# **SBML Model Report**

# Model name: "Heitzler2012\_GPCRsignalling"



May 5, 2016

## 1 General Overview

This is a document in SBML Level 2 Version 4 format. Table 1 gives an overview of the quantities of all components of this model.

Table 1: Number of components in this model, which are described in the following sections.

Element	Quantity	Element	Quantity
compartment types	0	compartments	1
species types	0	species	18
events	0	constraints	0
reactions	26	function definitions	0
global parameters	35	unit definitions	0
rules	0	initial assignments	0

#### **Model Notes**

This model is from the article:

Competing G protein-coupled receptor kinases balance G protein and -arrestin signaling Heitzler D, Durand G, Gallay N, Rizk A, Ahn S, Kim J, Violin JD, Dupuy L, Gauthier C, Piketty V, Crpieux P, Poupon A, Clment F, Fages F, Lefkowitz RJ, Reiter E. Mol Syst Biol. 2012; 8: 590. 22735336,

#### **Abstract:**

Seven-transmembrane receptors (7TMRs) are involved in nearly all aspects of chemical communications and represent major drug targets. 7TMRs transmit their signals not only via heterotrimeric G proteins but also through -arrestins, whose recruitment to the activated receptor

is regulated by G protein-coupled receptor kinases (GRKs). In this paper, we combined experimental approaches with computational modeling to decipher the molecular mechanisms as well as the hidden dynamics governing extracellular signal-regulated kinase (ERK) activation by the angiotensin II type 1A receptor (AT(1A)R) in human embryonic kidney (HEK)293 cells. We built an abstracted ordinary differential equations (ODE)-based model that captured the available knowledge and experimental data. We inferred the unknown parameters by simultaneously fitting experimental data generated in both control and perturbed conditions. We demonstrate that, in addition to its well-established function in the desensitization of G-protein activation, GRK2 exerts a strong negative effect on -arrestin-dependent signaling through its competition with GRK5 and 6 for receptor phosphorylation. Importantly, we experimentally confirmed the validity of this novel GRK2-dependent mechanism in both primary vascular smooth muscle cells naturally expressing the AT(1A)R, and HEK293 cells expressing other 7TMRs.

## 2 Unit Definitions

This is an overview of five unit definitions which are all predefined by SBML and not mentioned in the model.

#### 2.1 Unit substance

**Notes** Mole is the predefined SBML unit for substance.

**Definition** mol

#### 2.2 Unit volume

**Notes** Litre is the predefined SBML unit for volume.

Definition 1

#### 2.3 Unit area

**Notes** Square metre is the predefined SBML unit for area since SBML Level 2 Version 1.

**Definition** m<sup>2</sup>

#### 2.4 Unit length

**Notes** Metre is the predefined SBML unit for length since SBML Level 2 Version 1.

**Definition** m

#### 2.5 Unit time

**Notes** Second is the predefined SBML unit for time.

**Definition** s

# 3 Compartment

This model contains one compartment.

Table 2: Properties of all compartments.

Id	Name	SBO	Spatial Dimensions	Size	Unit	Constant	Outside
compartmentOne			3	1	litre	Ø	

# 3.1 Compartment compartmentOne

This is a three dimensional compartment with a constant size of one litre.

# 4 Species

This model contains 18 species. Section 7 provides further details and the derived rates of change of each species.

Table 3: Properties of each species.

Id	Name	Compartment	Derived Unit	Constant	Boundary Condi- tion
HR	H-R	compartmentOne	$\text{mol} \cdot l^{-1}$		
G	G	compartmentOne	$\text{mol} \cdot l^{-1}$		
ERK	ERK	compartmentOne	$\text{mol} \cdot l^{-1}$		
PIP2	PIP2	compartmentOne	$\text{mol} \cdot l^{-1}$		
DAG	DAG	compartmentOne	$\text{mol} \cdot l^{-1}$		
PKC	PKC	compartmentOne	$\text{mol} \cdot l^{-1}$		
$PKC_a$	PKC_a	compartmentOne	$\text{mol} \cdot l^{-1}$		
GpERK	GpERK	compartmentOne	$\text{mol} \cdot l^{-1}$		
bpERK	bpERK	compartmentOne	$\text{mol} \cdot l^{-1}$		
barr1	barr1	compartmentOne	$\text{mol} \cdot l^{-1}$		
barr2	barr2	compartmentOne	$\text{mol} \cdot l^{-1}$		
$G_a$	G_a	compartmentOne	$\text{mol} \cdot l^{-1}$		
HRP1	H-R~{P1}	compartmentOne	$\text{mol} \cdot l^{-1}$		
Hbarr1RP1	H-barr1-R~{P1}	compartmentOne	$\text{mol} \cdot l^{-1}$		
Hbarr2RP1	H-barr2-R~{P1}	compartmentOne	$\text{mol} \cdot l^{-1}$		
HRP2	H-R~{P2}	compartmentOne	$\text{mol} \cdot l^{-1}$		
HRbarr2	H-R-barr2	compartmentOne	$\text{mol} \cdot l^{-1}$		
Hbarr2RP2	$H$ -barr2- $R^{\sim}\{P2\}$	compartmentOne	$\text{mol} \cdot l^{-1}$		

# **5 Parameters**

This model contains 35 global parameters.

