## **SBML Model Report**

# Model name: "Winter2017 - Brain Energy Metabolism with PPP"



March 2, 2017

## 1 General Overview

This is a document in SBML Level 2 Version 3 format. This model was created by Felix Winter<sup>1</sup> at July 30<sup>th</sup> 2013 at 11:50 a. m. and last time modified at October 22<sup>nd</sup> 2014 at 9:29 a. m. Table 1 shows an overview of the quantities of all components of this model.

Table 1: Number of components in this model, which are described in the following sections.

Element	Quantity	Element	Quantity
compartment types	0	compartments	6
species types	0	species	65
events	0	constraints	0
reactions	64	function definitions	20
global parameters	103	unit definitions	2
rules	23	initial assignments	18

#### **Model Notes**

Winter2017 - Brain Energy Metabolism with PPP

This model is described in the article:Mathematical analysis of the influence of brain metabolism on the BOLD signal in Alzheimer's diseaseFelix Winter1,2, Catrin Bludszuweit-Philipp1 and Olaf Wolkenhauer2,3Journal of Cerebral Blood Flow & Metabolism

Abstract:

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Blood oxygen level-dependent functional magnetic resonance imaging (BOLD-fMRI) is a standard clinical tool for the detection of brain activation. In Alzheimers disease (AD), task-related and resting state fMRI have been used to detect brain dysfunction. It has been shown that the shape of the BOLD response is affected in early AD. To correctly interpret these changes, the mechanisms responsible for the observed behaviour need to be known. The parameters of the canonical hemodynamic response function (HRF) commonly used in the analysis of fMRI data have no direct biological interpretation and cannot be used to answer this question. We here present a model that allows relating AD-specific changes in the BOLD shape to changes in the underlying energy metabolism. According to our findings, the classic view that differences in the BOLD shape are only attributed to changes in strength and duration of the stimulus does not hold. Instead, peak height, peak timing and full width at half maximum are sensitive to changes in the reaction rate of several metabolic reactions. Our systems-theoretic approach allows the use of patient-specific clinical data to predict dementia- driven changes in the HRF, which can be used to improve the results of fMRI analyses in AD patients.

This model is hosted on BioModels Database and identified by: BIOMD0000000627.

To cite BioModels Database, please use: BioModels Database: An enhanced, curated and annotated resource for published quantitative kinetic models.

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#### 2 Unit Definitions

This is an overview of five unit definitions of which three are predefined by SBML and not mentioned in the model.

#### 2.1 Unit volume

Name volume

**Definition** ml

#### 2.2 Unit substance

Name substance

**Definition** mmol

#### 2.3 Unit area

**Notes** Square metre is the predefined SBML unit for area since SBML Level 2 Version 1.

**Definition** m<sup>2</sup>

## 2.4 Unit length

**Notes** Metre is the predefined SBML unit for length since SBML Level 2 Version 1.

**Definition** m

#### 2.5 Unit time

**Notes** Second is the predefined SBML unit for time.

**Definition** s

## 3 Compartments

This model contains six compartments.

Table 2: Properties of all compartments.

		•	•				
Id	Name	SBO	Spatial	Size	Unit	Constant	Outside
			Dimensions				
compartment_1	capillary	0000290	3	0.0055	ml	$\checkmark$	
$compartment_2$	neurons	0000290	3	0.45	ml		
$compartment_3$	astrocytes	0000290	3	0.25	ml		
$compartment_4$	extracellular_space	0000290	3	0.2	ml		
${\tt venous\_balloon}$	venous balloon	0000290	3	0.0237	ml		
artery	artery	0000290	3	0.0055	ml		

## 3.1 Compartment compartment\_1

This is a three dimensional compartment with a constant size of 0.0055 ml.

Name capillary

SBO:0000290 physical compartment

## **3.2 Compartment** compartment\_2

This is a three dimensional compartment with a constant size of 0.45 ml.

Name neurons

SBO:0000290 physical compartment

## **3.3 Compartment** compartment\_3

This is a three dimensional compartment with a constant size of 0.25 ml.

Name astrocytes

SBO:0000290 physical compartment

## 3.4 Compartment compartment\_4

This is a three dimensional compartment with a constant size of 0.2 ml.

Name extracellular\_space

SBO:0000290 physical compartment

## 3.5 Compartment venous\_balloon

This is a three dimensional compartment with a not constant size of 0.0237 ml.

Name venous balloon

SBO:0000290 physical compartment

## 3.6 Compartment artery

This is a three dimensional compartment with a constant size of 0.0055 ml.

Name artery

SBO:0000290 physical compartment

# 4 Species

This model contains 65 species. The boundary condition of five of these species is set to true so that these species' amount cannot be changed by any reaction. Section 10 provides further details and the derived rates of change of each species.

Table 3: Properties of each species.

Id	Name	Compartment	Derived Unit	Constant	Boundary
					Condi-
					tion
species_23	O2	${\tt compartment\_1}$	mmol		
species_24	CO2	${\tt compartment\_1}$	mmol		$\Box$
species_25	GLC	${\tt compartment\_1}$	mmol		$\Box$
species_26	LAC	${\tt compartment\_1}$	mmol		$\Box$
dHb	dHb	${\tt compartment\_1}$	mmol		$\Box$
species_1	GLC	${\tt compartment\_2}$	mmol		$\Box$
species_2	G6P	${\tt compartment\_2}$	mmol		$\Box$
species_3	ATP	${\tt compartment\_2}$	mmol		$\Box$
species_7	F6P	${\tt compartment\_2}$	mmol		$\Box$
species_9	GAP	${\tt compartment\_2}$	mmol		$\Box$
species_11	NADH	${\tt compartment\_2}$	mmol		$\Box$
species_12	PEP	${\tt compartment\_2}$	mmol		$\Box$
species_15	PYR	${\tt compartment\_2}$	mmol		
species_18	LAC	${\tt compartment\_2}$	mmol		$\Box$
species_16	O2	${\tt compartment\_2}$	mmol		$\Box$
species_21	PCr	${\tt compartment\_2}$	mmol		$\Box$
$Na\_neurons$	Na+	${\tt compartment\_2}$	mmol		$\Box$
$\operatorname{GLU}$ _neurons	GLU	${\tt compartment\_2}$	mmol		
ADP_neurons	ADP	${\tt compartment\_2}$	mmol		$\Box$
AMP_neurons	AMP	${\tt compartment\_2}$	mmol		$\Box$
$Cr\_neurons$	Cr	compartment_2	mmol		

Id	Name	Compartment	Derived Unit	Constant	Boundary Condi- tion
NAD_neurons	NAD	compartment_2	mmol		$\Box$
$G6L\_neurons$	G6L	${\tt compartment\_2}$	mmol		
P6G_neurons	P6G	${\tt compartment\_2}$	mmol		
$Ru5P_neurons$	Ru5P	${\tt compartment\_2}$	mmol		
X5P_neurons	X5P	${\tt compartment\_2}$	mmol		
$R5P_neurons$	R5P	${\tt compartment\_2}$	mmol		
$S7P\_neurons$	S7P	${\tt compartment\_2}$	mmol		
E4P_neurons	E4P	${\tt compartment\_2}$	mmol		
$\mathtt{NADPH\_neurons}$	NADPH	${\tt compartment\_2}$	mmol		
$\mathtt{NADP\_neurons}$	NADP	${\tt compartment\_2}$	mmol		
species_4	GLC	compartment_3	mmol		
species_5	ATP	compartment_3	mmol		
species_6	G6P	${\tt compartment\_3}$	mmol		
species_8	F6P	${\tt compartment\_3}$	mmol		
species_10	GAP	compartment_3	mmol		
species_13	NADH	compartment_3	mmol		
species_14	PEP	compartment_3	mmol		
species_17	PYR	compartment_3	mmol		
species_19	LAC	compartment_3	mmol		
species_20	O2	${\tt compartment\_3}$	mmol		
species_22	PCr	${\tt compartment\_3}$	mmol		
${\tt Na\_astrocytes}$	Na+	${\tt compartment\_3}$	mmol		
${ t GLU\_astrocytes}$	GLU	${\tt compartment\_3}$	mmol		
ADP_astrocytes	ADP	compartment_3	mmol		
AMP_astrocytes	AMP	compartment_3	mmol		
Cr_astrocytes	Cr	compartment_3	mmol		$\Box$
$\mathtt{NAD}_\mathtt{astrocytes}$	NAD	compartment_3	mmol		

Id	Name	Compartment	Derived Unit	Constant	Boundary Condi- tion
G6L_astrocytes	G6L	compartment_3	mmol		
$P6G_astrocytes$	P6G	${\tt compartment\_3}$	mmol		$\Box$
Ru5P_astrocytes	Ru5P	${\tt compartment\_3}$	mmol	$\Box$	$\Box$
X5P_astrocytes	X5P	${\tt compartment\_3}$	mmol		$\Box$
R5P_astrocytes	R5P	${\tt compartment\_3}$	mmol		$\Box$
S7P_astrocytes	S7P	$compartment_3$	mmol		$\Box$
E4P_astrocytes	E4P	compartment_3	mmol		$\Box$
NADP_astrocytes	NADP	compartment_3	mmol		$\Box$
NADPH_astrocytes	NADPH	compartment_3	mmol		$\Box$
species_27	GLC	compartment_4	mmol		
species_28	LAC	compartment_4	mmol		$\Box$
GLU-	GLU	compartment_4	mmol		
_extracellular- _space					
Na _extracellular- _space	Na+	${\tt compartment\_4}$	mmol	Ø	Z
02_artery	O2	artery	mmol		
CO2_artery	CO2	artery	mmol	$\mathbf{Z}$	$ \mathbf{Z} $
GLC_artery	GLC	artery	mmol	$ \mathbf{Z} $	
$\texttt{LAC}_{-}\texttt{artery}$	LAC	artery	mmol	$\mathbf{Z}$	$ \mathbf{Z} $

# **5 Parameters**

This model contains 103 global parameters.

Table 4: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
parameter_1	K_m_GLC		0.105		Ø
parameter_2	K_m_G6P		0.500		$\overline{Z}$
parameter_3	K_m_F6P_PGI		0.060		$\overline{Z}$
$parameter_4$	K_m_F6P_PFK		0.180		$\square$
$parameter_5$	K_I_ATP		1.000		$\square$
$parameter_6$	nH		4.000		$\square$
parameter_7	NADH_total- _neurons		0.220		$\square$
parameter_8	NADH_total- _astrocytes		0.220		
parameter_9	NAD_neurons		0.204		
parameter_10	NAD_astrocytes		0.162		
parameter_11	ANP		2.379		
parameter_12	$q\_AK$		0.920		$\mathbf{Z}$
parameter_14	K_m_ATP		0.015		$\overline{Z}$
parameter_16	$K_m\_ADP$		0.001		$\overline{Z}$
parameter_17	K_m_O2		0.003		$\overline{Z}$
parameter_18	K_m_PYR		0.063		$\overline{\mathbb{Z}}$
parameter_19	PCr_total		5.000		$\overline{\mathbf{Z}}$
$parameter_20$	Cr_neurons		3.559		
$parameter_21$	Cr_astrocytes		4.623		
parameter_25	Vmax_ATPase- _neurons		0.049		
parameter_26	Vmax_ATPase- _astrocytes		0.036		
parameter_43	Vmax_ec_LAC		0.033		
•	(wrt extracellular space)				•
F_0	F <sub>0</sub>		0.012		Ø
delta_F	delta_F		0.420		
t_0	t_0		200.000		
$t_{ ext{-end}}$	t_end		40.000		$ \mathbf{Z} $
$t_{-}1$	t_1		2.000		$\overline{\mathbf{Z}}$
$F_{-}$ in	F_in		0.012		
$F_{-}$ out	F_out		0.012		
tau_v	tau_v		35.000		
Hb_OP	Hb.OP		8.600		$\mathbf{Z}$

Id	Name	SBO Valu	ue Unit	Constant
Sm_g	Sm_g	1050	0.000	
$Sm_n$	Sm_n	4050	0.000	$\overline{\mathbf{Z}}$
$k_{-}pump$	k_pump		$3.17 \cdot 10^{-7}$	$\overline{\mathscr{Q}}$
$K_m_Na_pump$	K_m,Na-pump		0.424	$\overline{\mathbf{Z}}$
K_m_G6P_GLYS	K_m_G6P_GLYS		0.500	$\overline{\mathbf{Z}}$
$\mathtt{delta\_GLY}$	delta_GLY	6	2.000	$\overline{\mathbf{Z}}$
$K_m_GLY$	$K_m_GLY$		1.000	$\overline{\mathbf{Z}}$
g_Na_neurons	g_Na_neurons		0.004	$\overline{\mathbf{Z}}$
g_Na-	g_Na_astrocytes		0.003	$\overline{\mathbf{Z}}$
_astrocytes				
Vm	Vm	-7	0.000	$\square$
RT	RT	257734	0.000	$\overline{\mathbf{Z}}$
F	F	9650	0.000	$\mathbf{Z}$
vn_1_tp	vn_1		0.041	$\mathbf{Z}$
vn_2_tp	vn_2		1.440	$\mathbf{Z}$
t_stim_tp	t_stim_tp		2.000	<b>Z</b>
is-	is_stimulated		0.000	
_stimulated				_
$v\_\mathtt{stim}$	v_stim		0.000	
R_Na_GLU	R_Na_GLU		0.075	$\overline{\mathscr{L}}$
$V_{eg_max_GLU}$	V_eg_max_GLU		0.021	$\mathbf{Z}$
K_m_GLU	K_m_GLU		0.050	<b>Z</b>
V_gn_max_GLU	V_gn_max_GLU		0.300	$\mathbf{Z}$
delta_HK	delta_HK		0.600	<b>Z</b>
BOLD_signal	BOLD signal		0.000	
E0	E0		0.242	
K_m_ATP-	K_m_ATP(ATPase)		0.001	_ <b>✓</b>
_ATPase	,			
NULL	NULL		0.000	$\square$
Vmax_ne-	Vmax_ne_LAC		0.445	<b>Z</b>
_LACwrt-	(wrt extracellular			
_extracellula	•			
_space	1 /			
PS_cap-	PS_cap_astrocytes	1	1.162	
_astrocytes-	(wrt capillaries)			
wrt-	( 1 /			
_capillaries				
PS_cap-	PS_cap_neuron	1	8.016	Ø
_neuronwrt-	(wrt capillaries)	-	-	
_capillaries				

Id	Name	SBO Value	Unit	Constant
Vmax_eg- _GLUwrt-	Vmax_eg_GLU (wrt extracellular	0.026		Ø
$_{ extsf{c}}$ extracellular	r-space)			
_space				_
$K_T_GLC_ce$	K_T_GLC_ce	9.000		
_Aubert	(Aubert)			
Vmax_ce-	Vmax_ce_GLC	4.291		
_GLCwrt-	(wrt capillaries)			
_capillaries- Aubert	(Aubert)			
$Vmax_eg-$	Vmax_eg_GLC	1275.000		$\Box$
_GLCwrt-	(wrt astrocytes)			
_astrocytes Aubert_	(Aubert)			
K_T_GLC_eg	K_T_GLC_eg	9.000		$   \overline{\mathbf{Z}} $
$_{ extsf{ iny Aubert}}$	(Aubert)			
$K_T_GLC_en$	K_T_GLC_en	9.000		
$_{ extsf{ iny Aubert}}$	(Aubert)			
$Vmax_en_GLC$	Vmax_en_GLC	11767.500		
_wrt_neurons-	(wrt neurons)			
Aubert	(Aubert)			
$K_T_GLC_cg$	K_T_GLC_cg	9.000		
$\_\mathtt{Aubert}$	(Aubert)			
$Vmax\_cg-$	Vmax_cg_GLC	0.423		$\Box$
_GLCwrt-	(wrt capillaries)			
$\_$ capillaries-	(Aubert)			
Aubert				
Vmax_ec-	Vmax_ec_LAC	0.006		$\Box$
_LACwrt-	(wrt extracellular			
$_{ extsf{-}}$ extracellular	r-space) (Aubert)			
_space				
$_{ extsf{ iny Aubert}}$				
$Vmax\_gc-$	Vmax_gc_LAC	0.004		$\Box$
_LACwrt-	(wrt astrocytes)			
_astrocytes	(Aubert)			
$\_\_\mathtt{Aubert}$				
Vmax_ge-	Vmax_ge_LAC	0.057		
_LACwrt-	(wrt astrocytes)			
_astrocytes	(Aubert)			
$\_\_\mathtt{Aubert}$				

