	<pre>import numpy as np import pandas as pd import matplotlib.pyplot as plt import seaborn as sns from statsmodels.graphics.regressionplots import influence_plot import statsmodels.formula.api as smf import pandas.util.testing as tm </pre> <pre><ipython-input-1-19fc16e3f5f4>:7: FutureWarning: pandas.util.testing is deprecated. Use the functions in the public API at pandas.testing instead. import pandas.util.testing as tm</ipython-input-1-19fc16e3f5f4></pre>
[2]: [] [3]: [] [4]: [<pre>mporting the dataset df= pd.read_csv('/Users/SAURABH/Saurabh patil/DATA SCIENCE/Multiple REgression/50_Startups.csv') df.columns Index(['R&D Spend', 'Administration', 'Marketing Spend', 'State', 'Profit'], dtype='object') df.info() #no-null values colass 'nandas core frame DataFrame'></pre>
	<pre>cclass 'pandas.core.frame.DataFrame'> RangeIndex: 50 entries, 0 to 49 Data columns (total 5 columns): # Column Non-Null Count Dtype</pre>
t[5]:	df['State'].value_counts() #Checking the categories of State variable New York 17 California 17 Florida 16 Name: State, dtype: int64 #Getting dummy variables df1= pd.get_dummies(df,columns=['State']) df1.head()
	R&D Spend Administration Marketing Spend Profit State_California State_New York 0 165349.20 136897.80 471784.10 192261.83 0 0 1 1 162597.70 151377.59 443898.53 191792.06 1 0 0 2 153441.51 101145.55 407934.54 191050.39 0 1 0 3 144372.41 118671.85 383199.62 182901.99 0 0 1 4 142107.34 91391.77 366168.42 166187.94 0 1 0
[9]: [10]:	<pre>Index(['R&D Spend', 'Administration', 'Marketing Spend', 'Profit',</pre>
[11]: [12]: [12]: _	df1[df1.duplicated()].shape #checking for duplicates (0, 7) df1.corr() #correlation of profit with admin is very less rnd 1.000000 0.241955 0.724248 0.972900 -0.143165 0.105711 0.039068 0.241955 1.00000 -0.032154 0.200717 -0.015478 0.010493 0.005145
[ms 0.724248 -0.032154 1.000000 0.747766 -0.168875 0.205685 -0.033670 p 0.972900 0.200717 0.747766 1.000000 -0.145837 0.116244 0.031368 ca -0.143165 -0.015478 -0.168875 -0.145837 1.000000 -0.492366 -0.515152 fl 0.105711 0.010493 0.205685 0.116244 -0.492366 1.000000 Building the regression model
[13]: [14]: [14]:	model1 = smf.ols('p-rnd+admin+ms+ca+fl+ny', data=dfl).fit() model1.summary() OLS Regression Results Dep. Variable: p R-squared: 0.951 Model: OLS Adj. R-squared: 0.945 Method: Least Squares F-statistic: 169.9 Date: Fri, 18 Jun 2021 Prob (F-statistic): 1.34e-27
	Time: 01:11:05
	rnd 0.8060 0.046 17.369 0.000 0.712 0.900 admin -0.0270 0.052 -0.517 0.608 -0.132 0.078 ms 0.0270 0.017 1.574 0.123 -0.008 0.062 ca 1.249e+04 2449.797 5.099 0.000 7554.868 1.74e+04 fl 1.269e+04 2726.700 4.654 0.000 7195.596 1.82e+04 ny 1.245e+04 2486.364 5.007 0.000 7439.285 1.75e+04 Omnibus: 14.782 Durbin-Watson: 1.283
.]	Skew: -0.948 Prob(JB): 2.41e-05 Kurtosis: 5.572 Cond. No. 4.01e+21 Standard Errors assume that the covariance matrix of the errors is correctly specified. The smallest eigenvalue is 2.41e-31. This might indicate that there are
	As per model 1, admin and ms are not significant, hence checking individually model1a = smf.ols('p~admin', data=df1).fit() model1a.summary() OLS Regression Results Dep. Variable: p R-squared: 0.040
	Model: OLS Adj. R-squared: 0.020 Method: Least Squares F-statistic: 2.015 Date: Fri, 18 Jun 2021 Prob (F-statistic): 0.162 Time: 01:11:46 Log-Likelihood: -599.63 No. Observations: 50 AIC: 1203. Df Residuals: 48 BIC: 1207. Covariance Type: nonrobust nonrobust
	coef std err t P> t [0.025] 0.975] Intercept 7.697e+04 2.53e+04 3.040 0.004 2.61e+04 1.28e+05 admin 0.2887 0.203 1.419 0.162 -0.120 0.698 Omnibus: 0.126 Durbin-Watson: 0.099 Prob(Omnibus): 0.939 Jarque-Bera (JB): 0.110 Skew: 0.093 Prob(JB): 0.947 Kurtosis: 2.866 Cond. No. 5.59e+05
[: [: s	Notes: Istandard Errors assume that the covariance matrix of the errors is correctly specified. It is the condition number is large, 5.59e+05. This might indicate that there are trong multicollinearity or other numerical problems. As per model 1a, admin is not significant.