Table 4: Properties of each parameter.

Id	Name	SBO Value	Unit	Constant
k0	k0	3.11 ·	$10^{-4}$	
k1	k1	0.018	- 0	
k2	k2	7.600		
k3	k3	4.630		
k4	k4	0.079		
k5	k5	2.650		
k6	k6	5.099		
k7	k7	0.461		
k8	k8	1.770		
k9	k9	3.040		
k10	k10	2.270		
k11	k11	2.610		
k12	k12	2.590		
k13	k13	0.006		
k14	k14	0.031		$\Box$
k15	k15	6.54 ·	$10^{-5}$	$\Box$
k16	k16	0.072		
k17	k17	0.067		
k18	k18	0.590		
k19	k19	0.205		
k20	k20	1.040		
k21	k21		$10^{-4}$	
k22	k22	14.440		
k23	k23	1.050		
k24	k24	0.347		$\Box$
k25	k25	0.762		
GRK23	GRK23	0.899		$\Box$
GRK56	GRK56	1.518		$\Box$
GRK23_si	GRK23_si	0.479		$\Box$
GRK56_si	GRK56_si	0.001		
PO_Ro	P0_Ro	0.002	_	$\Box$
PO_a_Ro	P0_a_Ro	2.09075206 ·		
barr2_0_si	barr2_0_si	1.12306963 ·	$10^{-4}$	$\Box$
nDAG	nDAG	4.120		
nPKC	nPKC	7.209		

# 6 Reactions

This model contains 26 reactions. All reactions are listed in the following table and are subsequently described in detail. If a reaction is affected by a modifier, the identifier of this species is written above the reaction arrow.

Table 5: Overview of all reactions

Nº	Id	Name	Reaction Equation	SBO
1	$R_{-}1$		$G \xrightarrow{G} G_{-a}$	
2	R_2		$G + HRP1 \xrightarrow{G, HRP1} G_a + HRP1$	
3	R_3		$\mathrm{G} + \mathrm{HR} \xrightarrow{\mathrm{G}, \ \mathrm{HR}} \mathrm{G}_{-}\mathrm{a} + \mathrm{HR}$	
4	$R_{-}4$		$G_a + PIP2 \xrightarrow{G_a, PIP2} DAG + G_a$	
5	$R_{-}5$		$DAG + PKC \xrightarrow{DAG} PKC \longrightarrow DAG + PKC\_a$	
6	$R_{-}6$		$ERK + PKC_{-a} \xrightarrow{ERK, PKC_{-a}} GpERK + PKC_{-a}$	a
7	R_7		$G_{-}a \xrightarrow{G_{-}a} G$	
8	R_8		$DAG \xrightarrow{DAG} PIP2$	
9	$R_{-}9$		$PKC_a \xrightarrow{PKC_a} PKC$	
10	R_10		$GpERK \xrightarrow{GpERK} ERK$	
11	R_11		$HR \xrightarrow{HR} HRP1$	
12	R_12		$barr1 + HRP1 \xrightarrow{barr1, HRP1} Hbarr1RP1$	
13	$R_{-}13$		$Hbarr1RP1 \xrightarrow{Hbarr1RP1} barr1 + HRP1$	
14	R_14		$barr2 + HRP1 \xrightarrow{barr2, HRP1} Hbarr2RP1$	
15	R_15		$Hbarr2RP1 \xrightarrow{Hbarr2RP1} barr2 + HRP1$	
16	$R_{-}16$		$Hbarr1RP1 \xrightarrow{Hbarr1RP1} barr1 + HR$	

No	Id	Name	Reaction Equation	SBO
17	R_17		Hbarr2RP1 Hbarr2RP1 barr2 + HR	
18	R_18		$HR \xrightarrow{HR} HRP2$	
19	R_19		$HRP2 \xrightarrow{HRP2} HR$	
20	R_20		$barr2 + HR \xrightarrow{barr2, HR} HRbarr2$	
21	R_21		$HRbarr2 \xrightarrow{HRbarr2} barr2 + HR$	
22	R_22		$barr2 + HRP2 \xrightarrow{barr2, HRP2} Hbarr2RP2$	
23	R_23		$Hbarr2RP2 \xrightarrow{Hbarr2RP2} barr2 + HRP2$	
24	R_24		$ERK + HRbarr2 \xrightarrow{ERK, HRbarr2} bpERK + HRbarr2$	
25	R_25		ERK + Hbarr2RP2 ERK, Hbarr2RP2 bpERK +	
			Hbarr2RP2	
26	R_26		$bpERK \xrightarrow{bpERK} ERK$	

## 6.1 Reaction R\_1

This is an irreversible reaction of one reactant forming one product influenced by one modifier.

