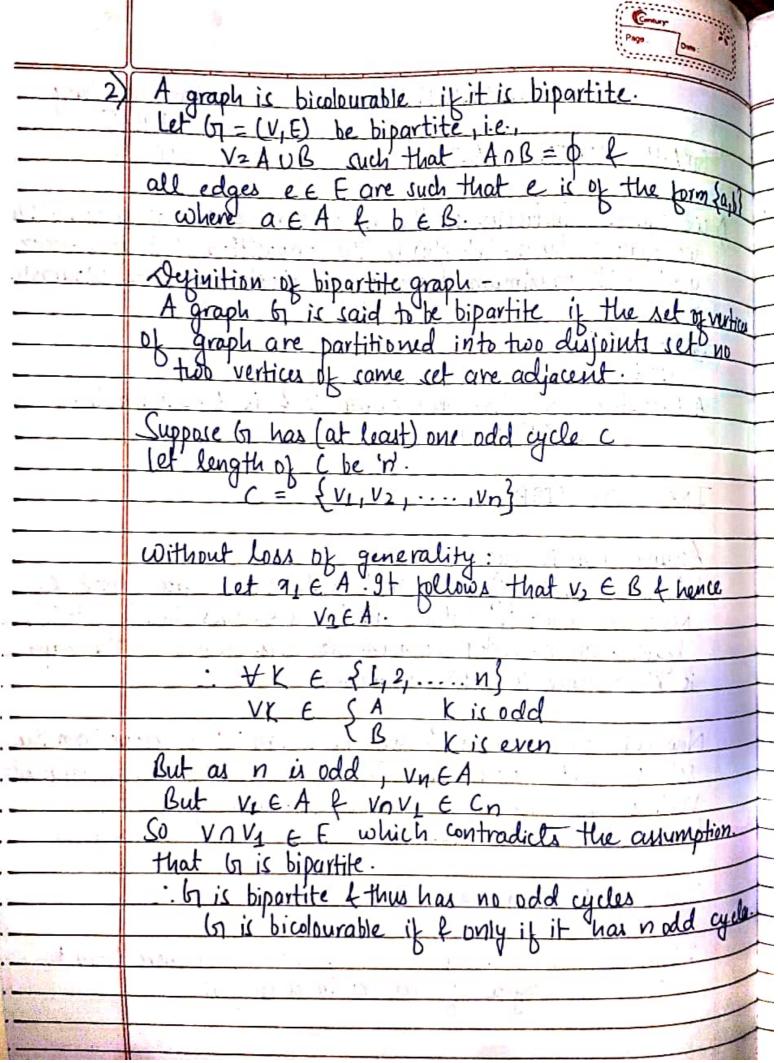
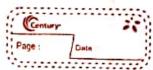


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	ASSIGNMENT 1 Saurar Chaudhary
	20184165
	GRAPH COLORING BASED CSE-C
100	
1	We can use induction on the no of vertices in the graph which
	we denote by n. let P(n) be the proposition that an n-vertex graph with maximum degree of at most k is (k+1) colourable.
	graph with maximum degree of at most k is (k+1) colourable.
131.1	O I I I I I I I I I I I I I I I I I I I
01	BASE CASE
8	N=1. per min in the min to make and
	A 1-vertea graph has man degree Of is 1-colourable.
	P(1) is true
	St in I Is I care the
	INQUITIVE STEP
	Assume P(n) is true
	let be an (n+1) verter graph with man degree atmost k.
	Remove a vertex 'v' (thus removing all edges incident to It).
	Assume P(n) is true Let 67 be an (n+1) verter graph with man degree atmost k. Remove a verter 'v' (thus removing all edges incident to it). Leaving an n-verter subgraph. The man degree of this graph is 'k' & hence is (k+1) colourable.
	is 'k' & hence is (k+1) colourable
	(1) colore from Hea
	Now add back vertex v. We can assign v a colour from the
	set of (K+1) colours that is different from an in adjuster
	vertices as there are atmost & vertices adjusted to
I H	Now add back verter's' we can assign 'v' a colour from the set of (k+1) colours that is different from all its adjacent vertices as there are atmost k vertices adjacent to v f thus afteast one of the (k+1) colours is still available.
5	
	: Gic (K+1) colourable.
E. A	will not exceed by more than I
	: Chromatic no. of agraph will not exceed by more than I the man degree of vertices in a graph.
	the man degree of voltas of grapes
1721	



