In [1]:
```python
import scipy.cluster.hierarchy as sch
from sklearn.cluster import AgglomerativeClustering
import numpy as np
import pandas as pd
from matplotlib import pyplot as plt
import seaborn as sn
import sklearn.cluster as cluster
from sklearn.cluster import KMeans
from scipy.spatial.distance import cdist
from sklearn.cluster import DBSCAN
from sklearn.preprocessing import StandardScaler
import seaborn as sns
from sklearn import metrics
from sklearn.decomposition import PCA
```

In [2]:
```python
df= pd.read_csv('/Users/SAURABH/Saurabh patil/DATA SCIENCE/PCA/wine.csv')
```

In [3]:
```python
df.head()
```

Out[3]:

	Type	Alcohol	Malic	Ash	Alcalinity	Magnesium	Phenols	Flavanoids	Nonflavanoids	Proanthocyanins	Color	Hue	Dilution	Proline
0	1	14.23	1.71	2.43	15.6	127	2.80	3.06	0.28	2.29	5.64	1.04	3.92	1065
1	1	13.20	1.78	2.14	11.2	100	2.65	2.76	0.26	1.28	4.38	1.05	3.40	1050
2	1	13.16	2.36	2.67	18.6	101	2.80	3.24	0.30	2.81	5.68	1.03	3.17	1185
3	1	14.37	1.95	2.50	16.8	113	3.85	3.49	0.24	2.18	7.80	0.86	3.45	1480
4	1	13.24	2.59	2.87	21.0	118	2.80	2.69	0.39	1.82	4.32	1.04	2.93	735

In [4]:
```python
df1= df.drop(['Type'],axis=1)
```

In [5]:
```python
df1.info()
```

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 178 entries, 0 to 177
Data columns (total 13 columns):
 #   Column           Non-Null Count  Dtype  
---  ------           --------------  -----  
 0   Alcohol          178 non-null    float64
 1   Malic            178 non-null    float64
 2   Ash              178 non-null    float64
 3   Alcalinity       178 non-null    float64
 4   Magnesium        178 non-null    int64  
 5   Phenols          178 non-null    float64
 6   Flavanoids       178 non-null    float64
 7   Nonflavanoids    178 non-null    float64
 8   Proanthocyanins  178 non-null    float64
 9   Color            178 non-null    float64
 10  Hue              178 non-null    float64
 11  Dilution         178 non-null    float64
 12  Proline          178 non-null    int64  
dtypes: float64(11), int64(2)
memory usage: 18.1 KB
```

Performing PCA

In [6]:
```python
# Converting into numpy array
DF1 = df1.values
```

In [7]:
```python
DF1
```

Out[7]:
```
array([[1.423e+01, 1.710e+00, 2.430e+00, ..., 1.040e+00, 3.920e+00,
        1.065e+03],
       [1.320e+01, 1.780e+00, 2.140e+00, ..., 1.050e+00, 3.400e+00,
        1.050e+03],
       [1.316e+01, 2.360e+00, 2.670e+00, ..., 1.030e+00, 3.170e+00,
        1.185e+03],
       ...,
       [1.327e+01, 4.280e+00, 2.260e+00, ..., 5.900e-01, 1.560e+00,
        8.350e+02],
       [1.317e+01, 2.590e+00, 2.370e+00, ..., 6.000e-01, 1.620e+00,
        8.400e+02],
       [1.413e+01, 4.100e+00, 2.740e+00, ..., 6.100e-01, 1.600e+00,
        5.600e+02]])
```

In [8]:
```python
# Normalization function
def norm_func(i):
    x = (i-i.min())/(i.max()-i.min())
    return (x)
```

In [9]:
```python
df_norm = norm_func(DF1)