Id	Name	SBO Value	Unit	Constant
Vmax_ne_LAC	Vmax_ne_LAC	0.218		
_wrt_neurons-	(wrt neurons)			
$\_\_$ Aubert	(Aubert)			
$K_T_LAC_ne$	K_T_LAC_ne	0.500		
_Aubert	(Aubert)			
K_T_LAC_ge	K_T_LAC_ge	0.500		
_Aubert	(Aubert)			
$K_T_LAC_gc$	K_T_LAC_gc	0.500		
_Aubert	(Aubert)			
$K_T_LAC_ec$	K_T_LAC_ec	0.500		
$\_\mathtt{Aubert}$	(Aubert)			
PS_cap-	PS_cap_astrocytes	4.705		$\Box$
_astrocytes-	(wrt capillaries)			
wrt-	(Aubert)			
$\_$ capillaries $ extsf{-}$				
$\_\_$ Aubert				
PS_cap-	PS_cap_neuron	40.500		$\Box$
_neuronwrt-	(wrt capillaries)			
$\_$ capillaries-	(Aubert)			
Aubert				
K_O2Aubert	K_O2 (Aubert)	0.036		
nh_02Aubert	nh_O2 (Aubert)	2.730		
$Vmax_f_PGI$	Vmax_f_PGI	0.500		
$_{ extsf{ iny Cloutier}}$	(Cloutier)			
$Vmax_r_PGI$	Vmax_r_PGI	0.450		
$_{ t C}$ loutier	(Cloutier)			
Vmax_ce_GLC	Vmax_ce_GLC	0.118		
$\_\mathtt{Aubert}$	(Aubert)			
${\tt Vmax\_cg\_GLC\}$	Vmax_cg_GLC	0.009		
$\_\_\mathtt{Aubert}$	(Aubert)			
${\tt Vmax\_eg\_GLC\}$	Vmax_eg_GLC	1020.000		
$\_\texttt{Aubert}_{\_}$	(Aubert)			
Vmax_en_GLC	Vmax_en_GLC	5230.000		
$\_\_\mathtt{Aubert}$	(Aubert)			
_sf	sf	0.750		
_PScap	_PScap	1.100		
${\tt f\_CBF\_dyn}$	f_CBF_dyn	1.000		
stimulus	stimulus	-3.87088868421524		
Metabolite-	Initial for O2	8.340		
_123				
${\tt Metabolite\_1}$	Initial for O2	7.332		
Metabolite_9	Initial for dHb	0.048		

Id	Name	SBO	Value	Unit	Constant
Compartment-	Initial for venous balloon		0.024		Ø
ModelValue- _54	Initial for E0		0.242		
ModelValue_7	Initial for NADH- _total_astrocytes		0.220		
ModelValue_6	Initial for NADH- _total_neurons		0.220		
ModelValue- _16	Initial for PCr_total		5.000		
ModelValue- _83	Initial for Vmax- _ce_GLC (Aubert)		0.118		
ModelValue- _84	Initial for Vmax- _cg_GLC (Aubert)		0.009		
ModelValue- _86	Initial for Vmax- _en_GLC (Aubert)		5230.000		
ModelValue- _43	Initial for vn <sub>−</sub> 1		0.041		

## 6 Initialassignments

This is an overview of 18 initial assignments.

## **6.1 Initialassignment AMP\_neurons**

**Derived unit** contains undeclared units

$$\textbf{Math} \ \left( parameter\_11 - \frac{ADP\_neurons}{vol(compartment\_2)} - \frac{species\_3}{vol(compartment\_2)} \right) \cdot vol\left(compartment\_2\right)$$

## 6.2 Initialassignment Cr\_neurons

Derived unit contains undeclared units

$$\textbf{Math} \ \left( parameter\_19 - \tfrac{species\_21}{vol(compartment\_2)} \right) \cdot vol\left( compartment\_2 \right)$$

## 6.3 Initialassignment NAD\_neurons

Derived unit contains undeclared units

$$\textbf{Math} \ \left( parameter\_7 - \frac{species\_11}{vol(compartment\_2)} \right) \cdot vol\left( compartment\_2 \right)$$

## **6.4 Initialassignment AMP\_astrocytes**

**Derived unit** contains undeclared units

$$\textbf{Math} \ \left( parameter\_11 - \frac{ADP\_astrocytes}{vol(compartment\_3)} - \frac{species\_5}{vol(compartment\_3)} \right) \cdot vol\left(compartment\_3\right)$$

## **6.5 Initialassignment** Cr\_astrocytes

Derived unit contains undeclared units

$$\textbf{Math} \ \left( parameter\_19 - \frac{species\_22}{vol(compartment\_3)} \right) \cdot vol\left( compartment\_3 \right)$$

## **6.6 Initialassignment NAD\_astrocytes**

Derived unit contains undeclared units

$$\textbf{Math} \ \left( parameter\_8 - \frac{species\_13}{vol(compartment\_3)} \right) \cdot vol\left( compartment\_3 \right)$$

## 6.7 Initialassignment Metabolite\_123

Derived unit mmol

Math O2\_artery

#### 6.8 Initialassignment Metabolite\_1

**Derived unit** mmol

Math species\_23

#### **6.9 Initialassignment Metabolite\_9**

**Derived unit** mmol

Math dHb

#### **6.10 Initialassignment** Compartment\_9

Derived unit ml

Math vol(venous\_balloon)

#### 6.11 Initialassignment ModelValue\_54

**Derived unit** contains undeclared units

Math E0

### **6.12 Initialassignment ModelValue\_7**

**Derived unit** contains undeclared units

Math parameter\_8

## 6.13 Initialassignment ModelValue\_6

Derived unit contains undeclared units

**Math** parameter\_7

#### **6.14 Initialassignment ModelValue\_16**

**Derived unit** contains undeclared units

Math parameter\_19

## 6.15 Initialassignment ModelValue\_83

**Derived unit** contains undeclared units

Math Vmax\_ce\_GLC\_\_Aubert

## **6.16 Initialassignment ModelValue\_84**

Derived unit contains undeclared units

**Math** Vmax\_cg\_GLC\_\_\_Aubert

## **6.17 Initialassignment ModelValue\_86**

**Derived unit** contains undeclared units

Math Vmax\_en\_GLC\_\_\_Aubert

#### **6.18 Initialassignment ModelValue\_43**

**Derived unit** contains undeclared units

Math  $vn_1tp$ 

## 7 Function definitions

This is an overview of 20 function definitions.

#### 7.1 Function definition vdHb\_in

Name vdHb\_in [1]

Arguments F\_in, O2\_a, O2\_c

**Mathematical Expression** 

$$F_{in} \cdot (O2_a - 2 \cdot O2_c - O2_a)$$
 (1)

#### 7.2 Function definition vdHb\_out

Name vdHb\_out

Arguments  $F_{-}out$ , dHb,  $V_{-}v$ 

**Mathematical Expression** 

$$\frac{F\_out \cdot dHb}{V\_v} \tag{2}$$

#### 7.3 Function definition vATPase

Name vATPase

Arguments VmaxATPase, ATP, Km\_ATP

**Mathematical Expression** 

$$VmaxATPase \cdot \frac{ATP}{ATP + Km\_ATP}$$
 (3)

#### 7.4 Function definition vPK

Name vPK

Arguments k\_PK, PEP, ADP

**Mathematical Expression** 

$$k_{-}PK \cdot PEP \cdot ADP$$
 (4)

## 7.5 Function definition vPGK

Name vPGK

Arguments k\_PGK, GAP, ADP, NAD, NADH

$$k\_PGK \cdot GAP \cdot ADP \cdot \frac{NAD}{NADH} \tag{5}$$

#### 7.6 Function definition vPFK

Name vPFK

Arguments k\_PFK, ATP, K\_I\_ATP, nH, F6P, K\_m\_F6P

#### **Mathematical Expression**

$$k\_PFK \cdot ATP \cdot \left(1 + \left(\frac{ATP}{K\_I\_ATP}\right)^{nH}\right)^{1} \cdot \frac{F6P}{F6P + K\_m\_F6P}$$
 (6)

## 7.7 Function definition facilitated\_transport\_\_inkl\_\_Volume

Name facilitated transport (inkl. Volume)

Arguments Vmax, S, K, P, Volume

#### **Mathematical Expression**

$$Vmax \cdot \left(\frac{S}{S+K} - \frac{P}{P+K}\right) \cdot Volume \tag{7}$$

#### 7.8 Function definition vGLU\_eg\_\_inkl\_\_Volumes

Name vGLU\_eg (inkl. Volumes)

Arguments Vmax\_GLU, GLU\_e, K\_m\_GLU, Volume

#### **Mathematical Expression**

$$Vmax\_GLU \cdot \frac{GLU\_e}{GLU\_e + K\_m\_GLU} \cdot Volume \tag{8}$$

#### 7.9 Function definition vGLU\_gn\_\_inkl\_\_Volume

Name vGLU\_gn (inkl. Volume)

Arguments Vmax\_GLU, GLU\_g, K\_m\_GLU, ATP\_g, K\_m\_ATP, Volume

$$Vmax\_GLU \cdot \frac{GLU\_g}{GLU\_g + K\_m\_GLU} \cdot \frac{ATP\_g}{ATP\_g + K\_m\_ATP} \cdot Volume \qquad (9)$$

#### 7.10 Function definition vGLU\_ne\_inkl\_\_Volume

Name vGLU\_ne (inkl. Volume)

Arguments vSTIM, ratio\_Na\_GLU, GLU\_n, Km\_GLU, Volume

#### **Mathematical Expression**

$$vSTIM \cdot ratio\_Na\_GLU \cdot \frac{GLU\_n}{GLU\_n + Km\_GLU} \cdot Volume \tag{10}$$

#### 7.11 Function definition vStim\_with\_volume

Name vStim (with volume)

Arguments vstim, Volume

#### **Mathematical Expression**

vstim · Volume 
$$(11)$$

#### 7.12 Function definition

modular\_rate\_law\_for\_two\_substrates\_\_two\_products

Name modular rate law for two substrates, two products

**Arguments** Vmax, K\_S1, K\_S2, S1, S2, P1, P2, Keq, K\_P1, K\_P2

#### **Mathematical Expression**

$$Vmax \cdot \frac{1}{K\_S1 \cdot K\_S2} \cdot \frac{S1 \cdot S2 - \frac{P1 \cdot P2}{Keq}}{\left(1 + \frac{S1}{K\_S1}\right) \cdot \left(1 + \frac{S2}{K\_S2}\right) + \left(1 + \frac{P1}{K\_P1}\right) \cdot \left(1 + \frac{P2}{K\_P2}\right) - 1} (12)$$

## 7.13 Function definition modular\_rate\_law\_for\_one\_substrate\_one\_product

Name modular rate law for one substrate, one product

Arguments Vmax, K\_S1, S1, P1, Keq, K\_P1

$$V_{\text{max}} \cdot \frac{1}{K_{-}S1} \cdot \frac{S1 - \frac{P1}{Keq}}{1 + \frac{S1}{K_{-}S1} + 1 + \frac{P1}{K_{-}P1} - 1}$$
 (13)

#### 7.14 Function definition Blood\_flow\_contribution\_inkl\_\_volume

Name Blood flow contribution inkl. volume

Arguments F\_in, V\_c, Volume, Substrate, Product

#### **Mathematical Expression**

$$\frac{2 \cdot F_{in}}{V_{c}} \cdot (Substrate - Product) \cdot Volume$$
 (14)

#### 7.15 Function definition 02\_transport\_function\_inkl\_\_volume

Name O2 transport function inkl. volume

Arguments PScap, Volume, KO2, HbOP, O2\_source, nh, O2\_destination, Volume1

#### **Mathematical Expression**

$$\frac{\text{PScap}}{\text{Volume}} \cdot \left( \text{KO2} \cdot \left( \frac{\text{HbOP}}{\text{O2\_source}} - 1 \right)^{\frac{1}{\text{nh}}} - \text{O2\_destination} \right) \cdot \text{Volume1} \quad (15)$$

#### 7.16 Function definition vLEAK\_Na\_inkl\_\_Volume

Name vLEAK\_Na inkl. Volume

Arguments Sm, gNA, Volume, F, RT, Na\_e, Na, Vm, Volume1

## **Mathematical Expression**

$$\frac{Sm \cdot gNA}{Volume \cdot F} \cdot \left(\frac{RT}{F} \cdot \left(\frac{Na\_e}{Na}\right) - Vm\right) \cdot Volume1 \tag{16}$$

#### 7.17 Function definition vPUMP\_volume\_dependent

Name vPUMP volume dependent

**Arguments** Sm, Volume, k\_pump, ATP, Na, Km\_pump

$$\frac{Sm}{Volume} \cdot k\_pump \cdot ATP \cdot Na \cdot \left(1 + \frac{ATP}{Km\_pump}\right)^{l}$$
 (17)

#### 7.18 Function definition vHK\_HS

Name vHK (HS)

Arguments k\_HK, ATP, G6P, K\_I\_G6P

#### **Mathematical Expression**

$$k\_HK \cdot ATP \cdot \left(1 + \frac{G6P}{K\_I\_G6P}\right)^{1}$$
 (18)

#### 7.19 Function definition facilitated\_transport\_inkl\_\_Volume\_\_\_scaled

Name facilitated transport (inkl. Volume) (scaled)

Arguments Vmax, sf, S, K, P, Volume

#### **Mathematical Expression**

$$Vmax \cdot sf \cdot \left(\frac{S}{S+K} - \frac{P}{P+K}\right) \cdot Volume \tag{19}$$

#### 7.20 Function definition vMITO2\_inkl\_\_Volumes

Name vMITO2 (inkl. Volumes)

**Arguments** v\_max\_mito, PYR, K\_m\_PYR, ADP, K\_m\_ADP, O2, K\_m\_O2, alpha, ATP, beta, Volume

#### **Mathematical Expression**

$$\begin{array}{l} v\_max\_mito \cdot \frac{PYR}{PYR + K\_m\_PYR} \cdot \frac{ADP}{ADP + K\_m\_ADP} \\ \cdot \frac{O2}{O2 + K\_m\_O2} \cdot \left(1 - \frac{1}{1 + exp\left(alpha \cdot \left(\frac{ATP}{ADP} - beta\right)\right)}\right) \cdot Volume \end{array} \tag{20}$$

#### 8 Rules

This is an overview of 23 rules.