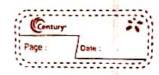


3) Let P be a Hamiltonian path of G, with origin u. Because the path P-u extends to a Hamiltonian path of G, the path Pentends to a Hamiltonian cycle Cof G. When C has no chord, 67= Cix a cycle. So let uv be a chord of C. Then u-v-is one too, because u-Cvu C-1v-is a Hamiltonian path of 61, likewise, uv-is a chord of C (where u-denotes the successor of u on C and u-visithe successor of u-). And if the length of uCv is at least four, uv and u-v-are also chords of C, in view of the Hamiltonian path u-- (v-u-v-C-1v-u-uv and the fact that uv-=(u)-v-When C has a chord uw of length two, let v=u-(=w-).
Then vw- E E. Morcover, if vw- E E, then vw- (-1) E E
in view of the Hamiltonian path w- (-1) cu w(w-v. 9f then to is complete, because uw is a chord of length two for all i. 91 Chas no thord of length two, every chord of Cis odd; moreover, every odd thord must be present.

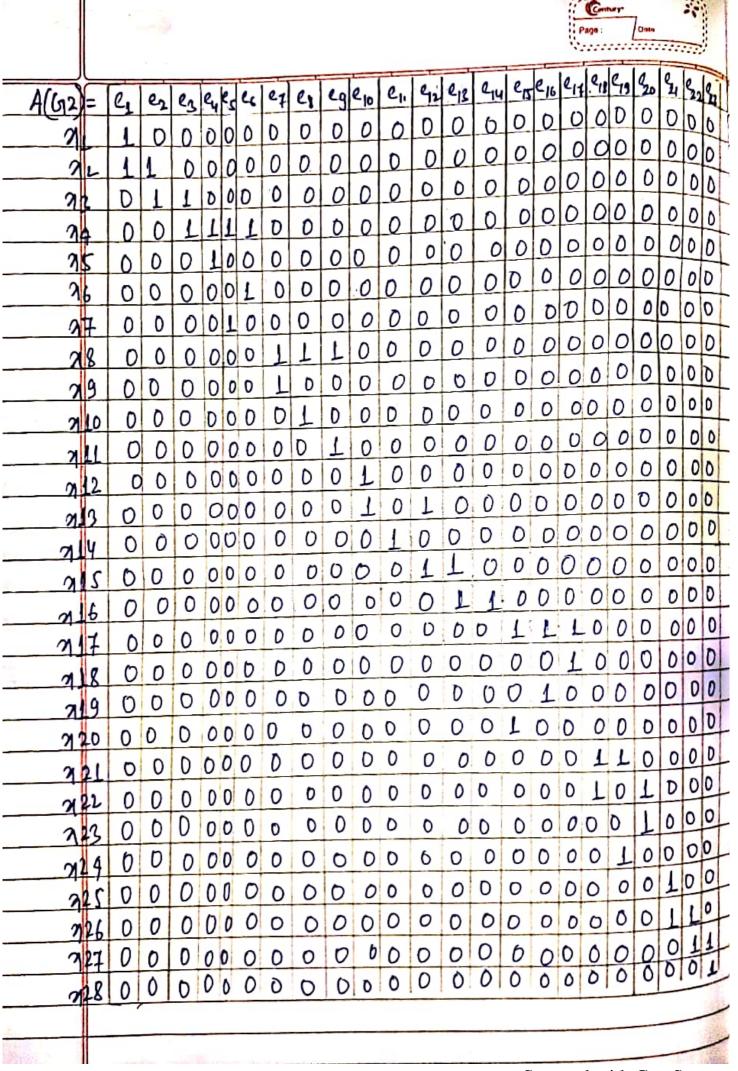
Thus, G= Kn, where | V (ln) = 2n.

