

# Lab3 Final, w203: Statistics for Data Science

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## 1. Introduction

Our team has been hired to provide research for a political campaign. The campaign has obtained a dataset of crime statistics for a selection of counties in North Carolina. Our task is to examine the data to help the campaign understand the determinants of crime and to generate policy suggestions that are applicable to local government.

The data provided consists of 25 variables and 97 different observations collected in a given year. Moreover the dataset obtained is a single cross-section of data collected from variety of different sources. For the analysis made in this research, we will assume that the data collected from different counties in NC were randomly sampled.

Our primary analysis of data will include ordinary least squares regressions to make causal estimates and we will clearly explain how omitted variables may affect our conclusions. We begin our research by conducting exploratory analysis of the dataset to gain a better understanding of the variables.

## 2. Data input and cleanup

Our first step is to detect anomalies such as missing and duplicate values and to clean up the dataset before deeper dive into regression analysis.

```
# Read the csv file
crime_data_raw = read.csv("crime_v2.csv")
```

```
summary(crime_data_raw)
tail(crime_data_raw, n=8)
```

There appears to be 6 rows of NA's across all variables. We can simply use `na.omit()`, because the number of all-NA rows matches the count on all the variables.

We noticed that 'prbconv' is a factor while the rest of the variables are numeric.

County and Year variables just represent the different counties and the year the data was collected. Year is always 87. Hence, we can safely remove these from the dataset for further analysis.

We also noticed a duplicate record (record #89) in the dataset. As this could potentially affect our regression analysis, we will remove the duplicate record.

```
# remove NA rows
crime_data = na.omit(crime_data_raw)
# convert factor to numeric for variable prbconv
crime_data$prbconv = as.numeric(levels(crime_data$prbconv)[crime_data$prbconv])
crime_data = crime_data %>% dplyr::select(-c(year, county))
# convert percentages into (0, 100) range
crime_data$pctmin80 = crime_data$pctmin80 * 100
crime_data$pctymle = crime_data$pctymle * 100
# convert probabilities into (0, 100) range
crime_data$prbarr = crime_data$prbarr * 100
crime_data$prbconv = crime_data$prbconv * 100
```

```
# remove duplicate record
duplicated(crime_data)[duplicated(crime_data)==TRUE]

## [1] TRUE

crime_data = distinct(crime_data)
```

## Influential outliers

We now present some influential outliers we found during our analysis that affect our regression fit.

In general, the outliers are counties that are heavy on tourism, but with low resident population. This causes high crime rates and police presence even in the presence of low density, because density probably counts only residents.

*wser*, observation #84: extremely high service wages. This observation is so skewed that it pulls the regression line of fit. The county (FIPS: 185) corresponds to Warren; there is nothing in Wikipedia to suggest that this county can command such high service wages.

We think this is a measurement error and we will remove it.

```
par(mfrow=c(2,4), mai=c(0.35,0.35,0.35,0.35))

# Notice the outlier
boxplot(crime_data$wser, main="Service wages")

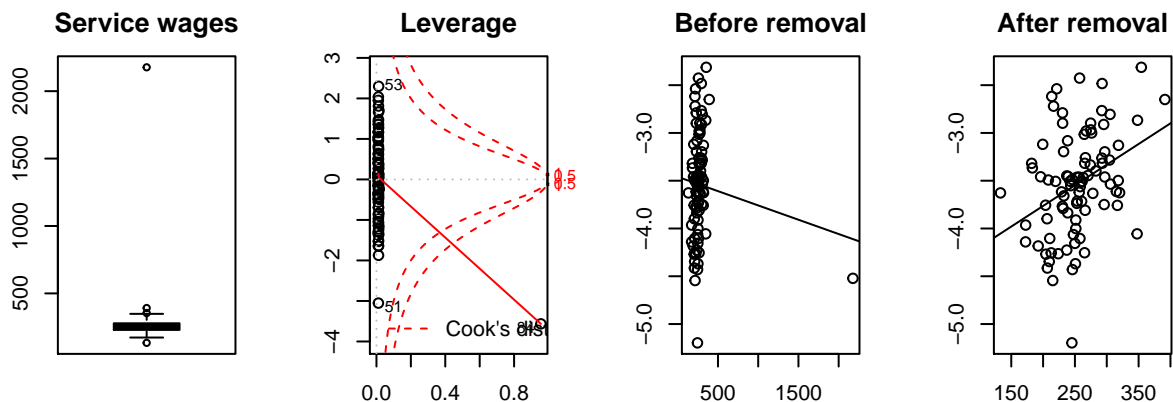
m <- lm(log(crmrte) ~ wser, data = crime_data)

# Notice the leverage of the data point
plot(m, which = 5, main = "Leverage", caption = NA)

# Note how the line of fit changes after removal
plot(crime_data$wser, log(crime_data$crmrte), main = "Before removal")
abline(m)

crime_data_tmp <- crime_data %>% dplyr::slice(-84)
plot(crime_data_tmp$wser, log(crime_data_tmp$crmrte), main = "After removal")
m <- lm(log(crmrte) ~ wser, data = crime_data_tmp)
abline(m)

# Remove
crime_data <- crime_data_tmp
```



*polpc*, observation #51: highly influential observation, which has very low crime rate, yet very high police per capita. This observation corresponds to Madison County in the mountains of western NC. This county gets a lot of tourists, so it may have more police than otherwise. This merits further investigation. We will remove it to improve our fit.

```
par(mfrow=c(2,4), mai=c(0.35,0.35,0.35,0.35))

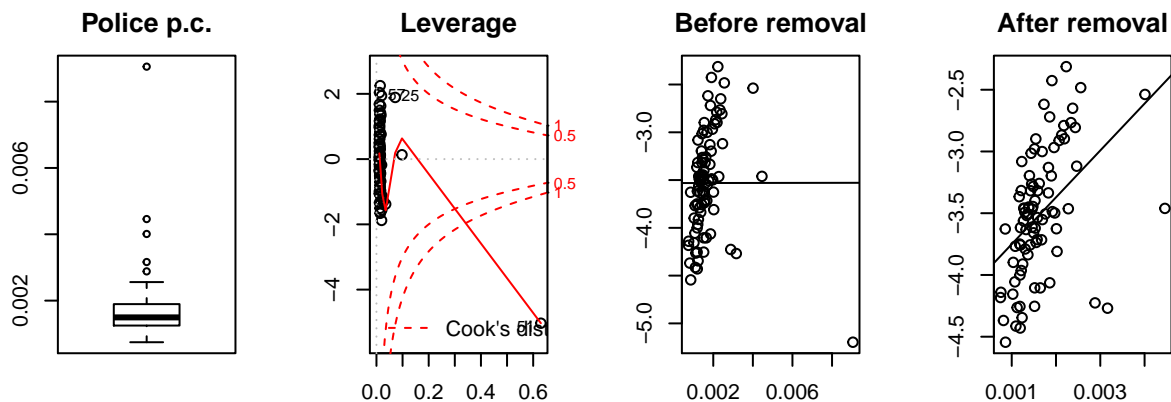
# Notice the outlier
boxplot(crime_data$polpc, main = "Police p.c.")
m <- lm(log(crmrte) ~ polpc, data = crime_data)

# Notice the leverage of the data point
plot(m, which = 5, main = "Leverage", caption = NA)

# Note how the line of fit changes after removal
plot(crime_data$polpc, log(crime_data$crmrte), main = "Before removal")
abline(m)

crime_data_tmp <- crime_data %>% dplyr::slice(-51)
plot(crime_data_tmp$polpc, log(crime_data_tmp$crmrte), main = "After removal")
m <- lm(log(crmrte) ~ polpc, data = crime_data_tmp)
abline(m)

# Remove
crime_data <- crime_data_tmp
```



*density*, observation #78: extremely low density. Looking at FIPS numbering for the county (173), we see that this corresponds to Swain County, western North Carolina. This county is almost entirely forested and an influential outlier. It also derives revenue from tourism. We can remove this county to improve our fit.

```
par(mfrow=c(2,4), mai=c(0.35,0.35,0.35,0.35))

# Notice the outlier
boxplot(log(crime_data$density), main = "Density")
m <- lm(log(crmrte) ~ log(density), data = crime_data)

# Notice the leverage
plot(m, which = 5, caption = NA, main = "Leverage")

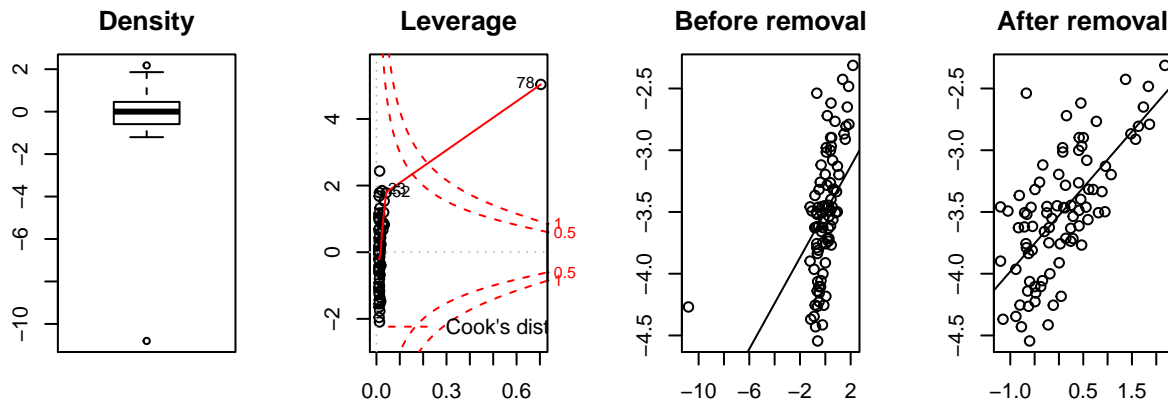
# Print "before-after" graphs
plot(log(crime_data$density), log(crime_data$crmrte), main = "Before removal")
abline(m)
```

```

crime_data_tmp <- crime_data %>% dplyr::slice(-78)
plot(log(crime_data_tmp$density), log(crime_data_tmp$crmrte), main = "After removal")
m <- lm(log(crmrte) ~ log(density), data = crime_data_tmp)
abline(m)

# Remove
crime_data <- crime_data_tmp
# See below
crime_data <- crime_data %>% slice(-25)

```



Finally, observation #25 causes outliers in the final model fit due to a lot of influence. It shows very high crime rate and very high police per capita, while also showing very low density, very low minority and highest tax per capita.

The observation corresponds to Dare County, which consists mostly of a sliver of an island. NCPedia lists seasonal tourism as the primary industry of the county. This can explain why there is high crime and police presence, even though there is low population density and high tax revenue.

This observation has a high Cook's distance ( $>1$ ). It also is an unusual, outlier county; we removed it to improve our model fit.