#### **8.1 Rule** E0

Rule E0 is an assignment rule for parameter E0:

$$E0 = 1 - \frac{2 \cdot Metabolite\_1 - Metabolite\_123}{\frac{O2\_artery}{vol(artery)}}$$
(21)

### 8.2 Rule BOLD\_signal

Rule BOLD\_signal is an assignment rule for parameter BOLD\_signal:

$$BOLD\_signal = Compartment\_9 \cdot 7 \cdot \left(1 - \frac{\frac{dHb}{vol(compartment\_1)}}{Metabolite\_9}\right) + 2 \cdot \frac{1 - \frac{\frac{dHb}{vol(compartment\_1)}}{Metabolite\_9}}{\frac{vol(venous\_balloon)}{Compartment\_9}} + (2 \cdot ModelValue\_54 - 0.2) \cdot \left(1 - \frac{vol(venous\_balloon)}{Compartment\_9}\right)$$
 (22)

### 8.3 Rule Vmax\_ce\_GLC\_\_wrt\_capillaries\_\_\_Aubert

Rule Vmax\_ce\_GLC\_wrt\_capillaries\_\_Aubert is an assignment rule for parameter Vmax\_ce\_GLC\_wrt\_capillaries\_\_Aubert:

$$Vmax\_ce\_GLC\_wrt\_capillaries\_\_Aubert = ModelValue\_83 \cdot \frac{vol(compartment\_4)}{vol(compartment\_1)}$$
 (23)

#### 8.4 Rule Vmax\_eg\_GLC\_\_wrt\_astrocytes\_\_\_Aubert\_

Rule Vmax\_eg\_GLC\_wrt\_astrocytes\_\_Aubert\_ is an assignment rule for parameter Vmax\_eg\_GLC\_wrt\_astrocytes\_\_Aubert\_:

$$Vmax\_eg\_GLC\_wrt\_astrocytes\_\_Aubert\_ = Vmax\_eg\_GLC\_Aubert\_ \cdot \frac{vol \, (compartment\_3)}{vol \, (compartment\_4)}$$
 (24)

#### 8.5 Rule Vmax\_en\_GLC\_wrt\_neurons\_\_Aubert

Rule Vmax\_en\_GLC\_\_wrt\_neurons\_\_\_Aubert is an assignment rule for parameter Vmax\_en\_GLC\_\_wrt\_neurons\_\_\_Aubert:

$$Vmax\_en\_GLC\_wrt\_neurons\_\_Aubert = ModelValue\_86 \cdot \frac{vol(compartment\_2)}{vol(compartment\_4)}$$
(25)

#### 8.6 Rule Vmax\_cg\_GLC\_\_wrt\_capillaries\_\_\_Aubert

Rule Vmax\_cg\_GLC\_wrt\_capillaries\_\_\_Aubert is an assignment rule for parameter Vmax\_cg\_GLC\_wrt\_capillaries\_\_\_Aubert:

$$Vmax\_cg\_GLC\_wrt\_capillaries\_\_Aubert = ModelValue\_84 \cdot \frac{vol(compartment\_3)}{vol(compartment\_1)}$$
 (26)

#### 8.7 Rule Vmax\_ec\_LAC\_\_wrt\_extracellular\_space\_\_\_Aubert

Rule Vmax\_ec\_LAC\_wrt\_extracellular\_space\_\_\_Aubert is an assignment rule for parameter Vmax\_ec\_LAC\_wrt\_extracellular\_space\_\_\_Aubert:

$$Vmax\_ec\_LAC\_wrt\_extracellular\_space\_\_Aubert = 0.00783 \cdot \_sf$$
 (27)

#### 8.8 Rule Vmax\_gc\_LAC\_\_wrt\_astrocytes\_\_\_Aubert

Rule Vmax\_gc\_LAC\_wrt\_astrocytes\_\_\_Aubert is an assignment rule for parameter Vmax\_gc-\_LAC\_wrt\_astrocytes\_\_\_Aubert:

$$V_{max\_gc\_LAC\_wrt\_astrocytes\_\_Aubert} = 0.0058 \cdot \_sf$$
 (28)

#### 8.9 Rule Vmax\_ge\_LAC\_wrt\_astrocytes\_\_Aubert

Rule Vmax\_ge\_LAC\_wrt\_astrocytes\_\_\_Aubert is an assignment rule for parameter Vmax\_ge\_ \_LAC\_wrt\_astrocytes\_\_\_Aubert:

$$Vmax\_ge\_LAC\_wrt\_astrocytes\_\_Aubert = 0.076 \cdot \_sf$$
 (29)

#### 8.10 Rule Vmax\_ne\_LAC\_\_wrt\_neurons\_\_Aubert

Rule Vmax\_ne\_LAC\_\_wrt\_neurons\_\_\_Aubert is an assignment rule for parameter Vmax\_ne\_ \_LAC\_\_wrt\_neurons\_\_\_Aubert:

$$Vmax\_ne\_LAC\_wrt\_neurons\_\_Aubert = 0.29 \cdot \_sf$$
 (30)

#### **8.11 Rule PS\_cap\_astrocytes\_wrt\_capillaries\_\_Aubert**

Rule PS\_cap\_astrocytes\_\_wrt\_capillaries\_\_\_Aubert is an assignment rule for parameter PS\_cap\_astrocytes\_\_wrt\_capillaries\_\_\_Aubert:

PS\_cap\_astrocytes\_wrt\_capillaries\_\_Aubert = 
$$0.414 \cdot 0.25 \cdot \frac{\text{vol (compartment\_3)}}{\text{vol (compartment\_1)}}$$
 (31)

## 8.12 Rule PS\_cap\_neuron\_wrt\_capillaries\_\_Aubert

Rule PS\_cap\_neuron\_\_wrt\_capillaries\_\_\_Aubert is an assignment rule for parameter PS\_cap\_neuron\_\_wrt\_capillaries\_\_\_Aubert:

$$PS\_cap\_neuron\_wrt\_capillaries\_\_Aubert = \_PScap \cdot 0.45 \cdot \frac{vol (compartment\_2)}{vol (compartment\_1)}$$
 (32)

## 8.13 Rule f\_CBF\_dyn

Rule f\_CBF\_dyn is an assignment rule for parameter f\_CBF\_dyn:

$$f\_CBF\_dyn = 1 + delta\_F \cdot \left(\frac{1}{1 + exp(4.59186 \cdot (time - t\_0 + t\_1 - 3))} - \frac{1}{1 + exp(4.59186 \cdot (time - (t\_0 + t\_1 + t\_end + 3))))}\right)$$
(33)

#### 8.14 Rule stimulus

Rule stimulus is an assignment rule for parameter stimulus:

$$stimulus = ModelValue\_43 + vn\_2\_tp \cdot \frac{time - t\_0}{t\_stim\_tp} \cdot exp\left(\frac{(time - t\_0)}{t\_stim\_tp}\right) \tag{34}$$

#### 8.15 Rule parameter\_9

Rule parameter\_9 is an assignment rule for parameter parameter\_9:

$$parameter\_9 = ModelValue\_6 - \frac{species\_11}{vol(compartment\_2)}$$
 (35)

#### 8.16 Rule parameter\_10

Rule parameter\_10 is an assignment rule for parameter parameter\_10:

$$parameter_10 = ModelValue_7 - \frac{species_13}{vol(compartment_3)}$$
 (36)

## 8.17 Rule parameter\_20

Rule parameter\_20 is an assignment rule for parameter parameter\_20:

$$parameter_20 = ModelValue_16 - \frac{species_21}{vol(compartment_2)}$$
 (37)

#### 8.18 Rule parameter\_21

Rule parameter\_21 is an assignment rule for parameter parameter\_21:

$$parameter_21 = ModelValue_16 - \frac{species_22}{vol(compartment_3)}$$
 (38)

#### 8.19 Rule F\_in

Rule F\_in is an assignment rule for parameter F\_in:

$$F_{in} = F_{0} \cdot f_{CBF_{in}}$$
(39)

## 8.20 Rule F\_out

Rule F\_out is an assignment rule for parameter F\_out:

$$F\_out = F\_0 \cdot \frac{\left(\frac{vol(venous\_balloon)}{Compartment\_9}\right)^{\frac{1}{0.5}} + \left(\frac{vol(venous\_balloon)}{Compartment\_9}\right)^{\frac{1}{2}} \cdot \frac{tau\_v}{Compartment\_9} \cdot F\_in}{1 + F\_0 \cdot \left(\frac{vol(venous\_balloon)}{Compartment\_9}\right)^{\frac{1}{2}} \cdot \frac{tau\_v}{Compartment\_9}}$$
(40)

## 8.21 Rule is\_stimulated

Rule  $is\_stimulated$  is an assignment rule for parameter  $is\_stimulated$ :

$$is\_stimulated = \begin{cases} 0 & if \ (time \le 200) \lor (time \ge t\_0 + t\_end) \\ 1 & otherwise \end{cases} \tag{41}$$

## 8.22 Rule v\_stim

Rule v\_stim is an assignment rule for parameter v\_stim:

$$v_stim = is_stimulated \cdot stimulus$$
 (42)

#### 8.23 Rule venous\_balloon

Rule venous\_balloon is a rate rule for compartment venous\_balloon:

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{vol}\left(\mathrm{venous\_balloon}\right) = \mathrm{F\_in} - \mathrm{F\_out} \tag{43}$$

# 9 Reactions

This model contains 64 reactions. All reactions are listed in the following table and are subsequently described in detail. If a reaction is affected by a modifier, the identifier of this species is written above the reaction arrow.

Table 5: Overview of all reactions

Nº	Id	Name	Reaction Equation	SBO
1	reaction_2	HK_astrocytes (R01786) (HeinrichSchuster)	species_5 + species_4 $\xrightarrow{\text{species}\_6}$ species_6 + ADP_astrocytes	0000176
2	reaction_5	PFK_neurons (R04779, R01070, R01015)	species_7 + species_3 $\longrightarrow$ 2 species_9 + ADP_neurons	0000395
3	reaction_6	PFK_astrocytes (R04779, R01070, R01015)	species_8 + species_5 $\longrightarrow$ 2 species_10 + ADP_astrocytes	0000395
4	reaction_7	PGK_neurons (R01061, R01512, R01518, R00658)	species_9 + ADP_neurons + NAD_neurons	0000395
5	reaction_8	PGK_astrocytes (R01061, R01512, R01518, R00658)	species_10 + ADP_astrocytes + NAD_astrocytes → species_13 + species_14 + species_5	0000395
6	reaction_9	PK_neurons (R00200)	species_12 + ADP_neurons → species_3 + species_15	0000176
7	reaction_10	PK_astrocytes (R00200)	species_14 + ADP_astrocytes → species_5 + species_17	0000176
8	reaction_13	mitochondrial_respiration_neurons (n.a.)	species_15 + 3 species_16 + species_11 + 15 ADP_neurons → 15 species_3 + 3 species_24 + NAD_neurons	0000395
9	reaction_14	mitochondrial_respiration_astrocytes (n.a.)	species_17 + 15 ADP_astrocytes + 3 species_20 + species_13 → 15 species_5 + 3 species_24 + NAD_astrocytes	0000395

Nº	Id	Name	Reaction Equation	SBO
10	reaction_17	GLC_exchange_extracellular_space_neurons (Aubert)	species_27 → species_1	0000185
11	reaction_18	GLC_exchange_extracellular_space- _astrocytes (Aubert)	species_27 → species_4	0000185
12	$reaction_19$	GLC_exchange_capillary_ec (Aubert)	species_25 → species_27	0000185
13	reaction_20	GLC_exchange_capillary_astrocytes (Aubert)	species_25 → species_4	0000185
14	reaction_21	LAC_exchange_ec_capillary	species_28 → species_26	0000185
15	reaction_22	LAC_exchange_neurons_ec	species_28 → species_18	0000185
16	reaction_23	LAC_exchange_astrocytes_ec	species_19 → species_28	0000185
17	reaction_24	LAC_exchange_astrocytes_capillary	species_19 → species_26	0000185
18	02_exchange- _capillary- _neurons	O2_exchange_capillary_neurons	species_23 → species_16	0000185
19	02_exchange- _capillary- _astrocytes	O2_exchange_capillary_astrocytes	species_23 → species_20	0000185
20	Blood_flow- _contribution- _to_capillary- _02	O2_exchange_artery_capillary	O2_artery —→ species_23	0000185
21	Blood_flow- _contribution- _to_capillary- _GLC	GLC_exchange_artery_capillary	GLC_artery → species_25	0000185
22	Blood_flow- _contribution- _to_capillary- _LAC	LAC_exchange_capillary_artery	species_26 → LAC_artery	0000185

Nº	Id	Name	Reaction Equation	SBO
23	Flow_of_CO2betweencapillaryand_vesselartery_	CO2_exchange_capillary_artery	species_24 → CO2_artery	0000185
24	vPUMP_neurons	Na+_exchange_neurons_extracellular_space (n.a.)	species_3 + 3 Na_neurons → ADP_neurons	0000185
25	vPUMP- _astrocytes	Na+_exchange_astrocytes_extracellular_space (n.a.)	species_5 + 3 Na_astrocytes → ADP_astrocytes	0000185
26	vLEAK_Na- _neurons	LEAK_Na_neurons (n.a.)	$Na\_extracellular\_space \longrightarrow Na\_neurons$	0000185
27	vLEAK_Na- _astrocytes	LEAK_Na_astrocytes (n.a)	$Na\_extracellular\_space \longrightarrow Na\_astrocytes$	0000185
28	vSTIM	Na+_exchange_extracellular_space_neurons (stimulation)	$Na\_extracellular\_space \longrightarrow Na\_neurons$	0000185
29	$vGLU\_ne$	GLU_exchange_neurons_extracellular_space	GLU_neurons → GLU_extracellular_space	0000185
30	vGLU_eg	GLU_exchange_extracellular_space- _astrocytes	GLU_extracellular_space → GLU_astrocytes + Na_astrocytes	0000185
31	vGLU_gn	GLU_exchange_astrocytes_neurons	GLU_astrocytes + species_5 → GLU_neurons + ADP_astrocytes	0000185
32	inflow_of_dHb	inflow of dHb	$\emptyset \xrightarrow{\text{O2\_artery, species\_23}} \text{dHb}$	0000631
33	outflow_of_dHb	outflow of dHb	$dHb \longrightarrow \emptyset$	0000631
34	ATPase_neurons	ATPase_neurons (n.a.)	species_3 → ADP_neurons	0000631
35	ATPase- _astrocytes	ATPase_astrocytes (n.a.)	species_5 → ADP_astrocytes	0000631
36	AK_neurons	AK_neurons (R00127)	2 ADP_neurons ⇒ species_3 + AMP_neurons	
37	$\mathtt{AK}_{\mathtt{-}}\mathtt{astrocytes}$	AK_astrocytes (R00127)	$2 \text{ ADP\_astrocytes} \Longrightarrow \text{species\_5} + \text{AMP\_astrocytes}$	

N₀	Id	Name	Reaction Equation	SBO
38	CK_astrocytes- _forward _R01881	CK_astrocytes (R01881)	ADP_astrocytes + species_22 ⇒ species_5 + Cr_astrocytes	
39	CK_neurons- _forward _R01881	CK_neurons (R01881)	species_21 + ADP_neurons ⇒ species_3 + Cr_neurons	
40	LDH_astrocytes- _forward _R00703	LDH_astrocytes (R00703)	species_17 + species_13 ⇒ species_19 + NAD_astrocytes	0000176
41	LDH_neurons- _forward _R00703	LDH_neurons (R00703)	species_15 + species_11 ⇒ species_18 + NAD_neurons	0000176
42	ZWF_astrocytes- R02736	ZWF_astrocytes (R02736)	species_ $6+NADP$ _astrocytes $\longrightarrow G6L$ _astrocytes + NADPH_astrocytes	0000176
43	ZWF_neurons _R02736	ZWF_neurons (R02736)	species_2 + NADP_neurons → G6L_neurons + NADPH_neurons	0000176
44	SOL_neurons _R02035	SOL_neurons (R02035)	$G6L\_neurons \longrightarrow P6G\_neurons$	0000176
45	SOL_astrocytes- R02035	SOL_astrocytes (R02035)	$G6L_astrocytes \longrightarrow P6G_astrocytes$	0000176
46	GND_neurons _R01528	GND_neurons (R01528)	P6G_neurons + NADP_neurons ← Ru5P_neurons + NADPH_neurons	0000176
47	GND_astrocytes- R01528	GND_astrocytes (R01528)	P6G_astrocytes + NADP_astrocytes → Ru5P_astrocy NADPH_astrocytes	rt <b>000</b> 0176
48	RPE_neurons _R01529	RPE_neurons (R01529)	Ru5P_neurons	0000176
49	RPE_astrocytes- R01529	RPE_astrocytes (R01529)	Ru5P_astrocytes	0000176

N₀	Id	Name	Reaction Equation	SBO
50	RKI_astrocytes- R01056	RKI_astrocytes (R01056)	Ru5P_astrocytes	0000176
51	RKI_neurons _R01056	RKI_neurons (R01056)	$Ru5P_neurons \Longrightarrow R5P_neurons$	0000176
52	TKL_1- _astrocytes- R01641	TKL-1_astrocytes (R01641)	$X5P_{astrocytes} + R5P_{astrocytes} \longrightarrow species_{10} + S7P_{astrocytes}$	0000176
53	TKL_1_neurons _R01641	TKL-1_neurons (R01641)	$X5P$ _neurons + $R5P$ _neurons $\longrightarrow$ species_9 + $S7P$ _neurons	0000176
54	TAL_astrocytes- R01827	TAL_astrocytes (R01827)	species_10 + S7P_astrocytes ⇒ species_8 + E4P_astrocytes	0000176
55	TAL_neurons _R01827	TAL_neurons (R01827)	species_9 + S7P_neurons ⇒ species_7 + E4P_neurons	0000176
56	TKL_2- _astrocytes- R01830	TKL-2_astrocytes (R01830)	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0000176
57	TKL_2_neurons _R01830	TKL-2_neurons (R01830)	species_7 + species_9 $\longrightarrow$ X5P_neurons + E4P_neurons	0000176
58	NADPH_oxidase- _neurons _R07172	NADPH oxidase neurons (R07172)	NADPH_neurons → NADP_neurons	0000631
59	NADPH_oxidase- _astrocytes _R07172	NADPH oxidase astrocytes (R07172)	NADPH_astrocytes → NADP_astrocytes	0000631
60	R5P_sink- _astrocytes- n_a_	R5P sink_astrocytes (n.a.)	R5P_astrocytes $\longrightarrow \emptyset$	0000631
61	R5P_sink- _neuronsn_a_	R5P sink_neurons (n.a.)	R5P_neurons $\longrightarrow \emptyset$	0000631

N₀	Id	Name	Reaction Equation	SBO
62	PGI_astrocytes- R02740HS	PGI_astrocytes (R02740) (HS)	species_6 <del>←</del> species_8	
63	HK_neurons- R01786	HK_neurons (R01786) (HeinrichSchuster)	species_3 + species_1 $\xrightarrow{\text{species}\_2}$ species_2 + ADP_neurons	0000176
64	_HeinrichSchuste: PGI_neurons _R02740HS	PGI_neurons (R02740) (HS)	species_2	

#### 9.1 Reaction reaction\_2

This is an irreversible reaction of two reactants forming two products influenced by one modifier.

