Programming Assignment 4 Checklist: 8 Puzzle

Frequently Asked Questions

Can I use different class names, method names, or method signatures from those prescribed in the API? No, as usual, your assignment will not be graded if it violates the API.

Is 0 a block? No, 0 represents the blank square. Do not treat it as a block when computing either the Hamming or Manhattan priority functions.

Can I assume that the puzzle inputs (arguments to the Board constructor and input to Solver) are valid? Yes, though it never hurts to include some basic error checking.

Do I have to implement my own stack, queue, and priority queue? You must use either MinPQ or MaxPQ for your priority queue (because we will intercept calls in order to do performance analysis). For the other data types, you may use versions from either algs4.jar or java.util.

How do I return an Iterable Board ? Add the items you want to a Stack Board > or Queue Board > and return that. Of course, your client code should not depend on whether the iterable returned is a stack or queue (because it could be some any iterable).

How do I implement equals()? Java has some arcane rules for implementing equals(), discussed on p. 103 of Algorithms, 4th edition. Note that the argument to equals() is required to be object. You can also inspect <u>Date.java</u> or <u>Transaction.java</u> for online examples.

Must I implement the tostring() method for Board exactly as specified? Yes. Be sure to include the board dimension and use 0 for the blank square. Use string.format() to format strings—it works like Stdout.printf(), but returns the string instead of printing it to standard output. For reference, our implementation is below, but yours may vary depending on your choice of instance variables.

```
public String toString() {
   StringBuilder s = new StringBuilder();
   s.append(N + "\n");
   for (int i = 0; i < N; i++) {
      for (int j = 0; j < N; j++) {
            s.append(String.format("%2d ", tiles[i][j]));
      }
      s.append("\n");
   }
   return s.toString();
}</pre>
```

Should the hamming() and manhattan() methods in Board return the Hamming and Manhattan priority functions, respectively? No, hamming() should return the number of blocks out of position and manhattan() should return the sum of the Manhattan distances between the blocks and their goal positions. Recall that the blank square is not considered a block. You will compute the priority function in solver by calling hamming() or manhattan() and adding to it the number of moves.

I'm a bit confused about the purpose of the twin() method. You will use it to determine whether a puzzle is solvable: exactly one of a board and its twin are solvable. A twin is obtained by swapping any pair of blocks (the blank square is not a block). For example, here is a board and several possible twins. Your solver will use only one twin.

```
1 3 3 1 1 3 1 3 6 3
4 2 5 4 2 5 2 4 5 4 5 2 4 2 5 4 2 5
7 8 6 7 8 6 7 8 6 7 8 6 8 7 6 7 8 1
board twin twin twin twin twin
```

How do I reconstruct the solution once I've dequeued the goal search node? Since each search node records the previous search node to get there, you can chase the pointers all the way back to the initial search node (and consider them in reverse order).

Can I terminate the search as soon as a goal search node is enqueued (instead of dequeued)? No, even though it does lead to a correct solution for the slider puzzle problem using the Hamming and Manhattan priority functions, it's not technically the A* algorithm (and will not find the correct solution for other problems and other priority functions).

I noticed that the priorities of the search nodes dequeued from the priority queue never decrease. Is this a property of the A* algorithm? Yes. In the language of the A* algorithm, the Hamming and Manhattan distances (before adding in the number of moves so far) are known as heuristics. If a heuristic is both admissible (never overestimates the number of moves to the goal search node) and consistent (satisfies a certain triangle inequality), then this noticed property is guaranteed. The Hamming and Manhattan heuristics are both admissible and consistent. You may use this noticed property as a debugging clue: if the priority of the search node dequeued from the priority queue decreases, then you know you did something wrong.

Even with the critical optimization, the priority queue may contain two or more search nodes corresponding to the same board. Should I try to eliminate these? In principle, you could do so with a set data type such as SET in algs4.jar or java.util.TreeSet or java.util.HashSet (provided that the Board data type were either Comparable or had a hashCode() method). However, almost all of the benefit from avoiding duplicate boards is already extracted from the critical optimization and the cost of identifying other duplicate boards will

be more than the remaining benefit from doing so.

Can I put the logic for detecting whether a puzzle is infeasible in Board instead of Solver? There is a elegant algorithm for determining whether a board is solvable that relies on a parity argument (and occasionally we change our API to require this solution). However, the current API requires you to detect infeasiblity in solver by using two synchronized A* searches (e.g., using two priority queues).