### 3. Exploratory Data Analysis

We will now try to get a sense of each variable in the dataset. First, a utility function to describe a variable.

```

# Utility function to describe a column variable
f_describe_col = function (col, do_log=FALSE, plot_model=FALSE, do_sqrt=FALSE) {
  y = log(crime_data$crmrte)
  par(mfrow=c(2,4), mai=c(0.35,0.35,0.35,0.35))
  if (is.numeric(col)) {
    hist(col, main="Histogram")
    boxplot(col, main="Box plot")
  }
  if (do_log == TRUE) {
    x = log(col)
    hist(x, main="Histogram, log")
  } else if (do_sqrt == TRUE) {
    x = sqrt(col)
    hist(x, main="Histogram, sqrt")
  } else {

```

```

  x = col
}
if (is.numeric(col)) {
  print(paste("Correlation: ", signif(cor(x, y), 3)))
}
m = lm(y ~ x)
plot(x, y, main="Cor. with crime rate",
     xlab="predictor",
     ylab="crime")
if (is.numeric(col))
  abline(m, col="blue")
if (plot_model == TRUE) {
  plot(m, which=5, caption=NA, main="Leverage")
}
}

```

## Single variable analysis

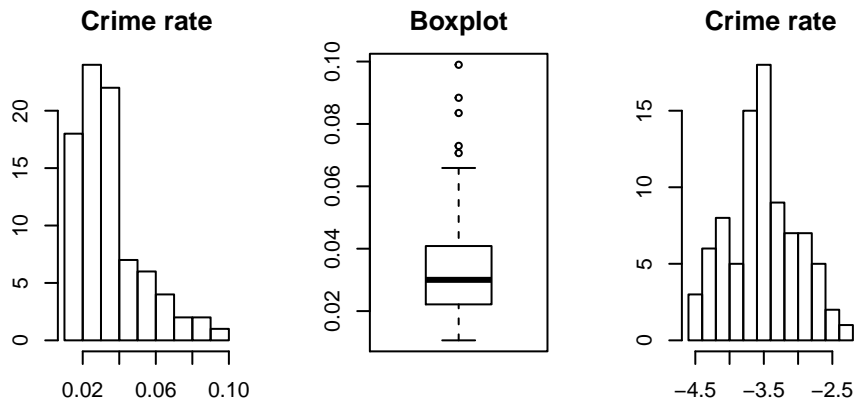
### Crime rate

Crime rate is the key dependent variable of interest.

```

par(mfrow=c(2,4), mai=c(0.35,0.35,0.35,0.35))
hist(crime_data$crmrte, main = "Crime rate",
     xlab="Crime Rate")
boxplot(crime_data$crmrte, main = "Boxplot")
hist(log(crime_data$crmrte), main = "Crime rate",
     xlab="Log of Crime Rate")
crime_data$log_crmrte = log(crime_data$crmrte)

```



Looking at the histogram, the distribution is positively skewed to the left. We can take the log transformation which makes the variable appear more normally distributed.

Crime rate is mostly low, but there are some observations that show high crime rate (positive outliers). This causes skew.

```

crime_data %>% filter(crmrte > 0.07) %>% dplyr::select(density, central, urban, prbarr, prbconv)

## # A tibble: 5 x 5
##   density central urban prbarr prbconv
##   <dbl>   <int> <int> <dbl>   <dbl>
## 1    3.93     0     1   15.5   26.0

```

```
## 2    5.67      1    1   13.3   45.9
## 3    8.83      1    1   14.9   34.8
## 4    6.29      0    1   23.7   39.3
## 5    1.57      1    0   18.3   34.3
```

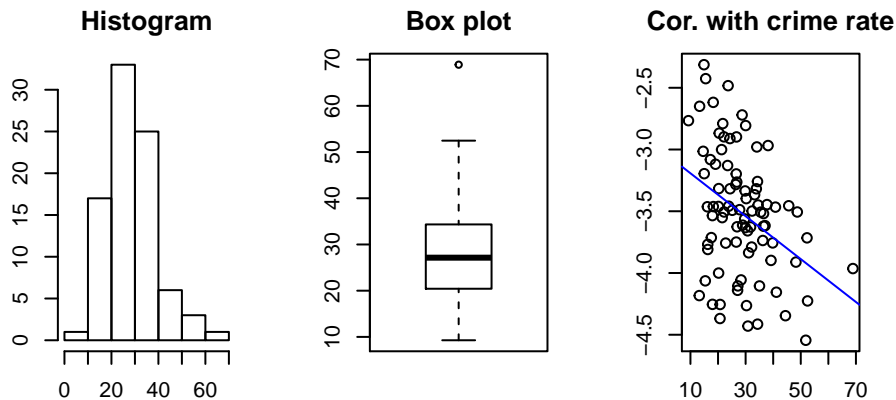
We see that outlier high-crime areas are in central, urban North Carolina.

---

## Probability of arrest

```
f_describe_col(crime_data$prbarr)
```

```
## [1] "Correlation: -0.37"
```



The plot looks fairly normal; there is only one outlier that corresponds to the high arrest probability of 0.7. It is not influential, so we will keep it.

There is fairly negative correlation of -0.37: as probability of arrests increases, crime rate goes down. It may be that arrests are a deterrent, indicating causality.

We will include `prbarr` in our model.

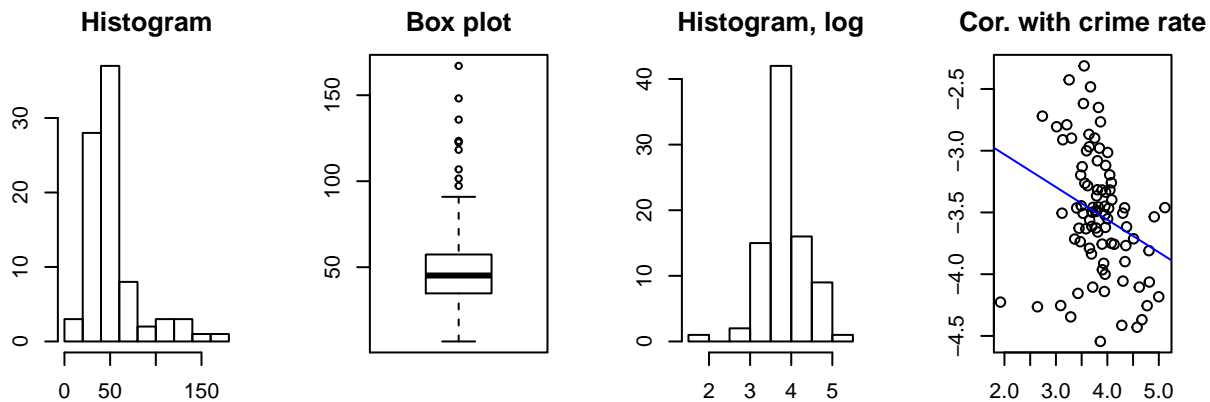
---

## Probability of conviction

```
f_describe_col(crime_data$prbconv, do_log=TRUE)
```

```
## [1] "Correlation: -0.275"
```

```
crime_data$log_prbconv = log(crime_data$prbconv)
```



This variable has quite a bit of left skew. It also has many outliers after the 3rd quartile. There are a few beyond 1 as well. Again, this is because we are not looking at a real probability but a ratio of convictions to arrests. It is possible, although perhaps uncommon, that a suspect is arrested once but convicted on multiple charges.

Taking a log transform improves the skew, although the spread is still quite a bit. There are no outliers with large influence as measured by Cook's distance.

There is moderate negative correlation with crime rate of -0.3. As convictions go up, crime rate goes down. Since we have already considered *prbarr*, let us check if *prbconv* has high correlation with *prbarr*:

```
print(cor(crime_data$prbarr, crime_data$prbconv))
```

```
## [1] -0.3058084
```

```
print(cor(crime_data$prbarr, crime_data$log_prbconv))
```

```
## [1] -0.299908
```

We don't see much correlation and so, will include *log\_prbconv* in our model.

## Police per capita

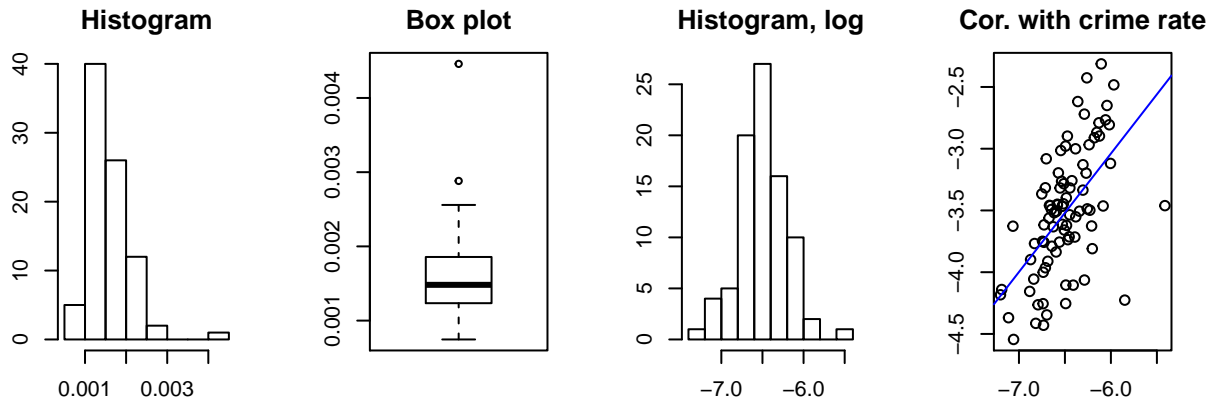
Note: In our first pass, we found an influential outlier with very low crime rate, even at very high police per capita. We removed it, as mentioned in the section on outliers.

Police per capita has positive skew. We observed that taking the log transformation made the distribution more normal.

```
f_describe_col(crime_data$polpc, do_log=TRUE)
```

```
## [1] "Correlation: 0.579"
```

```
crime_data$log_polpc = log(crime_data$polpc)
```



We see fairly strong positive correlation of 0.6 with crime rate: high number of police per capita is associated with high crime rate. It is probably a cause, rather than a result. More police may have been deployed to deal with higher amount of crime. If that is the case, it is worth questioning further why the additional police has not lowered the crime rate: are they ineffective?

For our first model, we will *not* include this variable.

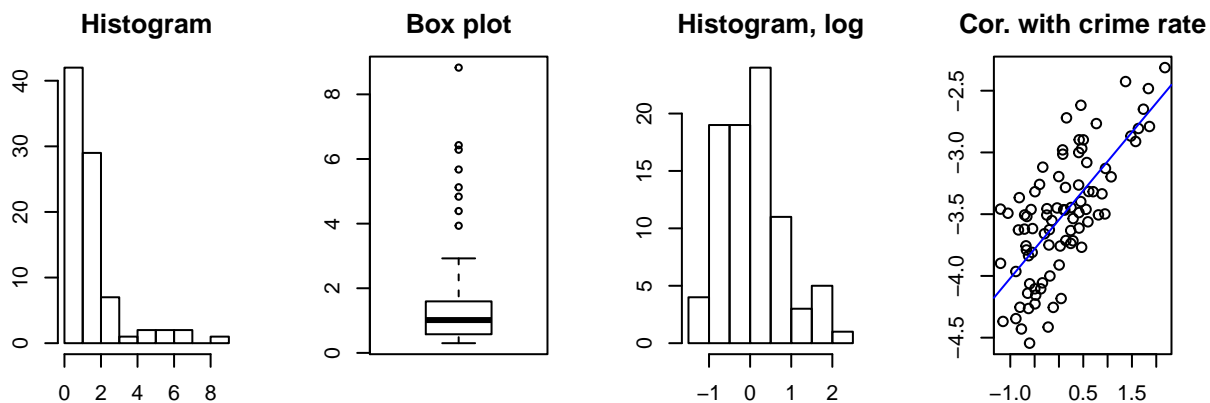
## Population density

In our first pass, we found an influential outlier where observation #79 has Cook's distance beyond 1, meaning extreme leverage. The value of 0.000020342 seems like an unlikely value for people per square mile. We thus removed it from consideration.

```
f_describe_col(crime_data$density, do_log=TRUE)
```

```
## [1] "Correlation: 0.715"
```

```
crime_data$log_density = log(crime_data$density)
```



The histogram of density shows quite a bit positive skew. The log transformation shows a more promising normal distribution. There are no outliers with large leverage as measured by Cook's distance.