[17]: [18]: [18]:	model1b = smf.ols('p-ms', data=df1).fit() model1b.summary() OLS Regression Results Dep. Variable: p R-squared: 0.559 Model: OLS Adj. R-squared: 0.550 Method: Least Squares F-statistic: 60.88
	Date: Fri, 18 Jun 2021 Prob (F-statistic): 4.38e-10 Time: 01:12:19 Log-Likelihood: -580.18 No. Observations: 50 AIC: 1164. Df Residuals: 48 BIC: 1168. Covariance Type: nonrobust coef std err t P> t [0.025 0.975] Intercept 6e+04 7684.530 7.808 0.000 4.46e+04 7.55e+04
	ms 0.2465
[: [:	In Standard Errors assume that the covariance matrix of the errors is correctly specified. If Standard Errors assume that the covariance matrix of the errors is correctly specified. If the condition number is large, 4.89e+05. This might indicate that there are trong multicollinearity or other numerical problems. If the condition number is large, 4.89e+05. This might indicate that there are trong multicollinearity or other numerical problems. If the condition number is large, 4.89e+05. This might indicate that there are trong multicollinearity or other numerical problems. If the condition number is large, 4.89e+05. This might indicate that there are trong multicollinearity or other numerical problems. If the condition number is large, 4.89e+05. This might indicate that there are trong multicollinearity or other numerical problems. If the condition number is large, 4.89e+05. This might indicate that there are trong multicollinearity or other numerical problems.
[Cook's distance teration -1 model_influence = model1.get_influence() (c, _) = model_influence.cooks_distance fig = nlt_subplots(figsize=(20, 7))
[20]:	<pre>fig = plt.subplots(figsize=(20, 7)) plt.stem(np.arange(len(df1)), np.round(c, 3)) plt.xlabel('Row index') plt.ylabel('Cooks Distance') plt.show()</pre>
	0.15 - 0.10 - 0.05 - 0.
