

## SBML Model Report

# Model name: “Tomida2003 - Calcium Oscillatory-induced translocation of nuclear factor of activated T cells”



May 17, 2018

## 1 General Overview

This is a document in SBML Level 2 Version 4 format. This model was created by Matthew Grant Roberts<sup>1</sup> at February 22<sup>nd</sup> 2018 at 3:25 p. m. and last time modified at March 14<sup>th</sup> 2018 at 9:35 a. m. Table 1 provides an overview of the quantities of all components of this model.

Table 1: Number of components in this model, which are described in the following sections.

Element	Quantity	Element	Quantity
compartment types	0	compartments	1
species types	0	species	4
events	0	constraints	0
reactions	4	function definitions	2
global parameters	11	unit definitions	2
rules	5	initial assignments	2

## Model Notes

Tomida2003 - NFAT functions CalciumOscillation

This model is described in the article:[NFAT functions as a working memory of Ca<sup>2+</sup> signals in decoding Ca<sup>2+</sup> oscillation](#). Tomida T, Hirose K, Takizawa A, Shibasaki F, Iino M. EMBO J. 2003 Aug; 22(15): 3825-3832

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#### Abstract:

Transcription by the nuclear factor of activated T cells (NFAT) is regulated by the frequency of  $\text{Ca}(2+)$  oscillation. However, why and how  $\text{Ca}(2+)$  oscillation regulates NFAT activity remain elusive. NFAT is dephosphorylated by  $\text{Ca}(2+)$ -dependent phosphatase calcineurin and translocates from the cytoplasm to the nucleus to initiate transcription. We analyzed the kinetics of dephosphorylation and translocation of NFAT. We show that  $\text{Ca}(2+)$ -dependent dephosphorylation proceeds rapidly, while the rephosphorylation and nuclear transport of NFAT proceed slowly. Therefore, after brief  $\text{Ca}(2+)$  stimulation, dephosphorylated NFAT has a lifetime of several minutes in the cytoplasm. Thus,  $\text{Ca}(2+)$  oscillation induces a build-up of dephosphorylated NFAT in the cytoplasm, allowing effective nuclear translocation, provided that the oscillation interval is shorter than the lifetime of dephosphorylated NFAT. We also show that  $\text{Ca}(2+)$  oscillation is more cost-effective in inducing the translocation of NFAT than continuous  $\text{Ca}(2+)$  signaling. Thus, the lifetime of dephosphorylated NFAT functions as a working memory of  $\text{Ca}(2+)$  signals and enables the control of NFAT nuclear translocation by the frequency of  $\text{Ca}(2+)$  oscillation at a reduced cost of  $\text{Ca}(2+)$  signaling.

This model is hosted on [BioModels Database](#) and identified by: [BIOMD0000000678](#).

To cite BioModels Database, please use: [Chelliah V et al. BioModels: ten-year anniversary. Nucl. Acids Res. 2015, 43\(Database issue\):D542-8.](#)

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## 2 Unit Definitions

This is an overview of five unit definitions of which three are predefined by SBML and not mentioned in the model.

### 2.1 Unit `volume`

**Name** `volume`

**Definition** `ml`

### 2.2 Unit `substance`

**Name** `substance`

**Definition** `mmol`

### 2.3 Unit `area`

**Notes** Square metre is the predefined SBML unit for area since SBML Level 2 Version 1.

**Definition** `m2`

## 2.4 Unit length

**Notes** Metre is the predefined SBML unit for length since SBML Level 2 Version 1.

**Definition** m

## 2.5 Unit time

**Notes** Second is the predefined SBML unit for time.

**Definition** s

# 3 Compartment

This model contains one compartment.

Table 2: Properties of all compartments.

Id	Name	SBO	Spatial Dimensions	Size	Unit	Constant	Outside
Jurkat_cell	Jurkat cell		3	1	litre	<input checked="" type="checkbox"/>	

## 3.1 Compartment Jurkat\_cell

This is a three dimensional compartment with a constant size of one ml.

**Name** Jurkat cell

## 4 Species

This model contains four species. The boundary condition of two of these species is set to true so that these species' amount cannot be changed by any reaction. Section 10 provides further details and the derived rates of change of each species.

Table 3: Properties of each species.

Id	Name	Compartment	Derived Unit	Constant	Boundary Condition
NFAT- _phosphorylated	NFAT_phosphorylated	Jurkat_cell	$\text{mmol} \cdot \text{ml}^{-1}$	<input type="checkbox"/>	<input type="checkbox"/>
NFAT- _dephosphorylated	NFAT_dephosphorylated	Jurkat_cell	$\text{mmol} \cdot \text{ml}^{-1}$	<input type="checkbox"/>	<input type="checkbox"/>
NFAT_transported	NFAT_transported	Jurkat_cell	$\text{mmol} \cdot \text{ml}^{-1}$	<input type="checkbox"/>	<input checked="" type="checkbox"/>
stimulus	stimulus	Jurkat_cell	$\text{mmol} \cdot \text{ml}^{-1}$	<input type="checkbox"/>	<input checked="" type="checkbox"/>

## 5 Parameters

This model contains eleven global parameters.

Table 4: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
k1	k1		0.359		<input checked="" type="checkbox"/>
k2	k2		0.147		<input checked="" type="checkbox"/>
k3	k3		0.060		<input checked="" type="checkbox"/>
k4	k4		0.035		<input checked="" type="checkbox"/>
stim- _frequency	stim_frequency		3.000		<input checked="" type="checkbox"/>
dNFAT	dNFAT%		0.000		<input type="checkbox"/>
pNFAT	pNFAT%		100.000		<input type="checkbox"/>
tNFAT	tNFAT%		0.000		<input type="checkbox"/>
stim- _duration	stim_duration		1.000		<input checked="" type="checkbox"/>
ModelValue- _17	Initial for stim- _duration		1.000		<input checked="" type="checkbox"/>
ModelValue- _13	Initial for stim- _frequency		3.000		<input checked="" type="checkbox"/>

## 6 Initialassignments

This is an overview of two initialassignments.

### 6.1 Initialassignment [ModelValue\\_17](#)

**Derived unit** contains undeclared units

**Math** stim\_duration

### 6.2 Initialassignment [ModelValue\\_13](#)

**Derived unit** contains undeclared units

**Math** stim\_frequency

## 7 Function definitions

This is an overview of two function definitions.

### 7.1 Function definition `function_for_modified_reaction_1`

**Name** `function_for_modified_reaction_1`

**Arguments** `[NFAT_phosphorylated]`, `k1`, `[stimulus]`

**Mathematical Expression**

$$k1 \cdot [\text{stimulus}] \cdot [\text{NFAT\_phosphorylated}] \quad (1)$$

### 7.2 Function definition `function_for_modified_reaction_0`

**Name** `function_for_modified_reaction`

**Arguments** `k1`, `[stimulus]`, `substrate`

**Mathematical Expression**

$$k1 \cdot [\text{stimulus}] \cdot \text{substrate} \quad (2)$$

## 8 Rules

This is an overview of five rules.

### 8.1 Rule `NFAT_transported`

Rule `NFAT_transported` is an assignment rule for species `NFAT_transported`:

$$\text{NFAT\_transported} = 1 - [\text{NFAT\_phosphorylated}] - [\text{NFAT\_dephosphorylated}] \quad (3)$$

### 8.2 Rule `pNFAT`

Rule `pNFAT` is an assignment rule for parameter `pNFAT`:

$$\text{pNFAT} = 100 \cdot [\text{NFAT\_phosphorylated}] \quad (4)$$

### 8.3 Rule `tNFAT`

Rule `tNFAT` is an assignment rule for parameter `tNFAT`:

$$\text{tNFAT} = 100 \cdot [\text{NFAT\_transported}] \quad (5)$$

### 8.4 Rule `dNFAT`

Rule `dNFAT` is an assignment rule for parameter `dNFAT`:

$$\text{dNFAT} = 100 \cdot [\text{NFAT\_dephosphorylated}] \quad (6)$$

## 8.5 Rule `stimulus`

Rule `stimulus` is an assignment rule for species `stimulus`:

$$\text{stimulus} = \begin{cases} 1 & \text{if } \text{time} - \left\lfloor \frac{\text{time}}{\text{ModelValue\_13}} \right\rfloor \cdot \text{ModelValue\_13} < \text{ModelValue\_17} \\ 0 & \text{otherwise} \end{cases} \quad (7)$$

## 9 Reactions

This model contains four reactions. All reactions are listed in the following table and are subsequently described in detail. If a reaction is affected by a modifier, the identifier of this species is written above the reaction arrow.

Table 5: Overview of all reactions

Nº	Id	Name	Reaction Equation	SBO
1	Dephosphorylation	Dephosphorylation	NFAT_phosphorylated $\xrightarrow{\text{stimulus}}$ NFAT_dephosphorylated	
2	Phosphorylation	Phosphorylation	NFAT_dephosphorylated $\longrightarrow$ NFAT_phosphorylated	
3	Translocation	Translocation	NFAT_dephosphorylated $\longrightarrow$ NFAT_transported	
4	Nuclear_export	Nuclear_export	NFAT_transported $\longrightarrow$ NFAT_phosphorylated	



## 9.1 Reaction Dephosphorylation

This is an irreversible reaction of one reactant forming one product influenced by one modifier.

**Name** Dephosphorylation

### Reaction equation



### Reactant

Table 6: Properties of each reactant.

Id	Name	SBO
NFAT_phosphorylated	NFAT_phosphorylated	

### Modifier

Table 7: Properties of each modifier.

Id	Name	SBO
stimulus	stimulus	

### Product

Table 8: Properties of each product.

Id	Name	SBO
NFAT_dephosphorylated	NFAT_dephosphorylated	

### Kinetic Law

**Derived unit** contains undeclared units

$$v_1 = \text{vol}(\text{Jurkat\_cell}) \cdot \text{function\_for\_modified\_reaction\_1}([\text{NFAT\_phosphorylated}], k_1, [\text{stimulus}]) \quad (9)$$

$$\begin{aligned} &\text{function\_for\_modified\_reaction\_1}([\text{NFAT\_phosphorylated}], k_1, [\text{stimulus}]) \\ &= k_1 \cdot [\text{stimulus}] \cdot [\text{NFAT\_phosphorylated}] \end{aligned} \quad (10)$$

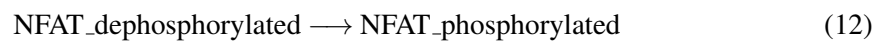
$$\begin{aligned} &\text{function\_for\_modified\_reaction\_1} ([\text{NFAT\_phosphorylated}], k1, [\text{stimulus}]) \\ &= k1 \cdot [\text{stimulus}] \cdot [\text{NFAT\_phosphorylated}] \end{aligned} \quad (11)$$

## 9.2 Reaction Phosphorylation

This is an irreversible reaction of one reactant forming one product.

**Name** Phosphorylation

### Reaction equation



### Reactant

Table 9: Properties of each reactant.

Id	Name	SBO
NFAT_dephosphorylated	NFAT_dephosphorylated	

### Product

Table 10: Properties of each product.

Id	Name	SBO
NFAT_phosphorylated	NFAT_phosphorylated	

### Kinetic Law

**Derived unit** contains undeclared units

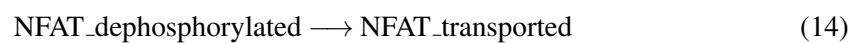
$$v_2 = \text{vol}(\text{Jurkat\_cell}) \cdot k2 \cdot [\text{NFAT\_dephosphorylated}] \quad (13)$$

## 9.3 Reaction Translocation

This is an irreversible reaction of one reactant forming one product.

**Name** Translocation

### Reaction equation



## Reactant

Table 11: Properties of each reactant.

Id	Name	SBO
NFAT_dephosphorylated	NFAT_dephosphorylated	

## Product

Table 12: Properties of each product.

Id	Name	SBO
NFAT_transport	NFAT_transport	

## Kinetic Law

**Derived unit** contains undeclared units

$$v_3 = \text{vol}(\text{Jurkat\_cell}) \cdot k_3 \cdot [\text{NFAT\_dephosphorylated}] \quad (15)$$

### 9.4 Reaction Nuclear\_export

This is an irreversible reaction of one reactant forming one product.

**Name** Nuclear\_export

#### Reaction equation



## Reactant

Table 13: Properties of each reactant.

Id	Name	SBO
NFAT_transport	NFAT_transport	

## Product

Table 14: Properties of each product.

Id	Name	SBO
NFAT_phosphorylated	NFAT_phosphorylated	

## Kinetic Law

**Derived unit** contains undeclared units

$$v_4 = \text{vol}(\text{Jurkat\_cell}) \cdot k_4 \cdot [\text{NFAT\_transported}] \quad (17)$$

## 10 Derived Rate Equations

When interpreted as an ordinary differential equation framework, this model implies the following set of equations for the rates of change of each species.

Identifiers for kinetic laws highlighted in gray cannot be verified to evaluate to units of SBML substance per time. As a result, some SBML interpreters may not be able to verify the consistency of the units on quantities in the model. Please check if

- parameters without an unit definition are involved or
- volume correction is necessary because the `hasOnlySubstanceUnits` flag may be set to `false` and `spacialDimensions` > 0 for certain species.

### 10.1 Species NFAT\_phosphorylated

**Name** NFAT\_phosphorylated

**Initial concentration** 1 mmol · ml<sup>-1</sup>

This species takes part in three reactions (as a reactant in [Dephosphorylation](#) and as a product in [Phosphorylation](#), [Nuclear\\_export](#)).

$$\frac{d}{dt} \text{NFAT\_phosphorylated} = v_2 + v_4 - v_1 \quad (18)$$

### 10.2 Species NFAT\_dephosphorylated

**Name** NFAT\_dephosphorylated

**Initial concentration** 0 mmol · ml<sup>-1</sup>

This species takes part in three reactions (as a reactant in [Phosphorylation](#), [Translocation](#) and as a product in [Dephosphorylation](#)).

$$\frac{d}{dt} \text{NFAT\_dephosphorylated} = v_1 - v_2 - v_3 \quad (19)$$

### 10.3 Species NFAT\_transported

**Name** NFAT\_transported

**Initial concentration** 0 mmol · ml<sup>-1</sup>

**Involved in rule** NFAT\_transported

This species takes part in two reactions (as a reactant in [Nuclear\\_export](#) and as a product in [Translocation](#)). Not these but one rule determines the species' quantity because this species is on the boundary of the reaction system.

### 10.4 Species stimulus

**Name** stimulus

**Initial concentration** 1 mmol · ml<sup>-1</sup>

**Involved in rule** [stimulus](#)

This species takes part in one reaction (as a modifier in [Dephosphorylation](#)). Not this but one rule determines the species' quantity because this species is on the boundary of the reaction system.

SBML2<sup>A</sup>TeX was developed by Andreas Dräger<sup>a</sup>, Hannes Planatscher<sup>a</sup>, Dieudonné M Wouamba<sup>a</sup>, Adrian Schröder<sup>a</sup>, Michael Hucka<sup>b</sup>, Lukas Endler<sup>c</sup>, Martin Golebiewski<sup>d</sup> and Andreas Zell<sup>a</sup>. Please see <http://www.ra.cs.uni-tuebingen.de/software/SBML2LaTeX> for more information.

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