

## SBML Model Report

**Model name:**  
**“Chay1997\_CalciumConcentration”**



May 5, 2016

### 1 General Overview

This is a document in SBML Level 2 Version 4 format. This model was created by the following two authors: Ishan Ajmera<sup>1</sup> and Catherine Lloyd<sup>2</sup> at September 29<sup>th</sup> 2011 at 10:17 p. m. and last time modified at April eighth 2016 at 5:08 p. m. Table 1 provides an overview of the quantities of all components of this model.

Table 1: Number of components in this model, which are described in the following sections.

| Element           | Quantity | Element              | Quantity |
|-------------------|----------|----------------------|----------|
| compartment types | 0        | compartments         | 1        |
| species types     | 0        | species              | 6        |
| events            | 0        | constraints          | 0        |
| reactions         | 0        | function definitions | 0        |
| global parameters | 49       | unit definitions     | 0        |
| rules             | 21       | initial assignments  | 0        |

### Model Notes

This a model from the article:

**Effects of extracellular calcium on electrical bursting and intracellular and luminal calcium oscillations in insulin secreting pancreatic beta-cells.**

Chay TR *Biophys J.*1997 Sep;73(3):1673-88. [9284334](#),

<sup>1</sup>EMBL-EBI, [ajmera@ebi.ac.uk](mailto:ajmera@ebi.ac.uk)

<sup>2</sup>The University of Auckland, The Bioengineering Institute, [c.lloyd@auckland.ac.nz](mailto:c.lloyd@auckland.ac.nz)

**Abstract:**

The extracellular calcium concentration has interesting effects on bursting of pancreatic beta-cells. The mechanism underlying the extracellular  $\text{Ca}^{2+}$  effect is not well understood. By incorporating a low-threshold transient inward current to the store-operated bursting model of Chay, this paper elucidates the role of the extracellular  $\text{Ca}^{2+}$  concentration in influencing electrical activity, intracellular  $\text{Ca}^{2+}$  concentration, and the luminal  $\text{Ca}^{2+}$  concentration in the intracellular  $\text{Ca}^{2+}$  store. The possibility that this inward current is a carbachol-sensitive and TTX-insensitive  $\text{Na}^{+}$  current discovered by others is discussed. In addition, this paper explains how these three variables respond when various pharmacological agents are applied to the store-operated model.

This model was taken from the [CellML repository](#) and automatically converted to SBML.

The original model was: [Chay TR \(1997\) - version05](#)

The original CellML model was created by:

**Lloyd, Catherine, May**

c.lloyd@auckland.ac.nz

The University of Auckland

The Bioengineering Institute

This model originates from BioModels Database: A Database of Annotated Published Models (<http://www.ebi.ac.uk/biomodels/>). It is copyright (c) 2005-2011 The BioModels.net Team.

For more information see the [terms of use](#).

To cite BioModels Database, please use: [Li C, Donizelli M, Rodriguez N, Dharuri H, Endler L, Chelliah V, Li L, He E, Henry A, Stefan MI, Snoep JL, Hucka M, Le Novre N, Laibe C \(2010\) BioModels Database: An enhanced, curated and annotated resource for published quantitative kinetic models. BMC Syst Biol., 4:92.](#)

## 2 Unit Definitions

This is an overview of five unit definitions which are all predefined by SBML and not mentioned in the model.

### 2.1 Unit `substance`

**Notes** Mole is the predefined SBML unit for substance.

**Definition** mol

### 2.2 Unit `volume`

**Notes** Litre is the predefined SBML unit for volume.

**Definition** l

### 2.3 Unit area

**Notes** Square metre is the predefined SBML unit for area since SBML Level 2 Version 1.

**Definition**  $\text{m}^2$

### 2.4 Unit length

**Notes** Metre is the predefined SBML unit for length since SBML Level 2 Version 1.

**Definition** m

### 2.5 Unit time

**Notes** Second is the predefined SBML unit for time.

**Definition** s

## 3 Compartment

This model contains one compartment.

Table 2: Properties of all compartments.

| Id          | Name        | SBO | Spatial<br>Dimensions | Size | Unit  | Constant                            | Outside |
|-------------|-------------|-----|-----------------------|------|-------|-------------------------------------|---------|
| Compartment | Compartment |     | 3                     | 1    | litre | <input checked="" type="checkbox"/> |         |

### 3.1 Compartment [Compartment](#)

This is a three dimensional compartment with a constant size of one litre.