We see high positive correlation with crime rate. It may be that high population density indicates greater scope for hiding or cooperation in order to commit crime, indicating causality. We will surely consider this variable in our model.

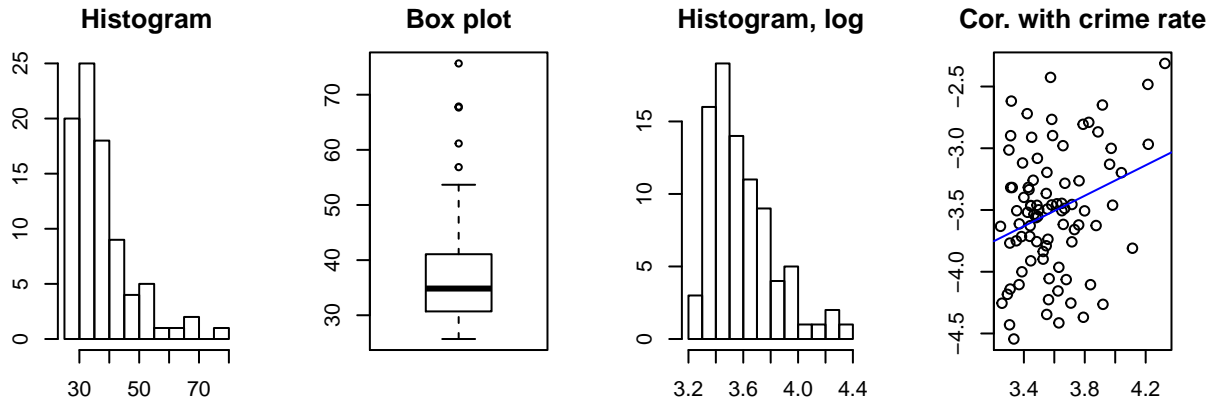


## Tax revenue per capita

```
f_describe_col(crime_data$taxpc, do_log=TRUE)
```

```
## [1] "Correlation: 0.29"
```

```
crime_data$log_taxpc = log(crime_data$taxpc)
```



Tax revenue also shows positive skew, with one outlier indicating high tax revenue per capita ( $>100$ ). It does not show a lot of leverage (Cook's distance  $> 1$ ), however, so we will keep the value.

We also see considerable positive correlation with crime rate. It may be that tax revenue is a proxy for wealth, and high amount of wealth attracts crime. On the other hand, it is worth checking if we are spending tax dollars wisely in combating crime: if that were the case, counties with higher tax revenue would probably see lower crime.

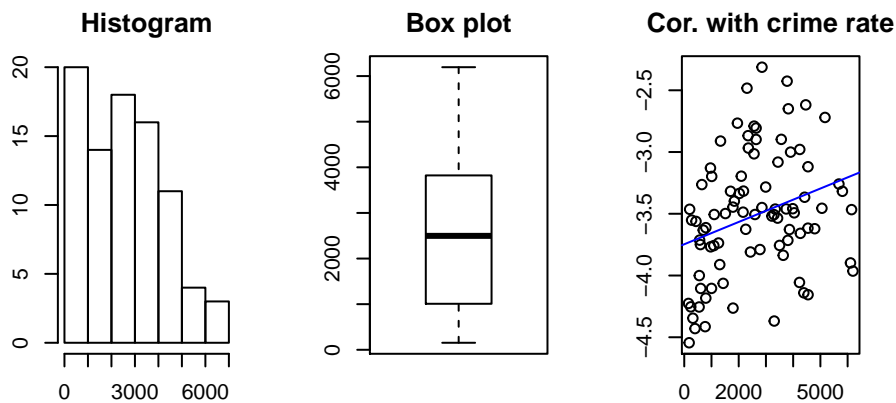
We will *not* include this variable in a first model.

---

## Percent minority

```
f_describe_col(crime_data$pctmin80)
```

```
## [1] "Correlation: 0.297"
```



Minority percentage has a bit positive skew, but no outliers. The range is quite limited.

There is a fair amount of positive correlation with crime rate (0.27). It may be that as minorities increase, there is loss of social homogeneity and/or hate crime.

We will include this variable in our model.

---

### West, Central, Urban

```
sqldf('SELECT COUNT(*) AS Only_Central FROM crime_data WHERE central =1 AND (west!=1 OR urban !=1)')

##    Only_Central
## 1              33

sqldf('SELECT COUNT(*) AS Only_West FROM crime_data WHERE west =1 AND (central!=1 OR urban !=1)')

##    Only_West
## 1           20

sqldf('SELECT COUNT(*) AS Only_Urban FROM crime_data WHERE urban =1 AND (central!=1 and west !=1)')

##    Only_Urban
## 1             2

sqldf('SELECT COUNT(*) AS All_regions FROM crime_data WHERE central =1 and west=1 and urban =1')

##    All_regions
## 1              0

sqldf('SELECT COUNT(*) AS Central_And_West FROM crime_data WHERE central =1 and west=1' )

##    Central_And_West
## 1                   1

sqldf('SELECT COUNT(*) AS West_And_Urban FROM crime_data WHERE west =1 and urban=1' )

##    West_And_Urban
## 1                   1

sqldf('SELECT COUNT(*) AS Central_And_Urban FROM crime_data WHERE central =1 and urban=1' )

##    Central_And_Urban
## 1                     5

sqldf('SELECT COUNT(*) AS No_Region FROM crime_data WHERE central !=1 AND west!=1 AND urban!=1' )

##    No_Region
## 1           32
```

We observe the below:

- 33 observations have been marked as central with no overlap on west or urban
- 19 observations have been marked as west with no overlap on central or urban
- 2 observations have been marked as urban with no overlap on central or west
- No observations is marked as urban and central and west
- 1 observation has been marked as both central and west.
- 1 observation has been marked as both west and urban
- 5 observations have been marked as both central and urban
- 31 observations have not been marked as either west nor central nor urban

We interpret this to mean that an attempt was made to mark the observations geographically as well as by urban (or rural). However, the assignment is not complete as we we can see. Some regions have been given any label as to their region; these may belong to a different geographical region or rural.

```
crime_data_central=sqldf('SELECT * FROM crime_data WHERE central =1 AND (west!=1 OR urban !=1)')
crime_data_west=sqldf('SELECT * FROM crime_data WHERE west =1 AND (central!=1 OR urban !=1)')
```

We can see that observations marked as central have a higher maximum crime rate compare to those marked as west.

```
summary(crime_data_central$crmrte)
```

```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
## 0.01210 0.02646 0.03176 0.03832 0.05142 0.09897
```

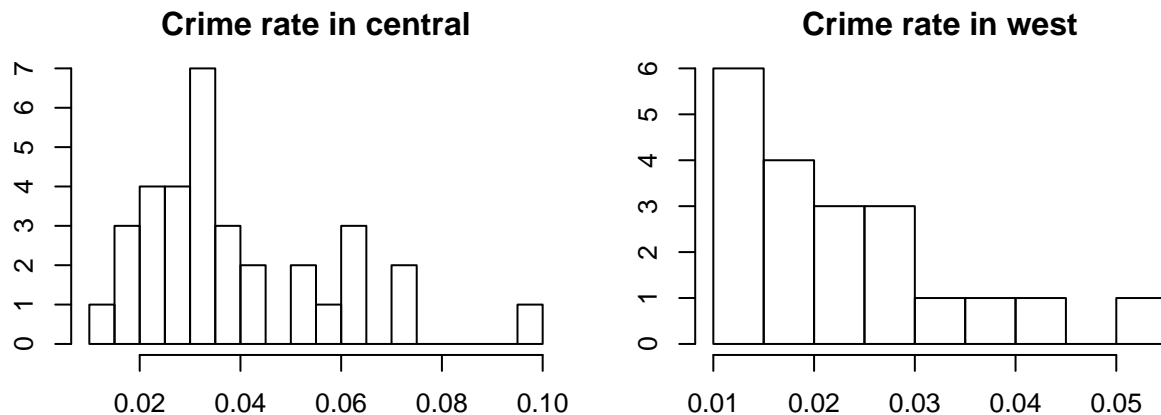
```
summary(crime_data_west$crmrte)
```

```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
## 0.01062 0.01451 0.01916 0.02333 0.02846 0.05441
```

The west region has more occurrences of lower crime rate than the central region. There is a significant overlap between the observations marked as west/central and those marked as urban. Also, there are no regions marked as rural. So, we are not analyzing the observations marked as urban.

```
par(mfrow=c(2,2), mai=c(0.35,0.35,0.35,0.35))
```

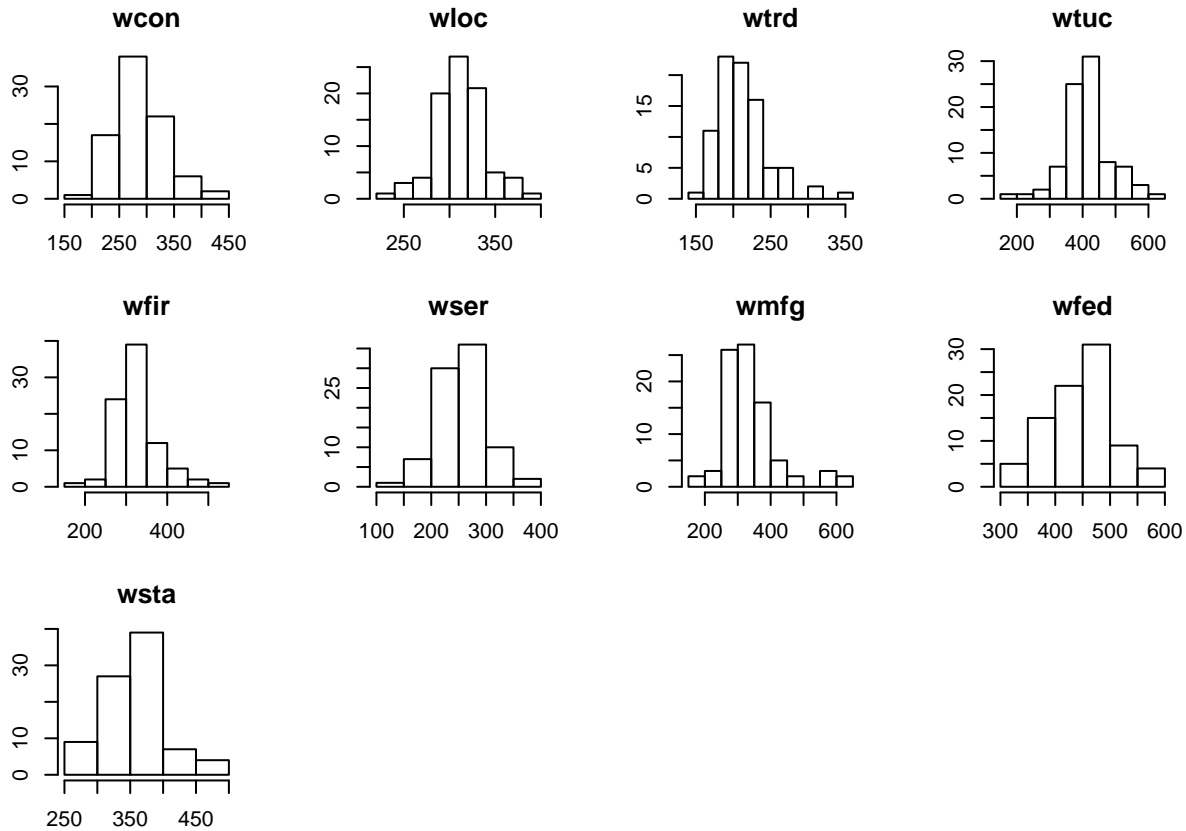
```
hist(crime_data_central$crmrte, main="Crime rate in central", breaks=15)
hist(crime_data_west$crmrte, main="Crime rate in west", breaks=15)
```



