EE4620 Spectral Domain Methods in EM

Lecture: Matlab Session on Artificial Dielectrics

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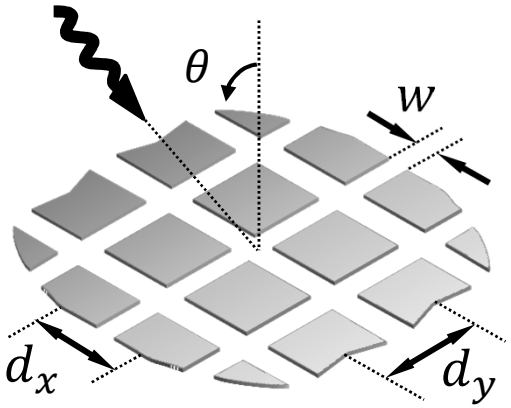
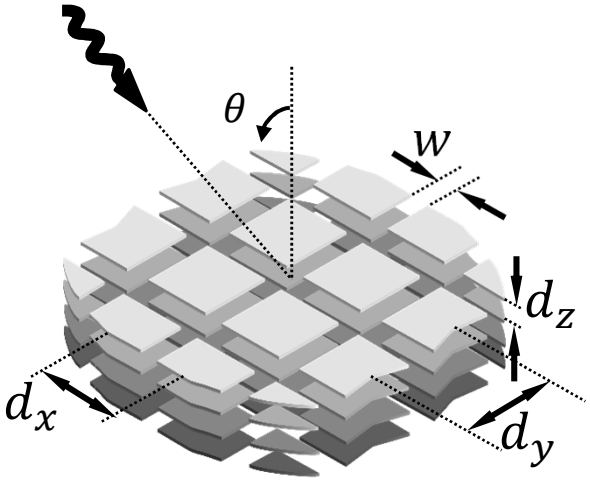
Problem

Implement the reflection and transmission coefficient of a plane wave impinging on

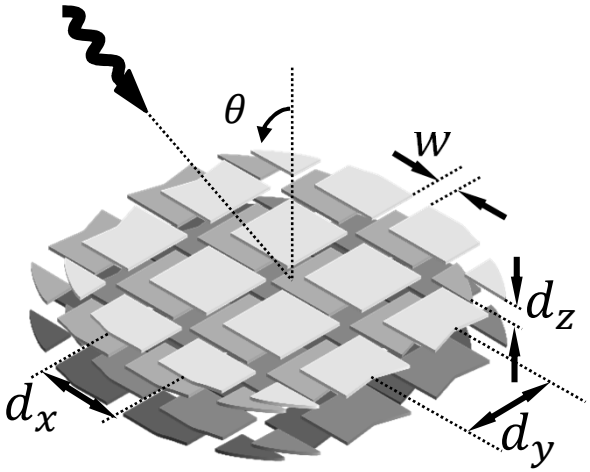
1. Single layer of sub-wavelength patches

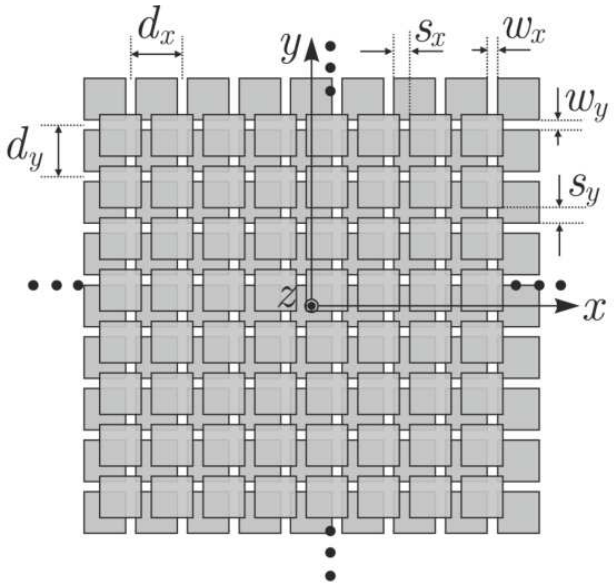


2. N-layer artificial dielectric (aligned)



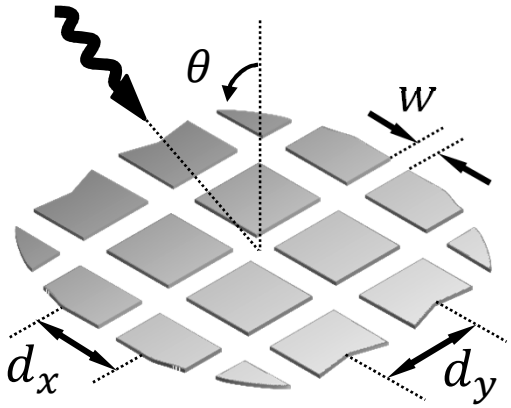
3. N-layer artificial dielectric (alternate shift)