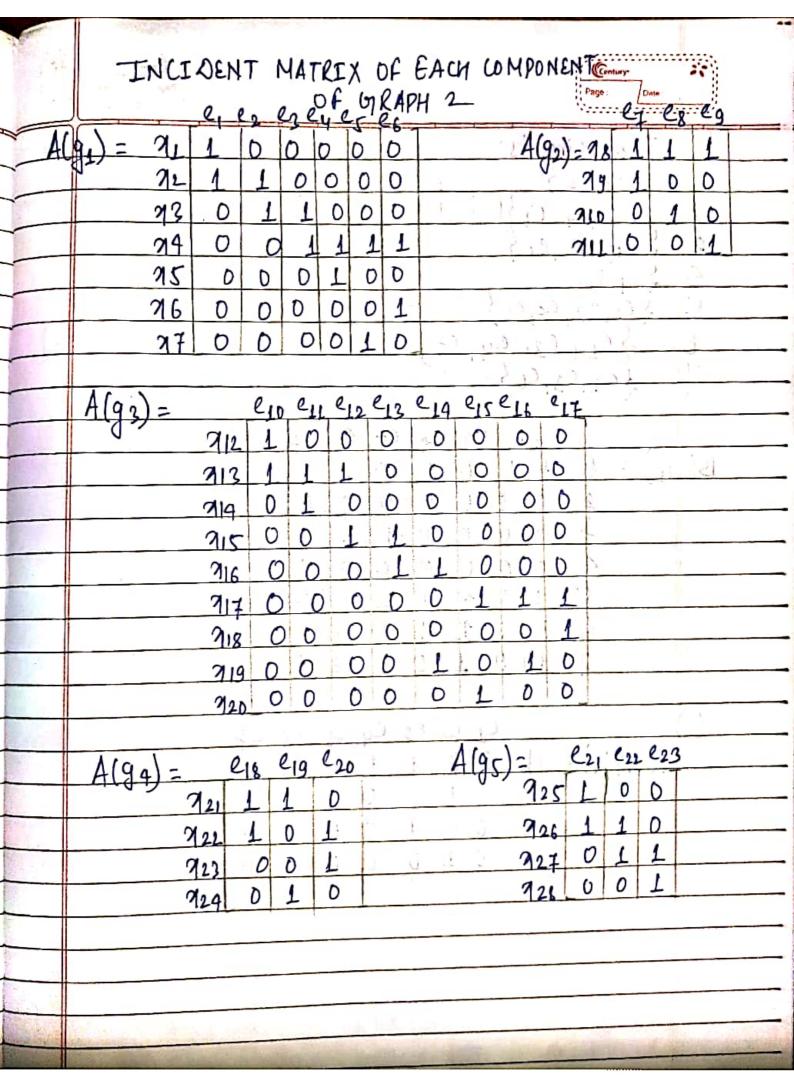


Toronto.	Verreneeren
4	Let the regions fedges of to be respectively donoted by ri,, rt and ej,, em. Let the vertices of to
14 .1	riser, ri and en em. Let the vertices of the
34	the vertices and edges of Grare in one to one correspondence with the regions of edges of Grand two vertices only if the corresponding regions of and sin is have the corresponding edge e as a common edge on their
	the vertices and edges of brare in one to one correspon
اد دارد	dence with the regions & edges of G and two vertices
He	rt and st in bit are joined by an edge e"if and
7100	only if the corresponding regions rand s in to have the
William	corresponding edge e as a common edge on their
wi	boundary:
HI	in a will be title on a supply of the contraction
10/	let G be k-region colorable we, whor the vertices in
	67* such that each vertex in 60 * gets the same colour
	as assigned to the region r in G. Since the vertices
a) =	or and it are only adjacent in by the
13-	corresponding regions rfs are adjacent in by. 6th is K-verter colorable
V 0.	6 is K- Vertez colorable
in)	
best!	Conversely, let be K-verten colourable. Now, color
2	the regions of G such that the region r in 67 gets the same colour as the vertex r* in 67 this
M 3	the same colour as the vertex in him to ". This
	gives a k-region coloring of G, since the regions r and s are adjacent in G only if the corresponding vertices r* and s* are adjacent in G*.
TO STATE OF	and s are adjacent in only if the corresponding
	vertices rot and 5th are adjacent in 11".
OR LEVE	
	157-5
100 m	
100	100 CT 100



	Page: Date:
	GRAPH REPRESENTATION IN MATRIX
1.(a	GRAPH 1
13.11	el e2 e3 e4 e5 e6 e7
11	$A(G_1) = 71 1 1 0 0 1 1 0$
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	5 0 1 1 1 1 0 0
-	6 1 0 1 1 1 0 0
	7 1 0 1 0 0 1 0
(c	e, e2 e3 e4 e5 e6 e7
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