# **Reaction equation**

$$G \xrightarrow{G} G_{-a}$$
 (1)

#### Reactant

Table 6: Properties of each reactant.

Id	Name	SBO
G	G	

#### **Modifier**

Table 7: Properties of each modifier.

Id	Name	SBO
G	G	

#### **Product**

Table 8: Properties of each product.

Id	Name	SBO
G_a	G_a	

## **Kinetic Law**

**Derived unit** contains undeclared units

$$v_1 = \mathbf{k} 0 \cdot [\mathbf{G}] \tag{2}$$

## 6.2 Reaction R\_2

This is an irreversible reaction of two reactants forming two products influenced by two modifiers.

# **Reaction equation**

$$G + HRP1 \xrightarrow{G, HRP1} G_a + HRP1$$
 (3)

#### **Reactants**

Table 9: Properties of each reactant.

Id	Name	SBO
G	G	
HRP1	H-R~{P1}	

#### **Modifiers**

Table 10: Properties of each modifier.

Id	Name	SBO
G	G	
HRP1	H-R~{P1}	

#### **Products**

Table 11: Properties of each product.

Id	Name	SBO
G_a	G_a	
HRP1	H-R~{P1}	

#### **Kinetic Law**

Derived unit contains undeclared units

$$v_2 = k1 \cdot [G] \cdot [HRP1] \tag{4}$$

# 6.3 Reaction R\_3

This is an irreversible reaction of two reactants forming two products influenced by two modifiers.

# **Reaction equation**

$$G + HR \xrightarrow{G, HR} G_{-}a + HR \tag{5}$$

## **Reactants**

Table 12: Properties of each reactant.

Id	Name	SBO
G	G	
HR	H-R	

## **Modifiers**

Table 13: Properties of each modifier.

Id	Name	SBO
G	G	
HR	H-R	

#### **Products**

Table 14: Properties of each product.

Id	Name	SBO
	G₋a H-R	

#### **Kinetic Law**

Derived unit contains undeclared units

$$v_3 = k2 \cdot [G] \cdot [HR] \tag{6}$$

## 6.4 Reaction R\_4

This is an irreversible reaction of two reactants forming two products influenced by two modifiers.

# **Reaction equation**

$$G_a + PIP2 \xrightarrow{G_a, PIP2} DAG + G_a$$
 (7)

Table 15: Properties of each reactant.

Id	Name	SBO
G_a	G_a	
PIP2	PIP2	

Table 16: Properties of each modifier.

Id	Name	SBO
G_a PTP2	G_a PIP2	
F1P2	FIFZ	

## **Products**

Table 17: Properties of each product.

Id	Name	SBO
DAG	DAG	
${\tt G\_a}$	G_a	

#### **Kinetic Law**

**Derived unit** contains undeclared units

$$v_4 = k3 \cdot [G_a] \cdot [PIP2] \tag{8}$$

# 6.5 Reaction R\_5

This is an irreversible reaction of two reactants forming two products influenced by two modifiers.

# **Reaction equation**

$$DAG + PKC \xrightarrow{DAG, PKC} DAG + PKC\_a$$
 (9)

Table 18: Properties of each reactant.

Id	Name	SBO
	DAG	
PKC	PKC	

Table 19: Properties of each modifier.

ame SBO
AG KC

## **Products**

Table 20: Properties of each product.

Id	Name	SBO
DAG	DAG	
$PKC_a$	PKC_a	

#### **Kinetic Law**

**Derived unit** contains undeclared units

$$v_5 = \mathbf{k4} \cdot [\mathsf{DAG}] \cdot [\mathsf{PKC}] \tag{10}$$

# 6.6 Reaction R\_6

This is an irreversible reaction of two reactants forming two products influenced by two modifiers.

# **Reaction equation**

$$ERK + PKC_{-}a \xrightarrow{ERK, PKC_{-}a} GpERK + PKC_{-}a$$
 (11)

Table 21: Properties of each reactant.

Id	Name	SBO
ERK PKC a	ERK PKC a	
$PKC_a$	PKC_a	

Table 22: Properties of each modifier.

Id	Name	SBO
ERK	ERK	
PKC_a	PKC_a	

#### **Products**

Table 23: Properties of each product.

Id	Name	SBO
GpERK PKC_a	GpERK PKC₋a	

# **Kinetic Law**

**Derived unit** contains undeclared units

$$v_6 = k5 \cdot [ERK] \cdot [PKC_a] \tag{12}$$

# **6.7 Reaction R\_7**

This is an irreversible reaction of one reactant forming one product influenced by one modifier.

# **Reaction equation**

$$G_{-a} \xrightarrow{G_{-a}} G \tag{13}$$

Table 24: Properties of each reactant.

Id	Name	SBO
G_a	G_a	

Table 25: Properties of each modifier.