Name HK\_astrocytes (R01786) (HeinrichSchuster)

SBO:0000176 biochemical reaction

## **Reaction equation**

$$species\_5 + species\_4 \xrightarrow{species\_6} species\_6 + ADP\_astrocytes$$
 (44)

#### **Reactants**

Table 6: Properties of each reactant.

Id	Name	SBO
species_5		

#### **Modifier**

Table 7: Properties of each modifier.

Id	Name	SBO
species_6	G6P	

#### **Products**

Table 8: Properties of each product.

	1	
Id	Name	SBO
species_6 ADP_astrocytes	G6P ADP	

#### **Kinetic Law**

Derived unit contains undeclared units

$$v_{1} = \text{vol (compartment\_3)} \\ \cdot \text{vHK\_HS}\left(\text{k\_HK}, \frac{\text{species\_5}}{\text{vol (compartment\_3)}}, \frac{\text{species\_6}}{\text{vol (compartment\_3)}}, \text{K\_I\_G6P}\right)$$
(45)

$$vHK\_HS\left(k\_HK,ATP,G6P,K\_I\_G6P\right) = k\_HK \cdot ATP \cdot \left(1 + \frac{G6P}{K\_I\_G6P}\right)^{1} \tag{46}$$

$$vHK\_HS(k\_HK,ATP,G6P,K\_I\_G6P) = k\_HK \cdot ATP \cdot \left(1 + \frac{G6P}{K\_I\_G6P}\right)^{1}$$
(47)

Table 9: Properties of each parameter.

Id	Name	SBO Value Unit	Constant
k_HK	k_HK	0.01	
$K_I_G6P$	K_I_G6P	0.02	$\checkmark$

#### 9.2 Reaction reaction\_5

This is an irreversible reaction of two reactants forming two products.

**Name** PFK\_neurons (R04779, R01070, R01015)

SBO:0000395 encapsulating process

#### **Reaction equation**

$$species_7 + species_3 \longrightarrow 2 species_9 + ADP\_neurons$$
 (48)

#### **Reactants**

Table 10: Properties of each reactant.

Id	Name	SBO
species_7	F6P	
species_3	ATP	

#### **Products**

Table 11: Properties of each product.

Id	Name	SBO
species_9 ADP_neurons	GAP ADP	

#### **Kinetic Law**

**Derived unit** contains undeclared units

$$v_{2} = \text{vol (compartment\_2)} \cdot \text{vPFK}\left(\text{k\_PFK}, \frac{\text{species\_3}}{\text{vol (compartment\_2)}}, \text{parameter\_5}, \right.$$

$$\text{parameter\_6}, \frac{\text{species\_7}}{\text{vol (compartment\_2)}}, \text{K\_m\_F6P}\right)$$

$$(49)$$

$$= k\_PFK \cdot ATP \cdot \left(1 + \left(\frac{ATP}{K\_I\_ATP}\right)^{nH}\right)^{1} \cdot \frac{F6P}{F6P + K\_m\_F6P}$$
(50)

$$vPFK(k\_PFK, ATP, K\_I\_ATP, nH, F6P, K\_m\_F6P)$$

$$= k\_PFK \cdot ATP \cdot \left(1 + \left(\frac{ATP}{K\_I\_ATP}\right)^{nH}\right)^{1} \cdot \frac{F6P}{F6P + K\_m\_F6P}$$
(51)

Table 12: Properties of each parameter.

Id	Name	SBO Value Unit	Constant
k_PFK	k_PFK	0.44	$ \mathcal{L} $
K_m_F6P	K_m_F6P	0.18	$\checkmark$

## 9.3 Reaction reaction\_6

This is an irreversible reaction of two reactants forming two products.

Name PFK\_astrocytes (R04779, R01070, R01015)

SBO:0000395 encapsulating process

#### **Reaction equation**

species\_8 + species\_5 
$$\longrightarrow$$
 2 species\_10 + ADP\_astrocytes (52)

#### Reactants

Table 13: Properties of each reactant.

Id	Name	SBO
species_8 species_5	F6P ATP	

#### **Products**

Table 14: Properties of each product.

Id	Name	SBO
species_10	GAP	
$\mathtt{ADP}_\mathtt{astrocytes}$	ADP	

#### **Kinetic Law**

**Derived unit** contains undeclared units

$$v_{3} = \text{vol} \left( \text{compartment\_3} \right) \cdot \text{vPFK} \left( \text{k\_PFK}, \frac{\text{species\_5}}{\text{vol} \left( \text{compartment\_3} \right)}, \text{parameter\_5}, \right.$$

$$\text{parameter\_6}, \frac{\text{species\_8}}{\text{vol} \left( \text{compartment\_3} \right)}, \text{K\_m\_F6P} \right)$$

$$(53)$$

 $vPFK(k\_PFK, ATP, K\_I\_ATP, nH, F6P, K\_m\_F6P)$ 

$$= k\_PFK \cdot ATP \cdot \left(1 + \left(\frac{ATP}{K\_I\_ATP}\right)^{nH}\right)^{1} \cdot \frac{F6P}{F6P + K\_m\_F6P}$$
(54)

vPFK (k\_PFK, ATP, K\_I\_ATP, nH, F6P, K\_m\_F6P)

$$= k\_PFK \cdot ATP \cdot \left(1 + \left(\frac{ATP}{K\_L\_ATP}\right)^{nH}\right)^{1} \cdot \frac{F6P}{F6P + K\_m\_F6P}$$
(55)

Table 15: Properties of each parameter.

Id	Name	SBO Value Unit	Constant
k_PFK	k_PFK	0.20	
K_m_F6P	K_m_F6P	0.18	$\square$

#### **9.4 Reaction** reaction\_7

This is an irreversible reaction of three reactants forming three products.

Name PGK\_neurons (R01061, R01512, R01518, R00658)

SBO:0000395 encapsulating process

## **Reaction equation**

$$species_9 + ADP\_neurons + NAD\_neurons \longrightarrow species_11 + species_12 + species_3$$
 (56)

#### **Reactants**

Table 16: Properties of each reactant.

Id	Name	SBO
species_9	GAP	
$\mathtt{ADP\_neurons}$	ADP	
$\mathtt{NAD\_neurons}$	NAD	

#### **Products**

Table 17: Properties of each product.

Id	Name	SBO
species_11	NADH	
species_12	PEP	
species_3	ATP	

#### **Kinetic Law**

Derived unit contains undeclared units

$$v_{4} = \text{vol} \left( \text{compartment\_2} \right) \cdot \text{vPGK} \left( \text{k\_PGK}, \frac{\text{species\_9}}{\text{vol} \left( \text{compartment\_2} \right)}, \frac{\text{ADP\_neurons}}{\text{vol} \left( \text{compartment\_2} \right)}, \frac{\text{NAD\_neurons}}{\text{vol} \left( \text{compartment\_2} \right)}, \frac{\text{species\_11}}{\text{vol} \left( \text{compartment\_2} \right)} \right)$$
(57)

$$vPGK\left(k\_PGK,GAP,ADP,NAD,NADH\right) = k\_PGK \cdot GAP \cdot ADP \cdot \frac{NAD}{NADH} \tag{58}$$

$$vPGK(k\_PGK,GAP,ADP,NAD,NADH) = k\_PGK \cdot GAP \cdot ADP \cdot \frac{NAD}{NADH}$$
 (59)

Table 18: Properties of each parameter.

Id	Name	SBO Value Unit	Constant
k_PGK	k_PGK	10.0	

#### 9.5 Reaction reaction\_8

This is an irreversible reaction of three reactants forming three products.

Name PGK\_astrocytes (R01061, R01512, R01518, R00658)

SBO:0000395 encapsulating process

## **Reaction equation**

$$species\_10 + ADP\_astrocytes + NAD\_astrocytes \longrightarrow species\_13 + species\_14 + species\_5 \eqno(60)$$

#### **Reactants**

Table 19: Properties of each reactant.

Id	Name	SBO
species_10	GAP	
$\mathtt{ADP}_\mathtt{astrocytes}$	ADP	
${\tt NAD\_astrocytes}$	NAD	

#### **Products**

Table 20: Properties of each product.

Name	SBO
NADH	
PEP	
ATP	
	NADH PEP

## **Kinetic Law**

**Derived unit** contains undeclared units

$$v_{5} = \text{vol} \left( \text{compartment}\_3 \right) \cdot \text{vPGK} \left( \text{k\_PGK}, \frac{\text{species}\_10}{\text{vol} \left( \text{compartment}\_3 \right)}, \frac{\text{ADP\_astrocytes}}{\text{vol} \left( \text{compartment}\_3 \right)}, \frac{\text{NAD\_astrocytes}}{\text{vol} \left( \text{compartment}\_3 \right)}, \frac{\text{species}\_13}{\text{vol} \left( \text{compartment}\_3 \right)} \right)$$

$$(61)$$

$$vPGK\left(k\_PGK,GAP,ADP,NAD,NADH\right) = k\_PGK \cdot GAP \cdot ADP \cdot \frac{NAD}{NADH} \tag{62}$$

$$vPGK(k\_PGK,GAP,ADP,NAD,NADH) = k\_PGK \cdot GAP \cdot ADP \cdot \frac{NAD}{NADH}$$
 (63)

Table 21: Properties of each parameter.

Id	Name	SBO Value Unit	Constant
k_PGK	k_PGK	3.0	$\checkmark$

#### 9.6 Reaction reaction\_9

This is an irreversible reaction of two reactants forming two products.

Name PK\_neurons (R00200)

SBO:0000176 biochemical reaction

## **Reaction equation**

$$species_12 + ADP\_neurons \longrightarrow species_3 + species_15$$
 (64)

#### **Reactants**

Table 22: Properties of each reactant.

Id	Name	SBO
species_12	PEP	
$\mathtt{ADP\_neurons}$	ADP	

#### **Products**

Table 23: Properties of each product.

Id	Name	SBO
species_3	ATP	
species_15	PYR	

**Derived unit** contains undeclared units

$$v_6 = \text{vol} (\text{compartment}\_2) \cdot \text{vPK} \left( \text{k\_PK}, \frac{\text{species}\_12}{\text{vol} (\text{compartment}\_2)}, \frac{\text{ADP\_neurons}}{\text{vol} (\text{compartment}\_2)} \right)$$
 (65)

$$vPK (k\_PK, PEP, ADP) = k\_PK \cdot PEP \cdot ADP$$
 (66)

$$vPK(k\_PK, PEP, ADP) = k\_PK \cdot PEP \cdot ADP$$
 (67)

Table 24: Properties of each parameter.

Id	Name	SBO Value Unit	Constant
k_PK	k_PK	44.0	

## 9.7 Reaction reaction\_10

This is an irreversible reaction of two reactants forming two products.

Name PK\_astrocytes (R00200)

SBO:0000176 biochemical reaction

# **Reaction equation**

$$species_14 + ADP_astrocytes \longrightarrow species_5 + species_17$$
 (68)

Table 25: Properties of each reactant.

Id	Name	SBO
species_14	PEP	
$\mathtt{ADP}_\mathtt{astrocytes}$	ADP	

Table 26: Properties of each product.

Id	Name	SBO
species_5	ATP	
species_17	PYR	

#### **Kinetic Law**

**Derived unit** contains undeclared units

$$v_7 = \text{vol} \left( \text{compartment\_3} \right) \cdot \text{vPK} \left( \text{k\_PK}, \frac{\text{species\_14}}{\text{vol} \left( \text{compartment\_3} \right)}, \frac{\text{ADP\_astrocytes}}{\text{vol} \left( \text{compartment\_3} \right)} \right)$$
 (69)

$$vPK (k\_PK, PEP, ADP) = k\_PK \cdot PEP \cdot ADP$$
 (70)

$$vPK(k\_PK, PEP, ADP) = k\_PK \cdot PEP \cdot ADP$$
 (71)

Table 27: Properties of each parameter.

Id	Name	SBO Value Unit	Constant
k_PK	k_PK	20.0	

## 9.8 Reaction reaction\_13

This is an irreversible reaction of four reactants forming three products.

Name mitochondrial\_respiration\_neurons (n.a.)

SBO:0000395 encapsulating process

## **Reaction equation**

$$species\_15 + 3 \, species\_16 + species\_11 + 15 \, ADP\_neurons \longrightarrow 15 \, species\_3 + 3 \, species\_24 + NAD\_neurons \tag{72}$$

Table 28: Properties of each reactant.

Id	Name	SBO
species_15	PYR	
species_16	O2	
species_11	NADH	
$\mathtt{ADP\_neurons}$	ADP	

Table 29: Properties of each product.

Id	Name	SBO
species_3	ATP	
species_24	CO2	
$\mathtt{NAD\_neurons}$	NAD	

#### **Kinetic Law**

$$v_{8} = vMITO2\_inkl\_Volumes \left(v\_max\_mito, \frac{species\_15}{vol (compartment\_2)}, parameter\_18, \frac{ADP\_neurons}{vol (compartment\_2)}, parameter\_16, \frac{species\_16}{vol (compartment\_2)}, parameter\_17, alpha, (73) \frac{species\_3}{vol (compartment\_2)}, beta, vol (compartment\_2)\right)$$

Table 30: Properties of each parameter.

Id	Name	SBO Value Unit	Constant
v_max_mito	v_max_mito	0.1	
alpha	alpha	5.0	$\overline{\checkmark}$
beta	beta	20.0	

### 9.9 Reaction reaction\_14

This is an irreversible reaction of four reactants forming three products.

Name mitochondrial\_respiration\_astrocytes (n.a.)

SBO:0000395 encapsulating process

## **Reaction equation**

$$species\_17 + 15 \, ADP\_astrocytes + 3 \, species\_20 + species\_13 \longrightarrow 15 \, species\_5 + 3 \, species\_24 + NAD\_astrocytes \tag{75}$$

### Reactants

Table 31: Properties of each reactant.

Id	Name	SBO
species_17	PYR	
$\mathtt{ADP}_\mathtt{-}\mathtt{astrocytes}$	ADP	
species_20	O2	
species_13	NADH	

## **Products**

Table 32: Properties of each product.

	r	
Id	Name	SBO
species_5 species_24 NAD_astrocytes	ATP CO2 NAD	
v		

#### **Kinetic Law**

$$v_{9} = vMITO2\_inkl\_Volumes \left(v\_max\_mito, \frac{species\_17}{vol (compartment\_3)}, parameter\_18, \frac{ADP\_astrocytes}{vol (compartment\_3)}, parameter\_16, \frac{species\_20}{vol (compartment\_3)}, parameter\_17, alpha, (76) \frac{species\_5}{vol (compartment\_3)}, beta, vol (compartment\_3)\right)$$

$$vMITO2\_inkl\_Volumes (v\_max\_mito, PYR, K\_m\_PYR, ADP, K\_m\_ADP, O2, K\_m\_O2, alpha, ATP, beta, Volume) = v\_max\_mito \cdot \frac{PYR}{PYR + K\_m\_PYR} \cdot \frac{ADP}{ADP + K\_m\_ADP}$$
 (77) 
$$\cdot \frac{O2}{O2 + K\_m\_O2} \cdot \left(1 - \frac{1}{1 + exp \left(alpha \cdot \left(\frac{ATP}{ADP} - beta\right)\right)}\right) \cdot Volume$$

Table 33: Properties of each parameter.

Id	Name	SBO V	alue Unit	Constant
v_max_mito	v_max_mito		0.01	
alpha beta	alpha beta		5.00 0.00	<b>☑</b>

### 9.10 Reaction reaction\_17

This is an irreversible reaction of one reactant forming one product.