I run out of memory when running some of the large sample puzzles. What should I do? Be sure to ask Java for additional memory, e.g., java -Xmx1600m Solver puzzle36.txt. We recommend running from the command line (and not from the DrJava interaction pane). You should expect to run out of memory when using the Hamming priority function. Be sure not to put the JVM option in the wrong spot or it will be treated as a command-line argument, e.g., java Solver -Xmx1600m puzzle36.txt.

My program can't solve some of the 4-by-4 puzzles, even if I give it a huge amount of space. What am I doing wrong? Probably nothing. The A* algorithm (with the Manhattan priority function) will struggle to solve even some 4-by-4 instances.

Testina

Input files. The directory <u>8puzzle</u> contains many sample puzzle input files. For convenience, <u>8puzzle-testing.zip</u> contains all of these files bundled together.

- The shortest solution to puzzle[T].txt requires exactly T moves.
- The shortest solution to puzzle4x4-hard1.txt and puzzle4x4-hard2.txt are 38 and 47, respectively.
- Warning: puzzle36.txt is especially difficult.

Test client. A good way to automatically run your program on our sample puzzles is to use the client PuzzleChecker.java.

Priority queue trace.

 Here are the contents of our priority queue (sorted by priority) just before dequeueing each node when using the Manhattan priority function on puzzle04.txt.

```
Step 0:
            priority
            moves
                          0
            manhattan =
            3
             0
                 1
                    3
             4
                2
                    5
             7
                8
                    6
            priority
Step 1:
                       = 4
                               priority
                                           = 6
            moves
                          1
                               moves
                         3
                               manhattan =
            manhattan
                                3
            3
             1
                 0
                    3
                                 4
                                    1
                                       3
                 2
                    5
                                 0
                                    2
                                       5
                 8
                                    8
                                                   priority
Step 2:
            priority
                               priority
            moves
                          2
                               moves
                                                   moves
            manhattan
                               manhattan
                                                   manhattan
                 2
                                                       3
             1
                    3
                                 4
                                                    1
                 0
                    5
                                 0
                                    2
                                       5
                                                    4
                                                       2
                                                           5
             4
             7
                 8
                    6
                                 7
                                    8
                                                    7
                                                        8
                                                           6
                                        6
Step 3:
            priority
                       = 4
                                priority
                                             6
                                                   priority
                                                              = 6
                                                                       priority
                                                                                  = 6
                                                                                          priority
            moves
                        =
                          3
                                moves
                                                   moves
                                                              =
                                                                       moves
                                                                                  = 3
                                                                                          moves
                                                                2
                                           = 3
            manhattan
                       =
                          1
                               manhattan
                                                   manhattan
                                                              = 4
                                                                       manhattan
                                                                                  = 3
                                                                                          manhattan = 5
             1
                2
                    3
                                 1
                                    2
                                       3
                                                    1
                                                       3
                                                           0
                                                                        1
                                                                           2
                                                                              3
                                                                                           4
                                                                                              1
                                                                                                  3
                 5
                    0
                                    8
                                       5
                                                        2
                                                           5
                                                                        0
                                                                           4
                                                                              5
                                                                                           0
                                                                                              2
                                                                                                  5
                 8
                                                        8
                                                           6
                                                                           8
                                                                                              8
                    6
                                    0
Step 4:
            priority
                       = 4
                               priority
                                          = 6
                                                   priority
                                                              = 6
                                                                       priority
                                                                                          priority
                                                                                                             priority
                                                                                                                         = 6
                                           = 3
            moves
                          4
                               moves
                                                   moves
                                                                 4
                                                                       moves
                                                                                    2
                                                                                          moves
                                                                                                     = 3
                                                                                                             moves
                                                                                                                           1
            manhattan
                          0
                               manhattan
                                                   manhattan
                                                              = 2
                                                                       manhat.t.an
                                                                                          manhat.t.an
                                                                                                             manhattan =
                                3
                                                   3
                                                                       3
                                                                                          3
                                                                                                             3
                 2
                                    2
                                                       2
                                                           0
                                                                           3
                                                                                           1
                                                                                              2
                                                                                                  3
                                                                                                               4
                                                                                                                     3
             1
                    3
                                 1
                                        3
                                                    1
                                                                        1
                                                                                                                  1
                 5
                    6
                                 0
                                    4
                                       5
                                                                           2
                                                                              5
                                                                                              8
                                                                                                  5
                                                                                                                  2
                                                                                                                     5
             4
                                                        5
                                                           3
                                                                        4
                                                                                           4
                                                                                                               0
                                                        8
                                                           6
                                                                           8
                                                                                              0
```

There were a total of 10 search nodes enqueued and 5 search nodes dequeued. In general, the number of search nodes enqueued and dequeued may vary slightly, depending the order in which the search nodes with equal priorities come off the priority queue, which depends on the order in which neighbors () returns the neighbors of a board. However, for this input, there are no such ties, so you should

have exactly 10 search nodes enqueued and 5 search nodes dequeued.