```

In [10]:
```python
df_norm
```

Out[10]:
```
array([[8.39350664e-03, 9.40548971e-04, 1.36915357e-03, ...,
        5.41708585e-04, 2.25612696e-03, 6.33900242e-01],
       [7.78036396e-03, 9.82218862e-04, 1.19652116e-03, ...,
        5.47661426e-04, 1.94657920e-03, 6.24970980e-01],
       [7.75655259e-03, 1.32748367e-03, 1.51202176e-03, ...,
        5.35755743e-04, 1.80966384e-03, 7.05334341e-01],
       ...,
       [7.82203385e-03, 2.47042926e-03, 1.26795526e-03, ...,
        2.73830713e-04, 8.51256347e-04, 4.96984886e-01],
       [7.76250543e-03, 1.46439903e-03, 1.33343652e-03, ...,
        2.79783555e-04, 8.86973397e-04, 4.99961307e-01],
       [8.33397822e-03, 2.36327811e-03, 1.55369165e-03, ...,
        2.85736396e-04, 8.75067714e-04, 3.33281742e-01]])
```

In [11]:
```python
pca = PCA(n_components = 13)
pca_values = pca.fit_transform(df_norm)
```

In [12]:
```python
pca_values
```

Out[12]:
```
array([[ 1.89635495e-01,  1.27939250e-02,  1.86367678e-03, ...,
         5.28219472e-05, -2.29467534e-05,  4.77801459e-05],
       [ 1.80429093e-01, -3.19353145e-03,  4.06152589e-03, ...,
         2.36793241e-05, -3.40452399e-05,  8.09154665e-06],
       [ 2.60770853e-01, -3.89155676e-03, -6.62684006e-04, ...,
         1.41540730e-04, -2.90486020e-05, -2.10779181e-05],
       ...,
       [ 5.26576900e-02,  1.11772248e-02, -1.33199385e-03, ...,
        -1.32777740e-04,  5.71761518e-05,  2.15343422e-05],
       [ 5.56330203e-02,  1.11144429e-02, -1.06460114e-03, ...,
        -1.81013009e-05, -3.10079415e-05,  7.90293761e-05],
       [-1.11284320e-01, -1.26992448e-04, -3.35175331e-03, ...,
         9.56770872e-05,  1.90015753e-05,  1.60351688e-05]])
```

In [13]:
```python
# The amount of variance that each PCA explains is
var = pca.explained_variance_ratio_
var
```

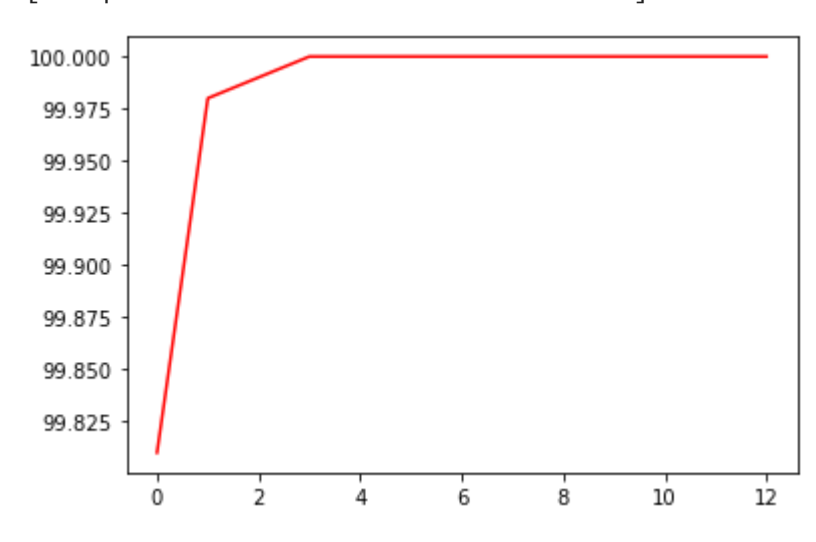
Out[13]:
```
array([9.98091230e-01, 1.73591562e-03, 9.49589576e-05, 5.02173562e-05,
       1.23636847e-05, 8.46213034e-06, 2.80681456e-06, 1.52308053e-06,
       1.12783044e-06, 7.21415811e-07, 3.78060267e-07, 2.12013755e-07,
       8.25392788e-08])
```

In [14]:
```python
# Cumulative variance
var1 = np.cumsum(np.round(var,decimals = 4)*100)
var1
```

Out[14]:
```
array([ 99.81,  99.98,  99.99, 100.  , 100.  , 100.  , 100.  , 100.  ,
       100.  , 100.  , 100.  , 100.  , 100.  ])
```

In [15]:
```python
# Variance plot for PCA components obtained
plt.plot(var1,color="red")
```

Out[15]:
```
[<matplotlib.lines.Line2D at 0x1115a48>]
```



In [16]:
```python
finaldf = pd.concat([pd.DataFrame(pca_values[:,0:3],columns=['pc1','pc2','pc3']), df[['Type']]], axis = 1)
```

In [17]:
```python
finaldf
```

Out[17]:

	pc1	pc2	pc3	Type
0	0.189635	0.012794	0.001864	1
1	0.180429	-0.003194	0.004062	1
2	0.260771	-0.003892	-0.000663	1
3	0.436486	0.000115	-0.000546	1
4	-0.006888	0.011007	-0.000330	1
...	...	...	...	...
