

```
In [1]: import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
import seaborn as sns
import warnings
warnings.filterwarnings("ignore")
```

```
In [2]: df = pd.read_excel('/Users/SAURABH/Saurabh patil/DATA SCIENCE/SW/Air/lines>Data.xlsx')
```

```
Out[2]:
```

	Month	Passengers
0	1995-01-01	112
1	1995-02-01	118
2	1995-03-01	132
3	1995-04-01	129
4	1995-05-01	121
...	...	...
91	2002-08-01	405
92	2002-09-01	355
93	2002-10-01	306
94	2002-11-01	271
95	2002-12-01	306

96 rows x 2 columns

```
In [3]: df.dtypes
```

```
Out[3]: Month      datetime64[ns]
Passengers      int64
dtype: object
```

```
In [4]: df1 = df.set_index('Month')
df1
```

```
Out[4]:
```

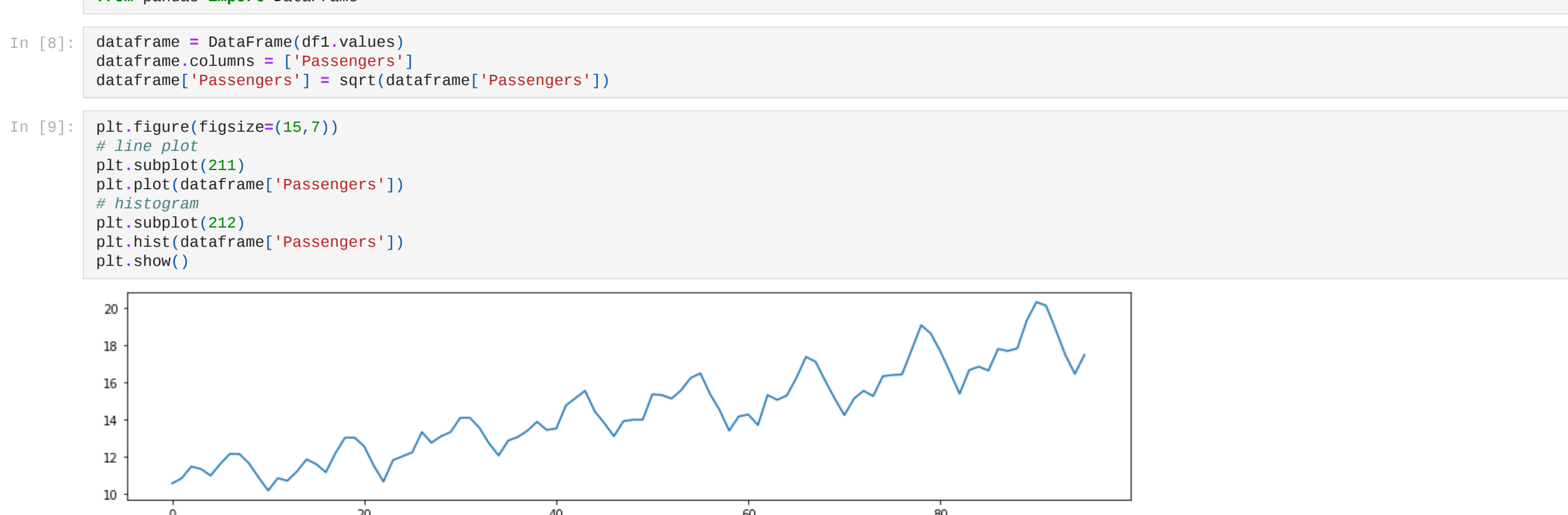
	Month	Passengers
1995-01-01	112	
1995-02-01	118	
1995-03-01	132	
1995-04-01	129	
1995-05-01	121	
...	...	
2002-08-01	405	
2002-09-01	355	
2002-10-01	306	
2002-11-01	271	
2002-12-01	306	

96 rows x 1 columns

```
In [5]: df1.dtypes
```

```
Out[5]: Passengers      int64
dtype: object
```

```
In [6]: plt.figure(figsize=(15,7))
# line plot
plt.subplot(211)
plt.plot(df1)
# histogram
plt.subplot(212)
plt.hist(df1)
plt.show()
```