## Wage distribution

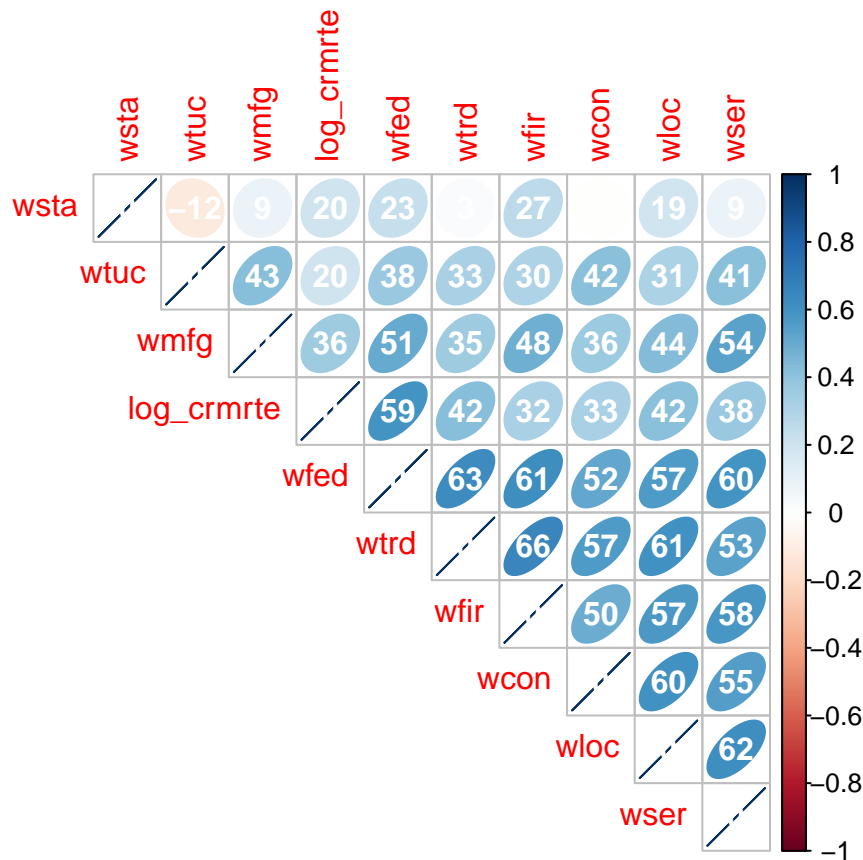
Note: In our first pass, we found an influential outlier in services wages and removed it, as mentioned in the section on outliers.

```
par(mfrow=c(3,4), mai=c(0.35,0.35,0.35,0.35))
hist(crime_data$wcon, main="wcon")
hist(crime_data$wloc, main="wloc")
hist(crime_data$wtrd, main="wtrd")
hist(crime_data$wtuc, main="wtuc")
hist(crime_data$wfir, main="wfir")
hist(crime_data$wser, main="wser")
hist(crime_data$wmfg, main="wmfg")
hist(crime_data$wfed, main="wfed")
hist(crime_data$wsta, main="wsta")
```



Most of the wage variables conform to normal distributions. We do not have to worry about transformations. Let us look which of them have high correlation with crime rate, considering all those with  $R > 0.25$  (arbitrarily).

```
wage_cols = c("log_crmrte", "wcon", "wloc", "wtrd", "wtuc", "wfir",
              "wser", "wmfg", "wfed", "wsta")
corrplot(cor(crime_data[, wage_cols]), type="upper", diag=TRUE, addCoef.col="white",
          addCoefasPercent = TRUE, order="hclust", method="ellipse")
```



Indeed, a lot of the wage categories above have a high degree of correlation among them, but all are less than 70. We cannot eliminate any wage categories this way.

A general remark is in order for the positive correlation of crime across the wage categories. Higher wages may indicate higher wealth or a different omitted variable, and cannot be causal in and of themselves.

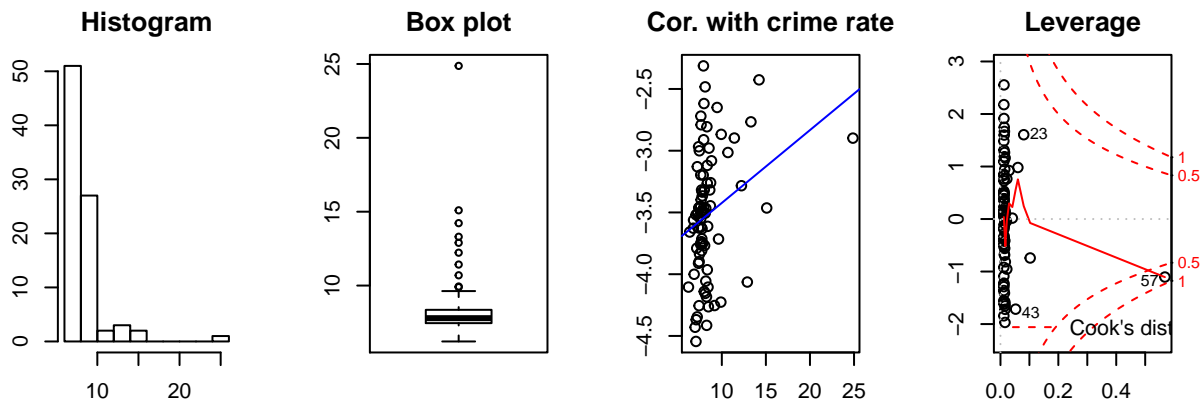
We will *not* include wages in a first model. We will use *wfed* as a proxy variable for all wages, for a second model we will propose.

---

### Percent of young males

```
f_describe_col(crime_data$pctymle, plot_model=TRUE)
```

```
## [1] "Correlation: 0.28"
```



We see moderate positive correlation with higher percentage of young males. Boxplot shows outliers, but none has outsized influence (Cook's distance > 1).

A high percentage of young males can indicate higher aggressiveness and risk, causing higher rate of crime. We may also see the effect of omitted variables like youth unemployment or low education levels.

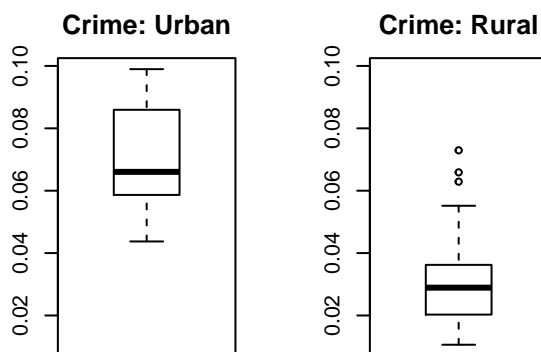
We will include this variable in our model.

## Urban population

```
print(length(crime_data$urban[crime_data$urban == 1]))

## [1] 8

urban_crime_data = crime_data %>% filter(urban == 1) %>% dplyr::select(-urban)
rural_crime_data = crime_data %>% filter(urban == 0) %>% dplyr::select(-urban)
par(mfrow=c(2,4), mai=c(0.35,0.35,0.35,0.35))
lmts = range(urban_crime_data$crmrte, rural_crime_data$crmrte)
boxplot(urban_crime_data$crmrte, main="Crime: Urban", ylim=lmts)
boxplot(rural_crime_data$crmrte, main="Crime: Rural", ylim=lmts)
```



It is worth noting that there are only 8 observations classified urban in this dataset. However, median crime rate in urban regions is double that of rural regions.

Let us check if there is correlation between “urban” and “density”:

```
cor(crime_data$density, crime_data$urban)
```

```
## [1] 0.8219415
```

This is quite high, so we run a risk of multicollinearity.

Therefore, and since we have already selected density (with an additional advantage of more number of observations), we will *not* include this variable in our model.

---

### Other variables ignored

The following variables show low to nonexistent correlation with crime rate. We will *not* consider them in our regression model.

- Probability of prison sentence ( $R = 0.0537$ )
- Offense mix ( $R = 0.0136$ )
- Average sentence duration ( $R = 0.0438$ )

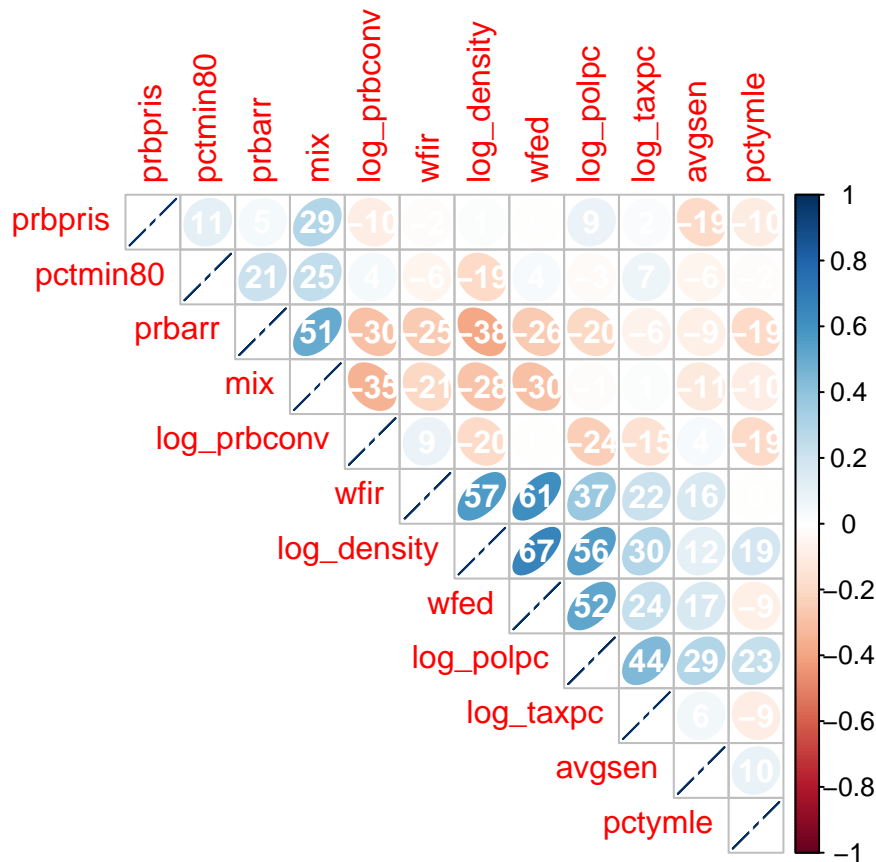
In addition, we will use geographic regions to come up with separate models, later in this analysis.