	0.00
[22]: [23]: [24]: [25]: [25]:	<pre>df2 = df2.drop(['index'], axis=1) mode12 = smf.ols('p~rnd+admin+ms+ca+fl+ny', data=df2).fit() mode12.summary()</pre>
	Method: Least Squares F-statistic: 216.6 Date: Fri, 18 Jun 2021 Prob (F-statistic): 2.51e-29 Time: 01:14:18 Log-Likelihood: -505.97 No. Observations: 49 AIC: 1024. Df Residuals: 43 BIC: 1035. Covariance Type: nonrobust -505.97
	Intercept 3.915e+04 4249.909 9.213 0.000 3.06e+04 4.77e+04 rnd 0.7836 0.039 20.056 0.000 0.705 0.862 admin -0.0220 0.044 -0.505 0.616 -0.110 0.066 ms 0.0258 0.014 1.804 0.078 -0.003 0.055 ca 1.422e+04 2081.663 6.833 0.000 1e+04 1.84e+04 ny 1.227e+04 2076.431 5.909 0.000 8082.828 1.65e+04
N	Omnibus: 0.051 Durbin-Watson: 1.667 Prob(Omnibus): 0.975 Jarque-Bera (JB): 0.207 Skew: 0.061 Prob(JB): 0.902 Kurtosis: 2.705 Cond. No. 2.98e+21
[: :s	1] Standard Errors assume that the covariance matrix of the errors is correctly specified. 2] The smallest eigenvalue is 4.36e-31. This might indicate that there are trong multicollinearity problems or that the design matrix is singular. Requared value has increased, ms and admin are still insignificant teration 2 model_influence = model2.get_influence()
	<pre>model_influence = model2.get_influence() (c1, _) = model_influence.cooks_distance fig = plt.subplots(figsize=(20, 7)) plt.stem(np.arange(len(df2)), np.round(c1, 3)) plt.xlabel('Row index') plt.ylabel('Cooks Distance') plt.show()</pre>
	0.20 -
	0.05
[28]: [29]: [30]: [31]: [32]: [32]:	df3 = df2.drop([48],axis=0).reset_index() df3 = df3.drop(['index'],axis=1) model3= smf.ols('p~rnd+admin+ms+ca+fl+ny',data=df3).fit() model3.summary() OLS Regression Results
	Dep. Variable: p R-squared: 0.963 Model: OLS Adj. R-squared: 0.958 Method: Least Squares F-statistic: 217.6 Date: Fri, 18 Jun 2021 Prob (F-statistic): 7.02e-29 Time: 01:15:44 Log-Likelihood: -493.23 No. Observations: 48 AIC: 998.5 Df Residuals: 42 BIC: 1010. Df Model: 5
	Covariance Type: nonrobust coef std err t P> t [0.025] 0.975] Intercept 4.409e+04 4569.825 9.648 0.000 3.49e+04 5.33e+04 rnd 0.7888 0.037 21.160 0.000 0.714 0.864 admin -0.0621 0.045 -1.381 0.174 -0.153 0.029 ms 0.0179 0.014 1.275 0.209 -0.010 0.046 ca 1.53e+04 2035.915 7.516 0.000 1.12e+04 1.94e+04 fl 1.415e+04 2261.128 6.259 0.000 9588.163 1.87e+04
	ny 1.464e+04 2223.793 6.581 0.000 1.01e+04 1.91e+04 Omnibus: 0.267 Durbin-Watson: 1.835 Prob(Omnibus): 0.875 Jarque-Bera (JB): 0.453 Skew: 0.108 Prob(JB): 0.797 Kurtosis: 2.576 Cond. No. 1.45e+21
[: : :s	Idets: 1] Standard Errors assume that the covariance matrix of the errors is correctly specified. 2] The smallest eigenvalue is 1.85e-30. This might indicate that there are trong multicollinearity problems or that the design matrix is singular. Requared value has increased, ms and admin are still insignificant teration 3
[33]:	<pre>model_influence = model3.get_influence() (c2, _) = model_influence.cooks_distance fig = plt.subplots(figsize=(20, 7)) plt.stem(np.arange(len(df3)), np.round(c2, 3)) plt.xlabel('Row index') plt.ylabel('Cooks Distance') plt.show()</pre>
	0.08 - 0.06 - 0.04 -
	0.02 - 0.00 - 10 20 Row index
	Since cook's distance of most of the points seems to lie in the same range, hence we can conculde that there are no more influence points #Checking VIF value to see if there's some collinearity in the variables rsq_rnd = smf.ols("rnd-admin+ms", data= df3).fit().rsquared viF_rnd = 1/(1-rsq_rnd) rsq_adm = smf.ols("admin-rnd+ms", data=df3).fit().rsquared viF_adm = 1/(1-rsq_adm)