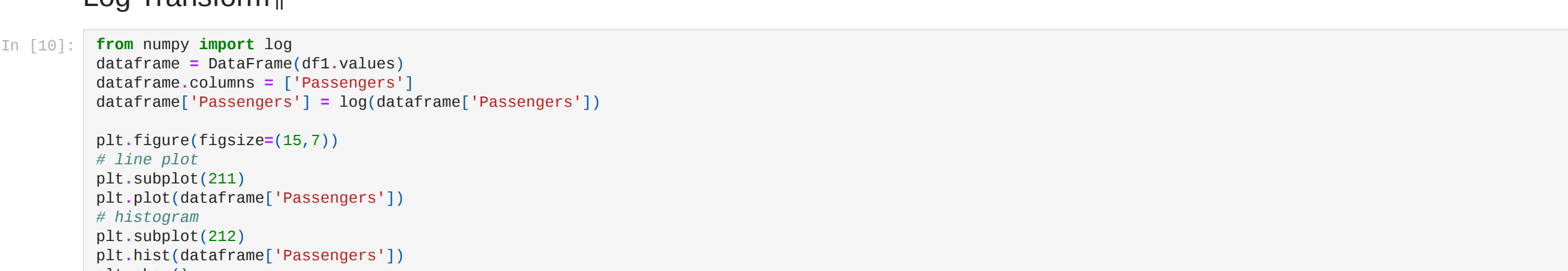


## Square Root Transform

```
In [7]: from numpy import sqrt
from pandas import DataFrame
```

```
In [8]: dataframe = DataFrame(df1.values)
dataframe.columns = ['Passengers']
dataframe['Passengers'] = sqrt(dataframe['Passengers'])
```

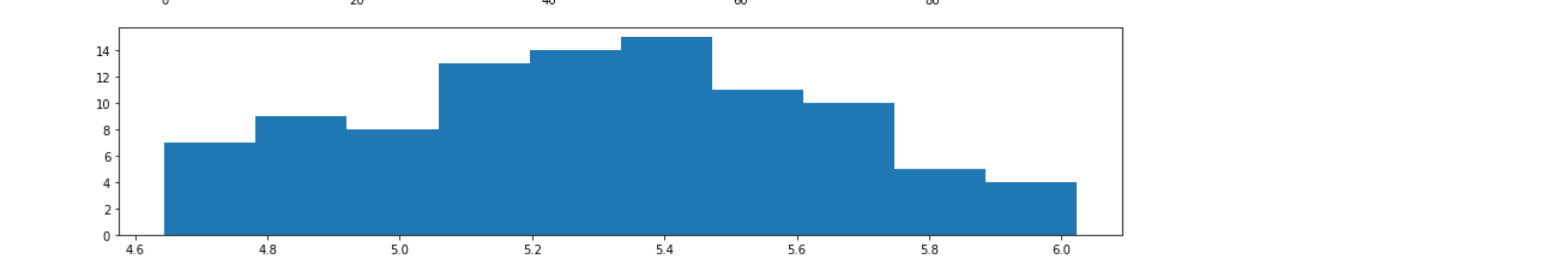
```
In [9]: plt.figure(figsize=(15,7))
# line plot
plt.subplot(211)
plt.plot(dataframe['Passengers'])
# histogram
plt.subplot(212)
plt.hist(dataframe['Passengers'])
plt.show()
```



