HW1 - Intro to Machine Learning

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1 Part 1 - HW01pb1data.csv

1.1 Attributes

The dataset has 800 observations of 5 variables. The first 3 columns are *integers* whereas the 4th and 5th columns are *factors*.

In R, this can be seen using the following commands:

```
setwd("/Users/Saurabh/Documents/ML_UCSC/week1/HW")
data<-read.csv("HW01pb1data.csv", header=FALSE)
class(data)
str(data)
#800 obs. of 5 variables. V1-3 are int, V4-5 are Factors
```

1.2 Reason for Categorical Variables

Columns 4 and 5 mostly have integers in them, but when one looks in to the levels, it is quickly visible that they also have strings "thirty five" and "twenty five", respectively. Consequently, R treats them as factors.

Below are the R commands which provide more details:

```
9 | 14<-levels(data[,4])
10 | #has integers, and "thirty five"
11 | which(data[,4]=="thirty_five")
12 | #[1] 405
13 |
14 | 15<-levels(data[,5])
15 | #has integers, and "twenty five"
16 | which(data[,5]=="twenty_five")
```

17 |# [1] 531

1.3 Plots for numeric and categorical variables

1. Plot of the 1st column (numerical data)

 $11 \mid \mathbf{plot}(\mathbf{data}[,1])$

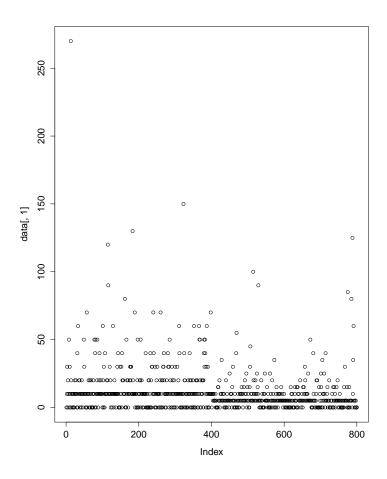


Figure 1: Plotting the numerical,1st column data

The y-axis of this plot are the values of the first column data, plotted against the index (row number) at which they occur in the dataset. This is a *scatter-plot* for a numerical data type

 $4 \mid \mathbf{plot}(\mathbf{data}[,4])$

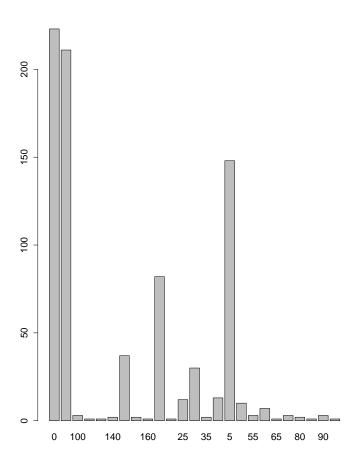


Figure 2: Plotting the categorical, 4th column data

This graph is a distribution: it is a *histogram* with the x-axis showing the values in the 4th column of our dataset, and the y-axis depicts the frequency with which values occur in a specified range. This graph is default since the 4th column data happens to be a categorical variable in our dataset.

2 Part 2 - HW01pb2data.csv

2.1 Extract a random sample of 10k observations

I used the *sample* command in R to obtain a smaller sample composed of 10,000 random records from our dataset.

Below are the R commands used to read and structure the data:

```
setwd("/Users/smadaan/Documents/ML_UCSC/week1/HW")
   data<-read.csv("HW01pb2data.csv", header=FALSE)
3
   str (data)
   # 'data.frame': 2000000 obs. of 1 variable:
   nrow(data)
7
   #[1] 2000000
9
   # selecting a sample of 10,000 random records
10
   ss < -seq(1, nrow(data))
   rand.ind<-sample(ss,10000,replace=F) #set of random indices for subset
11
   small_data<-data[,1][rand.ind]
   length (small_data)
13
   #[1] 10000
```

2.2 Descriptive Stats on Sample

Below are the commands used to compute the mean, max, variance and 1st quartile from the data.

The resulting values are included as comments in the below code (mean =9.41002, max=16.93748, var=4.004991).

```
19  #mean, max and other descriptive stats
20  mean(small_data)
21  #[1] 9.41002
22  max(small_data)
23  #[1] 16.93748
24  var(small_data)
25  #[1] 4.004991
quantile(small_data,0.25)
27  #8.079612
```

2.3 Descriptive Stats for the Entire data

Below is the R code to compute descriptive stats for the entire dataset.

```
32 mean(data)
33 #9.451468
34 max(data)
35 # [1] 18.96657
36 var(data)
37 # 4.001822
38 quantile(data[,1],0.25)
39 # 8.10388
```

The population values for these parameters are very close to those that we found for the smaller sample. The table below shows the comparison.