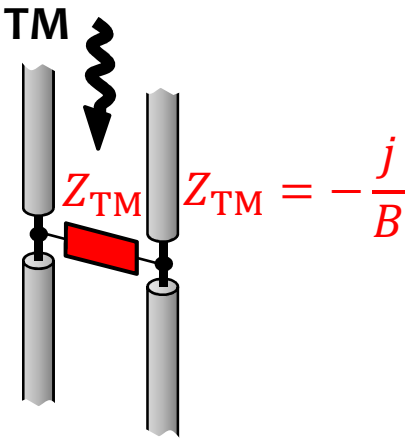




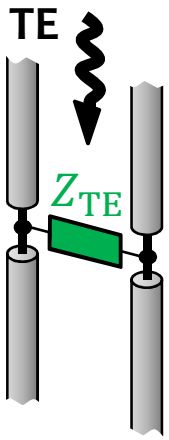
Problem 1

Single layer of sub-wavelength patches





$$Z_{TM} = -\frac{j}{B}$$



$$Z_{TE} = -\frac{j}{B}\frac{1}{1-\frac{\sin^2\theta}{2}}$$

Susceptance

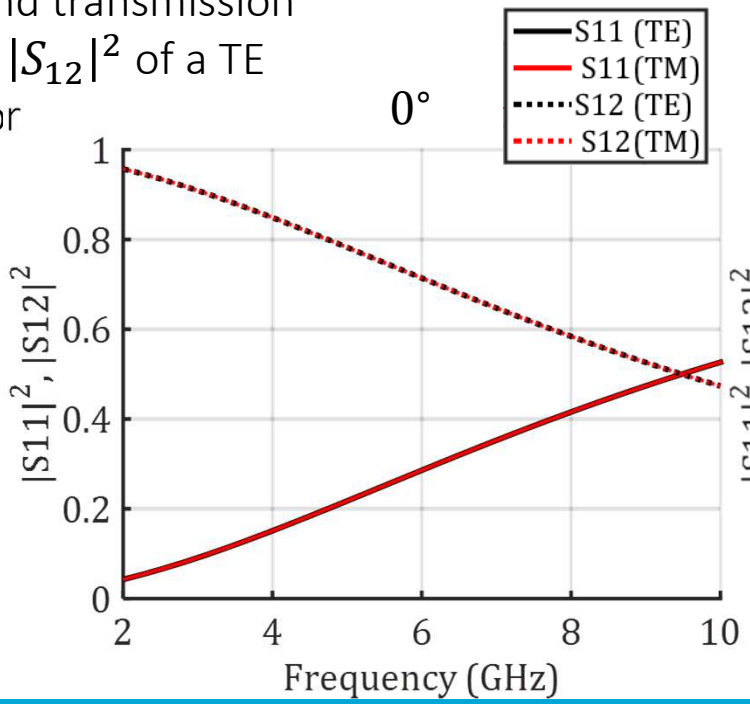
$$B \approx \frac{\omega\varepsilon_0 d_y}{\pi}\sum_{m\neq 0}\frac{\left|\mathrm{sinc}(\pi m w/d_y)\right|^2}{|m|}$$