## Log Transform

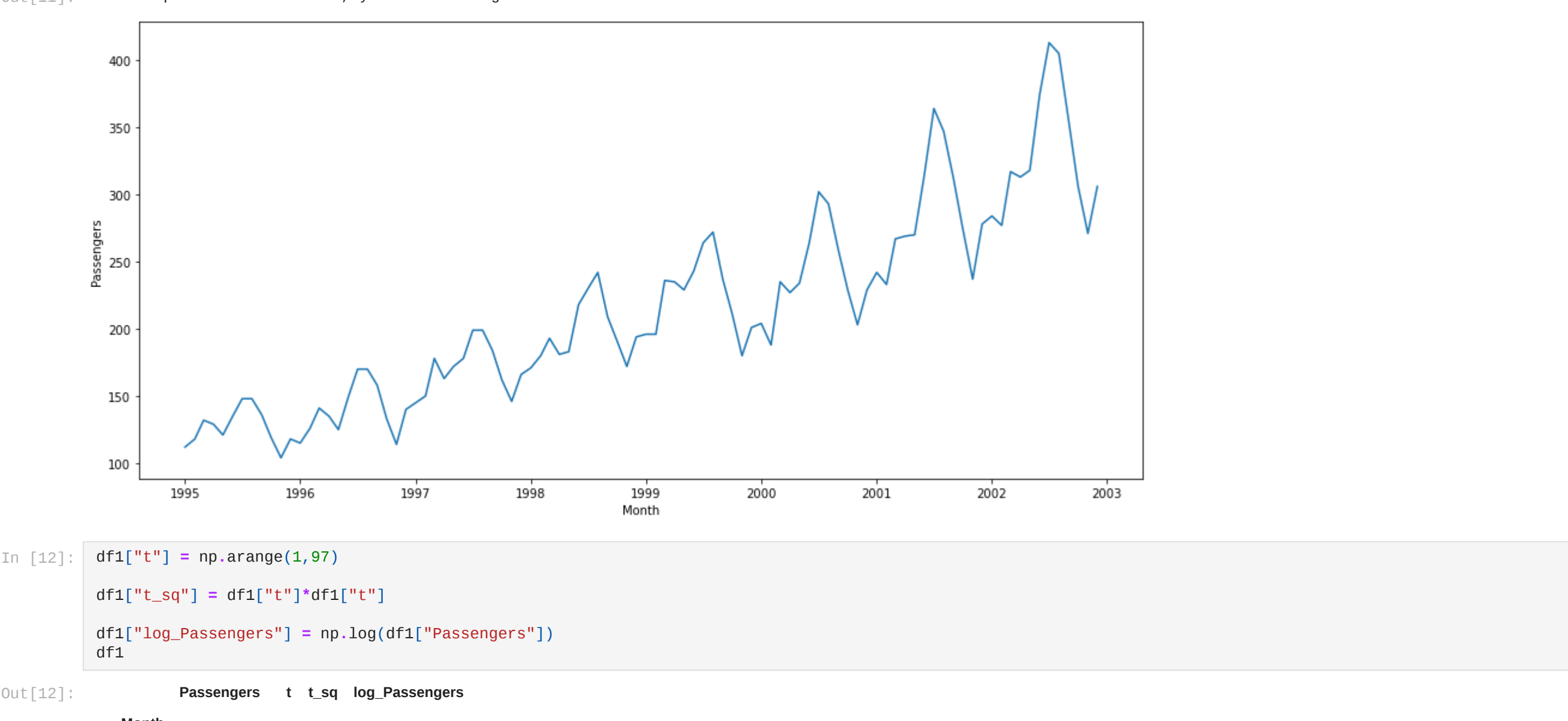
```
In [10]: from numpy import log
dataframe = DataFrame(df1.values)
dataframe.columns = ['Passengers']
dataframe['Passengers'] = log(dataframe['Passengers'])
```

```
plt.figure(figsize=(15,7))
# line plot
plt.subplot(211)
plt.plot(dataframe['Passengers'])
# histogram
plt.subplot(212)
plt.hist(dataframe['Passengers'])
plt.show()
```



```
In [11]: plt.figure(figsize=(15,7))
sns.lineplot(x="Month",y="Passengers",data=df1)
```

```
Out[11]: <AxesSubplot: xlabel='Month', ylabel='Passengers'>
```



```
In [12]: df1["t"] = np.arange(1,97)
df1["t_sq"] = df1["t"]*df1["t"]
df1["log_Passengers"] = np.log(df1["Passengers"])
df1
```

```
Out[12]:
```

	Month	Passengers	t	t_sq	log_Passengers
1995-01-01	112	1	1	4.718499	
1995-02-01	118	2	4	4.770685	
1995-03-01	132	3	9	4.882802	
1995-04-01	129	4	16	4.859812	
1995-05-01	121	5	25	4.795791	
...	...	...	...	...	
2002-08-01	405	92	8464	6.003887	
2002-09-01	355	93	8649	5.872138	
2002-10-01	306	94	8836	5.723585	
2002-11-01	271	95	9025	5.602118	
2002-12-01	306	96	9216	5.723585	