Name GLC\_exchange\_extracellular\_space\_neurons (Aubert)

SBO:0000185 transport reaction

# **Reaction equation**

$$species_27 \longrightarrow species_1$$
 (78)

#### Reactant

Table 34: Properties of each reactant.

Id	Name	SBO
species_27	GLC	

Table 35: Properties of each product.

Id	Name	SBO
species_1	GLC	

Derived unit contains undeclared units

$$v_{10} = facilitated\_transport\_inkl\_Volume\_\_\_scaled \left( Vmax\_en\_GLC\_wrt\_neurons\_\_Aubert, \frac{species\_27}{vol \, (compartment\_4)}, K\_T\_GLC\_en\_Aubert, \frac{species\_1}{vol \, (compartment\_2)}, vol \, (compartment\_4) \right)$$

$$\begin{split} & \text{facilitated\_transport\_inkl}\_\text{Volume}\_\_\text{scaled}\left(\text{Vmax}, \text{sf}, \text{S}, \text{K}, \text{P}, \text{Volume}\right) \\ &= \text{Vmax} \cdot \text{sf} \cdot \left(\frac{\text{S}}{\text{S} + \text{K}} - \frac{\text{P}}{\text{P} + \text{K}}\right) \cdot \text{Volume} \end{split}$$

## 9.11 Reaction reaction\_18

This is an irreversible reaction of one reactant forming one product.

Name GLC\_exchange\_extracellular\_space\_astrocytes (Aubert)

SBO:0000185 transport reaction

## **Reaction equation**

$$species_27 \longrightarrow species_4$$
 (81)

### Reactant

Table 36: Properties of each reactant.

Id	Name	SBO
species_27	GLC	

Table 37: Properties of each product.

Id	Name	SBO
species_4	GLC	

**Derived unit** contains undeclared units

$$v_{11} = facilitated\_transport\_inkl\_Volume\_\_\_scaled \left( Vmax\_eg\_GLC\_\_wrt\_astrocytes\_\_Aubert\_, \frac{species\_27}{vol (compartment\_4)}, K\_T\_GLC\_eg\_Aubert, \frac{species\_4}{vol (compartment\_3)}, vol (compartment\_4) \right)$$

$$\begin{split} & \text{facilitated\_transport\_inkl}\_\text{Volume}\_\_\text{scaled}\left(\text{Vmax}, \text{sf}, \text{S}, \text{K}, \text{P}, \text{Volume}\right) \\ &= \text{Vmax} \cdot \text{sf} \cdot \left(\frac{\text{S}}{\text{S} + \text{K}} - \frac{\text{P}}{\text{P} + \text{K}}\right) \cdot \text{Volume} \end{split}$$

## 9.12 Reaction reaction\_19

This is an irreversible reaction of one reactant forming one product.

Name GLC\_exchange\_capillary\_ec (Aubert)

SBO:0000185 transport reaction

## **Reaction equation**

$$species_25 \longrightarrow species_27$$
 (84)

### Reactant

Table 38: Properties of each reactant.

Id	Name	SBO
species_25	GLC	

Table 39: Properties of each product.

Id	Name	SBO
species_27	GLC	

**Derived unit** contains undeclared units

$$v_{12} = facilitated\_transport\_inkl\_Volume\_\_\_scaled \left( Vmax\_ce\_GLC\_wrt\_capillaries\_\_Aubert, \frac{species\_25}{vol (compartment\_1)}, K\_T\_GLC\_ce\_Aubert, \frac{species\_27}{vol (compartment\_4)}, vol (compartment\_1) \right)$$

$$\begin{split} & \text{facilitated\_transport\_inkl}\_\text{Volume}\_\_\text{scaled}\left(\text{Vmax}, \text{sf}, \text{S}, \text{K}, \text{P}, \text{Volume}\right) \\ &= \text{Vmax} \cdot \text{sf} \cdot \left(\frac{\text{S}}{\text{S} + \text{K}} - \frac{\text{P}}{\text{P} + \text{K}}\right) \cdot \text{Volume} \end{split}$$

## 9.13 Reaction reaction\_20

This is an irreversible reaction of one reactant forming one product.

Name GLC\_exchange\_capillary\_astrocytes (Aubert)

SBO:0000185 transport reaction

## **Reaction equation**

$$species_25 \longrightarrow species_4$$
 (87)

### Reactant

Table 40: Properties of each reactant.

Id	Name	SBO
species_25	GLC	

Table 41: Properties of each product.

Id	Name	SBO
species_4	GLC	

**Derived unit** contains undeclared units

$$v_{13} = facilitated\_transport\_inkl\_Volume\_\_\_scaled \left( Vmax\_cg\_GLC\_wrt\_capillaries\_\_Aubert, \frac{species\_4}{vol (compartment\_1)}, K\_T\_GLC\_cg\_\_Aubert, \frac{species\_4}{vol (compartment\_3)}, vol (compartment\_1) \right)$$

$$\begin{split} & \text{facilitated\_transport\_inkl}\_\text{Volume}\_\_\text{scaled}\left(\text{Vmax}, \text{sf}, \text{S}, \text{K}, \text{P}, \text{Volume}\right) \\ &= \text{Vmax} \cdot \text{sf} \cdot \left(\frac{\text{S}}{\text{S} + \text{K}} - \frac{\text{P}}{\text{P} + \text{K}}\right) \cdot \text{Volume} \end{split}$$

## 9.14 Reaction reaction\_21

This is an irreversible reaction of one reactant forming one product.

Name LAC\_exchange\_ec\_capillary

SBO:0000185 transport reaction

## **Reaction equation**

$$species_28 \longrightarrow species_26$$
 (90)

### Reactant

Table 42: Properties of each reactant.

Id	Name	SBO
species_28	LAC	

Table 43: Properties of each product.

Id	Name	SBO
species_26	LAC	

Derived unit contains undeclared units

$$v_{14} = facilitated\_transport\_\_inkl\_\_Volume \left( Vmax\_ec\_LAC\_\_wrt\_extracellular\_space\_\_Aubert, \frac{species\_28}{vol (compartment\_4)}, K\_T\_LAC\_ec\_\_Aubert, \frac{species\_26}{vol (compartment\_1)}, vol (compartment\_4) \right)$$

$$(91)$$

$$\begin{aligned} & \text{facilitated\_transport\_\_inkl}\_\text{Volume} \left( Vmax, S, K, P, Volume \right) \\ &= Vmax \cdot \left( \frac{S}{S+K} - \frac{P}{P+K} \right) \cdot \text{Volume} \end{aligned} \tag{92}$$

## 9.15 Reaction reaction\_22

This is an irreversible reaction of one reactant forming one product.

Name LAC\_exchange\_neurons\_ec

SBO:0000185 transport reaction

## **Reaction equation**

$$species_28 \longrightarrow species_18$$
 (93)

### Reactant

Table 44: Properties of each reactant.

Id	Name	SBO
species_28	LAC	

Table 45: Properties of each product.

Id	Name	SBO
species_18	LAC	

**Derived unit** contains undeclared units

$$v_{15} = facilitated\_transport\_\_inkl\_\_Volume \left( Vmax\_ne\_LAC\_\_wrt\_neurons\_\_Aubert, \frac{species\_28}{vol (compartment\_4)}, K_T\_LAC\_ne\_\_Aubert, \frac{species\_18}{vol (compartment\_2)}, (94) vol (compartment\_4) \right)$$

$$\begin{aligned} & \text{facilitated\_transport\_inkl}\_\text{Volume} \left( V \text{max}, S, K, P, \text{Volume} \right) \\ &= V \text{max} \cdot \left( \frac{S}{S+K} - \frac{P}{P+K} \right) \cdot \text{Volume} \end{aligned} \tag{95}$$

### 9.16 Reaction reaction\_23

This is an irreversible reaction of one reactant forming one product.

Name LAC\_exchange\_astrocytes\_ec

SBO:0000185 transport reaction

### **Reaction equation**

$$species_19 \longrightarrow species_28$$
 (96)

### Reactant

Table 46: Properties of each reactant.

Id	Name	SBO
species_19	LAC	

Table 47: Properties of each product.

Id	Name	SBO
species_28	LAC	

**Derived unit** contains undeclared units

$$v_{16} = facilitated\_transport\_inkl\_Volume \left( Vmax\_ge\_LAC\_wrt\_astrocytes\_\_Aubert, \frac{species\_19}{vol (compartment\_3)}, K\_T\_LAC\_ge\_Aubert, \frac{species\_28}{vol (compartment\_4)}, (97) \right)$$

$$\begin{aligned} & \text{facilitated\_transport\_inkl}\_\text{Volume} \left( V \text{max}, S, K, P, \text{Volume} \right) \\ &= V \text{max} \cdot \left( \frac{S}{S+K} - \frac{P}{P+K} \right) \cdot \text{Volume} \end{aligned} \tag{98}$$

### 9.17 Reaction reaction\_24

This is an irreversible reaction of one reactant forming one product.

Name LAC\_exchange\_astrocytes\_capillary

SBO:0000185 transport reaction

#### **Reaction equation**

$$species_19 \longrightarrow species_26$$
 (99)

### Reactant

Table 48: Properties of each reactant.

Id	Name	SBO
species_19	LAC	

Table 49: Properties of each product.

Id	Name	SBO
species_26	LAC	

**Derived unit** contains undeclared units

$$v_{17} = facilitated\_transport\_inkl\_Volume \left( Vmax\_gc\_LAC\_wrt\_astrocytes\_\_Aubert, \frac{species\_19}{vol (compartment\_3)}, K\_T\_LAC\_gc\_Aubert, \frac{species\_26}{vol (compartment\_1)}, (100) \\ vol (compartment\_3) \right)$$

$$\begin{split} & \text{facilitated\_transport\_inkl}\_\text{Volume} \left( V \text{max}, S, K, P, \text{Volume} \right) \\ &= V \text{max} \cdot \left( \frac{S}{S+K} - \frac{P}{P+K} \right) \cdot \text{Volume} \end{split} \tag{101}$$

## 9.18 Reaction 02\_exchange\_capillary\_neurons

This is an irreversible reaction of one reactant forming one product.

Name O2\_exchange\_capillary\_neurons

SBO:0000185 transport reaction

Notes 02 exchange between capillary and neurons

### **Reaction equation**

$$species_23 \longrightarrow species_16$$
 (102)

#### Reactant

Table 50: Properties of each reactant.

Id	Name	SBO
species_23	O2	

Table 51: Properties of each product.

Id	Name	SBO
species_16	O2	

**Derived unit** contains undeclared units

$$\label{eq:v18} \begin{split} v_{18} &= O2\_transport\_function\_inkl\_\_volume \left( PS\_cap\_neuron\_\_wrt\_capillaries\_\_Aubert, \\ vol \left( compartment\_2 \right), K\_O2\_Aubert, Hb\_OP, \frac{species\_23}{vol \left( compartment\_1 \right)}, nh\_O2\_Aubert, \\ \frac{species\_16}{vol \left( compartment\_2 \right)}, vol \left( compartment\_1 \right) \right) \end{split}$$

O2\_transport\_function\_inkl\_\_volume (PScap, Volume, KO2,

$$\begin{split} \text{HbOP,O2\_source,nh,O2\_destination,Volume1}) &= \frac{PScap}{Volume} \\ &\cdot \left( \text{KO2} \cdot \left( \frac{\text{HbOP}}{\text{O2\_source}} - 1 \right)^{\frac{1}{nh}} - \text{O2\_destination} \right) \cdot \text{Volume1} \end{split}$$

# **9.19 Reaction** O2\_exchange\_capillary\_astrocytes

This is an irreversible reaction of one reactant forming one product.

Name O2\_exchange\_capillary\_astrocytes

SBO:0000185 transport reaction

### **Reaction equation**

$$species_23 \longrightarrow species_20$$
 (105)

## Reactant

Table 52: Properties of each reactant.

Id	Name	SBO
species_23	O2	

Table 53: Properties of each product.

Id	Name	SBO
species_20	O2	

Derived unit contains undeclared units

$$v_{19} = O2\_transport\_function\_inkl\_\_volume \left( PScap, vol (compartment\_3), K\_O2\_Aubert, \frac{species\_23}{vol (compartment\_1)}, nh\_O2\_Aubert, \frac{species\_20}{vol (compartment\_3)}, vol (compartment\_1) \right)$$

$$vol (compartment\_1)$$

$$(106)$$

$$\begin{aligned} &O2\_transport\_function\_inkl\_\_volume \, (PScap, Volume, KO2, \\ &HbOP, O2\_source, nh, O2\_destination, Volume1) = \frac{PScap}{Volume} \\ &\cdot \left( KO2 \cdot \left( \frac{HbOP}{O2\_source} - 1 \right)^{\frac{1}{nh}} - O2\_destination \right) \cdot Volume1 \end{aligned} \tag{107}$$

Table 54: Properties of each parameter.

Id	Name	SBO Value Unit	Constant
PScap	PScap	10.0	

# 9.20 Reaction Blood\_flow\_contribution\_to\_capillary\_02

This is an irreversible reaction of one reactant forming one product.

Name O2\_exchange\_artery\_capillary

SBO:0000185 transport reaction

## **Reaction equation**

$$O2_{artery} \longrightarrow species_{23}$$
 (108)

Table 55: Properties of each reactant.

Id	Name	SBO
02_artery	O2	

Table 56: Properties of each product.

Id	Name	SBO
species_23	O2	

## **Kinetic Law**

Derived unit contains undeclared units

$$v_{20} = Blood\_flow\_contribution\_inkl\_\_volume \left(F\_in, vol (compartment\_1), vol (artery), \frac{O2\_artery}{vol (artery)}, \frac{species\_23}{vol (compartment\_1)}\right)$$

$$(109)$$

$$\begin{split} &Blood\_flow\_contribution\_inkl\_\_volume \left(F\_in, V\_c, Volume, Substrate, Product\right) \\ &= \frac{2 \cdot F\_in}{V\_c} \cdot \left(Substrate - Product\right) \cdot Volume \end{split} \tag{110}$$

# 9.21 Reaction Blood\_flow\_contribution\_to\_capillary\_GLC

This is an irreversible reaction of one reactant forming one product.

Name GLC\_exchange\_artery\_capillary

SBO:0000185 transport reaction

### **Reaction equation**

$$GLC\_artery \longrightarrow species\_25 \tag{111}$$

Table 57: Properties of each reactant.

Id	Name	SBO
$GLC_artery$	GLC	

Table 58: Properties of each product.

Id	Name	SBO
species_25	GLC	

### **Kinetic Law**

Derived unit contains undeclared units

$$v_{21} = Blood\_flow\_contribution\_inkl\_\_volume \left(F\_in, vol (compartment\_1), vol (artery), \frac{GLC\_artery}{vol (artery)}, \frac{species\_25}{vol (compartment\_1)}\right)$$
(112)

$$Blood\_flow\_contribution\_inkl\_\_volume (F\_in, V\_c, Volume, Substrate, Product) \\ = \frac{2 \cdot F\_in}{V\_c} \cdot (Substrate - Product) \cdot Volume$$
 (113)

# 9.22 Reaction Blood\_flow\_contribution\_to\_capillary\_LAC

This is an irreversible reaction of one reactant forming one product.

Name LAC\_exchange\_capillary\_artery

SBO:0000185 transport reaction

### **Reaction equation**

species\_26 
$$\longrightarrow$$
 LAC\_artery (114)

Table 59: Properties of each reactant.

Id	Name	SBO
species_26	LAC	

Table 60: Properties of each product.

Id	Name	SBO
LAC_artery	LAC	

### **Kinetic Law**

Derived unit contains undeclared units

$$v_{22} = Blood\_flow\_contribution\_inkl\_\_volume \left(F\_in, vol (compartment\_1), \frac{species\_26}{vol (compartment\_1)}, \frac{LAC\_artery}{vol (artery)}\right)$$
(115)

$$Blood\_flow\_contribution\_inkl\_volume (F\_in, V\_c, Volume, Substrate, Product) \\ = \frac{2 \cdot F\_in}{V\_c} \cdot (Substrate - Product) \cdot Volume$$
 (116)

# 9.23 Reaction Flow\_of\_CO2\_between\_capillary\_and\_vessel\_\_artery\_

This is an irreversible reaction of one reactant forming one product.

Name CO2\_exchange\_capillary\_artery

SBO:0000185 transport reaction

### **Reaction equation**

species\_24 
$$\longrightarrow$$
 CO2\_artery (117)

Table 61: Properties of each reactant.