Id	Name	SBO
G_a	G_a	

# **Product**

Table 26: Properties of each product.

Id	Name	SBO
G	G	

## **Kinetic Law**

**Derived unit** contains undeclared units

$$v_7 = \mathbf{k6} \cdot [\mathbf{G}_{-}\mathbf{a}] \tag{14}$$

## 6.8 Reaction R\_8

This is an irreversible reaction of one reactant forming one product influenced by one modifier.

# **Reaction equation**

$$DAG \xrightarrow{DAG} PIP2 \tag{15}$$

Table 27: Properties of each reactant.

Id	Name	SBO
DAG	DAG	

Table 28: Properties of each modifier.

Id	Name	SBO
DAG	DAG	

## **Product**

Table 29: Properties of each product.

Id	Name	SBO
PIP2	PIP2	

## **Kinetic Law**

**Derived unit** contains undeclared units

$$v_8 = k7 \cdot [DAG] \tag{16}$$

# 6.9 Reaction R\_9

This is an irreversible reaction of one reactant forming one product influenced by one modifier.

# **Reaction equation**

$$PKC_{-}a \xrightarrow{PKC_{-}a} PKC \tag{17}$$

#### Reactant

Table 30: Properties of each reactant.

Id	Name	SBO
PKC_a	PKC_a	

## **Modifier**

Table 31: Properties of each modifier.

Id	Name	SBO
PKC a	PKC a	

|--|

## **Product**

Table 32: Properties of each product.

Id	Name	SBO
PKC	PKC	

# **Kinetic Law**

Derived unit contains undeclared units

$$v_9 = k8 \cdot [PKC_-a] \tag{18}$$

# **6.10 Reaction R\_10**

This is an irreversible reaction of one reactant forming one product influenced by one modifier.

# **Reaction equation**

$$GpERK \xrightarrow{GpERK} ERK$$
 (19)

## Reactant

Table 33: Properties of each reactant.

Id	Name	SBO
GpERK	GpERK	

## **Modifier**

Table 34: Properties of each modifier.

Id	Name	SBO
GpERK	GpERK	

# **Product**

Table 35: Properties of each product.

Id	Name	SBO
ERK	ERK	

## **Kinetic Law**

**Derived unit** contains undeclared units

$$v_{10} = k9 \cdot [GpERK] \tag{20}$$

## **6.11 Reaction R\_11**

This is an irreversible reaction of one reactant forming one product influenced by one modifier.

# **Reaction equation**

$$HR \xrightarrow{HR} HRP1$$
 (21)

#### Reactant

Table 36: Properties of each reactant.

Id	Name	SBO
HR	H-R	

#### **Modifier**

Table 37: Properties of each modifier.

Id	Name	SBO
HR	H-R	

# **Product**

Table 38: Properties of each product.

Id	Name	SBO
HRP1	H-R~{P1}	

## **Kinetic Law**

**Derived unit** contains undeclared units

$$v_{11} = k10 \cdot GRK23 \cdot [HR] \tag{22}$$

## **6.12 Reaction R\_12**

This is an irreversible reaction of two reactants forming one product influenced by two modifiers.

# **Reaction equation**

$$barr1 + HRP1 \xrightarrow{barr1, HRP1} Hbarr1RP1$$
 (23)

#### **Reactants**

Table 39: Properties of each reactant.

Id	Name	SBO
barr1	barr1	
HRP1	H-R~{P1}	

#### **Modifiers**

Table 40: Properties of each modifier.

Id	Name	SBO
barr1 HRP1	barr1 H-R~{P1}	

## **Product**

Table 41: Properties of each product.

Id	Name	SBO
Hbarr1RP1	H-barr1-R <sup>~</sup> {P1]	}

#### **Kinetic Law**

Derived unit contains undeclared units

$$v_{12} = k11 \cdot [barr1] \cdot [HRP1] \tag{24}$$

## **6.13 Reaction R\_13**

This is an irreversible reaction of one reactant forming two products influenced by one modifier.

# **Reaction equation**

$$Hbarr1RP1 \xrightarrow{Hbarr1RP1} barr1 + HRP1$$
 (25)

#### Reactant

Table 42: Properties of each reactant.

Id	Name	SBO
Hbarr1RP1	H-barr1-R~{P1}	

#### **Modifier**

Table 43: Properties of each modifier.

Id	Name	SBO
Hbarr1RP1	H-barr1-R~{P1}	

#### **Products**

Table 44: Properties of each product.

Id	Name	SBO
barr1	barr1	
HRP1	H-R~{P1}	

#### **Kinetic Law**

**Derived unit** contains undeclared units

$$v_{13} = k13 \cdot [Hbarr1RP1] \tag{26}$$

#### **6.14 Reaction R\_14**

This is an irreversible reaction of two reactants forming one product influenced by two modifiers.