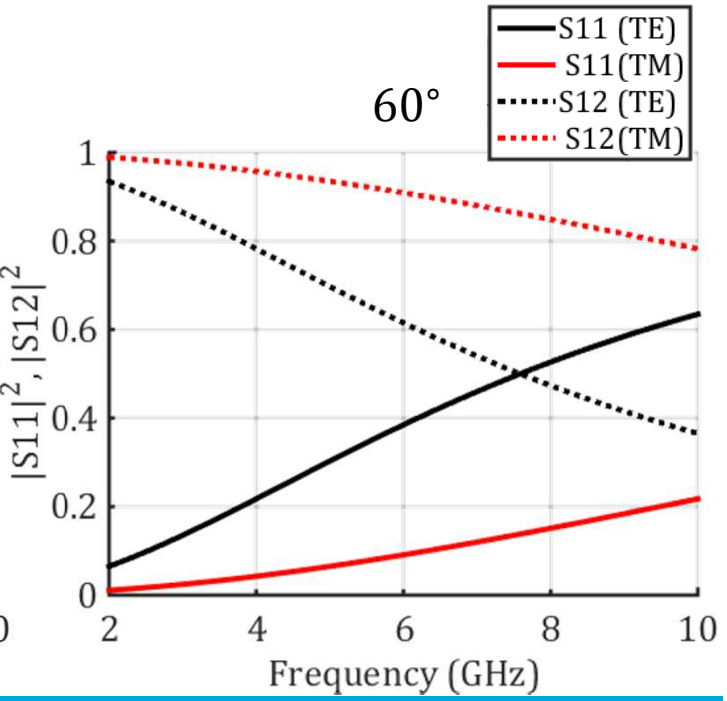
1. Plot the reflection and transmission coefficients $|S_{11}|^2$ and $|S_{12}|^2$ of a TE and TM plane waves for

- Normal incidence
- Incidence at $60°$

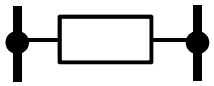
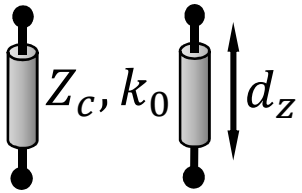
- Parameters

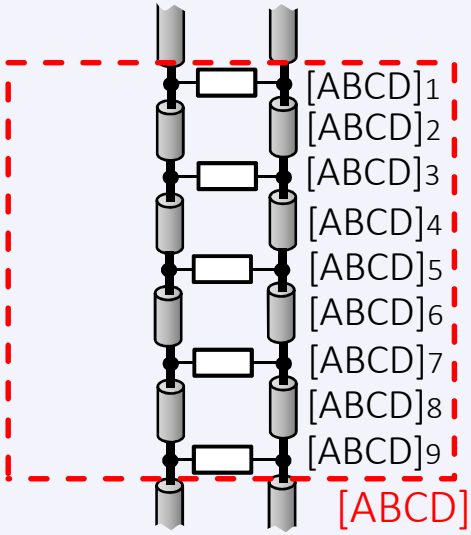
Freq. range: 2-10 GHz
$w = 0.01\lambda_0$
$d_x = d_y = 0.2\lambda_0$
λ_0 wavelength at 10 GHz





Reminder: ABCD Matrix, S-Matrix

		$\begin{bmatrix} A & B \\ C & D \end{bmatrix}$	$\begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix}$
Shunt impedance	$Z = 1/Y$ 	$\begin{bmatrix} 1 & 0 \\ Y & 1 \end{bmatrix}$	$S_{11} = \frac{-YZ_0}{2+YZ_0}, \; S_{12} = \frac{2}{2+YZ_0}$
Transmission line section		$\begin{bmatrix} \cos k_0 d_z & jZ_c \sin k_0 d_z \\ jY_c \sin k_0 d_z & \cos k_0 d_z \end{bmatrix}$	



Advantage: total ABCD matrix is product of the ABCD matrixes of the single components