	rsq_mar = smf.ols("ms-admin+rnd", data= df3).fit().rsquared ViF_mar = 1/(1-rsq_mar) d1 = {'Variables':['rnd', 'admin', 'ms'], 'VIF':[ViF_rnd, ViF_adm, ViF_mar]} Vif_frame = pd.DataFrame(d1) Vif_frame Variables VIF o
[36]:	Since all VIFs are below 10, hence there's no interdependency among the variables import statsmodels.api as sm fig = plt.figure(figsize=(15,10)) fig = sm.graphics.plot_regress_exog(model3, "rnd", fig=fig) plt.show() Regression Plots for rnd
	Y and Fitted vs. X Residuals versus rnd 15000 10000 10000 75000 -10000
	0 25000 50000 75000 100000 125000 150000 0 25000 50000 75000 100000 125000 150000 md Partial regression plot CCPR Plot
	40000 - 1000000 - 1000000 - 1000000 - 1000000 - 1000000 - 100000 - 100000 -
[37]:	-80000 -60000 -40000 -20000 0 20000 40000 60000 0 25000 50000 75000 100000 125000 150000 fig = plt.figure(figsize=(15,10)) fig = sm.graphics.plot_regress_exog(model3, "admin", fig=fig) plt.show() Regression Plots for admin Y and Fitted vs. X Residuals versus admin
	200000 - 175000 - 15000 - 1000000 - 100000 - 100000 - 100000 - 100000 - 100000 - 100000 - 1000000 - 100000 - 100000 - 100000 - 100000 - 100000 - 100000 - 1000000 - 100000 - 100000 - 100000 - 100000 - 100000 - 100000 - 1000000 - 100000 - 100000 - 100000 - 100000 - 100000 - 100000 - 1000000 - 100000 - 100000 - 100000 - 100000 - 100000 - 100000 - 1000000 - 100000 - 100000 - 100000 - 100000 - 100000 - 100000 - 1000000 - 100000 - 100000 - 100000 - 100000 - 100000 - 100000 - 100000000
	7500010000150
[38]:	-250004000020000
	20000 - P fitted 175000 - 100000 - 100000 - 5
	50000 - 100000 200000 300000 400000 0 100000 200000 300000 400000
	500050005000500010000 -
	e(ms X) sm. graphics.plot_partregress_grid(model3) Partial Begressign Blot
	-50000 0 50000 -200000 0 200000 e(admin X) e(ms X) \(\begin{align*}
	□ 10000
(Since the correlation of admin with profit is less, and also as per the p-value, it's insignificant, nence we can drop the admin variable final_model= smf.ols('p-rnd+ms+ca+fl+ny', data=df3).fit() final_model.summary()
[41]:	OLS Regression Results Dep. Variable: p R-squared: 0.961 Model: OLS Adj. R-squared: 0.958 Method: Least Squares F-statistic: 265.9 Date: Fri, 18 Jun 2021 Prob (F-statistic): 1.02e-29 Time: 01:19:02 Log-Likelihood: -494.30 No. Observations: 48 AIC: 998.6
	Df Residuals: 43 BIC: 1008. Df Model: 4 Covariance Type: nonrobust rod 0.7692 0.035 22.072 0.000 0.699 0.840 ms 0.0251 0.013 1.908 0.663 -0.001 0.052 ca 1.353e+04 1599.496 8.461 0.000 1.03e+04 1.68e+04
[: ; s	lotes: 1] Standard Errors assume that the covariance matrix of the errors is correctly specified. 2] The smallest eigenvalue is 1.72e-30. This might indicate that there are trong multicollinearity problems or that the design matrix is singular. Test for Normality of Residuals (Q-Q Plot) qqplot=sm.qqplot(final_model.resid,line='q') # line = 45 to draw the diagnoal line
[42]:	qqplot=sm.qqplot(final_model.resid,line='q') # line = 45 to draw the diagnoal line plt.title("Normal Q-Q plot of residuals") plt.show() Normal Q-Q plot of residuals 15000 -
	Residual Plot for Homoscedasticity
[43]:	#Residual Plot for Homoscedasticity def get_standardized_values(vals): return (vals - vals.mean())/vals.std() plt.scatter(get_standardized_values(final_model.fittedvalues),
[]:	-1.5 -1.0 -0.5 0.0 0.5 1.0 1.5 2.0 Standardized Fitted values