# **Reaction equation**

$$barr2 + HRP1 \xrightarrow{barr2, HRP1} Hbarr2RP1$$
 (27)

## **Reactants**

Table 45: Properties of each reactant.

Id	Name	SBO
barr2 HRP1	barr2 H-R~{P1}	

#### **Modifiers**

Table 46: Properties of each modifier.

Id	Name	SBO
barr2	barr2	
HRP1	H-R~{P1}	

#### **Product**

Table 47: Properties of each product.

Id	Name	SBO
Hbarr2RP1	H-barr2-R~{P1}	

## **Kinetic Law**

Derived unit contains undeclared units

$$v_{14} = k12 \cdot [barr2] \cdot [HRP1] \tag{28}$$

## 6.15 Reaction R\_15

This is an irreversible reaction of one reactant forming two products influenced by one modifier.

# **Reaction equation**

$$Hbarr2RP1 \xrightarrow{Hbarr2RP1} barr2 + HRP1$$
 (29)

Table 48: Properties of each reactant.

Id	Name	SBO
Hbarr2RP1	H-barr2-R~{P1}	

Table 49: Properties of each modifier.

Id	Name	SBO
Hbarr2RP1	H-barr2-R~{P1}	

## **Products**

Table 50: Properties of each product.

Id	Name	SBO
barr2	barr2	
HRP1	$H-R^{\sim}\{P1\}$	

## **Kinetic Law**

**Derived unit** contains undeclared units

$$v_{15} = k14 \cdot [Hbarr2RP1] \tag{30}$$

## **6.16 Reaction R\_16**

This is an irreversible reaction of one reactant forming two products influenced by one modifier.

# **Reaction equation**

$$Hbarr1RP1 \xrightarrow{Hbarr1RP1} barr1 + HR$$
 (31)

Table 51: Properties of each reactant.

Id	Name	SBO
Hbarr1RP1	H-barr1-R~{P1}	

Table 52: Properties of each modifier.

Zi Z		
Id	Name	SBO
Hbarr1RP1	H-barr1-R~{P1}	

# **Products**

Table 53: Properties of each product.

Id	Name	SBO
barr1	barr1	
HR	H-R	

## **Kinetic Law**

**Derived unit** contains undeclared units

$$v_{16} = k15 \cdot [Hbarr1RP1] \tag{32}$$

## **6.17 Reaction R\_17**

This is an irreversible reaction of one reactant forming two products influenced by one modifier.

# **Reaction equation**

$$Hbarr2RP1 \xrightarrow{Hbarr2RP1} barr2 + HR$$
 (33)

#### Reactant

Table 54: Properties of each reactant.

Id	Name	SBO
Hbarr2RP1	H-barr2-R~{P1}	

## **Modifier**

Table 55: Properties of each modifier.

Tuble 22: Troperties of each modifier:		
Id	Name	SBO
Hbarr2RP1	H-barr2-R~{P1}	

## **Products**

Table 56: Properties of each product.

Id	Name	SBO
barr2	barr2	
HR	H-R	

## **Kinetic Law**

**Derived unit** contains undeclared units

$$v_{17} = k16 \cdot [Hbarr2RP1] \tag{34}$$

# **6.18 Reaction R\_18**

This is an irreversible reaction of one reactant forming one product influenced by one modifier.

# **Reaction equation**

$$HR \xrightarrow{HR} HRP2$$
 (35)

#### Reactant

Table 57: Properties of each reactant.

Id	Name	SBO
HR	H-R	

#### **Modifier**

Table 58: Properties of each modifier.

Id	Name	SBO
HR	H-R	

## **Product**

Table 59: Properties of each product.

Id	Name	SBO
HRP2	H-R~{P2}	

## **Kinetic Law**

**Derived unit** contains undeclared units

$$v_{18} = k18 \cdot GRK56 \cdot [HR] \tag{36}$$

## **6.19 Reaction R\_19**

This is an irreversible reaction of one reactant forming one product influenced by one modifier.

# **Reaction equation**

$$HRP2 \xrightarrow{HRP2} HR \tag{37}$$

## Reactant

Table 60: Properties of each reactant.

Id	Name	SBO
HRP2	H-R~{P2}	

#### **Modifier**

Table 61: Properties of each modifier.

Id	Name	SBO
HRP2	H-R~{P2}	

## **Product**

Table 62: Properties of each product.

Id	Name	SBO
HR	H-R	

Id	Name	SBO

## **Kinetic Law**

**Derived unit** contains undeclared units

$$v_{19} = k17 \cdot [HRP2] \tag{38}$$

# **6.20 Reaction R\_20**

This is an irreversible reaction of two reactants forming one product influenced by two modifiers.

# **Reaction equation**

$$barr2 + HR \xrightarrow{barr2, HR} HRbarr2$$
 (39)

## **Reactants**

Table 63: Properties of each reactant.

Id	Name	SBO
barr2	barr2	
HR	H-R	

#### **Modifiers**

Table 64: Properties of each modifier.