$$[ABCD]_{TOT} = \prod_{i=1}^{9} [ABCD]_i$$

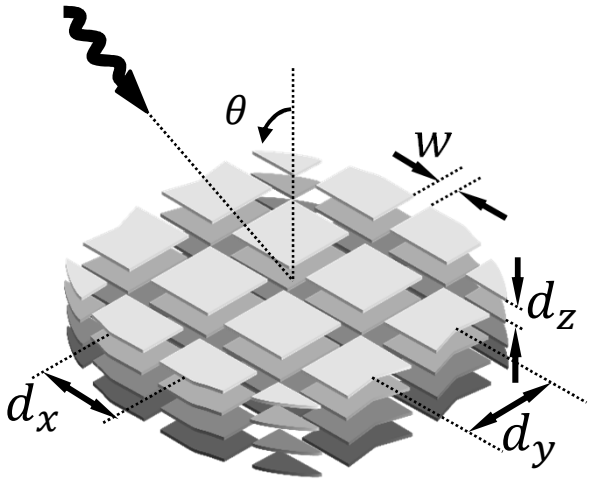
General conversion

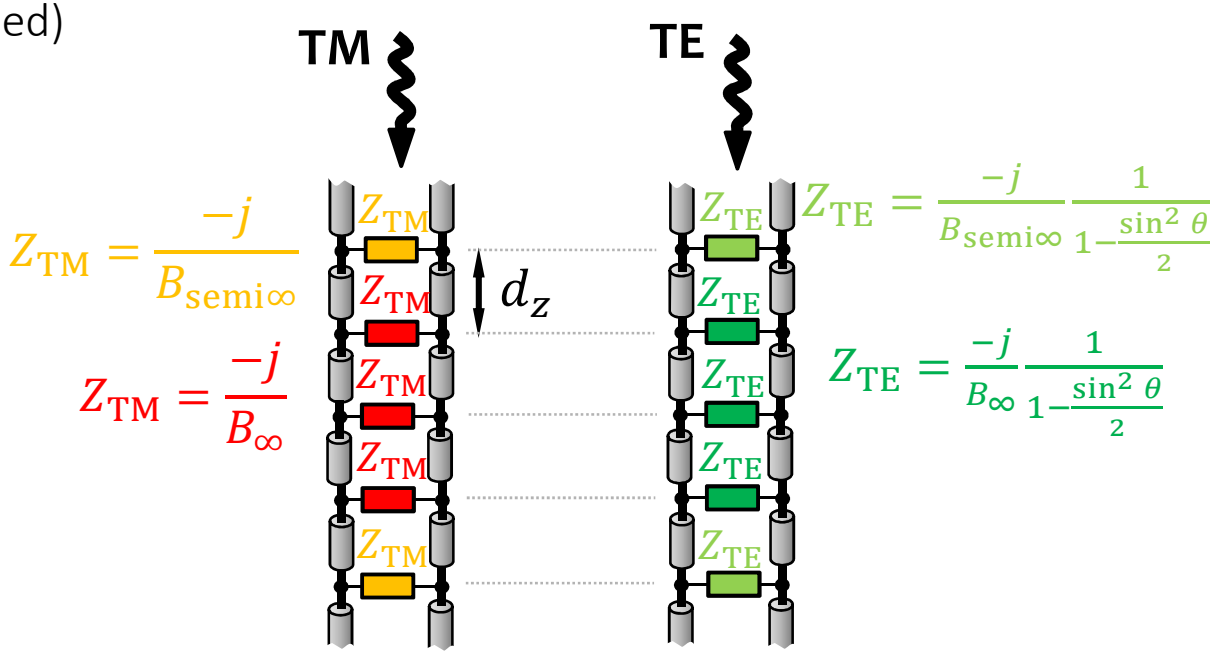
	$ABCD$
S_{11}	$\frac{A + B/Z_0 - CZ_0 - D}{A + B/Z_0 + CZ_0 + D}$
S_{12}	$\frac{2(AD - BC)}{A + B/Z_0 + CZ_0 + D}$
S_{21}	$\frac{2}{A + B/Z_0 + CZ_0 + D}$
S_{22}	$\frac{-A + B/Z_0 - CZ_0 + D}{A + B/Z_0 + CZ_0 + D}$

Z_0: normalization impedance

Problem 2

N-layer artificial dielectric (aligned)





Susceptance

$$B_{\infty} \approx \frac{\omega \varepsilon_0 d_y}{\pi} \sum_{m \neq 0} \frac{\left|\mathrm{sinc}\left(\pi m w / d_y\right)\right|^2}{|m|} \times j \tan\left(\frac{-j\pi |m| d_z}{d_y}\right)$$

$$B_{\mathrm{semi}-\infty} \approx \frac{\omega \varepsilon_0 d_y}{\pi} \sum_{m \neq 0} \frac{\left|\mathrm{sinc}\left(\pi m w / d_y\right)\right|^2}{|m|} \times \left(\frac{1}{2} + \frac{j}{2} \tan\left(\frac{-j\pi |m| d_z}{d_y}\right)\right)$$