96 rows x 4 columns

```
In [13]: Train = df1.head(77)
Test = df1.tail(19)
```

```
In [14]: #Linear Model
import statsmodels.formula.api as smf
```

```
linear_model = smf.ols('Passengers~t',data=Train).fit()
pred_linear = pd.Series(linear_model.predict(pd.DataFrame(Test[['t','t_sq']]]))
rmse_linear = np.sqrt(np.mean((np.array(Test['Passengers'])-np.array(pred_linear))**2))
rmse_linear
```

```
Out[14]: 58.14854431956879
```

```
In [15]: #Exponential
Exp = smf.ols('log_Passengers~t',data=Train).fit()
pred_Exp = pd.Series(Exp.predict(pd.DataFrame(Test[['t','t_sq']]]))
rmse_Exp = np.sqrt(np.mean((np.array(Test['Passengers'])-np.array(np.exp(pred_Exp))**2))
rmse_Exp
```

```
Out[15]: 47.889965425183992
```

```
In [16]: #Quadratic
Quad = smf.ols('Passengers~t+t_sq',data=Train).fit()
pred_Quad = pd.Series(Quad.predict(Test[['t','t_sq']]))
rmse_Quad = np.sqrt(np.mean((np.array(Test['Passengers'])-np.array(pred_Quad))**2))
rmse_Quad
```

```
Out[16]: 58.92632852818824
```

```
In [17]: #Compare the results
data = {"MODEL":pd.Series(["rmse_linear","rmse_Exp","rmse_Quad"]), "RMSE_Values":pd.Series([rmse_linear,rmse_Exp,rmse_Quad])}
table_rmse=pd.DataFrame(data)
table_rmse.sort_values(['RMSE_Values'])
```

```
Out[17]:
```

	MODEL	RMSE_Values
1	rmse_Exp	47.8899654
0	rmse_linear	58.148544
2	rmse_Quad	58.926329

```
In [18]: df2 = df1.iloc[:,0:1]
df2
```

```
Out[18]:
```

	Month	Passengers
1995-01-01	112	
1995-02-01	118	
1995-03-01	132	
1995-04-01	129	
1995-05-01	121	
...	...	
2002-08-01	405	
2002-09-01	355	
2002-10-01	306	
2002-11-01	271	
2002-12-01	306	

96 rows x 1 columns

```
In [19]: # separate out a validation dataset
split_point = len(df2) - 10
dataset_validation = df2[0:split_point], df2[split_point:]
print('Dataset %d, Validation %d' % (len(dataset), len(validation)))
dataset.to_csv('dataset.csv', header=False)
validation.to_csv('validation.csv', header=False)
```

Dataset 86, Validation 10

## Persistence/ Base model

```
In [21]: # evaluate a persistence model
from pandas import read_csv
from sklearn.metrics import mean_squared_error
from math import sqrt
```

```
# load data
train = read_csv('dataset.csv', header=None, index_col=0, parse_dates=True, squeeze=True)
# prepare data
X = train.values
X = X.astype('float32')
train_size = int(len(X) * 0.50)
train, test = X[0:train_size], X[train_size:]
```

```
In [22]: # walk-forward validation
history = [x for x in train]
predictions = list()
for i in range(len(test)):
    yhat = history[-1]
    predictions.append(yhat)
# observation
obs = test[1]
history.append(obs)
print('>Predicted=%3f, Expected=%3f' % (yhat, obs))
# report performance
rmse = sqrt(mean_squared_error(test, predictions))
print('RMSE: %3f' % rmse)
```

```
>Predicted=239.000, Expected=242.000
>Predicted=242.000, Expected=209.000
>Predicted=209.000, Expected=191.000
>Predicted=191.000, Expected=172.000
>Predicted=172.000, Expected=184.000
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>Predicted=342.000, Expected=274.000
>Predicted=274.000, Expected=278.000
>Predicted=278.000, Expected=284.000
>Predicted=284.000, Expected=277.000
RMSE: 25.680
```

## ARIMA Hyperparameters

```
In [23]: # grid search ARIMA parameters for a time series
import warnings
from pandas import read_csv
from statsmodels.tsa.arima.model import ARIMA
from sklearn.metrics import mean_squared_error
from math import sqrt
```

```
# evaluate an ARIMA model for a given order (p,d,q) and return RMSE
def evaluate_arima_model(X, arima_order):
# prepare training dataset
X = X.astype('float32')
train_size = int(len(X) * 0.50)
train, test = X[0:train_size], X[train_size:]
history = [x for x in train]
```

```
# make predictions
predictions = list()
for i in range(len(test)):
    model = ARIMA(history, order=arima_order)
    model_fit = model.fit(disp=0)
    yhat = model_fit.forecast()[0]
    predictions.append(yhat)
    history.append(test[i])
# calculate out of sample error
rmse = sqrt(mean_squared_error(test, predictions))
return rmse
```

```
# walk-forward validation
history = [x for x in train]
predictions = list()
for i in range(len(test)):
    yhat = history[-1]
    predictions.append(yhat)
# observation
obs = test[1]
history.append(obs)
print('>Predicted=%3f, Expected=%3f' % (yhat, obs))
# report performance
rmse = sqrt(mean_squared_error(test, predictions))
print('RMSE: %3f' % rmse)
```

```
>Predicted=239.000, Expected=242.000
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