## 4. Correlation Analysis

Let us check for correlations across predictor pairs.

The correlation plot between the different predictors is as follows:

```
corrplot(
  cor(crime_data[,
    c("prbarr", "log_prbconv", "prbpris", "avgsen",
      "log_polpc", "log_density", "log_taxpc", "pctmin80", "mix",
      "pctymle", "wfir", "wfed")
  ]),
  type = "upper",
  diag=TRUE, addCoef.col="white", addCoefasPercent = TRUE, order="hclust", method="ellipse")
```



The following correlations are worth a remark:

- We do not see high correlations ( $>0.7$ ), both positive or negative. This helps us avoid multicollinearity issues.
- Wages correlate highly (0.67) with population density, probably because it is tuned to cost of living.
- Police per capita correlates highly with density (0.56) and tax revenue (0.44), perhaps indicating federal laws on police counts.
- Probability of arrest correlates negatively (-0.38) with density, indicating that criminals get away with crime in populous areas. It also correlates negatively (-0.30) with probability of conviction, indicating higher chance of false arrests when a large number of arrests are made.

## 5. Model development

### Summary of variables

We will now fit three models based on our analysis. A quick overview:

- Model 1 will have variables we think are causal in nature
- Model 2 will have a few additional variables that show high correlation
- Model 3 will have almost all variables: a useful benchmark

Here is a summary table of variables we will use in our models.

Variable	Transform?	Model1?	Model2?	Model3?	Remarks
county	N/A				Unused



Variable	Transform?	Model1?	Model2?	Model3?	Remarks
year	N/A				Unused
prbarr		Y	Y	Y	Causal
prbconv	log	Y	Y	Y	Causal
prbpris				Y	No corr. found
avgsen				Y	No corr. found
polpc	log		Y	Y	Effect, not cause
density	log	Y	Y	Y	Causal
taxpc	log		Y	Y	Omit var: wealth
west	N/A				Categ, sep. model
central	N/A				Categ, sep. model
urban					Cor. with density
pctmin80		Y	Y	Y	Causal
wcon					Omit var: wealth
wtuc					Proxied
wtrd					“-
wfir				Y	
wser					
wmfg					
wfed			Y	Y	Proxy
wsta					Proxied
wloc					Proxied
mix	log			Y	No corr. found
pctymle		Y	Y	Y	Causal, weak cor

## Model 1

For the first model, here are the variables we will consider:

- We believe that the following can directly cause higher crime: high density, higher percentage of minorities, higher percentage of young men.
- We also think the following cause lower crime: high probability of arrest and conviction.

$$\log(\text{crmte}) = \beta_0 + \beta_1 \text{prbarr} + \beta_2 \log(\text{prbconv}) + \beta_3 \log(\text{density}) + \beta_4 \text{pctmin80} + \beta_6 \text{pctymle}$$

Let us fit the model:

```
model1 = lm(log_crmte ~ prbarr + log_prbconv + log_density +
            pctmin80 + pctymle, data=crime_data)
summary(model1)

##
## Call:
## lm(formula = log_crmte ~ prbarr + log_prbconv + log_density +
##     pctmin80 + pctymle, data = crime_data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.6248 -0.1170  0.0273  0.1285  0.5151
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
```

```
## (Intercept) -2.744e+00  3.039e-01 -9.031 7.65e-14 ***
## prbarr      -1.384e-02  2.942e-03 -4.705 1.05e-05 ***
## log_prbconv -2.365e-01  5.622e-02 -4.207 6.72e-05 ***
## log_density  4.201e-01  3.875e-02 10.841 < 2e-16 ***
## pctmin80     1.502e-04  1.592e-05  9.434 1.23e-14 ***
## pctymle      1.375e-02  1.128e-02  1.219  0.226
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.2339 on 80 degrees of freedom
## Multiple R-squared:  0.7963, Adjusted R-squared:  0.7836
## F-statistic: 62.57 on 5 and 80 DF,  p-value: < 2.2e-16
```

The model shows a fit of about 0.784 as measured by adjusted  $R^2$ .

The model gets a very low p-value based on its F-statistic, therefore we can reject the null hypothesis. The coefficients are significant.

### Statistical significance:

The model shows that *pctymle* is not statistically significant in our model. We will proceed to remove it. On the other hand, all our other independent variables are highly statistically significant.

```
model1 = lm(log_crmrte ~ prbarr + log_prbconv + log_density +
             pctmin80, data=crime_data)
summary(model1)

##
## Call:
## lm(formula = log_crmrte ~ prbarr + log_prbconv + log_density +
##     pctmin80, data = crime_data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.62711 -0.11987  0.01341  0.15066  0.50466
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -2.542e+00  2.556e-01  -9.946 1.09e-15 ***
## prbarr      -1.468e-02  2.870e-03  -5.116 2.05e-06 ***
## log_prbconv -2.534e-01  5.464e-02  -4.638 1.33e-05 ***
## log_density  4.218e-01  3.884e-02 10.859 < 2e-16 ***
## pctmin80     1.514e-04  1.593e-05   9.500 8.16e-15 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.2346 on 81 degrees of freedom
## Multiple R-squared:  0.7926, Adjusted R-squared:  0.7823
## F-statistic: 77.37 on 4 and 81 DF,  p-value: < 2.2e-16
```

The model becomes:

$$\log(\text{crmte}) = -2.542 - 0.0147 \cdot \text{prbarr} - 0.253 \cdot \log(\text{prbconv}) + 0.422 \cdot \log(\text{density}) + 0.000151 \cdot \text{pctmin80}$$

### Practical significance:

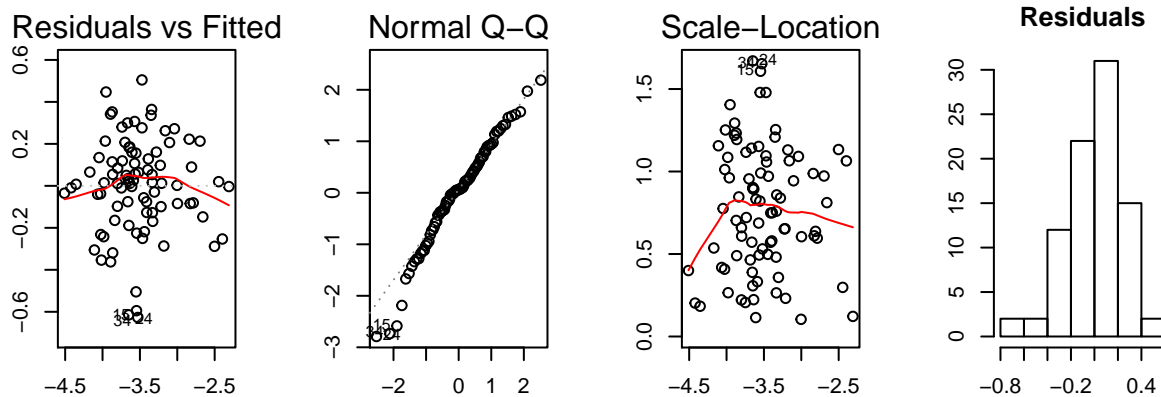
From the above regression equation, we can infer the following. All statements have *ceteris paribus* assumptions:

- If we hold all other variables constant, we have a “base crime rate” of  $e^{-2.542} = 0.079$ .
- For a unit increase in “probability” of arrest, crime rate goes down by approximately  $|e^{-0.0147} - 1| = 0.0146$ , or 1.46%. This is a large effect. It shows that law enforcement is a very good deterrent to crime.
- For a 1% increase in “probability” of conviction, crime rate decreases by about 0.25%. This is not a lot. It may be because most of the effect is already absorbed by *prbarr*.
- For a 1% increase in density, crime rate increases by about 0.42%. This is a large effect. As we put more people closer, crime is easier to commit and harder to spot.
- For a 1% increase in minorities, crime rate increases by about  $|e^{0.000151} - 1| = 0.015\%$ . This is a minuscule effect. Compared to the animosity the majority may have over minorities, the effect is very little.

## CLM on Model 1

Let us verify if the linear model assumptions hold.

```
par(mfrow=c(2,4), mai=c(0.35,0.35,0.35,0.35))
plot(model1, which=c(1,2,3))
hist(model1$residuals, main="Residuals")
```



## CLM 1.0 - Linear in parameters

Our model is represented as:

$$\log(\text{crmrte}) = \beta_0 + \beta_1 \text{prbarr} + \beta_2 \log(\text{prbconv}) + \beta_3 \log(\text{density}) + \beta_4 \text{pctmin80} + u$$

Any population distribution could be represented as a linear model plus some error (error might be poorly behaved). We chose the above model such that the dependent variable is a linear function of the explanatory variables. Therefore the CLM.1 assumption is met for all of our models we created.

## CLM 2.0 - Random Sampling

For this assumption, the data needs to be a random sample drawn from the population.

We first note that the U.S. state of North Carolina is divided in 100 counties (information from Wikipedia). Our dataset contained information from 90 different counties. Though we didn't use data from all counties, there was no indication of non-random sampling during our analysis. We therefore assume that the counties sampled are indeed random and thus our assumption is met for all the models we created.

We do note that variables such as crime rate are prone to clustering effects but we can get away with bootstrapping measurements.