173	-0.004155	-0.002703	-0.001473	3
174	0.001864	0.001390	-0.002566	3
175	0.052658	0.011177	-0.001332	3
176	0.055633	0.011114	-0.001065	3
177	-0.111284	-0.000127	-0.003352	3

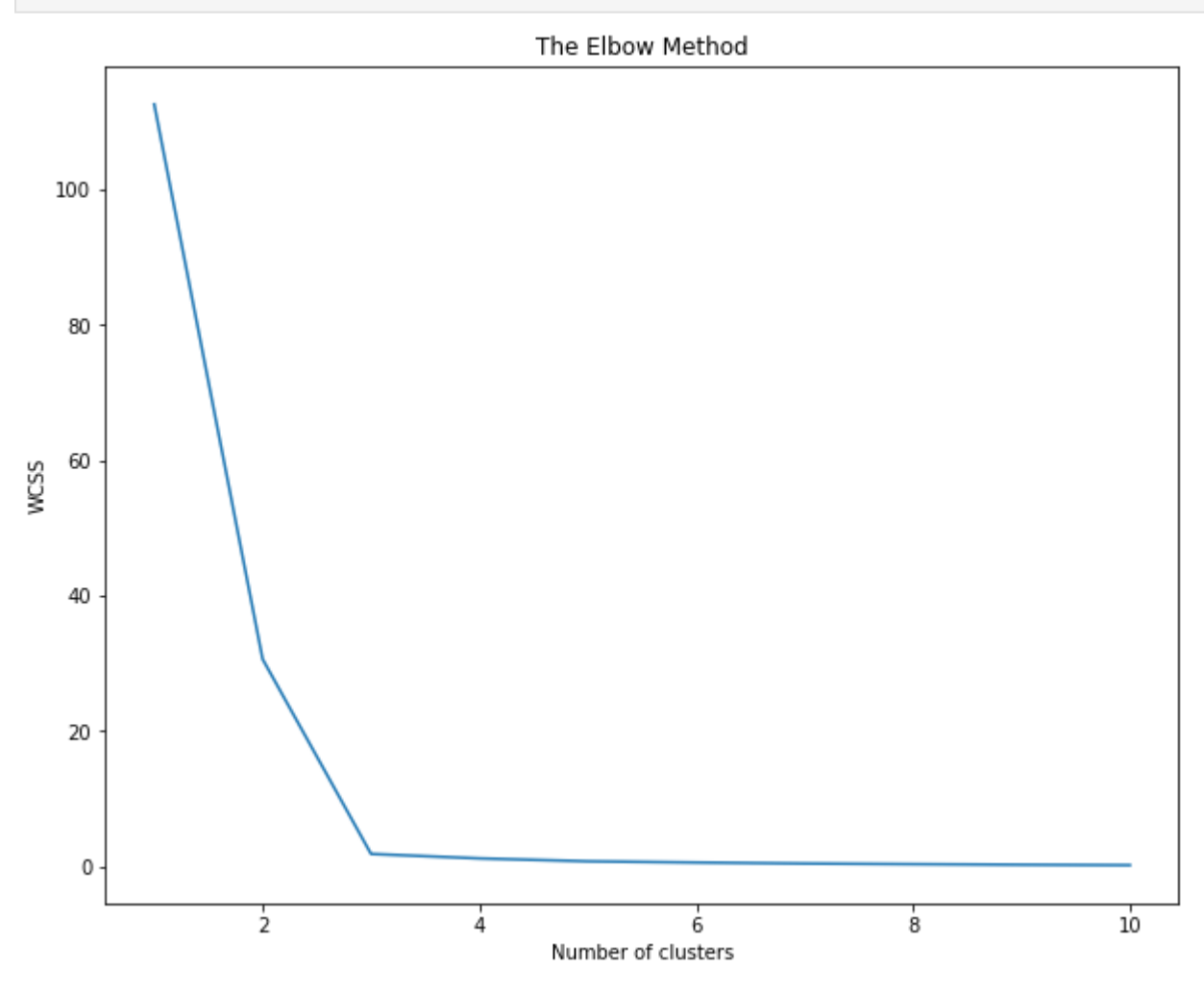
178 rows × 4 columns

Performing K-Means Clustering

Using with Elbow method to find the optimum no of clusters

In [18]:
```python
wcss = []
for i in range(1, 11):
    kmeans = KMeans(n_clusters = i, init = 'k-means++', random_state = 200)
    kmeans.fit(finaldf)
    wcss.append(kmeans.inertia_)

plt.figure(figsize=(10, 8))
plt.plot(range(1, 11), wcss)
plt.title('The Elbow Method')
plt.xlabel('Number of clusters')
plt.ylabel('WCSS')
plt.show()
```



As per this plot, optimum number of clusters= 3

To confirm the same, using Silhouette score's method

In [19]:
```python
for i in range(2,12):
    labels=cluster.KMeans(n_clusters=i,init="k-means++",random_state=200).fit(finaldf).labels_
    print ("Silhouette score for k(clusters) = "+str(i)+" is "
           +str(metrics.silhouette_score(finaldf,labels,metric="euclidean",sample_size=1000,random_state=200)))
```

```
Silhouette score for k(clusters) = 2 is 0.7046376244196589