Id	Name	SBO
barr2	barr2	
HR	H-R	

#### **Product**

Table 65: Properties of each product.

Id	Name	SBO
HRbarr2	H-R-barr2	

## **Kinetic Law**

**Derived unit** contains undeclared units

$$v_{20} = k19 \cdot [barr2] \cdot [HR] \tag{40}$$

## **6.21 Reaction R\_21**

This is an irreversible reaction of one reactant forming two products influenced by one modifier.

# **Reaction equation**

$$HRbarr2 \xrightarrow{HRbarr2} barr2 + HR \tag{41}$$

## Reactant

Table 66: Properties of each reactant.

Id	Name	SBO
HRbarr2	H-R-barr2	

#### **Modifier**

Table 67: Properties of each modifier.

Id	Name	SBO
HRbarr2	H-R-barr2	

#### **Products**

Table 68: Properties of each product.

Id	Name	SBO
barr2	barr2	
HR	H-R	

## **Kinetic Law**

Derived unit contains undeclared units

$$v_{21} = k23 \cdot [HRbarr2] \tag{42}$$

## **6.22 Reaction** R\_22

This is an irreversible reaction of two reactants forming one product influenced by two modifiers.

# **Reaction equation**

$$barr2 + HRP2 \xrightarrow{barr2, HRP2} Hbarr2RP2$$
 (43)

#### **Reactants**

Table 69: Properties of each reactant.

Id	Name	SBO
barr2	barr2	
HRP2	H-R~{P2}	

#### **Modifiers**

Table 70: Properties of each modifier.

Id	Name	SBO
barr2		
HRP2	H-R~{P2}	

## **Product**

Table 71: Properties of each product.

	1 1	
Id	Name	SBO
Hbarr2RP2	H-barr2-R~{P2}	

#### **Kinetic Law**

Derived unit contains undeclared units

$$v_{22} = k20 \cdot [barr2] \cdot [HRP2] \tag{44}$$

## **6.23 Reaction R\_23**

This is an irreversible reaction of one reactant forming two products influenced by one modifier.

## **Reaction equation**

$$Hbarr2RP2 \xrightarrow{Hbarr2RP2} barr2 + HRP2$$
 (45)

#### Reactant

Table 72: Properties of each reactant.

Id Name SBO

Hbarr2RP2 H-barr2-R^{P2}

#### **Modifier**

Table 73: Properties of each modifier.

Id	Name	SBO
Hbarr2RP2	H-barr2-R~{P2}	-

#### **Products**

Table 74: Properties of each product.

Id	Name	SBO
barr2		
HRP2	$H-R^{\sim}\{P2\}$	

## **Kinetic Law**

**Derived unit** contains undeclared units

$$v_{23} = k24 \cdot [Hbarr2RP2] \tag{46}$$

# **6.24 Reaction R\_24**

This is an irreversible reaction of two reactants forming two products influenced by two modifiers.

## **Reaction equation**

$$ERK + HRbarr2 \xrightarrow{ERK, HRbarr2} bpERK + HRbarr2$$
 (47)

Table 75: Properties of each reactant.

Id	Name	SBO
ERK	ERK	
HRbarr2	H-R-barr2	

Table 76: Properties of each modifier.

Id	Name	SBO
ERK	ERK	
HRbarr2	H-R-barr2	

#### **Products**

Table 77: Properties of each product.

Id	Name	SBO
bpERK HRbarr2	bpERK H-R-barr2	

# **Kinetic Law**

Derived unit contains undeclared units

$$v_{24} = k21 \cdot [ERK] \cdot [HRbarr2] \tag{48}$$

# **6.25 Reaction R\_25**

This is an irreversible reaction of two reactants forming two products influenced by two modifiers.

# **Reaction equation**

$$ERK + Hbarr2RP2 \xrightarrow{ERK, Hbarr2RP2} bpERK + Hbarr2RP2$$
 (49)

Table 78: Properties of each reactant.

Tueste / el l'imperiore el tuest l'eutenie.		
Id	Name	SBO
ERK Hbarr2RP2	ERK H-barr2-R~{P2}	

Table 79: Properties of each modifier.

Id	Name	SBO
ERK	ERK	
Hbarr2RP2	$H$ -barr2- $R^{\sim}\{P2\}$	

#### **Products**

Table 80: Properties of each product.

Id	Name	SBO
bpERK Hbarr2RP2	bpERK H-barr2-R~{P2}	

#### **Kinetic Law**

Derived unit contains undeclared units

$$v_{25} = k22 \cdot [ERK] \cdot [Hbarr2RP2] \tag{50}$$

# **6.26 Reaction R\_26**

This is an irreversible reaction of one reactant forming one product influenced by one modifier.

# **Reaction equation**

$$bpERK \xrightarrow{bpERK} ERK$$
 (51)

Table 81: Properties of each reactant.