### CLM 3.0 - No Perfect Multicollinearity

From our EDA it was apparent that none of our variables had constant values. In addition, inspection of the correlation plot we generated indicates there are no perfectly correlated variable pairs.

```
vif(model1)
```

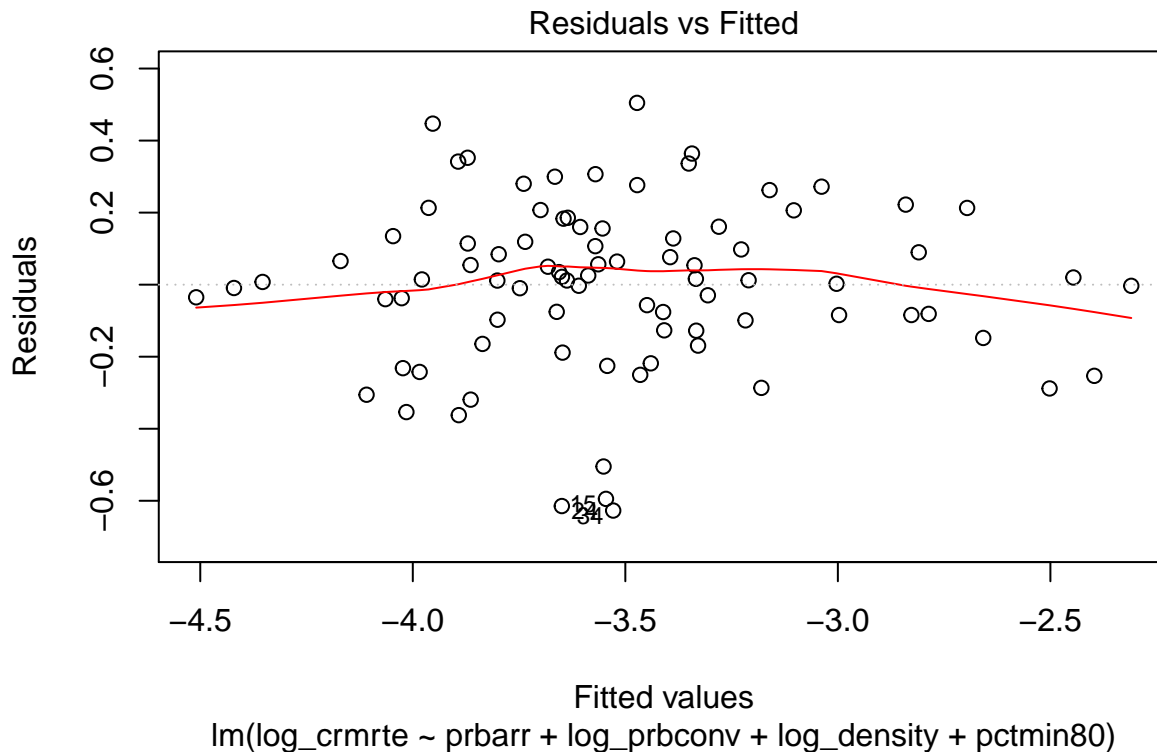
```
##      prbarr log_prbconv log_density    pctmin80  
##      1.458117  1.266171  1.349454  1.070684
```

The variance inflation factor does not provide any evidence of multicollinearity as well. We therefore assume CLM 3.0 condition is satisfied

### CLM 4.0 - Zero Conditional Mean

By examining the residuals versus fitted values plot for model, we conclude that the assumption of zero conditional mean is met. The red spline curve does not deviate much from zero and appears fairly flat.

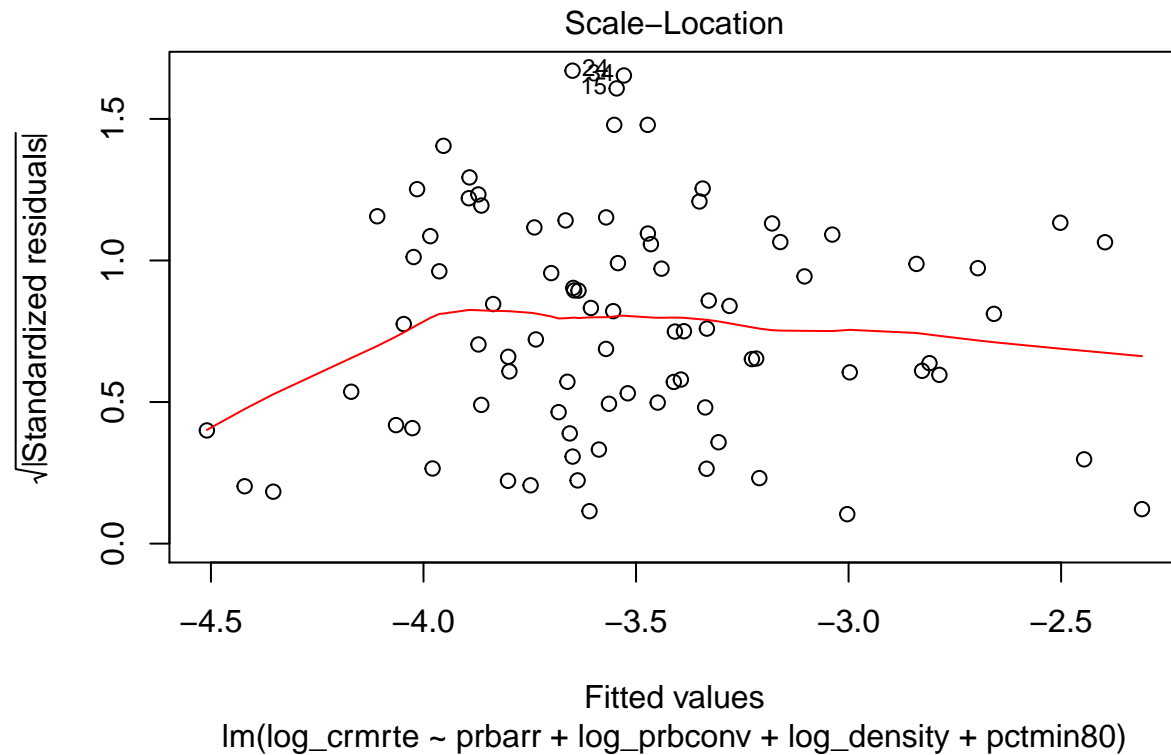
```
plot(model1, which = 1)
```



### CLM 5.0 - Homoskedasticity

When we examined the residuals versus fitted values plot, it was apparent that the variance of errors in the middle of the plot is higher than the variance of errors in the edges of the plot. This suggested heteroskedasticity, so we examined the scale-location plot. The spline curve on the scale-location plot is curved rather than flat, indicating heteroskedasticity. Despite this violation of CLM, we are able to proceed with our OLS model by using heteroskedasticity-robust standard errors.

```
plot(model1, which = 3)
```



```
bptest(model1)
```

```
##
## studentized Breusch-Pagan test
##
## data: model1
## BP = 8.3477, df = 4, p-value = 0.07964
```

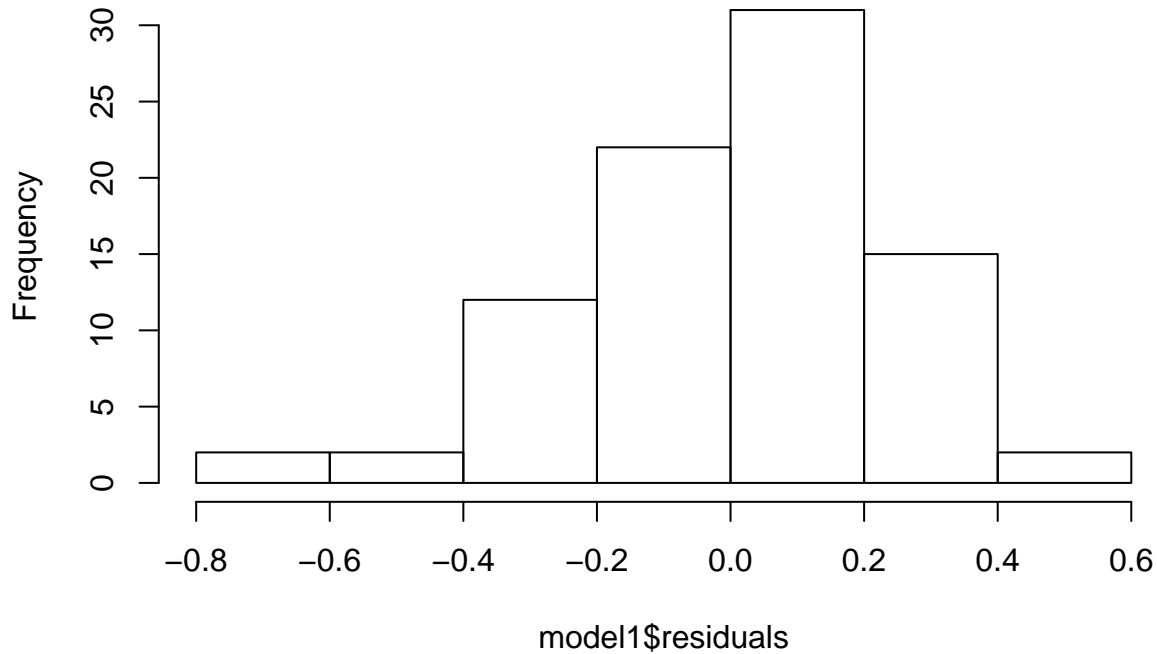
We also conducted the studentized Breusch-Pagan test where the null hypothesis states that the model supports homoskedasticity. The p-value obtained indicates statistical significance that rejects the null hypothesis.

### CLM 6.0 - Normality of error terms

Looking at the histogram of the residual term indicates a more or less normal distribution. This can further be confirmed by the Shapiro test. The null hypothesis of this test is that residuals have a normal distribution. The p-value indicates we do not reject this null hypothesis.

```
hist(model1$residuals)
```

## Histogram of model1\$residuals



```
shapiro.test(model1$residuals)
```

```
##  
## Shapiro-Wilk normality test  
##  
## data:  model1$residuals  
## W = 0.97539, p-value = 0.09953
```

## Model 2

Next, let us include some more variables, as model2.

In this model we also include three variables that show positive correlation with crime rate, albeit not causal. We think they are all the result of wealthy, urban demographics: high police per capita, high tax revenue and high federal wages. It is an omitted variable.

We do not include outcome variables that absorb causal effect (by having negative correlation).

```
model2 = lm(log_crmrte ~ prbarr + log_prbconv + log_density +  
            pctmin80 + pctymle  
            + log_polpc + log_taxpc + wfed,  
            data=crime_data)  
summary(model2)
```

```
##  
## Call:  
## lm(formula = log_crmrte ~ prbarr + log_prbconv + log_density +  
##     pctmin80 + pctymle + log_polpc + log_taxpc + wfed, data = crime_data)  
##  
## Residuals:  
##      Min       1Q   Median       3Q      Max
```

```
## -0.52733 -0.13295 0.01054 0.13749 0.50838
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -1.521e+00 1.166e+00 -1.304 0.1960
## prbarr      -1.346e-02 2.829e-03 -4.759 8.93e-06 ***
## log_prbconv -2.317e-01 5.546e-02 -4.178 7.69e-05 ***
## log_density 3.211e-01 5.254e-02 6.113 3.76e-08 ***
## pctmin80    1.412e-04 1.594e-05 8.863 2.20e-13 ***
## pctymle     1.493e-02 1.200e-02 1.244 0.2174
## log_polpc   2.290e-01 1.137e-01 2.014 0.0475 *
## log_taxpc   -5.304e-02 1.208e-01 -0.439 0.6618
## wfed        9.976e-04 6.476e-04 1.540 0.1275
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.2244 on 77 degrees of freedom
## Multiple R-squared: 0.8196, Adjusted R-squared: 0.8009
## F-statistic: 43.74 on 8 and 77 DF, p-value: < 2.2e-16
```

The fit improves to 0.80 (adjusted  $R^2$ ). This is because some of the newly added variables are more normal in distribution (=less skew).

### Statistical significance:

We continue to see *pctymle* as not significant. In addition, *log\_taxpc* and *wfed* are also not statistically significant. *polpc* is significant at  $p=0.05$ .