Statistic	Small Sample	Entire-Dataset
Mean	9.41002	9.451468
Max	16.93748	18.96657
Variance	4.004991	4.001822
1st Quartile	8.079612	8.10388

Table 1: Comparison of statistics between the sample and entire-population datasets

3 Analysis of Ocean-view and Desert Home Prices

3.1 Box Plots for Pricing Data

R code for box plots:

```
boxplot(data.desert[,1], data.ocean[,1],col=c("red","blue"),
main="House_Box_Plots:_Comparison_of_House_Prices",
names=c("Desert_View","Ocean_View"),ylab="Prices_(in_thousand_dollars)")
```

The BoxPlot shows the distribution of prices between the two kinds of houses. Desert View houses have a much lower price than Ocean-view houses. The edges of the box indicate the 1st and last quartiles—the median value (bold line) is much closer to the 25th percentile for desert view houses, indicating that the median is lower than the mean for desert houses. Finally, although the desert view houses are less expensive on average, the most expensive desert homes have a higher price (over 2.5 million dollars) than the most expensive ocean-view houses (less than 2.5 million dollars).

House Box Plots: Comparison of House Prices

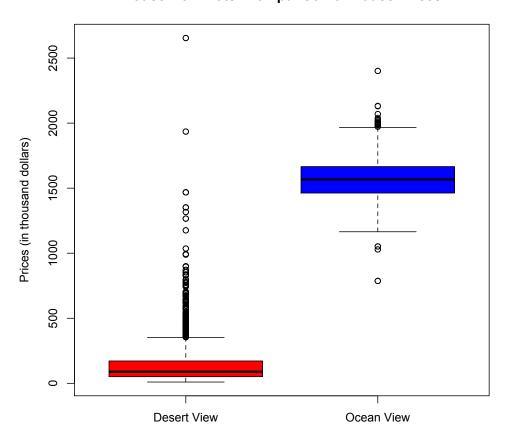


Figure 3: Comparison of prices between desert and ocean-view and desert houses

3.2 Frequency Histogram for Ocean-view Houses

R code for histogram:

```
11 hist (data.ocean[,1], breaks=seq(from=0,to=3000,by=500),

12 xlab="Price_(in_thousand_dollars)", main="Price_Distribution_of_Ocean-view_Houses")
```

Price Distribution of Ocean-view Houses

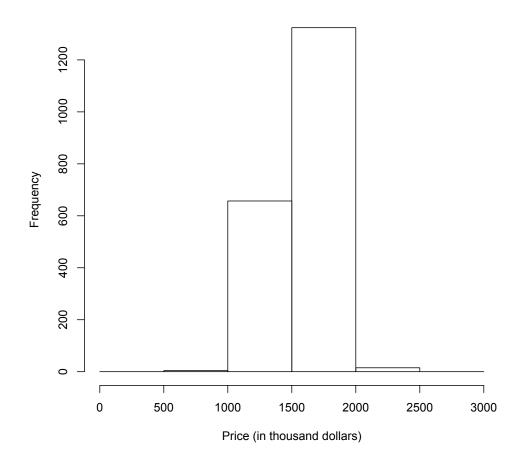


Figure 4: Histogram for prices of the ocean-view houses (0 to 3 million dollars)

3.3 ECDF for House Prices

R code for eddf plots:

```
11 hist (data.ocean[,1], breaks=seq(from=0,to=3000,by=500),

12 xlab="Price_(in_thousand_dollars)", main="Price_Distribution_of_Ocean-view_Houses")
```

Empirical Cumulative Distribution for Houses

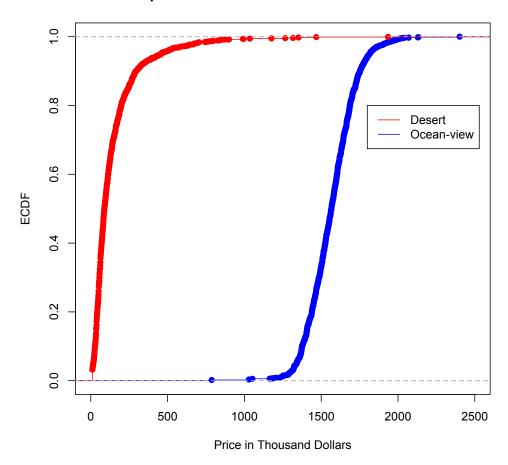


Figure 5: ECDF for Desert and Ocean-view Houses

4 Analyzing Data for Orange Trees

4.1 Age vs. Circumference relation

We first explore the data to identify the 3 variables: Tree, age, circumference. Using the summary command on the dataset outputs useful information, including the (min,max) parameters for age and circumference, and the different levels for 'Tree' (1,2,3,4,5).

x-axis (age) ranges from 118-152, and y-axis (circumference) ranges from 30-214.