**Name** Compartment

## 4 Species

This model contains six species. Section 7 provides further details and the derived rates of change of each species.

Table 3: Properties of each species.

| Id                          | Name                   | Compartment | Derived Unit                     | Constant  | Boundary Condition |
|-----------------------------|------------------------|-------------|----------------------------------|-----------|--------------------|
| V_membrane                  | V_membrane             | Compartment | $\text{mol} \cdot \text{l}^{-1}$ | $\square$ | $\square$          |
| h                           | h                      | Compartment | $\text{mol} \cdot \text{l}^{-1}$ | $\square$ | $\square$          |
| d                           | d                      | Compartment | $\text{mol} \cdot \text{l}^{-1}$ | $\square$ | $\square$          |
| n                           | n                      | Compartment | $\text{mol} \cdot \text{l}^{-1}$ | $\square$ | $\square$          |
| Ca_i_cytosolic-<br>_calcium | Ca_i_cytosolic_calcium | Compartment | $\text{mol} \cdot \text{l}^{-1}$ | $\square$ | $\square$          |
| Ca_lum                      | Ca_lum                 | Compartment | $\text{mol} \cdot \text{l}^{-1}$ | $\square$ | $\square$          |

## 5 Parameters

This model contains 49 global parameters.

Table 4: Properties of each parameter.

| Id          | Name       | SBO     | Value     | Unit | Constant                            |
|-------------|------------|---------|-----------|------|-------------------------------------|
| R           | R          | 0000567 | 8314.000  |      | <input checked="" type="checkbox"/> |
| T           | T          | 0000002 | 310.000   |      | <input checked="" type="checkbox"/> |
| F           | F          | 0000568 | 96485.000 |      | <input checked="" type="checkbox"/> |
| Cm          | Cm         | 0000247 | 1.000     |      | <input checked="" type="checkbox"/> |
| i_fast      | i_fast     |         | −96.640   |      | <input type="checkbox"/>            |
| g_fast      | g_fast     | 0000009 | 600.000   |      | <input checked="" type="checkbox"/> |
| V_fast      | V_fast     | 0000009 | 80.000    |      | <input checked="" type="checkbox"/> |
| m_infinity  | m_infinity | 0000009 | 0.185     |      | <input type="checkbox"/>            |
| Vm          | Vm         | 0000009 | −25.000   |      | <input checked="" type="checkbox"/> |
| Sm          | Sm         | 0000009 | 9.000     |      | <input checked="" type="checkbox"/> |
| lamda_h     | lamda_h    |         | 12.500    |      | <input checked="" type="checkbox"/> |
| tau_h       | tau_h      | 0000009 | 0.032     |      | <input type="checkbox"/>            |
| h_infinity  | h_infinity | 0000009 | 0.201     |      | <input type="checkbox"/>            |
| Vh          | Vh         | 0000009 | −48.000   |      | <input checked="" type="checkbox"/> |
| Sh          | Sh         | 0000009 | −7.000    |      | <input checked="" type="checkbox"/> |
| i_Ca        | i_Ca       | 0000009 | −24.125   |      | <input type="checkbox"/>            |
| K_Ca        | K_Ca       | 0000009 | 1.000     |      | <input checked="" type="checkbox"/> |
| P_Ca        | P_Ca       | 0000009 | 2.000     |      | <input checked="" type="checkbox"/> |
| Ca_o        | Ca_o       | 0000009 | 2500.000  |      | <input checked="" type="checkbox"/> |
| lamda_d     | lamda_d    | 0000009 | 2.500     |      | <input checked="" type="checkbox"/> |
| tau_d       | tau_d      |         | 0.023     |      | <input type="checkbox"/>            |
| d_infinity  | d_infinity |         | 0.003     |      | <input type="checkbox"/>            |
| Vd          | Vd         | 0000009 | −10.000   |      | <input checked="" type="checkbox"/> |
| Sd          | Sd         | 0000009 | 5.000     |      | <input checked="" type="checkbox"/> |
| f_infinity  | f_infinity |         | 0.500     |      | <input type="checkbox"/>            |
| Ca_i-       | Ca_i       |         | 1.000     |      | <input checked="" type="checkbox"/> |
| _calcium-   |            |         |           |      |                                     |
| _current_f- |            |         |           |      |                                     |
| _gate       |            |         |           |      |                                     |
| i_NS        | i_NS       | 0000009 | −6.241    |      | <input type="checkbox"/>            |
| g_NS        | g_NS       | 0000009 | 5.000     |      | <input checked="" type="checkbox"/> |
| K_NS        | K_NS       | 0000009 | 50.000    |      | <input checked="" type="checkbox"/> |
| VNS         | VNS        | 0000009 | −20.000   |      | <input checked="" type="checkbox"/> |
| i_K_dr      | i_K_dr     |         | 25.015    |      | <input type="checkbox"/>            |
| V_K         | V_K        | 0000009 | −75.000   |      | <input checked="" type="checkbox"/> |
| g_K_dr      | g_K_dr     | 0000009 | 600.000   |      | <input checked="" type="checkbox"/> |
| lamda_n     | lamda_n    | 0000009 | 12.500    |      | <input checked="" type="checkbox"/> |