- The contents of our priority queue (sorted by priority) just before dequeueing each node when using the Hamming priority function on puzzle04.txt turns out to be identical to the results above: for this input file, throughout the A* algorithm, a block is never more than one position away from its goal position, which implies that the Hamming function and the Manhattan functions are equal.
- Write the class solver that uses the A* algorithm to solve puzzle instances. -->

Enrichment

How can I reduce the amount of memory a Board uses? For starters, recall that an N-by-N int[][] array in Java uses about 24 + 32N + 4N^2 bytes; when N equals 3, this is 156 bytes. To save memory, consider using an N-by-N char[][] array or a length N^2 char[] array. In principle, each board is a permutation of size N^2, so you need only about lg ((N^2)!) bits to represent it; when N equals 3, this is only 19 bits.

Any ways to speed up the algorithm? Yes there are many opportunities for optimization here.

- Use a 1d array instead of a 2d array (as suggested above).
- Cache either the Manhattan distance of a board (or Manhattan priority of a search node). It is waste to recompute the same quantity over and over again.
- Exploit the fact that the difference in Manhattan distance between a board and a neighbor is either +1, -1, or 0, based on the direction that the block moves.
- Use only one PQ to run the A* algorithm on the initial board and its twin.
- When two search nodes have the same Manhattan priority, you can break ties however you want, e.g., by comparing either the Hamming or Manhattan distances of the two boards.
- Use a parity argument to determine whether a puzzle is unsolvable (instead of two synchronous A* searches). However, this will either break the API or will require a fragile dependence on the tostring() method, so don't do it.

Is there an efficient way to solve the 8-puzzle and its generalizations? Finding a shortest solution to an N-by-N slider puzzle is \underline{NP} -hard, so it's unlikely that an efficient solution exists.

What if I'm satisfied with any solution and don't need one that uses the fewest number of moves? Yes, change the priority function to put more weight on the Manhattan distance, e.g., 100 times the Manhattan distance plus the number of moves made already. This paper describes an algorithm that guarantees to perform at most N^3 moves.

Are there better ways to solve 8- and 15-puzzle instances using the minimum number of moves? Yes, there are a number of approaches.

- Use the A* algorithm with a better admissible priority function:
 - Linear conflict: add two to the Manhattan priority function whenever two tiles are in their goal row (or column) but are reversed relative to their goal position.
 - Pattern database: For each possible configuration of 4 tiles and the blank, determine the minimum number of moves to put just these tiles in their proper position and store these values in a database. The heuristic value is the maximum over all configurations, plus the number of moves made so far. This can reduce the number of search nodes examined for random 15-puzzle instances by a factor of 1000.
- Use a variant of the A* algorithm known as IDA* (for iterative deepening). This paper describes its application to the 15-slider puzzle.
- Another approach is to use <u>bidirectional search</u>, where you simultaneously search from the initial board to find the goal board and from the goal board to find the initial board, and have the two search trees meet in the middle. Handling the stopping condition is delicate.

Can a puzzle have more than one shortest solution? Yes. See puzzle07.txt.

So	lut	ion	1																				
1	2 7	3 6	1 7	2	3 6	1 7	2 4	3 6	1 7	2 4	3 6	1	2 4	3 6	1 4	2	3 6	1 4	2 5	3 6	1 4	2 5	3
5	4	8	5	4	8	5		8		5	8	7	5	8	7	5	8	7		8	7	8	
So 1	lut 2 7	ion 3 6	2 1 5	2 7	3 6	1 5	2 7	 3 6	1 5	2	3 6	1	2 5	 3 6	1 4	 2 5	3 6	1 4	2 5	 3 6	1 4	2 5	 3 6
5	4	8		4	8	4		8	4	7	8	4	7	8		7	8	7		8	7	8	

In such cases, you are required to output any one such solution.