Below is the R code for the same:

```
#-- explore the data
   head (orange)
5
   levels (orange [,1])
   str (orange)
8
   summary(orange)
   # 3 variables: Tree(factor), age (numeric), circumference (numeric)
10
   # range for age: 118-1582
11
   # range for circumference: 30-214
12
13
14
   #-- plot age vs circumference
   plot (orange $age, orange $circumference, xlab="Age_of_Tree_(days_since_
15
       1968/12/31)",
            ylab="Trunk_Circumference_(mm)", pch=20,main="Circumference_vs.
16
               _Age_for_Trees",
            col=orange$Tree)
17
   legend('bottomright', legend = levels(factor(orange$Tree)),
18
19
                    text.col=seq_along(levels(orange$Tree)), title="Tree_
                        Type")
```

The resulting plot shows the variation of tree circumference with age, for the different groups/levels of trees.

Circumference vs. Age for Trees

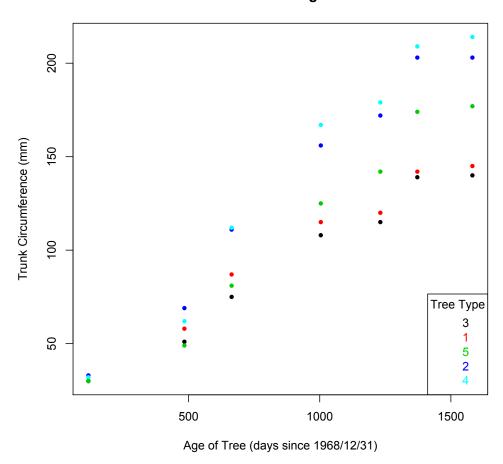


Figure 6: Age vs. Circumference, for the 5 groups of Orange Trees $\,$

4.2 Correlation between age and circumference for 1st Tree type

The two variables (age, circumference) are strongly correlated, with a correlation value of 0.9854675.

R code:

```
23 | orange.1<-orange [which (orange$Tree==1),]
24 | cor(orange.1$age,orange.1$circumference)
25 | # [1] 0.9854675
```

4.3 Covariance and Correlation for Each Tree-type

Approach: Create an empty data frame with the different tree groups as the first column. Then, leverage the *by* command to calculate the parameters for each group. This saves having to individually calculate and *merge* results.

Below is the R code with results:

```
names (orange)
30
   t.levels<-sort(levels(orange$Tree))
31
32
   stats<-data.frame(matrix(nrow=length(t.levels),ncol=0))
33
   stats$Tree<-t.levels
   stats $COVARIANCE <- as.matrix (by (orange, orange $Tree,
34
                           function(x) {cov(x$age,x$circumference)}))
35
   stats $CORRELATION -as.matrix(by(orange, orange $Tree,
36
37
                           function(x) {cor(x$age,x$circumference)}))
38
   stats
39
40
   >   stats 
41
   __Tree_COVARIANCE_CORRELATION
42
   1 = 22239.83 = 0.9881766
   43
   3___30442.81__0.9877376
45
   4 - - - 34290.45 - - 0.9873624
46
   5 = 2 = 5 = 37062.62 = 0.9844610
47
```

4.4 Effect of Adding 10 to each Circumference value

Correlation and covariance remain unchanged.

Below is the R code with results:

```
new.stats<-data.frame(matrix(nrow=length(t.levels),ncol=0))
60
   new.stats$Tree<-t.levels
   61
                           function(x) {cov(x$age,x$circumference+10)}))
62
63
   new.stats$CORRELATION<-as.matrix(by(orange, orange$Tree,
                           function (x) \{ cor(x \text{ sage}, x \text{ scircumference} + 10) \})
64
65
   new.stats
66
   # no change in covariance or correlation
67
68
   >_new.stats
   __Tree_COVARIANCE_CORRELATION
69
70
   1 = 22239.83 = 0.9881766
   2 = 2 = 2 = 22340.07 = 0.9854675
71
   3___30442.81__00.9877376
73
   4 = 2 \cdot 4 = 34290.45 = 0.9873624
74
   5 = 2 \cdot 5 = 37062.62 = 0.9844610
75
```

4.5 Effect of Doubling Circumference

Covariance doubles and correlation remains unchanged.