| Id         | Name       | SBO     | Value   | Unit | Constant                            |
|------------|------------|---------|---------|------|-------------------------------------|
| Vn         | Vn         | 0000009 | −18.000 |      | <input checked="" type="checkbox"/> |
| Sn         | Sn         | 0000009 | 14.000  |      | <input checked="" type="checkbox"/> |
| n_infinity | n_infinity |         | 0.190   |      | <input type="checkbox"/>            |
| tau_n      | tau_n      |         | 0.031   |      | <input type="checkbox"/>            |
| i_K_Ca     | i_K_Ca     |         | 46.208  |      | <input type="checkbox"/>            |
| g_K_Ca     | g_K_Ca     |         | 5.000   |      | <input checked="" type="checkbox"/> |
| i_K_ATP    | i_K_ATP    |         | 73.317  |      | <input type="checkbox"/>            |
| g_K_ATP    | g_K_ATP    |         | 2.000   |      | <input checked="" type="checkbox"/> |
| i_NaL      | i_NaL      |         | −35.502 |      | <input type="checkbox"/>            |
| g_NaL      | g_NaL      | 0000009 | 0.300   |      | <input checked="" type="checkbox"/> |
| V_Na       | V_Na       | 0000009 | 80.000  |      | <input checked="" type="checkbox"/> |
| k_rel      | k_rel      | 0000009 | 0.200   |      | <input checked="" type="checkbox"/> |
| k_Ca       | k_Ca       | 0000009 | 7.000   |      | <input checked="" type="checkbox"/> |
| k_pump     | k_pump     | 0000009 | 30.000  |      | <input checked="" type="checkbox"/> |
| omega      | omega      | 0000009 | 0.200   |      | <input checked="" type="checkbox"/> |

## 6 Rules

This is an overview of 21 rules.

### 6.1 Rule `m_infinity`

Rule `m_infinity` is an assignment rule for parameter `m_infinity`:

$$m\_infinity = \frac{1}{1 + \exp\left(\frac{V_m - [V\_membrane]}{S_m}\right)} \quad (1)$$

### 6.2 Rule `i_fast`

Rule `i_fast` is an assignment rule for parameter `i_fast`:

$$i\_fast = g\_fast \cdot m\_infinity^3 \cdot [h] \cdot ([V\_membrane] - V\_fast) \quad (2)$$

### 6.3 Rule `tau_h`

Rule `tau_h` is an assignment rule for parameter `tau_h`:

$$\tau\_h = \frac{1}{\lambda\_h \cdot \left( \exp\left(\frac{V_h - [V\_membrane]}{2 \cdot S_h}\right) + \exp\left(\frac{[V\_membrane] - V_h}{2 \cdot S_h}\right) \right)} \quad (3)$$

#### 6.4 Rule `h_infinity`

Rule `h_infinity` is an assignment rule for parameter `h_infinity`:

$$h\_infinity = \frac{1}{1 + \exp\left(\frac{V_h - [V\_membrane]}{S_h}\right)} \quad (4)$$

#### 6.5 Rule `tau_d`

Rule `tau_d` is an assignment rule for parameter `tau_d`:

$$\tau\_d = \frac{1}{\lambda\_d \cdot \left( \exp\left(\frac{V_d - [V\_membrane]}{2 \cdot S_d}\right) + \exp\left(\frac{[V\_membrane] - V_d}{2 \cdot S_d}\right) \right)} \quad (5)$$