Id	Name	SBO
species_24	CO2	

Table 62: Properties of each product.

Id	Name	SBO
CO2_artery	CO2	

### **Kinetic Law**

Derived unit contains undeclared units

$$v_{23} = Blood\_flow\_contribution\_inkl\_\_volume \left(F\_in, vol (compartment\_1), \frac{species\_24}{vol (compartment\_1)}, \frac{CO2\_artery}{vol (artery)}\right)$$
(118)

$$Blood\_flow\_contribution\_inkl\_volume (F\_in, V\_c, Volume, Substrate, Product) \\ = \frac{2 \cdot F\_in}{V\_c} \cdot (Substrate - Product) \cdot Volume$$
 (119)

# 9.24 Reaction vPUMP\_neurons

This is an irreversible reaction of two reactants forming one product.

Name Na+\_exchange\_neurons\_extracellular\_space (n.a.)

SBO:0000185 transport reaction

### **Reaction equation**

species\_
$$3 + 3 \text{ Na\_neurons} \longrightarrow \text{ADP\_neurons}$$
 (120)

Table 63: Properties of each reactant.

Name	SBO
ATP Na+	
	Name ATP Na+

Table 64: Properties of each product.

Id	Name	SBO
ADP_neurons	ADP	

#### **Kinetic Law**

Derived unit contains undeclared units

$$v_{24} = vol \left(compartment\_2\right) \cdot vPUMP\_volume\_dependent \left(Sm\_n, vol \left(compartment\_2\right), \\ k\_pump, \frac{species\_3}{vol \left(compartment\_2\right)}, \frac{Na\_neurons}{vol \left(compartment\_2\right)}, K\_m\_Na\_pump\right)$$
 (121)

vPUMP\_volume\_dependent (Sm, Volume, k\_pump, ATP, Na, Km\_pump)

$$= \frac{\text{Sm}}{\text{Volume}} \cdot \text{k\_pump} \cdot \text{ATP} \cdot \text{Na} \cdot \left(1 + \frac{\text{ATP}}{\text{Km\_pump}}\right)^{1}$$
 (122)

vPUMP\_volume\_dependent (Sm, Volume, k\_pump, ATP, Na, Km\_pump)

$$= \frac{\text{Sm}}{\text{Volume}} \cdot \text{k\_pump} \cdot \text{ATP} \cdot \text{Na} \cdot \left(1 + \frac{\text{ATP}}{\text{Km\_pump}}\right)^{1}$$
(123)

# **9.25 Reaction** vPUMP\_astrocytes

This is an irreversible reaction of two reactants forming one product.

Name Na+\_exchange\_astrocytes\_extracellular\_space (n.a.)

SBO:0000185 transport reaction

## **Reaction equation**

species\_
$$5 + 3 \text{ Na}_{-}$$
astrocytes  $\longrightarrow \text{ADP}_{-}$ astrocytes (124)

Table 65: Properties of each reactant.

Id	Name	SBO
species_5	ATP	
${\tt Na\_astrocytes}$	Na+	

Table 66: Properties of each product.

	1	
Id	Name	SBO
ADP_astrocytes	ADP	

#### **Kinetic Law**

Derived unit contains undeclared units

$$v_{25} = vol (compartment\_3) \cdot vPUMP\_volume\_dependent \left(Sm\_g, vol (compartment\_3), \\ k\_pump, \frac{species\_5}{vol (compartment\_3)}, \frac{Na\_astrocytes}{vol (compartment\_3)}, K\_m\_Na\_pump\right)$$
 (125)

vPUMP\_volume\_dependent (Sm, Volume, k\_pump, ATP, Na, Km\_pump)

$$= \frac{\text{Sm}}{\text{Volume}} \cdot \text{k\_pump} \cdot \text{ATP} \cdot \text{Na} \cdot \left(1 + \frac{\text{ATP}}{\text{Km\_pump}}\right)^{1}$$
 (126)

vPUMP\_volume\_dependent (Sm, Volume, k\_pump, ATP, Na, Km\_pump)

$$= \frac{\mathrm{Sm}}{\mathrm{Volume}} \cdot \mathrm{k\_pump} \cdot \mathrm{ATP} \cdot \mathrm{Na} \cdot \left(1 + \frac{\mathrm{ATP}}{\mathrm{Km\_pump}}\right)^{\mathrm{l}} \tag{127}$$

### 9.26 Reaction vLEAK\_Na\_neurons

This is an irreversible reaction of one reactant forming one product.

Name LEAK\_Na\_neurons (n.a.)

SBO:0000185 transport reaction

# **Reaction equation**

$$Na\_extracellular\_space \longrightarrow Na\_neurons$$
 (128)

Table 67: Properties of each reactant.

Id	r	Name	
Na_	_extracellular_space	Na+	

Table 68: Properties of each product.

Id	Name	SBO
Na_neurons	Na+	

### **Kinetic Law**

Derived unit contains undeclared units

$$v_{26} = vLEAK_Na_inkl_Volume \left(Sm_n, g_Na_neurons, vol (compartment_2), F, RT, \frac{Na_extracellular_space}{vol (compartment_4)}, \frac{Na_neurons}{vol (compartment_2)}, Vm, vol (compartment_2)\right)$$
(129)

$$\begin{aligned} & vLEAK\_Na\_inkl\_\_Volume \left(Sm,gNA,Volume,F,RT,Na\_e,Na,Vm,Volume1\right) \\ & = \frac{Sm \cdot gNA}{Volume \cdot F} \cdot \left(\frac{RT}{F} \cdot \left(\frac{Na\_e}{Na}\right) - Vm\right) \cdot Volume1 \end{aligned}$$

# **9.27 Reaction** vLEAK\_Na\_astrocytes

This is an irreversible reaction of one reactant forming one product.

Name LEAK\_Na\_astrocytes (n.a)

SBO:0000185 transport reaction

### **Reaction equation**

$$Na\_extracellular\_space \longrightarrow Na\_astrocytes$$
 (131)

Table 69: Properties of each reactant.

Id	Name	
Naextracellular_space	Na+	

Table 70: Properties of each product.

Id	Name	SBO
Naastrocytes	Na+	

#### **Kinetic Law**

Derived unit contains undeclared units

$$v_{27} = vLEAK_Na_inkl_Volume \left(Sm_g,gNA,vol(compartment_3),F,RT, \\ \frac{Na_extracellular\_space}{vol(compartment_4)}, \frac{Na_eastrocytes}{vol(compartment_3)},Vm,vol(compartment_3)\right)$$
(132)

$$vLEAK\_Na\_inkl\_\_Volume (Sm, gNA, Volume, F, RT, Na\_e, Na, Vm, Volume 1)$$

$$= \frac{Sm \cdot gNA}{Volume \cdot F} \cdot \left(\frac{RT}{F} \cdot \left(\frac{Na\_e}{Na}\right) - Vm\right) \cdot Volume 1$$

$$(133)$$

Table 71: Properties of each parameter.

Id	Name	SBO Value Unit	Constant
gNA	gNA	0.004	$\blacksquare$

### 9.28 Reaction vSTIM

This is an irreversible reaction of one reactant forming one product.

**Name** Na+\_exchange\_extracellular\_space\_neurons (stimulation)

SBO:0000185 transport reaction

## **Reaction equation**

$$Na\_extracellular\_space \longrightarrow Na\_neurons$$
 (134)

### Reactant

Table 72: Properties of each reactant.

Id	Name	SBO
Na_extracellular_space	Na+	

## **Product**

Table 73: Properties of each product.

Id	Name	SBO
Na_neurons	Na+	

### **Kinetic Law**

**Derived unit** contains undeclared units

$$v_{28} = vStim_-with_volume(v_stim, vol(compartment_2))$$
 (135)

$$vStim_{with_volume}(vstim, Volume) = vstim \cdot Volume$$
 (136)

## 9.29 Reaction vGLU\_ne

This is an irreversible reaction of one reactant forming one product.

Name GLU\_exchange\_neurons\_extracellular\_space

SBO:0000185 transport reaction

Notes Glutamate release by neurons to extracellular space

## **Reaction equation**

$$GLU_neurons \longrightarrow GLU_extracellular_space$$
 (137)

Table 74: Properties of each reactant.

Id	Name	SBO
GLU_neurons	GLU	

Table 75: Properties of each product.

Id	Name	
GLU_extracellular_space	GLU	

#### **Kinetic Law**

**Derived unit** contains undeclared units

$$v_{29} = vGLU\_ne\_inkl\_Volume \left(v\_stim, R\_Na\_GLU, \frac{GLU\_neurons}{vol (compartment\_2)}, K\_m\_GLU, \frac{vol (compartment\_2)}{vol (compartment\_2)}\right)$$
(138)

$$vGLU\_ne\_inkl\_Volume (vSTIM, ratio\_Na\_GLU, GLU\_n, Km\_GLU, Volume) \\ = vSTIM \cdot ratio\_Na\_GLU \cdot \frac{GLU\_n}{GLU\_n + Km\_GLU} \cdot Volume$$
 (139)

# 9.30 Reaction vGLU\_eg

This is an irreversible reaction of one reactant forming two products.

Name GLU\_exchange\_extracellular\_space\_astrocytes

SBO:0000185 transport reaction

## **Reaction equation**

$$GLU\_extracellular\_space \longrightarrow GLU\_astrocytes + Na\_astrocytes$$
 (140)

### Reactant

Table 76: Properties of each reactant.

Id	Name	SBO
GLU_extracellular_space	GLU	

Table 77: Properties of each product.

Id	Name	SBO
GLU_astrocytes	GLU	
${\tt Na\_astrocytes}$	Na+	

**Derived unit** contains undeclared units

$$v_{30} = vGLU\_eg\_inkl\_Volumes \left(Vmax\_eg\_GLU\_wrt\_extracellular\_space, \\ \frac{GLU\_extracellular\_space}{vol (compartment\_4)}, K\_m\_GLU, vol (compartment\_4) \right)$$
 (141)

$$vGLU\_eg\_inkl\_Volumes (Vmax\_GLU, GLU\_e, K\_m\_GLU, Volume) = Vmax\_GLU \cdot \frac{GLU\_e}{GLU\_e + K\_m\_GLU} \cdot Volume$$

$$(142)$$

## 9.31 Reaction vGLU\_gn

This is an irreversible reaction of two reactants forming two products.

Name GLU\_exchange\_astrocytes\_neurons

SBO:0000185 transport reaction

### **Reaction equation**

$$GLU_astrocytes + species_5 \longrightarrow GLU_neurons + ADP_astrocytes$$
 (143)

### Reactants

Table 78: Properties of each reactant.

Id	Name	SBO
${\tt GLU\_astrocytes}$	GLU	
species_5	ATP	

Table 79: Properties of each product.

Id	Name	SBO
GLU_neurons	GLU	
$\mathtt{ADP}_\mathtt{astrocytes}$	ADP	

**Derived unit** contains undeclared units

$$v_{31} = vGLU\_gn\_inkl\_Volume \left(V\_gn\_max\_GLU, \frac{GLU\_astrocytes}{vol (compartment\_3)}, K\_m\_GLU, \frac{species\_5}{vol (compartment\_3)}, parameter\_14, vol (compartment\_3)\right)$$

$$(144)$$

$$vGLU\_gn\_inkl\_Volume \\ (Vmax\_GLU,GLU\_g,K\_m\_GLU,ATP\_g,K\_m\_ATP,Volume) \\ = Vmax\_GLU \cdot \frac{GLU\_g}{GLU\_g + K\_m\_GLU} \cdot \frac{ATP\_g}{ATP\_g + K\_m\_ATP} \cdot Volume$$
 (145)

### 9.32 Reaction inflow\_of\_dHb

This is an irreversible reaction of no reactant forming one product influenced by two modifiers.

Name inflow of dHb

SBO:0000631 pseudoreaction

## **Reaction equation**

$$\emptyset \xrightarrow{\text{O2\_artery, species\_23}} \text{dHb}$$
 (146)

#### **Modifiers**

Table 80: Properties of each modifier.

Id	Name	SBO
02_artery	O2	
species_23	O2	

Table 81: Properties of each product.

Id	Name	SBO
dHb	dHb	

**Derived unit** contains undeclared units

$$v_{32} = \text{vol} \left( \text{compartment\_1} \right) \cdot \text{vdHb\_in} \left( \text{F\_in}, \frac{\text{O2\_artery}}{\text{vol} \left( \text{artery} \right)}, \frac{\text{species\_23}}{\text{vol} \left( \text{compartment\_1} \right)} \right)$$
 (147)

$$vdHb_{in}(F_{in},O2_{a},O2_{c}) = F_{in} \cdot (O2_{a} - 2 \cdot O2_{c} - O2_{a})$$
 (148)

$$vdHb_{in}(F_{in},O2_{a},O2_{c}) = F_{in} \cdot (O2_{a} - 2 \cdot O2_{c} - O2_{a})$$
(149)

### 9.33 Reaction outflow\_of\_dHb

This is an irreversible reaction of one reactant forming no product.

Name outflow of dHb

SBO:0000631 pseudoreaction

### **Reaction equation**

$$dHb \longrightarrow \emptyset \tag{150}$$

## Reactant

Table 82: Properties of each reactant.

Id	Name	SBO
dHb	dHb	

### **Kinetic Law**

$$v_{33} = vol (compartment_1) \cdot vdHb\_out \left(F\_out, \frac{dHb}{vol (compartment_1)}, vol (venous\_balloon)\right)$$
(151)

$$vdHb\_out(F\_out, dHb, V\_v) = \frac{F\_out \cdot dHb}{V\_v}$$
 (152)

$$vdHb\_out(F\_out,dHb,V\_v) = \frac{F\_out \cdot dHb}{V\_v} \tag{153}$$

## 9.34 Reaction ATPase\_neurons

This is an irreversible reaction of one reactant forming one product.

Name ATPase\_neurons (n.a.)

SBO:0000631 pseudoreaction

## **Reaction equation**

$$species_3 \longrightarrow ADP\_neurons \tag{154}$$

### Reactant

Table 83: Properties of each reactant.

Id	Name	SBO
species_3	ATP	

### **Product**

Table 84: Properties of each product.

Id	Name	SBO
ADP_neurons	ADP	

#### **Kinetic Law**

$$v_{34} = vol\left(compartment\_2\right) \cdot vATPase\left(VmaxATPase, \frac{species\_3}{vol\left(compartment\_2\right)}, K_m\_ATP\_ATPase\right) \tag{155}$$

$$vATPase\left(VmaxATPase,ATP,Km\_ATP\right) = VmaxATPase \cdot \frac{ATP}{ATP + Km\_ATP} \qquad (156)$$

$$vATPase\left(VmaxATPase,ATP,Km\_ATP\right) = VmaxATPase \cdot \frac{ATP}{ATP + Km\_ATP} \qquad (157)$$

Table 85: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
VmaxATPase	VmaxATPase		0.07		

# 9.35 Reaction ATPase\_astrocytes

This is an irreversible reaction of one reactant forming one product.

Name ATPase\_astrocytes (n.a.)

SBO:0000631 pseudoreaction

# **Reaction equation**

species\_5 
$$\longrightarrow$$
 ADP\_astrocytes (158)

### Reactant

Table 86: Properties of each reactant.

Id	Name	SBO
species_5	ATP	

## **Product**

Table 87: Properties of each product.

	F	
Id	Name	SBO
$\mathtt{ADP}_\mathtt{astrocytes}$	ADP	

### **Kinetic Law**

$$v_{35} = \text{vol} \left( \text{compartment\_3} \right) \cdot \text{vATPase} \left( \text{VmaxATPase}, \frac{\text{species\_5}}{\text{vol} \left( \text{compartment\_3} \right)}, \text{K\_m\_ATP\_ATPase} \right)$$
(159)

$$vATPase\left(VmaxATPase,ATP,Km\_ATP\right) = VmaxATPase \cdot \frac{ATP}{ATP + Km\_ATP} \qquad (160)$$

$$vATPase\left(VmaxATPase,ATP,Km\_ATP\right) = VmaxATPase \cdot \frac{ATP}{ATP + Km\_ATP} \qquad (161)$$

Table 88: Properties of each parameter.

Id	Name	SBO Value Unit	Constant
VmaxATPase	VmaxATPase	0.035	

### 9.36 Reaction AK\_neurons

This is a reversible reaction of one reactant forming two products.