Silhouette score for k(clusters) = 3 is 0.8906887433929623
Silhouette score for k(clusters) = 4 is 0.7934893991312625
Silhouette score for k(clusters) = 5 is 0.6822063035193922
Silhouette score for k(clusters) = 6 is 0.6914427573862947
Silhouette score for k(clusters) = 7 is 0.5852242596504906
Silhouette score for k(clusters) = 8 is 0.5991039010559479
Silhouette score for k(clusters) = 9 is 0.6002899535946947
Silhouette score for k(clusters) = 10 is 0.5808685430101755
Silhouette score for k(clusters) = 11 is 0.5854630977632279
```

As per the Silhouette score also, K= 3 is the optimum number of clusters

In [20]:
```python
#Hence
model=KMeans(n_clusters=3)
model.fit(finaldf)
model.labels_
```

Out[20]:
```
array([1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1,
       1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1,
       1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 0, 0, 0, 0, 0, 0, 0,
       0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
       0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
       0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 2, 2,
       2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2,
       2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2,
       2, 2])
```

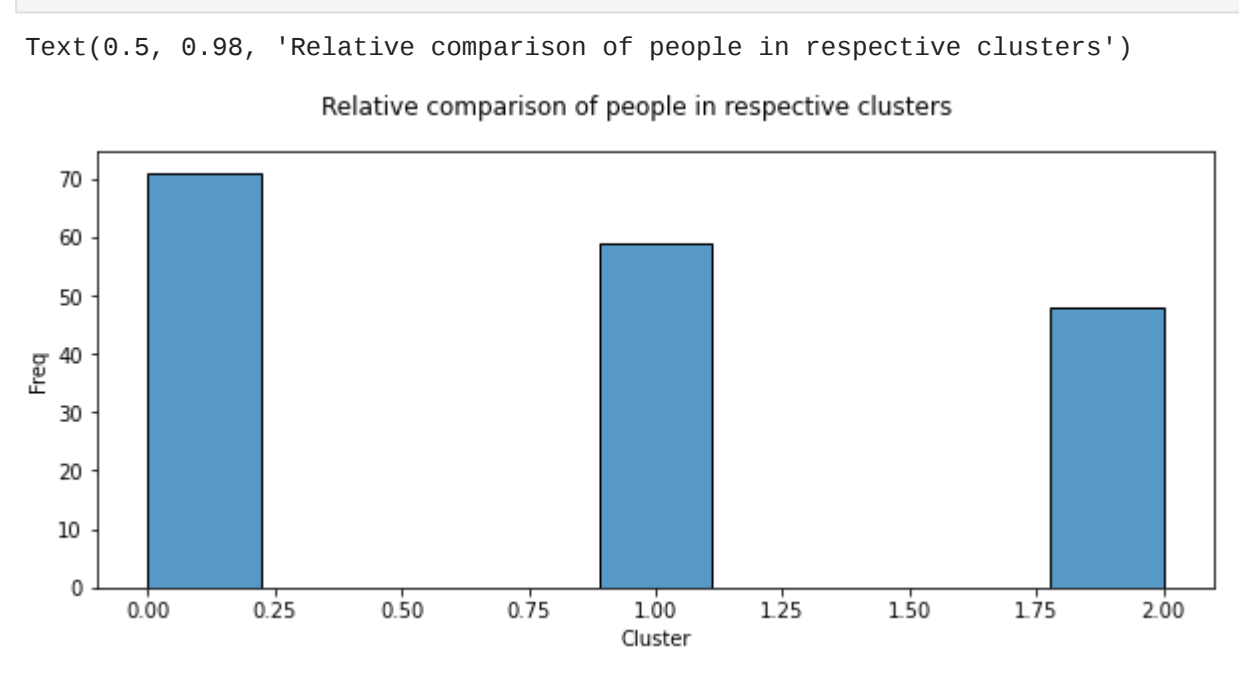
In [21]:
```python
km = pd.Series(model.labels_)
df['kclust']= km
df.iloc[:,1:7].groupby(df.kclust).mean()
```

Out[21]:

kclust	Alcohol	Malic	Ash	Alcalinity	Magnesium	Phenols
0	12.278732	1.932676	2.244789	20.238028	94.549296	2.258873
1	13.744746	2.010678	2.455593	17.037288	106.338983	2.840169
2	13.153750	3.333750	2.437083	21.416667	99.312500	1.678750

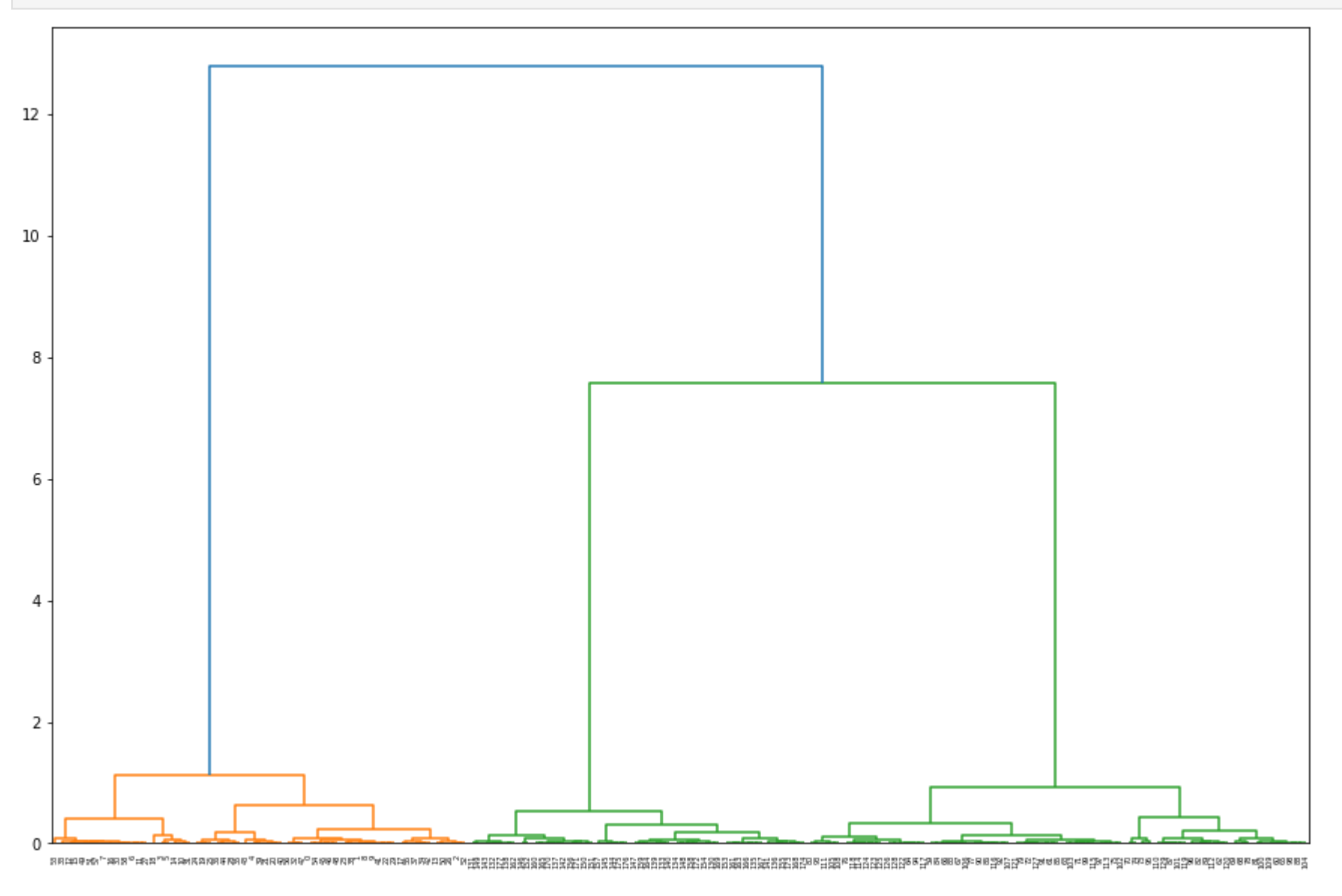
In [22]:
```python
plt.figure(figsize=(10,4))
sns.histplot (x='kclust', data=df)
plt.xlabel('Cluster')
plt.ylabel('Freq')
plt.suptitle('Relative comparison of people in respective clusters')
```

Out[22]:
```
Text(0.5, 0.98, 'Relative comparison of people in respective clusters')
```



Hierarchical Clustering

In [23]:
```python
# create dendrogram
plt.figure(figsize=(15, 10))
dendrogram = sch.dendrogram(sch.linkage(finaldf, method='ward'))
```