Therefore, we will remove the insignificant variables. The new model becomes:

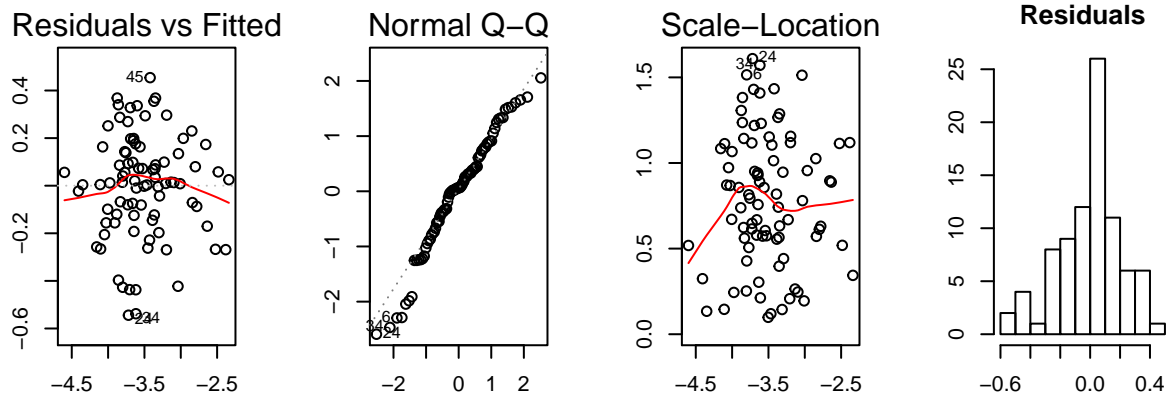
```
model2 = lm(log_crmrte ~ prbarr + log_prbconv + log_density +
             pctmin80 + log_polpc,
             data=crime_data)
summary(model2)

##
## Call:
## lm(formula = log_crmrte ~ prbarr + log_prbconv + log_density +
##     pctmin80 + log_polpc, data = crime_data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.54423 -0.12429  0.01372  0.14186  0.45399
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.8548476  0.6530846  -1.309 0.19430
## prbarr      -0.0140652  0.0027655  -5.086 2.36e-06 ***
## log_prbconv -0.2265010  0.0533682  -4.244 5.86e-05 ***
## log_density  0.3656711  0.0424043   8.623 4.83e-13 ***
## pctmin80     0.0001466  0.0000154   9.514 8.60e-15 ***
## log_polpc    0.2759052  0.0989495   2.788 0.00662 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.2254 on 80 degrees of freedom
## Multiple R-squared: 0.8109, Adjusted R-squared: 0.7991
```

```
## F-statistic: 68.63 on 5 and 80 DF, p-value: < 2.2e-16
```

Practical significance:

```
par(mfrow=c(2,4), mai=c(0.35,0.35,0.35,0.35))
plot(model2, which=c(1,2,3))
hist(model2$residuals, main="Residuals")
```



### Model 3

We will now build a third model that includes almost all the variables, for the sake of completeness and comparison. We only exclude wages because their distribution is highly alike.

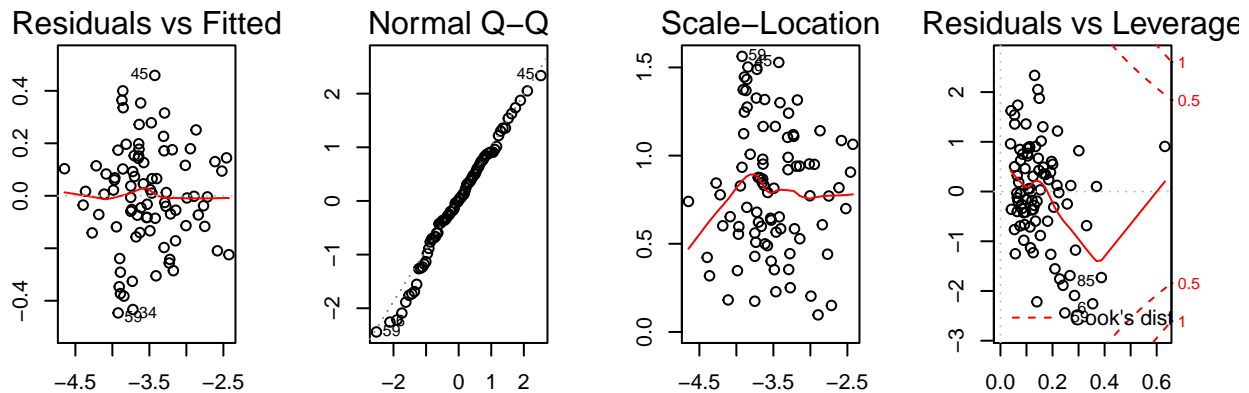
```
model3 = lm(log_crmrte ~ prbarr + log_prbconv + log_density +
             pctmin80 + pctymle
             + log_polpc + log_taxpc
             + prbpris + avgsgen + wfir + wfed + mix,
             data=crime_data)
summary(model3)
```

```
##
## Call:
## lm(formula = log_crmrte ~ prbarr + log_prbconv + log_density +
##     pctmin80 + pctymle + log_polpc + log_taxpc + prbpris + avgsgen +
##     wfir + wfed + mix, data = crime_data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.44642 -0.11582  0.00227  0.12932  0.45885
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -8.348e-01  1.223e+00  -0.683  0.49698
## prbarr       -1.384e-02  2.802e-03  -4.942  4.78e-06 ***
## log_prbconv  -1.811e-01  5.559e-02  -3.257  0.00171 **
## log_density   3.549e-01  5.157e-02   6.881  1.73e-09 ***
## pctmin80      1.362e-04  1.549e-05   8.793  4.55e-13 ***
## pctymle       1.663e-02  1.158e-02   1.436  0.15533
## log_polpc     2.897e-01  1.148e-01   2.525  0.01376 *
## log_taxpc     -4.862e-02  1.146e-01  -0.424  0.67251
## prbpris       -3.379e-01  3.287e-01  -1.028  0.30730
## avgsgen       -2.207e-02  9.791e-03  -2.254  0.02721 *
```



```
## wfir      -1.579e-03  5.698e-04  -2.771  0.00708 **
## wfed      1.722e-03  6.669e-04   2.582  0.01183 *
## mix       3.513e-01  4.053e-01   0.867  0.38892
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.2107 on 73 degrees of freedom
## Multiple R-squared:  0.8492, Adjusted R-squared:  0.8244
## F-statistic: 34.26 on 12 and 73 DF,  p-value: < 2.2e-16

par(mfrow=c(2,4), mai=c(0.35,0.35,0.35,0.35))
plot(model3)
```



This tops fit at about 0.824 (adjusted  $R^2$ ). However, it is worth noting that the benefit is not much: all those extra variables improved the fit by less than 2%.

In addition to what we had in model2, only *avgsen*, *wfir* and *wfed* are seen to be practically significant. We can ignore *prbpris*, *mix*, *taxpc*, and *pctymle*.

```
coeftest(model3, vcov = vcovHC)
```

```
##
## t test of coefficients:
##
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -8.3484e-01 1.6498e+00 -0.5060  0.61435
## prbarr      -1.3845e-02 3.1111e-03 -4.4501 3.021e-05 ***
## log_prbconv -1.8107e-01 9.2515e-02 -1.9572  0.05415 .
## log_density  3.5488e-01 6.7576e-02  5.2516 1.430e-06 ***
## pctmin80     1.3618e-04 1.6775e-05  8.1181 8.447e-12 ***
## pctymle      1.6627e-02 1.4015e-02  1.1863  0.23933
## log_polpc    2.8971e-01 1.8112e-01  1.5995  0.11402
## log_taxpc   -4.8620e-02 1.4773e-01 -0.3291  0.74302
## prbpris     -3.3788e-01 3.4205e-01 -0.9878  0.32650
## avgsen      -2.2069e-02 1.0841e-02 -2.0356  0.04542 *
## wfir        -1.5789e-03 8.1055e-04 -1.9479  0.05527 .
## wfed         1.7220e-03 8.0120e-04  2.1493  0.03492 *
## mix         3.5130e-01 4.6870e-01  0.7495  0.45596
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

We will now build a variation of model3 that includes all the wage variable in addition to the model3 variables.

```

model3b = lm(log_cmrte ~ prbarr + log_prbconv + log_density +
             pctmin80 + pctymle
             + log_polpc + log_taxpc
             + prbpris + avgsgen
             + wcon + wloc + wtrd + wtuc + wfir + wser + wmfg + wfed + wsta
             + mix,
             data=crime_data)
summary(model3b)$adj.r.squared

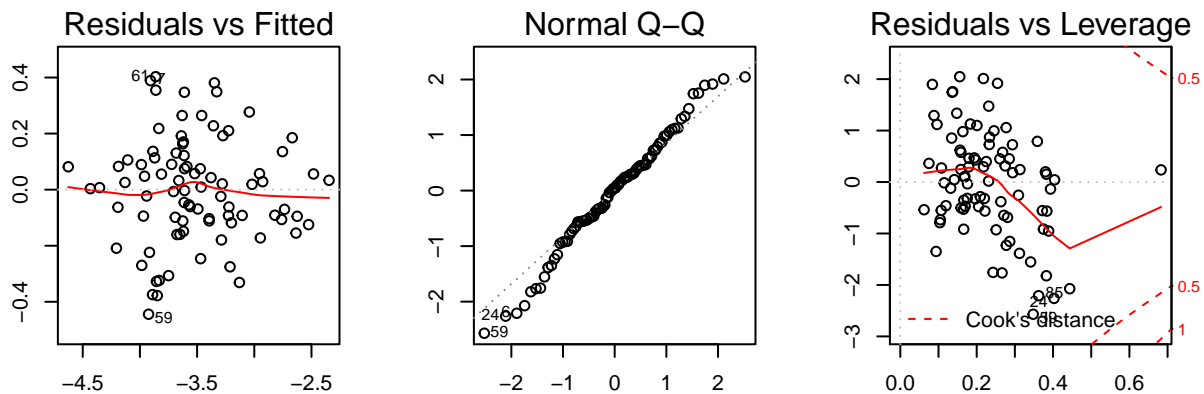
```

```
## [1] 0.8185732
```

```

par(mfrow=c(2,3), mai=c(0.35,0.35,0.35,0.35))
plot(model3b, which=c(1,2,5))

```



The coeftest confirms that none of the wage variables have a significant effect.