Id	Name	SBO
bpERK	bpERK	

Table 82: Properties of each modifier.

Id	Name	SBO
bpERK	bpERK	

#### **Product**

Table 83: Properties of each product.

Id	Name	SBO
ERK	ERK	

#### **Kinetic Law**

**Derived unit** contains undeclared units

$$v_{26} = k25 \cdot [bpERK] \tag{52}$$

# 7 Derived Rate Equations

When interpreted as an ordinary differential equation framework, this model implies the following set of equations for the rates of change of each species.

Identifiers for kinetic laws highlighted in gray cannot be verified to evaluate to units of SBML substance per time. As a result, some SBML interpreters may not be able to verify the consistency of the units on quantities in the model. Please check if

- parameters without an unit definition are involved or
- volume correction is necessary because the hasOnlySubstanceUnits flag may be set to false and spacialDimensions> 0 for certain species.

# 7.1 Species HR

#### Name H-R

Initial concentration  $0.08 \text{ mol} \cdot l^{-1}$ 

This species takes part in 13 reactions (as a reactant in R\_3, R\_11, R\_18, R\_20 and as a product in R\_3, R\_16, R\_17, R\_19, R\_21 and as a modifier in R\_3, R\_11, R\_18, R\_20).

$$\frac{\mathrm{d}}{\mathrm{d}t} HR = |v_3| + |v_{16}| + |v_{17}| + |v_{19}| + |v_{21}| - |v_3| - |v_{11}| - |v_{18}| - |v_{20}|$$
(53)

# 7.2 Species G

#### Name G

Initial concentration  $56.99 \text{ mol} \cdot l^{-1}$ 

This species takes part in seven reactions (as a reactant in R<sub>-1</sub>, R<sub>-2</sub>, R<sub>-3</sub> and as a product in R<sub>-7</sub> and as a modifier in R<sub>-1</sub>, R<sub>-2</sub>, R<sub>-3</sub>).

$$\frac{d}{dt}G = |v_7| - |v_1| - |v_2| - |v_3| \tag{54}$$

#### 7.3 Species ERK

#### Name ERK

Initial concentration 4.243 mol·l<sup>-1</sup>

This species takes part in eight reactions (as a reactant in R\_6, R\_24, R\_25 and as a product in R\_10, R\_26 and as a modifier in R\_6, R\_24, R\_25).

$$\frac{\mathrm{d}}{\mathrm{d}t} \text{ERK} = |v_{10}| + |v_{26}| - |v_{6}| - |v_{24}| - |v_{25}| \tag{55}$$

## 7.4 Species PIP2

#### Name PIP2

Initial concentration  $0.997 \text{ mol} \cdot l^{-1}$ 

This species takes part in three reactions (as a reactant in R\_4 and as a product in R\_8 and as a modifier in R\_4).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{PIP2} = |v_8| - |v_4| \tag{56}$$

#### 7.5 Species DAG

## Name DAG

Initial concentration  $0.0090 \text{ mol} \cdot l^{-1}$ 

This species takes part in six reactions (as a reactant in R\_5, R\_8 and as a product in R\_4, R\_5 and as a modifier in R\_5, R\_8).

$$\frac{d}{dt}DAG = |v_4| + |v_5| - |v_8|$$
 (57)

## 7.6 Species PKC

#### Name PKC

Initial concentration 8.842 mol·1<sup>-1</sup>

This species takes part in three reactions (as a reactant in R\_5 and as a product in R\_9 and as a modifier in R\_5).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{PKC} = |v_9| - |v_5| \tag{58}$$

## 7.7 Species PKC\_a

#### Name PKC\_a

Initial concentration  $0.0020 \text{ mol} \cdot l^{-1}$ 

This species takes part in six reactions (as a reactant in  $R_6$ ,  $R_9$  and as a product in  $R_5$ ,  $R_6$  and as a modifier in  $R_6$ ,  $R_9$ ).

$$\frac{d}{dt}PKC_{-}a = |v_5| + |v_6| - |v_6| - |v_9|$$
 (59)

## 7.8 Species GpERK

## Name GpERK

Initial concentration  $0.015 \text{ mol} \cdot l^{-1}$ 

This species takes part in three reactions (as a reactant in R\_10 and as a product in R\_6 and as a modifier in R\_10).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{GpERK} = |v_6| - |v_{10}| \tag{60}$$

# 7.9 Species bpERK

# Name bpERK

Initial concentration  $0.015 \text{ mol} \cdot l^{-1}$ 

This species takes part in four reactions (as a reactant in R\_26 and as a product in R\_24, R\_25 and as a modifier in R\_26).

$$\frac{d}{dt}bpERK = |v_{24}| + |v_{25}| - |v_{26}|$$
 (61)

## 7.10 Species barr1

Name barr1

Initial concentration  $0.858 \text{ mol} \cdot l^{-1}$ 

This species takes part in four reactions (as a reactant in R\_12 and as a product in R\_13, R\_16 and as a modifier in R\_12).

$$\frac{d}{dt}barr1 = v_{13} + v_{16} - v_{12}$$
 (62)

## 7.11 Species barr2

Name barr2

Initial concentration  $0.483 \text{ mol} \cdot 1^{-1}$ 

This species takes part in ten reactions (as a reactant in R\_14, R\_20, R\_22 and as a product in R\_15, R\_17, R\_21, R\_23 and as a modifier in R\_14, R\_20, R\_22).

$$\frac{d}{dt}barr2 = |v_{15}| + |v_{17}| + |v_{21}| + |v_{23}| - |v_{14}| - |v_{20}| - |v_{22}|$$
(63)

# 7.12 Species G\_a

Name G\_a

Initial concentration  $0 \text{ mol} \cdot l^{-1}$ 

This species takes part in eight reactions (as a reactant in R\_4, R\_7 and as a product in R\_1, R\_2, R\_3, R\_4 and as a modifier in R\_4, R\_7).

$$\frac{\mathrm{d}}{\mathrm{d}t}G_{-}a = |v_1| + |v_2| + |v_3| + |v_4| - |v_4| - |v_7| \tag{64}$$

## 7.13 Species HRP1

Name H-R<sup>\*</sup>{P1}

Initial concentration  $0 \text{ mol} \cdot l^{-1}$ 

This species takes part in ten reactions (as a reactant in R<sub>2</sub>, R<sub>12</sub>, R<sub>14</sub> and as a product in R<sub>2</sub>, R<sub>11</sub>, R<sub>13</sub>, R<sub>15</sub> and as a modifier in R<sub>2</sub>, R<sub>12</sub>, R<sub>14</sub>).

$$\frac{d}{dt}HRP1 = |v_2| + |v_{11}| + |v_{13}| + |v_{15}| - |v_2| - |v_{12}| - |v_{14}|$$
(65)

## 7.14 Species Hbarr1RP1

Name H-barr1-R<sup>~</sup>{P1}

Initial concentration  $0 \text{ mol} \cdot l^{-1}$ 

This species takes part in five reactions (as a reactant in  $R_13$ ,  $R_16$  and as a product in  $R_12$  and as a modifier in  $R_13$ ,  $R_16$ ).

$$\frac{d}{dt}Hbarr1RP1 = |v_{12}| - |v_{13}| - |v_{16}|$$
 (66)

## 7.15 Species Hbarr2RP1

Name H-barr2-R<sup>~</sup>{P1}

Initial concentration  $0 \text{ mol} \cdot l^{-1}$ 

This species takes part in five reactions (as a reactant in  $R_15$ ,  $R_17$  and as a product in  $R_14$  and as a modifier in  $R_15$ ,  $R_17$ ).

$$\frac{d}{dt}Hbarr2RP1 = v_{14} - v_{15} - v_{17}$$
 (67)

# 7.16 Species HRP2

Name H-R<sup>\*</sup>{P2}

Initial concentration  $0 \text{ mol} \cdot l^{-1}$ 

This species takes part in six reactions (as a reactant in  $R_19$ ,  $R_22$  and as a product in  $R_18$ ,  $R_23$  and as a modifier in  $R_19$ ,  $R_22$ ).

$$\frac{d}{dt}HRP2 = |v_{18}| + |v_{23}| - |v_{19}| - |v_{22}|$$
(68)

## 7.17 Species HRbarr2

Name H-R-barr2

Initial concentration  $0 \text{ mol} \cdot l^{-1}$ 

This species takes part in six reactions (as a reactant in R\_21, R\_24 and as a product in R\_20, R\_24 and as a modifier in R\_21, R\_24).

$$\frac{\mathrm{d}}{\mathrm{d}t} \text{HRbarr2} = |v_{20}| + |v_{24}| - |v_{21}| - |v_{24}| \tag{69}$$

# 7.18 Species Hbarr2RP2

Name H-barr2-R<sup>~</sup>{P2}

Initial concentration  $0 \text{ mol} \cdot l^{-1}$ 

This species takes part in six reactions (as a reactant in  $R_23$ ,  $R_25$  and as a product in  $R_23$ ,  $R_25$  and as a modifier in  $R_23$ ,  $R_25$ ).

$$\frac{d}{dt}Hbarr2RP2 = |v_{22}| + |v_{25}| - |v_{23}| - |v_{25}|$$
 (70)

 $\mathfrak{BML2}^{lAT}$ EX was developed by Andreas Dräger<sup>a</sup>, Hannes Planatscher<sup>a</sup>, Dieudonné M Wouamba<sup>a</sup>, Adrian Schröder<sup>a</sup>, Michael Hucka<sup>b</sup>, Lukas Endler<sup>c</sup>, Martin Golebiewski<sup>d</sup> and Andreas Zell<sup>a</sup>. Please see http://www.ra.cs.uni-tuebingen.de/software/SBML2LaTeX for more information.

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