#### 6.6 Rule `f_infinity`

Rule `f_infinity` is an assignment rule for parameter `f_infinity`:

$$f\_infinity = \frac{K\_Ca}{K\_Ca + Ca\_i\_cytosolic\_calcium\_current\_f\_gate} \quad (6)$$

#### 6.7 Rule `i_Ca`

Rule `i_Ca` is an assignment rule for parameter `i_Ca`:

$$i\_Ca = \frac{\frac{P\_Ca \cdot [d] \cdot f\_infinity \cdot 2 \cdot F \cdot [V\_membrane]}{R \cdot T} \cdot \left( Ca\_o - [Ca\_i\_cytosolic\_calcium] \cdot \exp\left(\frac{2 \cdot F \cdot [V\_membrane]}{R \cdot T}\right) \right)}{1 - \exp\left(\frac{2 \cdot F \cdot [V\_membrane]}{R \cdot T}\right)} \quad (7)$$

#### 6.8 Rule `d_infinity`

Rule `d_infinity` is an assignment rule for parameter `d_infinity`:

$$d\_infinity = \frac{1}{1 + \exp\left(\frac{V_d - [V\_membrane]}{S_d}\right)} \quad (8)$$

#### 6.9 Rule `i_NS`

Rule `i_NS` is an assignment rule for parameter `i_NS`:

$$i\_NS = \frac{g\_NS \cdot K\_NS^2}{K\_NS^2 + [Ca\_lum]^2} \cdot \left( \frac{[V\_membrane] - VNS}{1 - \exp(0.1 \cdot (VNS - [V\_membrane]))} - 10 \right) \quad (9)$$

### 6.10 Rule `i_K_dr`

Rule `i_K_dr` is an assignment rule for parameter `i_K_dr`:

$$i\_K\_dr = g\_K\_dr \cdot [n]^4 \cdot ([V\_membrane] - V\_K) \quad (10)$$

### 6.11 Rule `n_infinity`

Rule `n_infinity` is an assignment rule for parameter `n_infinity`:

$$n\_infinity = \frac{1}{1 + \exp\left(\frac{Vn - [V\_membrane]}{S_n}\right)} \quad (11)$$

### 6.12 Rule `tau_n`

Rule `tau_n` is an assignment rule for parameter `tau_n`:

$$\tau\_n = \frac{1}{\text{lamda}_n \cdot \left( \exp\left(\frac{Vn - [V\_membrane]}{2 \cdot S_n}\right) + \exp\left(\frac{[V\_membrane] - Vn}{2 \cdot S_n}\right) \right)} \quad (12)$$

### 6.13 Rule `i_K_ATP`

Rule `i_K_ATP` is an assignment rule for parameter `i_K_ATP`:

$$i\_K\_ATP = g\_K\_ATP \cdot ([V\_membrane] - V\_K) \quad (13)$$

### 6.14 Rule `i_K_Ca`

Rule `i_K_Ca` is an assignment rule for parameter `i_K_Ca`:

$$i\_K\_Ca = \frac{g\_K\_Ca \cdot [Ca\_i\_cytosolic\_calcium]^3}{K\_Ca^3 + [Ca\_i\_cytosolic\_calcium]^3} \cdot ([V\_membrane] - V\_K) \quad (14)$$

### 6.15 Rule `i_NaL`

Rule `i_NaL` is an assignment rule for parameter `i_NaL`:

$$i\_NaL = g\_NaL \cdot ([V\_membrane] - V\_Na) \quad (15)$$

### 6.16 Rule `V_membrane`

Rule `V_membrane` is a rate rule for species `V_membrane`:

$$\frac{d}{dt} V\_membrane = \frac{(i\_K\_dr + i\_K\_Ca + i\_K\_ATP + i\_fast + i\_Ca + i\_NS + i\_NaL)}{Cm} \quad (16)$$



### 6.17 Rule `h`

Rule `h` is a rate rule for species `h`:

$$\frac{d}{dt}h = \frac{h\_infinity - [h]}{\tauau\_h} \quad (17)$$

### 6.18 Rule `d`

Rule `d` is a rate rule for species `d`:

$$\frac{d}{dt}d = \frac{d\_infinity - [d]}{\tauau\_d} \quad (18)$$

### 6.19 Rule `n`

Rule `n` is a rate rule for species `n`:

$$\frac{d}{dt}n = \frac{n\_infinity - [n]}{\tauau\_n} \quad (19)$$

### 6.20 Rule `Ca_i_cytosolic_calcium`

Rule `Ca_i_cytosolic_calcium` is a rate rule for species `Ca_i_cytosolic_calcium`:

$$\begin{aligned} \frac{d}{dt}Ca\_i\_cytosolic\_calcium = & k\_rel \cdot ([Ca\_lum] - [Ca\_i\_cytosolic\_calcium]) - (\omega\epsilon a \cdot i\_Ca + k\_Ca \\ & \cdot [Ca\_i\_cytosolic\_calcium] + k\_pump \cdot [Ca\_i\_cytosolic\_calcium]) \end{aligned} \quad (20)$$

