q2: As $V_{DS} (= 0.8V) \geq V_{GS} - V_{TH} (= 0.8 - 0.5 = 0.3V)$,

$$I_D = \frac{\mu_n C_{ox}}{2} \left(\frac{W_2}{L_2} \right) (V_{GS} - V_{TH})^2$$

$$\Rightarrow 0.5 \times 10^{-3} = \frac{250 \times 10^{-6}}{2} \times \frac{W_2 \times 10^{-6}}{0.25 \times 10^{-6}} (0.8 - 0.5)^2$$

$$\Rightarrow W_2 = \frac{10}{0.09} \times 10^{-6} = 11.11 \mu m$$

For Q1: $V_{DS} (= 1V) \geq V_{GS} - V_{TH}$
($1V - 0.5V = 0.5V$)

$$I_D = \frac{\mu_n C_{ox}}{2} \left(\frac{W_1}{L_1} \right) (V_{GS} - V_{TH})^2$$

$$\Rightarrow 0.5m = \frac{250 \mu}{2} \left(\frac{W_1}{0.25 \mu} \right) (1 - 0.5)^2$$

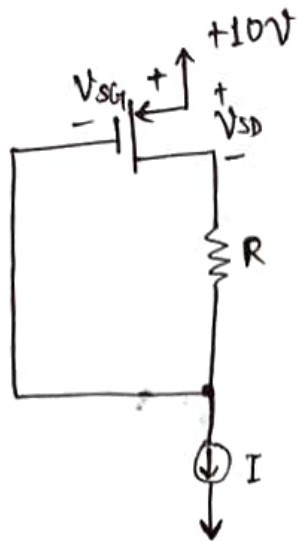
$$\Rightarrow W_1 = \frac{2}{0.5} \mu = 4 \mu m$$

$$\therefore R = 1.4k\Omega, W_1 = 4\mu m, W_2 = 11.11\mu m$$

⑥ For the circuit shown below,

① Show that for the PMOS transistor to be in saturation, the following condition must be satisfied: $IR \leq |V_{tp}|$.

② If the transistor is specified to have $|V_{tp}| = 1V$ and $k_p = 0.2mA/V^2$, and for $I = 0.1mA$, find the voltages V_{SD} and V_{SG} for $R = 10k\Omega$ and $100k\Omega$.



Soln: For the PMOS transistor to be in the saturation region,

$$V_{SD} \geq V_{SG} - |V_{th}|$$

$$\Rightarrow V_S - V_D \geq V_S - V_G - |V_{th}|$$

$$\Rightarrow |V_{th}| \geq V_D - V_G$$

$$\Rightarrow |V_{th}| \geq IR \quad (\because V_D - V_G = IR)$$

⑥ As $|V_{th}| = 1V \geq IR$ ($= 0.1 \times 10^{-3} \times 10 \times 10^3 = 1V$) for $R = 10K\Omega$, the device is in saturation region.

$$\therefore I_D = \frac{K_P}{2} (V_{SG} - |V_{th}|)^2$$

$$\Rightarrow 0.1mA = \frac{0.2mA}{2} (V_{SG} - 1)^2$$

$$\Rightarrow V_{SG} - 1 = \pm 1$$

$$\Rightarrow V_{SG} = 0 \text{ or } 2$$

$$\Rightarrow V_{SG} = 2V \quad (\because V_S \neq V_G)$$

For $R = 10K\Omega$

$$V_{SD} = V_{SG} - V_{DG}$$

$$= V_{SG} - IR$$

$$= 2 - (0.1 \times 10^{-3} \times 10 \times 10^3)$$

$$= 2 - 1$$

$$= 1V$$

For $R = 100K\Omega$

$$V_{SD} = V_{SG} - IR$$

$$= 2 - (0.1 \times 10^{-3} \times 100 \times 10^3)$$

$$= 2 - 10$$

$$= -8V$$

$$I_D = \frac{K_P}{2} (V_{SG1} - V_{TP})^2$$

$$= \frac{0.2 \text{ m}}{2} (2-1)^2$$

$$= 0.1 (1) \text{ m}$$

$$= 0.1 \text{ m}$$

$$\therefore V_{SD} = V_{SG1} - IR$$

$$= 2 - 0.1 \text{ m} \times 100 \text{ K}$$

$$= 2 - 10$$

$$I_D = K_P \left[(V_{SG1} - |V_{TP}|) V_{SD} - \frac{1}{2} V_{SD}^2 \right]$$

$$\Rightarrow 0.1 \text{ m} = 0.2 \text{ m} \left[\left(\frac{V_{SG1}}{2} - 1 \right) (V_{SG1} - IR) - \frac{1}{2} (V_{SG1} - IR)^2 \right]$$

$$\Rightarrow 1 = 2 \left[(V_{SG1} - 1) (V_{SG1} - 10) - \frac{1}{2} (V_{SG1} - 10)^2 \right]$$

$$\Rightarrow 2 = 4 V_{SG1}^2 + 40 - 44 V_{SG1} - V_{SG1}^2 + 100 - 20 V_{SG1}$$

$$\Rightarrow 3 V_{SG1}^2 - 64 V_{SG1} + 138 = 0$$

$$\Rightarrow 1 = 2 V_{SG1}^2 + 20 - 22 V_{SG1} - V_{SG1}^2 - 100 + 20 V_{SG1}$$

$$\Rightarrow V_{SG1}^2 - 2 V_{SG1} - 81 = 0$$

$$\Rightarrow V_{SG1} = \frac{2 + \sqrt{4 + 4 \times 81}}{2}$$

$$= 10.055 \text{ V.}$$

$$\therefore V_{SD} = V_{SG1} - IR$$

$$= 10.055 - (0.1 \text{ m} \times 100 \text{ K})$$

$$= 0.055 \text{ V.}$$