The x-axis contains the samples and y-axis represents the distance between these samples. The vertical line with maximum distance is the blue line. If we decide a threshold of 2 and cut the dendrogram:

In [24]:
```python
plt.figure(figsize=(15, 10))
plt.title("Dendrograms")
dend = sch.dendrogram(sch.linkage(finaldf, method='ward'))
plt.axhline(y=2, color='r', linestyle='--')
plt.show()
```

Now, testing for optimum no of clusters in the case of original dataset (without PCA)

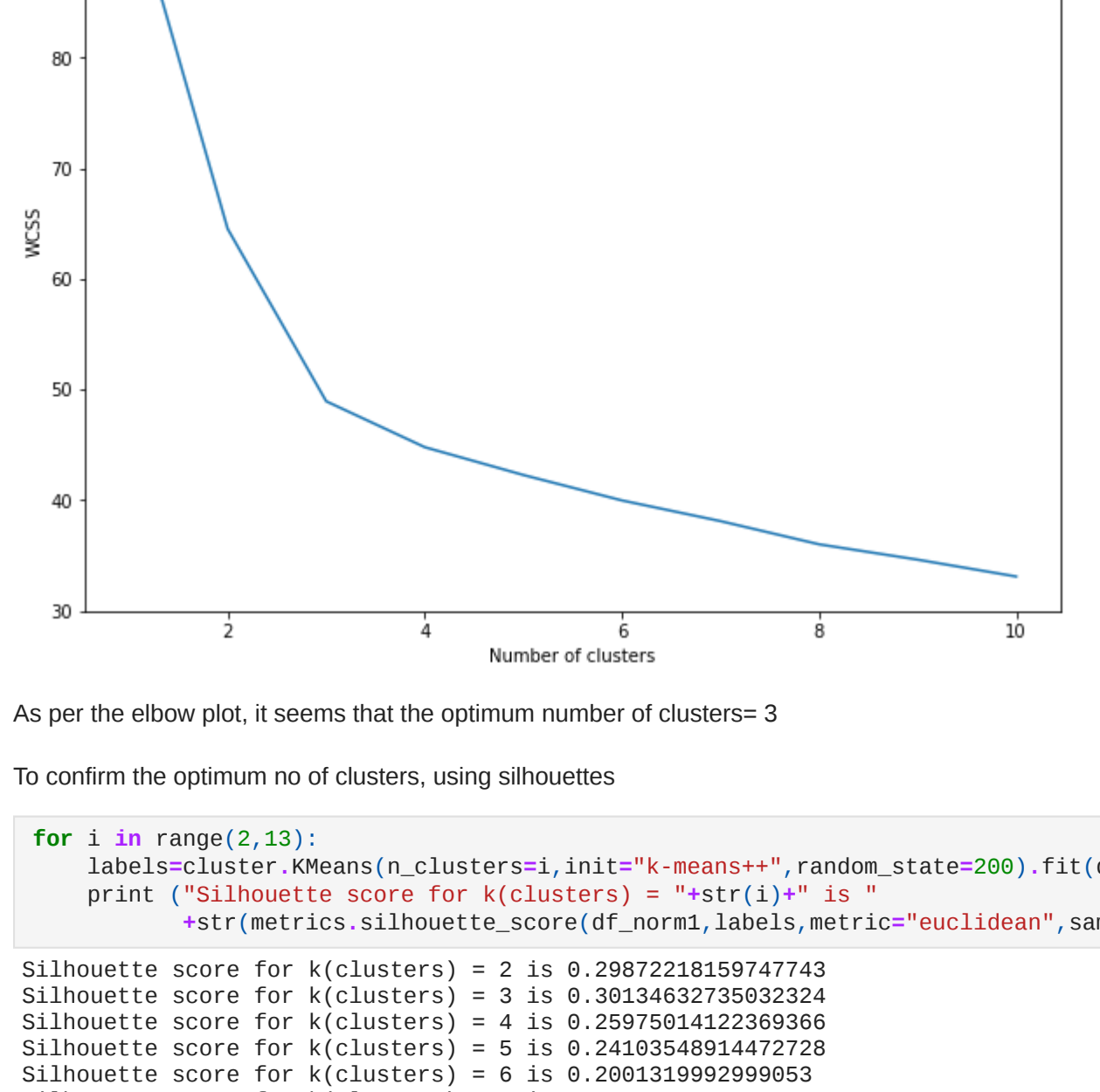
In [25]:
```python
df_norm1 = norm_func(df1)
```

Performing K-Means Clustering

Using elbow method:

In [26]:
```python
wcss1 = []
for k in range(1, 11):
    kmeans1 = KMeans(n_clusters = k, init = 'k-means++', random_state = 200)
    kmeans1.fit(df_norm1)
    wcss1.append(kmeans1.inertia_)

plt.figure(figsize=(10, 8))
plt.plot(range(1, 11), wcss1)
plt.title('The Elbow Method')
plt.xlabel('Number of clusters')
plt.ylabel('WCSS')
plt.show()
```



As per the elbow plot, it seems that the optimum number of clusters= 3

To confirm the optimum no of clusters, using silhouettes

In [27]:
```python
for i in range(2,13):
    labels=cluster.KMeans(n_clusters=i,init="k-means++",random_state=200).fit(df_norm1).labels_
    print ("Silhouette score for k(clusters) = "+str(i)+" is "
           +str(metrics.silhouette_score(df_norm1,labels,metric="euclidean",sample_size=1000,random_state=200)))
```

```
Silhouette score for k(clusters) = 2 is 0.29872218159747743
Silhouette score for k(clusters) = 3 is 0.30134632735032324
Silhouette score for k(clusters) = 4 is 0.25975014122369366
Silhouette score for k(clusters) = 5 is 0.24103548914472728
Silhouette score for k(clusters) = 6 is 0.2001319992999053
Silhouette score for k(clusters) = 7 is 0.13262302760860342
Silhouette score for k(clusters) = 8 is 0.1493889274699824
Silhouette score for k(clusters) = 9 is 0.13953165088987174
Silhouette score for k(clusters) = 10 is 0.14145049854808603
Silhouette score for k(clusters) = 11 is 0.14388798417780793
Silhouette score for k(clusters) = 12 is 0.14473079778938786
```

Performing Hierarchical clustering

In [28]:
```python
# create dendrogram
plt.figure(figsize=(15, 10))
dendrogram = sch.dendrogram(sch.linkage(df_norm1, methSo number of clusters is the same (=3)od='ward'))
```

So number of clusters is the same (=3)

In [ ]: