## Design And Analysis of Algorithms

Assignment - L

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UNIVERSITY ROLL > 2014-845

SECTION -> F

CLASS ROLL -> 50

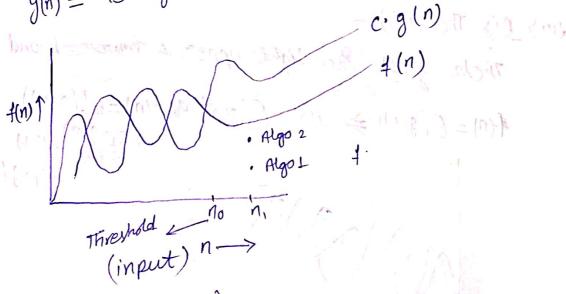
SEMESTER -> 5th.

1) -> When we have analyse the complixity of any algorithm in term of time and space, we never provide an exact number to define the time required and the space required by algorithm, so, we use Asymptotic notation.

The three types of Asymptotic notation are:-

x1> Biga on(0):

f(n) = O(g(n)) g(n) = is "Hight" upper bound of f(n) g(n) = is "Hight" upper bound of f(n)



$$f(n) = O(g(n))$$
  
if only if  
 $f(n) \leq c \cdot g(n)$   
 $f(n) \leq n \cdot g(n)$   
 $f(n) \leq n \cdot g(n)$   
 $f(n) \leq n \cdot g(n)$ 

We the state of the

Ex: Algo1 
$$\Rightarrow$$
  $O(n^2+3n+4)$   $\Rightarrow$   $O(n^2+n)$   $\Rightarrow$   $O(n^2)$ 

Algo2  $\Rightarrow$   $O(2n^2+4)$   $\Rightarrow$   $O(n^2)$ 
 $\forall (n) \Rightarrow O(n^2)$ 
 $\forall (n) \Rightarrow$ 

$$\begin{array}{l}
\textcircled{2} \Rightarrow \text{ for } (i=1 \pm 0 n) \\
& \text{ fi} = i \neq 2 \\
& \text{ g} \\
& \text{ 1, 2, 3, ---} n \\
& \text{ } n = 1 + (k-1) \textcircled{2} 1 \\
& \text{ } n \textcircled{2} = k-1+1 \\
& \text{ } k = n \textcircled{2} \\
& \text{ Time complexity} = O(n).}
\end{aligned}$$

$$\begin{array}{l}
\textcircled{3} \Rightarrow T(n) = \$3T(n-1) & \text{ if } n > 0, \text{ otherwise } 1\$2 \\
& \text{ bose case } T(1) = 1 \\
& \text{ } T(n) = 3T(n-1) \longrightarrow 0
\end{aligned}$$

$$\begin{array}{l}
\text{ put } n = n-1 \\
& \text{ } T(n-1) = 3T(n-2) \longrightarrow 2
\end{aligned}$$

$$\begin{array}{l}
\text{ put the } T(n-1) & \text{ in } \textcircled{2} n \bigcirc 0
\end{aligned}$$

$$\begin{array}{l}
\text{ } T(n) = 3 \cdot 3 \cdot T(n-2) \longrightarrow 3
\end{aligned}$$

$$\begin{array}{l}
\text{ } Now \text{ put } n = n-2 \text{ in } \textcircled{2} n \bigcirc 0
\end{aligned}$$

$$\begin{array}{l}
\text{ } T(n-2) = 3 \cdot T(n-3) \longrightarrow 6
\end{aligned}$$

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\end{aligned}$$

(5) 
$$\rightarrow$$
 inti=1, s=1;  
while(s<=n)  
i++;  
s=s+i;  
print("#');  
}  
 $T(n) = 1+2+3+--++n$ .  
 $T(n) = 1+2+3+--++\sqrt{n}$   
i.  $\sqrt{n} = 1+(n-1)d$   
 $\sqrt{n} = 1+(k-1)1$   
 $\sqrt{n} = k-1+1$   
 $k = \sqrt{n}$   
 $T(n) = 0(\sqrt{n})$   
for(i=1; i<=n; i++)  $\longrightarrow$   $O(\frac{n}{2})$   
for(j=1; i<=n; j=j\*2)  $\longrightarrow$   $O(\log n)$   
 $for(k=1; k<=n; k=k^2)  $\longrightarrow$   $O(\log n)$   
 $for(k=1; k<=n; k=k^2)  $\longrightarrow$   $O(\log n)$   
 $for(n) = 0$$$ 

$$0 \rightarrow void function (int n) for (i=10n) s \rightarrow O(n) for (i=10n) s \rightarrow O(n) for (i=10n) s \rightarrow O(n)$$

$$for (i=10n) s \rightarrow O(n)$$

$$frint("x")$$

$$f(n) = n^{K} \quad \{k \geq 13\} \text{ are constant}$$

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(1) 
$$\Rightarrow$$
 ind the fiblint n)

if  $(n <= 1)$ 

seturn; else

seturn fibl(n-1) + fibl(n-2);