### 6.21 Rule `Ca_lum`

Rule `Ca_lum` is a rate rule for species `Ca_lum`:

$$\frac{d}{dt}Ca\_lum = k\_rel \cdot ([Ca\_lum] - [Ca\_i\_cytosolic\_calcium]) + k\_pump \cdot [Ca\_i\_cytosolic\_calcium] \quad (21)$$

## 7 Derived Rate Equations

When interpreted as an ordinary differential equation framework, this model implies the following set of equations for the rates of change of each species.

### 7.1 Species [V\\_membrane](#)

**Name** [V\\_membrane](#)

**SBO:0000259** voltage

**Initial amount** -38.34146 mol

**Involved in rule** [V\\_membrane](#)

One rule which determines this species' quantity.

### 7.2 Species [h](#)

**Name** [h](#)

**Initial amount** 0.214723 mol

**Involved in rule** [h](#)

One rule which determines this species' quantity.

### 7.3 Species [d](#)

**Name** [d](#)

**Initial amount** 0.0031711238 mol

**Involved in rule** [d](#)

One rule which determines this species' quantity.

### 7.4 Species [n](#)

**Name** [n](#)

**Initial amount** 0.1836403 mol

**Involved in rule** [n](#)

One rule which determines this species' quantity.

### 7.5 Species [Ca\\_i\\_cytosolic\\_calcium](#)

**Name** [Ca\\_i\\_cytosolic\\_calcium](#)

**Initial amount** 0.6959466 mol

**Involved in rule** [Ca\\_i\\_cytosolic\\_calcium](#)

One rule which determines this species' quantity.

## 7.6 Species `Ca_lum`

**Name** `Ca_lum`

**Initial amount** 102.686 mol

**Involved in rule** `Ca_lum`

One rule which determines this species' quantity.

## A Glossary of Systems Biology Ontology Terms

**SBO:0000002 quantitative systems description parameter:** A numerical value that defines certain characteristics of systems or system functions. It may be part of a calculation, but its value is not determined by the form of the equation itself, and may be arbitrarily assigned

**SBO:0000009 kinetic constant:** Numerical parameter that quantifies the velocity of a chemical reaction

**SBO:0000247 simple chemical:** Simple, non-repetitive chemical entity

**SBO:0000259 voltage:** Difference of electrical potential between two points of an electrical network, expressed in volts

**SBO:0000567 universal gas constant:** A physical constant featured in many fundamental equations in the physical sciences. It is equivalent to the Boltzmann constant, but expressed in units of energy per temperature increment per mole (rather than energy per temperature increment per particle). It has the value 8.314 J.K<sup>-1</sup>.mol<sup>-1</sup> and is denoted by the symbol R

**SBO:0000568 Faraday constant:** Named after Michael Faraday, it is the magnitude of electric charge per mole of electrons. It has the value 96,485.3365 C/mol (Coulombs per Mole), and the symbol F

SBML<sup>2</sup>TeX was developed by Andreas Dräger<sup>a</sup>, Hannes Planatscher<sup>a</sup>, Dieudonné M Wouamba<sup>a</sup>, Adrian Schröder<sup>a</sup>, Michael Hucka<sup>b</sup>, Lukas Endler<sup>c</sup>, Martin Golebiewski<sup>d</sup> and Andreas Zell<sup>a</sup>. Please see <http://www.ra.cs.uni-tuebingen.de/software/SBML2LaTeX> for more information.

<sup>a</sup>Center for Bioinformatics Tübingen (ZBIT), Germany

<sup>b</sup>California Institute of Technology, Beckman Institute BNMC, Pasadena, United States

<sup>c</sup>European Bioinformatics Institute, Wellcome Trust Genome Campus, Hinxton, United Kingdom

<sup>d</sup>EML Research gGmbH, Heidelberg, Germany