Below is the R code with results:

```
new2.stats<-data.frame(matrix(nrow=length(t.levels),ncol=0))
80
   new2.stats$Tree<-t.levels
81
   new2.stats$COVARIANCE<-as.matrix(by(orange, orange$Tree,
82
                             function(x) {cov(x$age,x$circumference*2)}))
   new2.stats$CORRELATION<-as.matrix(by(orange, orange$Tree,
83
84
                             function(x) {cor(x$age,x$circumference*2)}))
85
   new2.stats
86
87
   > _{\rm new2.stats}
   __Tree_COVARIANCE_CORRELATION
88
89
   1 = 2 = 44479.67 = 20.9881766
   2___244680.14___0.9854675
90
91
   3 = 3 = 3 = 60885.62 = 0.9877376
   4 - - - 4 - - - 68580.90 - - - 0.9873624
92
93
   5 - - - 5 - - 74125.24 - - 0.9844610
94
   # covariance doubles, correlation remains same
95
```

4.6 Effect of Multiplying Circumference by -2

Covariance becomes negative (and double in magnitude compared to the original dataset), and correlation becomes *negative* of its original value. Results:

```
New covariance = original covariance * (-2)
```

New correlation = -original correlation

Below is the R code with results:

```
new3.stats<-data.frame(matrix(nrow=length(t.levels),ncol=0))
99
100
    new3.stats$Tree<-t.levels
    new3.stats$COVARIANCE<-as.matrix(by(orange, orange$Tree,
101
                              function(x) {cov(x$age,x$circumference*(-2))}))
102
103
    new3.stats$CORRELATION<-as.matrix(by(orange, orange$Tree,
104
                              function (x) {cor(x$age,x$circumference*(-2))}))
105
    new3.stats
106
107
    >_new3.stats
    __Tree_COVARIANCE_CORRELATION
108
109
    1 = 2 = 1 = -44479.67 = -0.9881766
    2 - 2 - 2 - 44680.14 - -0.9854675
110
111
    3 = 3 = 3 = -60885.62 = -0.9877376
    4 - - 4 - -68580.90 - -0.9873624
112
113
    5 - - 5 - -74125.24 - -0.9844610
114
115
    \# new.corr = orig.corr*-2, correlation becomes -ve
```

5 Desert Homes: Revisited

5.1 Calculating the Median Price

Approach: R does not have a native median function, so we define a custom median function to calculate the median home price. This results in:

Below is the R code with results:

```
17 | median=ifelse(is.integer(1/2),sv[1/2],sv[1/2+1]);
18 | return(median);
19 | }
20 | | median(data.desert[,1])
23 | #89 | mean(data.desert[,1])
25 | #144.0348
```

Median value: 89

Mean value: 144.0348

(note: the values are in units of thousand dollars).

Median is smaller than the mean.

5.2 Characteristics of the Distribution

We found earlier that the median is lower than the mean. This generally indicates that the distribution is positively, or *right-skewed*.

This can be further confirmed by plotting a histogram to get a sense of the distribution, as shown below.

```
29 | hist(data.desert[,1], main="Distribution_of_Desert_Home_Prices", 30 | xlab="Home_Price", ylab="Number_of_Homes") 31 | # also, median < mean, positive/right skewed
```

Distribution of Desert Home Prices

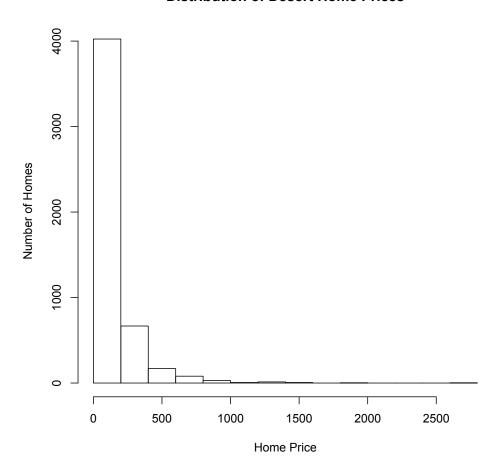


Figure 7: Histogram showing desert home prices

5.3 Effect of Higher Home Prices on Median Value

If we increase house price by 10 (thousand dollars) each, the median value *increases* by the same amount.

Specifically, the new median (99k) is higher than the old median (89k) by 10 (thousand dollars). Below is the R code with results:

```
35 | median(data.desert[,1]+10)
36 | #99
37 | #median also increases by 10k
```

5.4 Effect of Doubling Home Prices on Median Value

If home prices double, the median value also doubles.

Specifically, the new median (178k) is twice the old median (89k). Below is the R code with results:

```
41 median(data.desert[,1]*2)
42 #178
43 #median also doubles
```

6 Closing Notes and References

I read material from *The Art of R Programming* by Norman Matloff for an introduction to R, and googled online references for the use of the by command.

Tools used include the R package for Mac, TeXShop for writing Latex files. I did not collaborate with another class member on this assignment.

Included in my submission is this pdf file, and all the R files where my code is programmed.