3

$$T(n) = T(n-1) + T(n-2) + L$$

Let assume  $T(n-1)$  y  $T(n-2)$ 

$$T(n) = 2*T(T-1)+1 - O$$

now putting  $T(n-1)$  in  $T(n-2)$  in  $T(n-1) = 2*T(n-2) + L$ 

By putting  $T(n-1)$  in  $T(n-1)$  in  $T(n-1) = 2*T(n-2) + L + L$ 

now putting  $T(n-1)$  in  $T(n-1)$  in  $T(n-1) = 2*L^2 + T(n-2) + L + L$ 

putting  $T(n-1)$  in  $T(n-1)$  in  $T(n-1) = 2*L^2 + T(n-1) + L + L + L + L + L$ 

$$T(n) = 2*L^2 + T(n-1) + L + L + L + L + L + L + L$$

$$T(n) = 2*L^2 + T(n-1) + L + L + L + L + L + L$$

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$$T(n) = 2*L^2 + T(n-1) + L + L$$

$$T(n) = 2*L^2 + T(n-1) +$$

$$T(n) = \frac{2}{2} \times 1 + 2^{n} - 1$$

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8/10(1) 'expression

for lint 
$$i=2$$
;  $i < n$ ;  $i = pow(i, k)$ 

$$\begin{cases}
1/ & O(1) & e \times p \\
2/ & 2^{k}, (2^{k})^{k} \\
2/ & (2^{k})^{k}$$

- $(3) \rightarrow (3) \rightarrow 100 < log log n < log n < log (n) < log (n) < n < n < n < n < 2^n < 2^n < 2^n = 4^n$ 

  - ©  $\rightarrow 16 < \log_8(n) < \log_2 n = n \log_8(n) < \log_2 n < n \log_2 n < s n < 8(2n)$
- ineorSearch (arr, n, rey)

  if (arr[n-1] == key)

  return to n;

  femp = arr[n-1]

  arr[n-1] == key.

  for (i=0, i+t)

  if (arr[i] == key)

  arr[n-1] = demp;

  return (i x n-1)

  return (i x n-1)

```
Insertionsort (int arr [], Int n)

for i=1 to i<v

fint remsp = arotiji

int j= i t

while (j>0 xc arr [i-1] > temp)

arr [j] = arr [j-1]

j--

orr [j] = value

}
```

## Iteration Insertion Sort

```
Insertionsort (int arr[], int i', int n)

int temp = arr[i];

int j = i

while (j>0 == arr[j-i]>temp)

arr[j] = arr[j-i]

j--

arr[j] = temp;

if l(i+1 <=n)

Insertionsort (arr, i+1 n);
```

## Recursive Insertion sort

Insertion sort is an online algorithm which processes its input piece-by piece in a serial way, i.e. in the order that the input is fed to the algorithm, without having the entire input available from the begining.

Selection Sort → Offline Merge Sort → offline

Best Average Worst 
$$2l \rightarrow 8ubble Sort \rightarrow 0(n)$$
  $0(n^2)$   $0(n^2)$   $0(n^2)$  Selection  $Sort \rightarrow 0(n^2)$   $0(n^2)$   $0(n^2)$  Insertion  $Sort \rightarrow 0(n)$   $0(n^2)$   $0(n^2)$   $0(n^2)$  Merge  $Sort \rightarrow 0(nlog(n))$   $0(nlog n)$   $0(nlog n)$ 

THE THE THE

```
Recursive Binary Search
                int binarysearch (int arr [], intl, intr, inter)
            ( i+( x >= 4) §
            int mid < (1+8)/2;
                                      if (arr [mid] == x) (1) <- 1008 montholis
    return and, (ii) - the months all
     elseit (arr[mid] >x)
                                           return binary search (arr, Limid-1, x);
                                                return binarysearch (arr, mid + L, r, x);
       spren 3 return -1/ montales | mon
Recursive Binary Search
                                                     Time complixity > O(log_n)
                                                           space complixity > O(logen)
           Iterative Birnous search
                                                                Time \rightarrow 0(log_2n)
                                                                space -> 0(1)
    Recursive linear Search
                                                                         Time > O(n)
```

Herotive Bioang Linear search

T > 0(n) Space -> 0(1)

space -> O(n)

$$(24)$$
  $T(n) = T(\frac{n}{2}) + 1$ .