Problem 2

2. Plot the reflection and transmission coefficients $|S_{11}|^2$ and $|S_{12}|^2$ of a TE and TM plane waves for

- Normal incidence
- Incidence at $60°$

- Parameters

$N = 5$

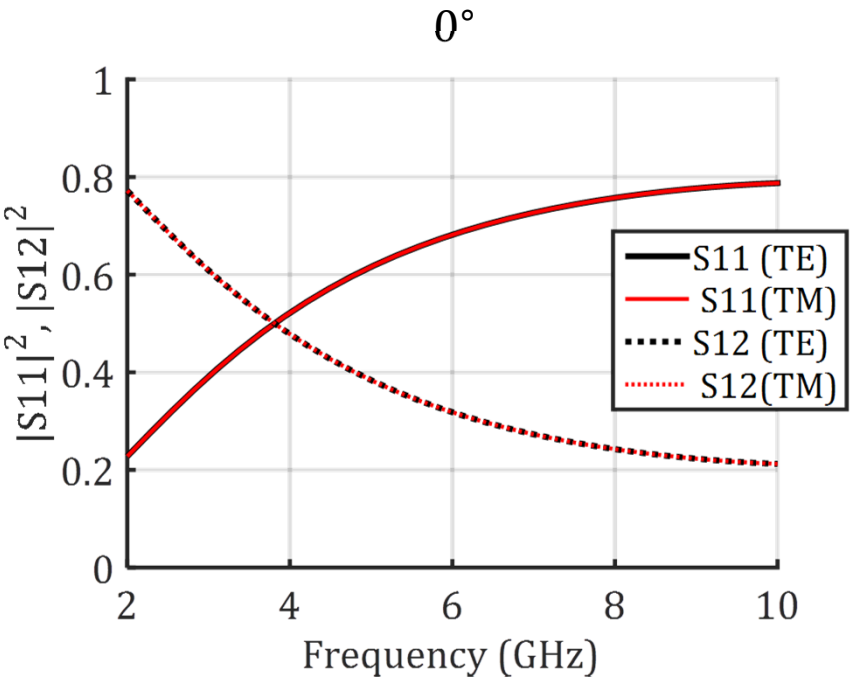
Freq. range: 2-10 GHz

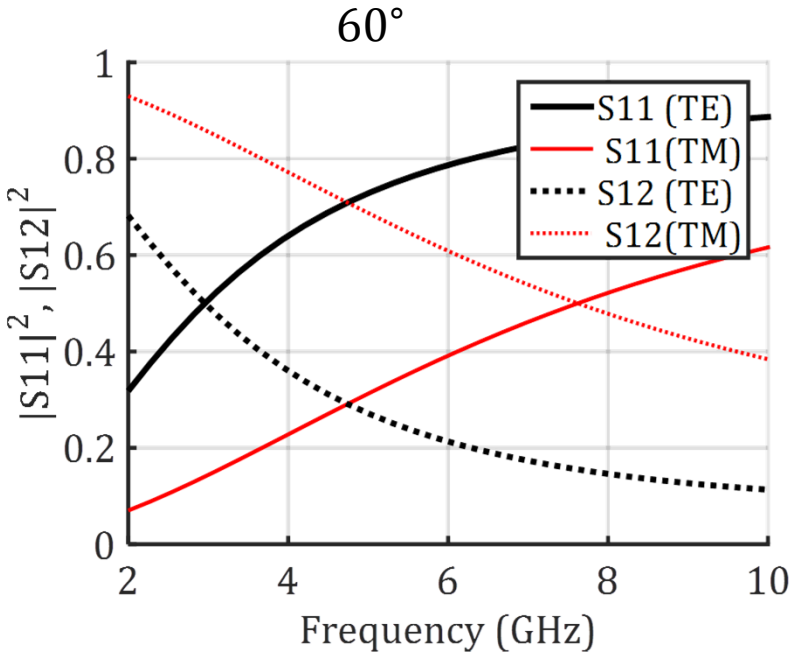
$w = 0.01\lambda_0$

$d_z = 0.01\lambda_0$

$d_x = d_y = 0.2\lambda_0$

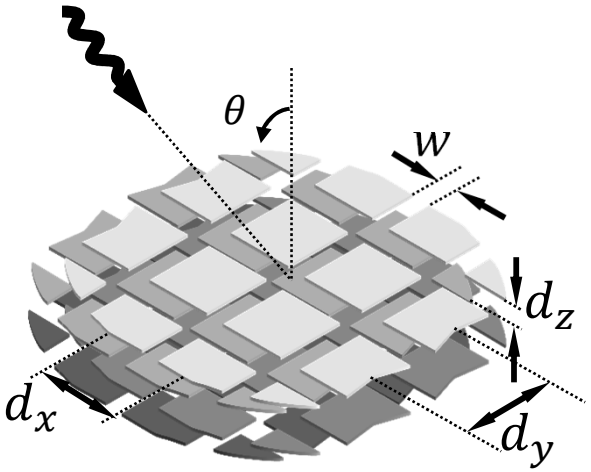
λ_0 wavelength at 10 GHz

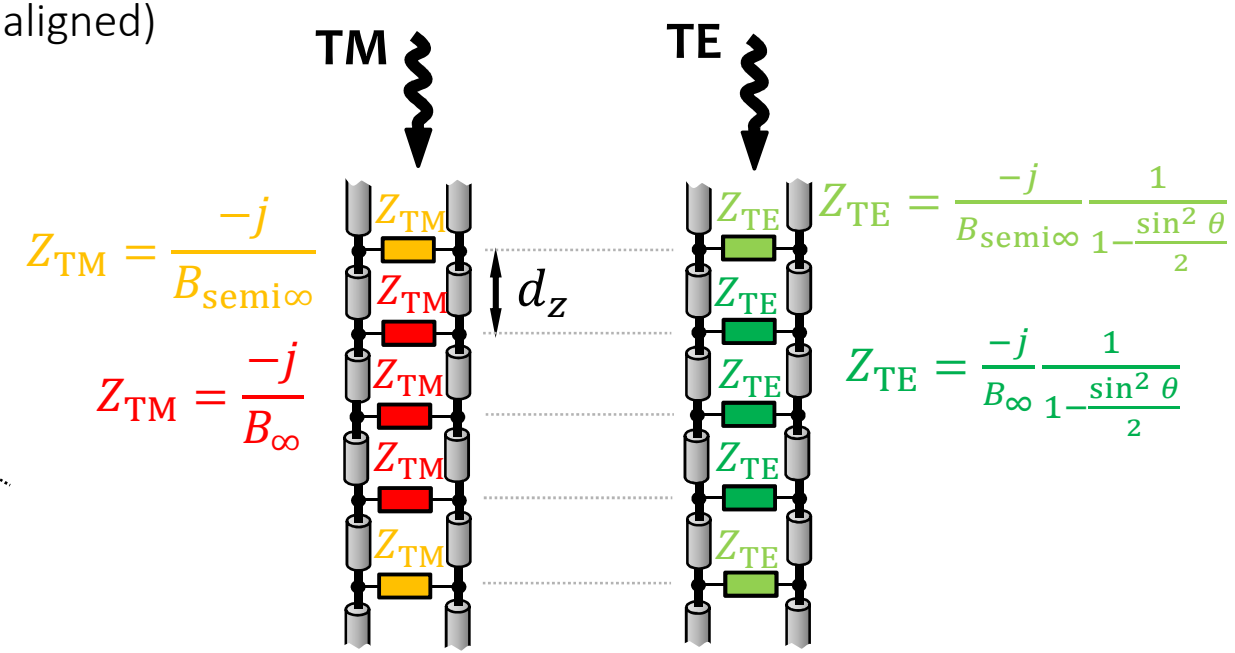




Problem 3

N-layer artificial dielectric (nonaligned)





Susceptance

$$B_{\infty} \approx \frac{k_0}{\zeta_0}\frac{d_y}{\pi}\sum_{m\neq 0}\frac{\left|\operatorname{sinc}(\pi m w_x/d_y)\right|^2}{|m|}\left(-j\cot\left(\frac{-j2\pi|m|d_z}{d_y}\right)+j\,e^{j2\pi m s_y/d_y}\csc\left(\frac{-j2\pi|m|d_z}{d_y}\right)\right)$$

$$B_{semi\infty} \approx \frac{k_0}{\zeta_0}\frac{d_y}{\pi}\sum_{m\neq 0}\frac{\left|\operatorname{sinc}\left(\frac{\pi m w}{d_y}\right)\right|^2}{|m|}\left(\frac{1}{2}-\frac{j}{2}\cot\left(\frac{-j2\pi|m|d_z}{d_y}\right)+\frac{j}{2}e^{j2\pi m\frac{s_y}{d_y}}\csc\left(\frac{-j2\pi|m|d_z}{d_y}\right)\right)$$