```
coeftest(model3b, vcov = vcovHC)
```

```

##
## t test of coefficients:
##
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -5.3340e-01 1.9385e+00 -0.2752  0.78405
## prbarr      -1.4337e-02 3.1072e-03 -4.6142 1.871e-05 ***
## log_prbconv -1.8377e-01 1.0687e-01 -1.7196  0.09019 .
## log_density  3.4374e-01 7.3305e-02  4.6892 1.422e-05 ***
## pctmin80     1.3434e-04 1.7413e-05  7.7152 8.562e-11 ***
## pctymle      2.2401e-02 9.5690e-03  2.3410  0.02226 *
## log_polpc     3.2635e-01 2.2317e-01  1.4623  0.14839
## log_taxpc    -3.2255e-02 1.7298e-01 -0.1865  0.85265
## prbpris      -4.0212e-01 3.6261e-01 -1.1090  0.27147
## avgsgen      -2.3623e-02 1.2256e-02 -1.9274  0.05824 .
## wcon          1.2810e-04 7.0972e-04  0.1805  0.85732
## wloc          3.8380e-04 1.7515e-03  0.2191  0.82723
## wtrd          1.0253e-03 1.2273e-03  0.8354  0.40650
## wtuc          1.8438e-04 4.9261e-04  0.3743  0.70938
## wfir         -1.5605e-03 9.3759e-04 -1.6644  0.10077
## wser         -1.3247e-03 1.0028e-03 -1.3210  0.19107
## wmfg          4.7941e-05 3.9550e-04  0.1212  0.90389
## wfed          1.7027e-03 9.0298e-04  1.8856  0.06375 .
## wsta         -5.8974e-04 7.2093e-04 -0.8180  0.41628
## mix           2.3734e-01 4.9780e-01  0.4768  0.63510
## ---

```

```
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

We will investigate if the wage figures together make a difference.

```
f_check_null <- function(in_field_name, in_db_name ){
  sql=sprintf("SELECT COUNT(1) as COUNT_NULL_OR_NA FROM %s WHERE (%s IS \"NA\" or %s IS NULL or %s = '
  sqldf(sql)
}
```

Before combining the wage figures, we have to check if any of them are NA.

```
# (Evaluate manually to verify)
f_check_null("wcon", "crime_data")
f_check_null("wloc", "crime_data")
f_check_null("wtrd", "crime_data")
f_check_null("wtuc", "crime_data")
f_check_null("wfir", "crime_data")
f_check_null("wser", "crime_data")
f_check_null("wmfg", "crime_data")
f_check_null("wfed", "crime_data")
f_check_null("wsta", "crime_data")
```

We also check if the wage types are all numeric.

```
# (Evaluate manually to verify)
typeof(crime_data$wcon)
typeof(crime_data$wloc)
typeof(crime_data$wtrd)
typeof(crime_data$wtuc)
typeof(crime_data$wfir)
typeof(crime_data$wser)
typeof(crime_data$wmfg)
typeof(crime_data$wfed)
typeof(crime_data$wsta)
```

```
crime_tmp = sqldf("SELECT *, wcon+wloc+wtrd+wtuc+wfir+wser+wmfg+wfed+wsta AS 'sum_wages'
FROM crime_data" )
```

```
sqldf('SELECT sum_wages from crime_tmp LIMIT 5')
```

```
##      sum_wages
## 1    3054.890
## 2    2652.879
## 3    2553.648
## 4    2823.133
## 5    2759.238
```

```
crime_data = crime_tmp
```

```
model3c = lm(log_crmrte ~ prbarr + log_prbconv + log_density +
  pctmin80 + pctymle
  + log_polpc + log_taxpc
  + prbpris + avgsen
  + sum_wages
  +mix,
  data=crime_data)
summary(model3c)$adj.r.squared
```

```
## [1] 0.8011389
coeftest(model3c, vcov = vcovHC)

##
## t test of coefficients:
##
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)  4.4192e-01 1.6235e+00  0.2722  0.78623
## prbarr       -1.3665e-02 3.2455e-03 -4.2104 7.089e-05 ***
## log_prbconv  -2.0639e-01 1.0475e-01 -1.9703  0.05255 .
## log_density   3.7020e-01 7.4823e-02  4.9477 4.571e-06 ***
## pctmin80      1.4654e-04 1.6476e-05  8.8943 2.634e-13 ***
## pctymle       7.3485e-03 1.2566e-02  0.5848  0.56047
## log_polpc     3.7807e-01 2.0025e-01  1.8880  0.06294 .
## log_taxpc    -1.0089e-01 1.5434e-01 -0.6537  0.51532
## prbpris      -3.4859e-01 3.2485e-01 -1.0731  0.28671
## avgscen      -2.3496e-02 1.0439e-02 -2.2509  0.02736 *
## sum_wages    -2.0079e-05 1.9984e-04 -0.1005  0.92024
## mix          5.4113e-02 4.8271e-01  0.1121  0.91105
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

linearHypothesis(model3c, c("sum_wages = 0"), vcov = vcovHC)

## Linear hypothesis test
##
## Hypothesis:
## sum_wages = 0
##
## Model 1: restricted model
## Model 2: log_crmrte ~ prbarr + log_prbconv + log_density + pctmin80 +
##          pctymle + log_polpc + log_taxpc + prbpris + avgscen + sum_wages +
##          mix
##
## Note: Coefficient covariance matrix supplied.
##
##   Res.Df Df      F Pr(>F)
## 1      75
## 2      74  1 0.0101 0.9202

#waldtest(model3b, model3c, vcov = vcovHC)
```

We can see from the `coeftest` that the sum of wages has no significant effect on the model. A similar conclusion can be drawn from the `linearHypothesis` test.

```
AIC(model1, model2, model3)
```

```
##           df          AIC
## model1    6  1.557403
## model2    7 -4.418964
## model3   14 -9.867252
```

The AIC scores also reflect the fit: the last model has the best (least) score, whereas the first model has the worst.

### CLM observations for other models (1 & 3)

For both our other models (1 and 3), we observed that most of the CLM assumptions were satisfied. They both supported: linear in parameters, random sampling, multicollinearity and had normal residuals. The one difference was that these other models actually satisfied Homoskedasticity as well. We believe that by adding all the variables, as in model3, we are likely canceling out variances in errors.

#### Model 4

We will now attempt to develop a custom model based on geographical region.

```
crime_west = crime_data %>% filter(west==1)
crime_central = crime_data %>% filter(central==1)
crime_other_region = crime_data %>% filter(central==0 & west==0)

formula = log_crmrte ~ log_density + pctymle + pctmin80 +
  prbarr + log_prbconv + log_taxpc

logcrmte.west.lm4a = lm(formula, data=crime_west)
summary(logcrmte.west.lm4a)$r.squared

## [1] 0.8948345

logcrmte.central.lm4b = lm(formula, data=crime_central)
summary(logcrmte.central.lm4b)$r.squared

## [1] 0.8311449

logcrmte.other_rgn.lm4c = lm(formula, data=crime_other_region)
summary(logcrmte.other_rgn.lm4c)$r.squared

## [1] 0.7467755
```

The models for West and Central regions are better than the general model 2 we have in terms of adjusted  $R^2$ .

However, for other regions, our model has lower adjusted  $R^2$  than West or Central. This shows that the observations for other regions need to be analyzed with a model different from the generic one. It could also be that our model is influenced heavily by the observations from the urban areas in West and Central.

<i>Dependent variable:</i>			
	log_crmrte		
	(1)	(2)	(3)
prbarr	−0.015*** (0.003)	−0.014*** (0.003)	−0.014*** (0.003)
log_prbconv	−0.253*** (0.073)	−0.227* (0.094)	−0.181 (0.093)
log_density	0.422*** (0.047)	0.366*** (0.053)	0.355*** (0.068)
pctmin80	0.0002*** (0.00002)	0.0001*** (0.00002)	0.0001*** (0.00002)
pctymle			0.017 (0.014)
log_polpc		0.276 (0.179)	0.290 (0.181)
log_taxpc			−0.049 (0.148)
prbpris			−0.338 (0.342)
avgsen			−0.022* (0.011)
wfir			−0.002 (0.001)
wfed			0.002* (0.001)
mix			0.351 (0.469)
Constant	−2.542*** (0.345)	−0.855 (1.108)	−0.835 (1.650)
Observations	86	86	86
R <sup>2</sup>	0.793	0.811	0.849
Adjusted R <sup>2</sup>	0.782	0.799	0.824
Residual Std. Error	0.235 (df = 81)	0.225 (df = 80)	0.211 (df = 73)
F Statistic	77.370*** (df = 4; 81)	68.628*** (df = 5; 80)	34.258*** (df = 12; 73)

*Note:*

\*p<0.05; \*\*p<0.01; \*\*\*p<0.001

## 6. Omitted variables

We have talked about omitted variables as part of our EDA. Here we continue the discussion and also talk about the direction of bias.

The important omitted variables that come to mind are:

- Median level of education in the county: The median level of education in the county may have a negative correlation to crime rate. This OV will also have a negative correlation with prbarr, prbconv, prbpris, avgsen. So, if a model uses prbarr, prbconv, prbpris, avgsen, the OVB bias would be positive.
- Median ratio of total household income to number of family members: The median ratio of total household income to number of family members in the county may have a negative correlation to crime rate. This OV will also have a negative correlation with prbarr, prbconv, prbpris, avgsen, and a positive correlation with taxpc. So, if a model uses prbarr, prbconv, prbpris, avgsen, the OVB bias would be positive. For a model using taxpc, the OVB bias would be negative.
- Total number of neighbourhood crime watch groups in the county: The total number of neighbourhood crime watch groups in the county may have a negative correlation to crime rate. This OV will also have a negative correlation with prbarr, prbconv, prbpris, avgsen. So, if a model uses prbarr, prbconv, prbpris, avgsen, the OVB bias would be positive.
- Family cohesiveness such as divorce rate, domestic violence: This maybe difficult to measure. The family cohesiveness measure may have a positive correlation to crime rate. This OV will also have a positive correlation with prbarr, prbconv, prbpris, avgsen. So, if a model uses prbarr, prbconv, prbpris, avgsen, the OVB bias would be positive.
- Any extreme climate change when the crime occurred. This can be a significant change compared to the expected climate in that month. Higher temperatures lead to high tempers and may have a positive correlation to crime rate. This OV will also have a positive correlation with prbarr, prbconv, prbpris, avgsen. So, if a model uses prbarr, prbconv, prbpris, avgsen, the OVB bias would be positive.
- Alcoholism and substance abuse: Patient data from hospitals and police data can be a good marker to judge this. High number of cases of drug abuse correlates with higher crime rate to a large extent. This OV will also have a positive correlation with prbarr, prbconv, prbpris, avgsen. So, if a model uses prbarr, prbconv, prbpris, avgsen, the OVB bias would be positive.
- Repeat crimes: The data does not have information about serial criminals as against first-time offenders. If most of the crime is due to repeat offenders, then we will have to accommodate our policies accordingly.
- Underreporting and unreported crimes: It is also worth checking via other sources how much crime goes unreported in North Carolina, and whether data is often “corrected” as time goes by.

## 7. Conclusion

Based on the above study, here are the conclusions we would like to offer the political campaign:

- Crime rate is most correlated (0.7) with population density. Median crime in urban areas is more than double those in rural areas. Our policies should make our cities safer, in order to reduce crime significantly.
- As probability of arrest and/or conviction increase, crime decreases. Law enforcement is a good deterrent to crime.
- Prison by itself does not correlate with crime, nor does the length of prison sentence. We should use this data to argue for shorter sentences and alternatives to prison, such as reform and counselling. We should be careful to continue to provide strong disincentives to crime, however.

- Police per capita correlates positively with crime: this may mean we have not improved the effectiveness of our police in crime-infested areas. This may also be due to omitted variables and is worth exploring further.
- Similarly, wealth as proxied by tax revenue begets crime. This may also suggest that we have the money and should be able to reroute tax dollars better to fight crime in high-crime areas.
- Minorities have moderate correlation with crime. Our policies should address integration of minorities into the mainstream and reduce segregation.
- Similarly, we should investigate correlation of crime with young men. If these men are driven to crime due to lack of education or unemployment (omitted variables in this dataset), we should pay attention to reforming our education or job market.