Problem 3

3. Plot the reflection and transmission coefficients $|S_{11}|^2$ and $|S_{12}|^2$ of a TE and TM plane waves for

- Normal incidence
- Incidence at $60°$

- Parameters

$N = 2$

Freq. range: 2-10 GHz

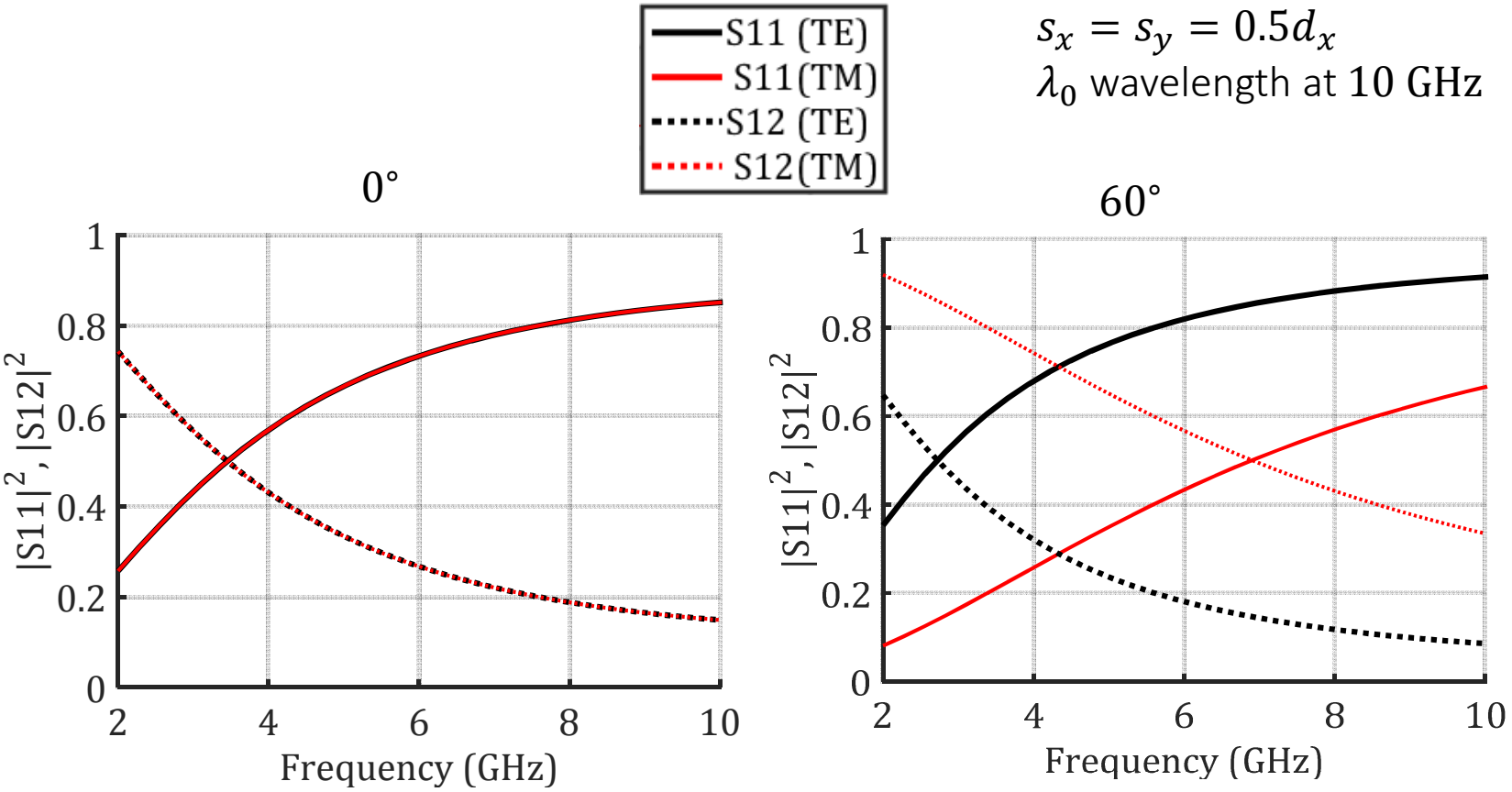
$w = 0.01\lambda_0$

$d_z = 0.02\lambda_0$

$d_x = d_y = 0.2\lambda_0$

$s_x = s_y = 0.5d_x$

λ_0 wavelength at 10 GHz



Behaves almost the same as 5 layers of aligned layers