Name AK\_neurons (R00127)

# **Reaction equation**

$$2 \text{ ADP\_neurons} \Longrightarrow \text{species\_}3 + \text{AMP\_neurons}$$
 (162)

#### Reactant

Table 89: Properties of each reactant.

Id	Name	SBO
ADP_neurons	ADP	

### **Products**

Table 90: Properties of each product.

Id	Name	SBO
species_3	ATP	
$\mathtt{AMP\_neurons}$	AMP	

### **Kinetic Law**

$$v_{36} = \text{vol (compartment\_2)} \cdot \left( \text{k1} \cdot \left( \frac{\text{ADP\_neurons}}{\text{vol (compartment\_2)}} \right)^2 - \text{k2} \right)$$

$$\cdot \frac{\text{species\_3}}{\text{vol (compartment\_2)}} \cdot \frac{\text{AMP\_neurons}}{\text{vol (compartment\_2)}} \right)$$
(163)

Table 91: Properties of each parameter.

Id	Name	SBO Value Unit	Constant
k1	k1	1000.0	
k2	k2	920.0	$\square$

# 9.37 Reaction AK\_astrocytes

This is a reversible reaction of one reactant forming two products.

Name AK\_astrocytes (R00127)

## **Reaction equation**

$$2 \text{ ADP\_astrocytes} \Longrightarrow \text{species\_5} + \text{AMP\_astrocytes}$$
 (164)

#### Reactant

Table 92: Properties of each reactant.

Id	Name	SBO
ADP_astrocytes	ADP	

#### **Products**

Table 93: Properties of each product.

Id	Name	SBO
species_5	ATP	
AMP_astrocytes	AMP	

### **Kinetic Law**

$$v_{37} = \text{vol} \left(\text{compartment}\_3\right) \cdot \left(\text{k1} \cdot \left(\frac{\text{ADP\_astrocytes}}{\text{vol} \left(\text{compartment}\_3\right)}\right)^2 - \text{k2}\right)$$

$$\cdot \frac{\text{species}\_5}{\text{vol} \left(\text{compartment}\_3\right)} \cdot \frac{\text{AMP\_astrocytes}}{\text{vol} \left(\text{compartment}\_3\right)}$$
(165)

Table 94: Properties of each parameter.

Id	Name	SBO Value Unit	Constant
k1	k1	1000.0	
k2	k2	920.0	$\square$

# 9.38 Reaction CK\_astrocytes\_forward\_\_R01881

This is a reversible reaction of two reactants forming two products.

Name CK\_astrocytes (R01881)

## **Reaction equation**

ADP\_astrocytes + species\_22 
$$\rightleftharpoons$$
 species\_5 + Cr\_astrocytes (166)

#### Reactants

Table 95: Properties of each reactant.

Id	Name	SBO
ADP_astrocytes species_22	ADP PCr	

#### **Products**

Table 96: Properties of each product.

Id	Name	SBO
species_5	ATP	
${\tt Cr\_astrocytes}$	Cr	

#### **Kinetic Law**

$$v_{38} = \text{vol (compartment\_3)} \cdot \left( \text{k1} \cdot \frac{\text{ADP\_astrocytes}}{\text{vol (compartment\_3)}} \cdot \frac{\text{species\_22}}{\text{vol (compartment\_3)}} - \text{k2} \right)$$

$$\cdot \frac{\text{species\_5}}{\text{vol (compartment\_3)}} \cdot \frac{\text{Cr\_astrocytes}}{\text{vol (compartment\_3)}} \right)$$
(167)

Table 97: Properties of each parameter.

Id	Name	SBO Value Unit	Constant
k1	k1	0.50	
k2	k2	0.01	$\square$

### 9.39 Reaction CK\_neurons\_forward\_\_R01881

This is a reversible reaction of two reactants forming two products.

Name CK\_neurons (R01881)

## **Reaction equation**

$$species_21 + ADP\_neurons \Longrightarrow species_3 + Cr\_neurons$$
 (168)

#### Reactants

Table 98: Properties of each reactant.

Id	Name	SBO
species_21	PCr	
ADP_neurons	ADP	

#### **Products**

Table 99: Properties of each product.

Id	Name	SBO
species_3	ATP	
$\mathtt{Cr}\_\mathtt{neurons}$	Cr	

#### **Kinetic Law**

$$v_{39} = \text{vol (compartment\_2)} \cdot \left( \text{k1} \cdot \frac{\text{species\_21}}{\text{vol (compartment\_2)}} \cdot \frac{\text{ADP\_neurons}}{\text{vol (compartment\_2)}} - \text{k2} \right)$$

$$\cdot \frac{\text{species\_3}}{\text{vol (compartment\_2)}} \cdot \frac{\text{Cr\_neurons}}{\text{vol (compartment\_2)}} \right)$$
(169)

Table 100: Properties of each parameter.

Id	Name	SBO Value Unit	Constant
k1	k1	0.50	Ø
k2	k2	0.01	

## **9.40 Reaction** LDH\_astrocytes\_forward\_\_R00703

This is a reversible reaction of two reactants forming two products.

Name LDH\_astrocytes (R00703)

SBO:0000176 biochemical reaction

### **Reaction equation**

$$species_17 + species_13 \Longrightarrow species_19 + NAD_astrocytes$$
 (170)

#### Reactants

Table 101: Properties of each reactant.

Id	Name	SBO
species_17	PYR	
species_13	NADH	

#### **Products**

Table 102: Properties of each product.

Id	Name	SBO
species_19	LAC	
${\tt NAD\_astrocytes}$	NAD	

#### **Kinetic Law**

$$v_{40} = \text{vol} \left( \text{compartment\_3} \right) \cdot \left( \text{k1} \cdot \frac{\text{species\_17}}{\text{vol} \left( \text{compartment\_3} \right)} \cdot \frac{\text{species\_13}}{\text{vol} \left( \text{compartment\_3} \right)} - \text{k2} \right)$$

$$\cdot \frac{\text{species\_19}}{\text{vol} \left( \text{compartment\_3} \right)} \cdot \frac{\text{NAD\_astrocytes}}{\text{vol} \left( \text{compartment\_3} \right)}$$

$$(171)$$

Table 103: Properties of each parameter.

Id	Name	SBO Value Unit	Constant
k1	k1	780.0	$\overline{Z}$
k2	k2	32.0	$   \overline{\checkmark} $

#### 9.41 Reaction LDH\_neurons\_forward\_\_R00703

This is a reversible reaction of two reactants forming two products.

Name LDH\_neurons (R00703)

SBO:0000176 biochemical reaction

### **Reaction equation**

$$species_15 + species_11 \Longrightarrow species_18 + NAD_neurons$$
 (172)

#### Reactants

Table 104: Properties of each reactant.

Id	Name	SBO
species_15	PYR	
species_11	NADH	

#### **Products**

Table 105: Properties of each product.

Id	Name	SBO
species_18	LAC	
$\mathtt{NAD\_neurons}$	NAD	

#### **Kinetic Law**

$$v_{41} = \text{vol} \left( \text{compartment\_2} \right) \cdot \left( \text{k1} \cdot \frac{\text{species\_15}}{\text{vol} \left( \text{compartment\_2} \right)} \cdot \frac{\text{species\_11}}{\text{vol} \left( \text{compartment\_2} \right)} - \text{k2} \right)$$

$$\cdot \frac{\text{species\_18}}{\text{vol} \left( \text{compartment\_2} \right)} \cdot \frac{\text{NAD\_neurons}}{\text{vol} \left( \text{compartment\_2} \right)}$$

$$(173)$$

Table 106: Properties of each parameter.

Id	Name	SBO Value Unit	Constant
k1	k1	2000.0	
k2	k2	15.0	

# **9.42 Reaction** ZWF\_astrocytes\_\_R02736

This is an irreversible reaction of two reactants forming two products.

Name ZWF\_astrocytes (R02736)

SBO:0000176 biochemical reaction

## **Reaction equation**

species\_
$$6 + NADP_a$$
strocytes  $\longrightarrow G6L_a$ strocytes  $+ NADPH_a$ strocytes (174)

#### **Reactants**

Table 107: Properties of each reactant.

Id	Name	SBO
species_6 NADP_astrocytes	G6P NADP	

#### **Products**

Table 108: Properties of each product.

	•	
Id	Name	SBO
G6L_astrocytes	G6L	
NADPH_astrocytes	NADPH	

### **Kinetic Law**

 $\textit{v}_{42} = vol\left(compartment\_3\right) \cdot modular\_rate\_law\_for\_two\_substrates\_\_two\_products\left(Vmax, was a constant and was a constant$ 

$$K\_S1, K\_S2, \frac{species\_6}{vol \, (compartment\_3)}, \frac{NADP\_astrocytes}{vol \, (compartment\_3)}, \frac{G6L\_astrocytes}{vol \, (compartment\_3)}, \frac{NADPH\_astrocytes}{vol \, (compartment\_3)}, Keq, K\_P1, K\_P2 \right)$$

$$(175)$$

 $modular\_rate\_law\_for\_two\_substrates\_\_two\_products (Vmax, K\_S1,$ 

$$K\_S2,S1,S2,P1,P2,Keq,K\_P1,K\_P2) = Vmax \cdot \frac{1}{K\_S1 \cdot K\_S2}$$

$$S1 \cdot S2 - \frac{P1 \cdot P2}{Keq}$$

$$(176)$$

$$\frac{(1 + \frac{S1}{K\_S1}) \cdot (1 + \frac{S2}{K\_S2}) + (1 + \frac{P1}{K\_P1}) \cdot (1 + \frac{P2}{K\_P2}) - 1}{(1 + \frac{P2}{K\_P2}) \cdot (1 + \frac{P2}{K\_P2}) - 1}$$

modular\_rate\_law\_for\_two\_substrates\_\_two\_products (Vmax, K\_S1,

$$K\_S2, S1, S2, P1, P2, Keq, K\_P1, K\_P2) = Vmax \cdot \frac{1}{K\_S1 \cdot K\_S2}$$

$$\cdot \frac{S1 \cdot S2 - \frac{P1 \cdot P2}{Keq}}{\left(1 + \frac{S1}{K\_S1}\right) \cdot \left(1 + \frac{S2}{K\_S2}\right) + \left(1 + \frac{P1}{K\_P1}\right) \cdot \left(1 + \frac{P2}{K\_P2}\right) - 1}$$

$$(177)$$

Table 109: Properties of each parameter.

Id Name SBO Value Unit	Constant
	Constant
Vmax Vmax 0.291	$\overline{Z}$
$K_{-}S1$ $K_{-}S1$ $6.91392 \cdot 10^{-5}$	
$K_{-}S2$ $K_{-}S2$ $1.31616 \cdot 10^{-5}$	$\overline{\mathbf{Z}}$
Keq Keq 22906.400	$\overline{\mathbf{Z}}$
K_P1	$\overline{\mathbf{Z}}$
$K_{-}P2$ $K_{-}P2$ $5.0314 \cdot 10^{-4}$	$\overline{\mathbf{Z}}$

#### 9.43 Reaction ZWF\_neurons\_\_R02736

This is an irreversible reaction of two reactants forming two products.

Name ZWF\_neurons (R02736)

SBO:0000176 biochemical reaction

#### **Reaction equation**

species\_2 + NADP\_neurons 
$$\longrightarrow$$
 G6L\_neurons + NADPH\_neurons (178)

### **Reactants**

Table 110: Properties of each reactant.

Id	Name	SBO
species_2 NADP_neurons	G6P NADP	

#### **Products**

Table 111: Properties of each product.

Id	Name	SBO
G6L_neurons NADPH_neurons	G6L NADPH	

#### **Kinetic Law**

#### Derived unit contains undeclared units

$$v_{43} = vol \\ (compartment\_2) \\ \cdot \\ modular\_rate\_law\_for\_two\_substrates\_two\_products \\ \left( \\ Vmax, \\ \frac{K\_S1, K\_S2}{vol \\ (compartment\_2)}, \\ \frac{NADP\_neurons}{vol \\ (compartment\_2)}, \\ \frac{NADPH\_neurons}{vol \\ (compartment\_2)}, \\ Keq, K\_P1, K\_P2 \right) \\ (179)$$

 $modular\_rate\_law\_for\_two\_substrates\_\_two\_products (Vmax, K\_S1,$ 

$$K\_S2, S1, S2, P1, P2, Keq, K\_P1, K\_P2) = Vmax \cdot \frac{1}{K\_S1 \cdot K\_S2}$$

$$\cdot \frac{S1 \cdot S2 - \frac{P1 \cdot P2}{Keq}}{\left(1 + \frac{S1}{K\_S1}\right) \cdot \left(1 + \frac{S2}{K\_S2}\right) + \left(1 + \frac{P1}{K\_P1}\right) \cdot \left(1 + \frac{P2}{K\_P2}\right) - 1}$$
(180)

 $modular\_rate\_law\_for\_two\_substrates\_\_two\_products (Vmax, K\_S1,$ 

$$K\_S2, S1, S2, P1, P2, Keq, K\_P1, K\_P2) = Vmax \cdot \frac{1}{K\_S1 \cdot K\_S2}$$

$$\cdot \frac{S1 \cdot S2 - \frac{P1 \cdot P2}{Keq}}{\left(1 + \frac{S1}{K\_S1}\right) \cdot \left(1 + \frac{S2}{K\_S2}\right) + \left(1 + \frac{P1}{K\_P1}\right) \cdot \left(1 + \frac{P2}{K\_P2}\right) - 1}$$
(181)

Table 112: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
Vmax	Vmax		0.586		$ \overline{\checkmark} $
K_S1	$K_{-}S1$	6	$5.91392 \cdot 10^{-3}$	5	$\overline{\mathbf{Z}}$
K_S2	$K_{-}S2$	1	1.31616 · 10-	5	
Keq	Keq		22906.400		
K_P1	K_P1		0.018		
K_P2	K_P2		$5.0314 \cdot 10^{-6}$	4	$\overline{\mathbf{Z}}$

## 9.44 Reaction SOL\_neurons\_R02035

This is an irreversible reaction of one reactant forming one product.

Name SOL\_neurons (R02035)

SBO:0000176 biochemical reaction

## **Reaction equation**

$$G6L\_neurons \longrightarrow P6G\_neurons$$
 (182)

### Reactant

Table 113: Properties of each reactant.

Id	Name	SBO
G6L_neurons	G6L	

#### **Product**

Table 114: Properties of each product.

Id	Name	SBO
P6G_neurons	P6G	

## **Kinetic Law**

$$v_{44} = vol (compartment\_2) \cdot modular\_rate\_law\_for\_one\_substrate\_\_one\_product \left(Vmax, \frac{G6L\_neurons}{vol (compartment\_2)}, \frac{P6G\_neurons}{vol (compartment\_2)}, Keq, K\_P1\right)$$
 (183)

 $modular\_rate\_law\_for\_one\_substrate\_one\_product(Vmax, K\_S1, S1, P1, Keq, K\_P1)$ 

$$= V max \cdot \frac{1}{K\_S1} \cdot \frac{S1 - \frac{P1}{Keq}}{1 + \frac{S1}{K\_S1} + 1 + \frac{P1}{K\_P1} - 1}$$
(184)

 $modular\_rate\_law\_for\_one\_substrate\_one\_product(Vmax, K\_S1, S1, P1, Keq, K\_P1)$ 

$$= V \max \cdot \frac{1}{K \_S1} \cdot \frac{S1 - \frac{P1}{Keq}}{1 + \frac{S1}{K \_S1} + 1 + \frac{P1}{K \_P1} - 1}$$
(185)

Table 115: Properties of each parameter.

	- I	I	
Name	SBO V	Value Unit	Constant
Vmax		0.373	lacksquare
K_S1		0.018	
Keq	531	174.000	
K_P1		2.286	$\mathbf{Z}$
	Vmax K_S1 Keq	Name SBO V Vmax K_S1 Keq 531	Vmax 0.373 K_S1 0.018 Keq 531174.000

## 9.45 Reaction SOL\_astrocytes\_\_R02035

This is an irreversible reaction of one reactant forming one product.

Name SOL\_astrocytes (R02035)

SBO:0000176 biochemical reaction

#### **Reaction equation**

$$G6L\_astrocytes \longrightarrow P6G\_astrocytes$$
 (186)

#### Reactant

Table 116: Properties of each reactant.

Id	Name	SBO
G6L_astrocytes	G6L	

#### **Product**

Table 117: Properties of each product

Id	Name	
P6G_astrocytes	P6G	

#### **Kinetic Law**

**Derived unit** contains undeclared units

$$v_{45} = vol (compartment\_3) \cdot modular\_rate\_law\_for\_one\_substrate\_\_one\_product \left(Vmax, \\ K\_S1, \frac{G6L\_astrocytes}{vol (compartment\_3)}, \frac{P6G\_astrocytes}{vol (compartment\_3)}, Keq, K\_P1\right)$$
 (187)

 $modular\_rate\_law\_for\_one\_substrate\_one\_product(Vmax, K\_S1, S1, P1, Keq, K\_P1)$ 

$$= V max \cdot \frac{1}{K\_S1} \cdot \frac{S1 - \frac{Pl}{Keq}}{1 + \frac{Sl}{K\_S1} + 1 + \frac{Pl}{K\_Pl} - 1}$$
 (188)

 $modular\_rate\_law\_for\_one\_substrate\_one\_product(Vmax, K\_S1, S1, P1, Keq, K\_P1)$ 

$$= V \max \cdot \frac{1}{K \cdot S1} \cdot \frac{S1 - \frac{P1}{Keq}}{1 + \frac{S1}{K \cdot S1} + 1 + \frac{P1}{K \cdot P1} - 1}$$
(189)

Table 118: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
Vmax	Vmax		0.185		$\overline{Z}$
KS1	$K_{-}S1$		0.018		
Keq	Keq	5	531174.000		
K_P1	K_P1		2.286		$\checkmark$

## 9.46 Reaction GND\_neurons\_\_\_R01528

This is a reversible reaction of two reactants forming two products.

Name GND\_neurons (R01528)

SBO:0000176 biochemical reaction

#### **Reaction equation**

$$P6G_neurons + NADP_neurons \rightleftharpoons Ru5P_neurons + NADPH_neurons$$
 (190)

#### **Reactants**

Table 119: Properties of each reactant.

Id	Name	SBO
P6G_neurons	P6G	
${\tt NADP\_neurons}$	NADP	

#### **Products**

Table 120: Properties of each product.

Id	Name	SBO
Ru5P_neurons NADPH_neurons	Ru5P NADPH	

#### **Kinetic Law**

### Derived unit contains undeclared units

$$v_{46} = vol (compartment\_2) \cdot modular\_rate\_law\_for\_two\_substrates\_\_two\_products \left( Vmax, \\ K\_S1, K\_S2, \frac{P6G\_neurons}{vol (compartment\_2)}, \frac{NADP\_neurons}{vol (compartment\_2)}, \frac{Ru5P\_neurons}{vol (compartment\_2)}, \\ \frac{NADPH\_neurons}{vol (compartment\_2)}, Keq, K\_P1, K\_P2 \right)$$

$$(191)$$

 $modular\_rate\_law\_for\_two\_substrates\_\_two\_products (Vmax, K\_S1,$ 

$$K\_S2, S1, S2, P1, P2, Keq, K\_P1, K\_P2) = Vmax \cdot \frac{1}{K\_S1 \cdot K\_S2}$$

$$\cdot \frac{S1 \cdot S2 - \frac{P1 \cdot P2}{Keq}}{\left(1 + \frac{S1}{K\_S1}\right) \cdot \left(1 + \frac{S2}{K\_S2}\right) + \left(1 + \frac{P1}{K\_P1}\right) \cdot \left(1 + \frac{P2}{K\_P2}\right) - 1}$$

$$(192)$$

 $modular\_rate\_law\_for\_two\_substrates\_\_two\_products (Vmax, K\_S1,$ 

$$K\_S2,S1,S2,P1,P2,Keq,K\_P1,K\_P2) = V \max \cdot \frac{1}{K\_S1 \cdot K\_S2}$$

$$\cdot \frac{S1 \cdot S2 - \frac{P1 \cdot P2}{Keq}}{\left(1 + \frac{S1}{K\_S1}\right) \cdot \left(1 + \frac{S2}{K\_S2}\right) + \left(1 + \frac{P1}{K\_P1}\right) \cdot \left(1 + \frac{P2}{K\_P2}\right) - 1}$$
(193)

Table 121: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
Vmax	Vmax		2.658		$\overline{Z}$
K_S1	$K_{-}S1$		$.23421 \cdot 10^{-3}$		
K_S2	$K_{-}S2$	3	$.11043 \cdot 10^{-6}$	6	
Keq	Keq		$4.0852 \cdot 10^{\circ}$	7	
K_P1	K_P1		0.054		
$K_{-}P2$	K_P2		$5.0314 \cdot 10^{-4}$	4	$\checkmark$

## **9.47 Reaction** GND\_astrocytes\_\_R01528

This is an irreversible reaction of two reactants forming two products.

Name GND\_astrocytes (R01528)

SBO:0000176 biochemical reaction

## **Reaction equation**

$$P6G\_astrocytes + NADP\_astrocytes \longrightarrow Ru5P\_astrocytes + NADPH\_astrocytes$$
 (194)

#### **Reactants**

Table 122: Properties of each reactant.

Id	Name	SBO
P6G_astrocytes	P6G	
NADP_astrocytes	NADP	

### **Products**

Table 123: Properties of each product.

Table 123. I Toperties of each product.			
Id	Name	SBO	
Ru5P_astrocytes NADPH_astrocytes	Ru5P NADPH		

#### **Kinetic Law**

#### **Derived unit** contains undeclared units

$$v_{47} = vol (compartment\_3) \cdot modular\_rate\_law\_for\_two\_substrates\_\_two\_products \left( Vmax, K\_S1, K\_S2, \frac{P6G\_astrocytes}{vol (compartment\_3)}, \frac{NADP\_astrocytes}{vol (compartment\_3)}, \frac{Ru5P\_astrocytes}{vol (compartment\_3)}, \frac{NADPH\_astrocytes}{vol (compartment\_3)}, Keq, K\_P1, K\_P2 \right)$$

$$(195)$$

 $modular\_rate\_law\_for\_two\_substrates\_\_two\_products (Vmax, K\_S1,$ 

$$K\_S2,S1,S2,P1,P2,Keq,K\_P1,K\_P2) = Vmax \cdot \frac{1}{K\_S1 \cdot K\_S2}$$

$$\cdot \frac{S1 \cdot S2 - \frac{P1 \cdot P2}{Keq}}{\left(1 + \frac{S1}{K\_S1}\right) \cdot \left(1 + \frac{S2}{K\_S2}\right) + \left(1 + \frac{P1}{K\_P1}\right) \cdot \left(1 + \frac{P2}{K\_P2}\right) - 1}$$
(196)

 $modular\_rate\_law\_for\_two\_substrates\_two\_products (Vmax, K\_S1,$ 

$$K\_S2,S1,S2,P1,P2,Keq,K\_P1,K\_P2) = Vmax \cdot \frac{1}{K\_S1 \cdot K\_S2}$$

$$S1 \cdot S2 - \frac{P1 \cdot P2}{Keq}$$

$$(197)$$

$$\frac{(1 + \frac{S1}{K\_S1}) \cdot (1 + \frac{S2}{K\_S2}) + (1 + \frac{P1}{K\_P1}) \cdot (1 + \frac{P2}{K\_P2}) - 1}{(1 + \frac{P2}{K\_P2}) - 1}$$

Table 124: Properties of each parameter.

Id         Name         SBO         Value         Unit         Constant           Vmax         Vmax         1.317         ✓           K_S1         K_S1         3.23421 · 10 <sup>-5</sup> ✓           K_S2         K_S2         3.11043 · 10 <sup>-6</sup> ✓           Keq         Keq         4.0852 · 10 <sup>7</sup> ✓           K_P1         K_P1         5.0314 · 10 <sup>-4</sup> ✓           K_P2         0.054         ✓			·· F	F		
K_S1       K_S1 $3.23421 \cdot 10^{-5}$ K_S2       K_S2 $3.11043 \cdot 10^{-6}$ Keq $4.0852 \cdot 10^7$ K_P1 $5.0314 \cdot 10^{-4}$	Id	Name	SBO	Value	Unit	Constant
K_S2 $K_S2$ $3.11043 \cdot 10^{-6}$ $2$ Keq $K_S2 \cdot 10^7$ $2$ K_P1 $K_S2 \cdot 10^7$ $2$	Vmax	Vmax		1.317		$ \overline{\square} $
Keq $4.0852 \cdot 10^7$ K_P1 $5.0314 \cdot 10^{-4}$	K_S1	K_S1	3	$.23421 \cdot 10^{-3}$	5	$\overline{\mathbf{Z}}$
Keq $4.0852 \cdot 10^7$ K_P1 $5.0314 \cdot 10^{-4}$	K_S2	KS2	3	$.11043 \cdot 10^{-6}$	6	$\overline{\checkmark}$
K_P1 $K_P1$ 5.0314·10 <sup>-4</sup>	Keq	Keq		$4.0852 \cdot 10^{\circ}$	7	
— <u> </u>	K_P1	K_P1		$5.0314 \cdot 10^{-4}$	4	
	K_P2	K_P2		0.054		

### 9.48 Reaction RPE\_neurons\_\_R01529

This is a reversible reaction of one reactant forming one product.

Name RPE\_neurons (R01529)

SBO:0000176 biochemical reaction

#### **Reaction equation**

$$Ru5P_neurons \rightleftharpoons X5P_neurons$$
 (198)

#### Reactant

Table 125: Properties of each reactant.

Id	Name	SBO
Ru5P_neurons	Ru5P	

#### **Product**

Table 126: Properties of each product.

Id	Name	SBO
X5P_neurons	X5P	

#### **Kinetic Law**

#### Derived unit contains undeclared units

$$v_{48} = vol \left( compartment\_2 \right) \cdot modular\_rate\_law\_for\_one\_substrate\_\_one\_product \left( Vmax, \\ K\_S1, \frac{Ru5P\_neurons}{vol \left( compartment\_2 \right)}, \frac{X5P\_neurons}{vol \left( compartment\_2 \right)}, Keq, K\_P1 \right)$$
 (199)

 $modular\_rate\_law\_for\_one\_substrate\_\_one\_product (Vmax, K\_S1, S1, P1, Keq, K\_P1)$ 

$$= V \max \cdot \frac{1}{K\_S1} \cdot \frac{S1 - \frac{Pl}{Keq}}{1 + \frac{S1}{K\_S1} + 1 + \frac{Pl}{K\_P1} - 1}$$
(200)

 $modular\_rate\_law\_for\_one\_substrate\_\_one\_product(Vmax, K\_S1, S1, P1, Keq, K\_P1)$ 

$$= V \max \cdot \frac{1}{K\_S1} \cdot \frac{S1 - \frac{P1}{Keq}}{1 + \frac{S1}{K\_S1} + 1 + \frac{P1}{K\_P1} - 1}$$
 (201)

Table 127: Properties of each parameter.

Id	Name	SBO Value Unit	Constant
Vmax	Vmax	0.016	$\overline{Z}$
K_S1	K_S1	0.054	
Keq	Keq	39.257	
K_P1	K_P1	0.603	

## 9.49 Reaction RPE\_astrocytes\_\_R01529

This is a reversible reaction of one reactant forming one product.

Name RPE\_astrocytes (R01529)

SBO:0000176 biochemical reaction

#### **Reaction equation**

Ru5P\_astrocytes 
$$\rightleftharpoons$$
 X5P\_astrocytes (202)

#### Reactant

Table 128: Properties of each reactant.

Id	Name	SBO
Ru5P_astrocytes	Ru5P	

#### **Product**

Table 129: Properties of each product.

Id	Name	SBO
X5P_astrocytes	X5P	

#### **Kinetic Law**

$$v_{49} = vol (compartment\_3) \cdot modular\_rate\_law\_for\_one\_substrate\_\_one\_product \left(Vmax, \frac{Ru5P\_astrocytes}{vol (compartment\_3)}, \frac{X5P\_astrocytes}{vol (compartment\_3)}, Keq, K\_P1\right)$$
 (203)

 $modular\_rate\_law\_for\_one\_substrate\_\_one\_product(Vmax, K\_S1, S1, P1, Keq, K\_P1)$ 

$$= V \max \cdot \frac{1}{K \cdot S1} \cdot \frac{S1 - \frac{P1}{Keq}}{1 + \frac{S1}{KS1} + 1 + \frac{P1}{KP1} - 1}$$
(204)

$$\begin{split} & \text{modular\_rate\_law\_for\_one\_substrate\_\_one\_product} \left( Vmax, K\_S1, S1, P1, Keq, K\_P1 \right) \\ &= Vmax \cdot \frac{1}{K\_S1} \cdot \frac{S1 - \frac{P1}{Keq}}{1 + \frac{S1}{K\_S1} + 1 + \frac{P1}{K\_P1} - 1} \end{split} \tag{205}$$

Table 130: Properties of each parameter.

Id	Name	SBO Value Unit	Constant
Vmax	Vmax	0.008	
K_S1	K_S1	0.054	
Keq	Keq	39.257	
K_P1	K_P1	0.603	

## 9.50 Reaction RKI\_astrocytes\_\_R01056

This is a reversible reaction of one reactant forming one product.

Name RKI\_astrocytes (R01056)

SBO:0000176 biochemical reaction

### **Reaction equation**

Ru5P\_astrocytes 
$$\rightleftharpoons$$
 R5P\_astrocytes (206)

#### Reactant

Table 131: Properties of each reactant.

Id	Name	SBO
Ru5P_astrocytes	Ru5P	

### **Product**

Table 132: Properties of each product.

Id	Name	SBO
R5P_astrocytes	R5P	

#### **Kinetic Law**

**Derived unit** contains undeclared units

$$v_{50} = vol (compartment\_3) \cdot modular\_rate\_law\_for\_one\_substrate\_one\_product \left(Vmax, \frac{Ru5P\_astrocytes}{vol (compartment\_3)}, \frac{R5P\_astrocytes}{vol (compartment\_3)}, Keq, K\_P1\right)$$

$$(207)$$

 $modular\_rate\_law\_for\_one\_substrate\_\_one\_product(Vmax, K\_S1, S1, P1, Keq, K\_P1)$ 

$$= V \max \cdot \frac{1}{K_{-}S1} \cdot \frac{S1 - \frac{P1}{Keq}}{1 + \frac{S1}{K-S1} + 1 + \frac{P1}{K-P1} - 1}$$
(208)

 $modular\_rate\_law\_for\_one\_substrate\_one\_product(Vmax, K\_S1, S1, P1, Keq, K\_P1)$ 

$$= V \max \cdot \frac{1}{K\_S1} \cdot \frac{S1 - \frac{P1}{Keq}}{1 + \frac{S1}{K\_S1} + 1 + \frac{P1}{K\_P1} - 1}$$
(209)

Table 133: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
Vmax	Vmax	8	3.21984 · 10 <sup>-4</sup>	4	$\overline{Z}$
K_S1	K_S1		0.054		$   \overline{\mathscr{L}} $
Keq	Keq		35.453		$   \overline{\mathscr{L}} $
K_P1	K_P1		0.778		$\checkmark$

#### 9.51 Reaction RKI\_neurons\_\_R01056

This is a reversible reaction of one reactant forming one product.

Name RKI\_neurons (R01056)

SBO:0000176 biochemical reaction

#### **Reaction equation**

$$Ru5P_neurons \rightleftharpoons R5P_neurons$$
 (210)

#### Reactant

Table 134: Properties of each reactant.

Id	Name	SBO
Ru5P_neurons	Ru5P	

#### **Product**

Table 135: Properties of each product.

Id	Name	SBO
R5P_neurons	R5P	

### **Kinetic Law**

#### **Derived unit** contains undeclared units

$$v_{51} = vol\left(compartment\_2\right) \cdot modular\_rate\_law\_for\_one\_substrate\_\_one\_product\left(Vmax, \\ K\_S1, \frac{Ru5P\_neurons}{vol\left(compartment\_2\right)}, \frac{R5P\_neurons}{vol\left(compartment\_2\right)}, Keq, K\_P1\right)$$
 (211)

 $modular\_rate\_law\_for\_one\_substrate\_one\_product(Vmax, K\_S1, S1, P1, Keq, K\_P1)$ 

$$= V max \cdot \frac{1}{K\_S1} \cdot \frac{S1 - \frac{P1}{Keq}}{1 + \frac{S1}{K\_S1} + 1 + \frac{P1}{K\_P1} - 1}$$
 (212)

 $modular\_rate\_law\_for\_one\_substrate\_\_one\_product (Vmax, K\_S1, S1, P1, Keq, K\_P1)$ 

$$= V \max \cdot \frac{1}{K \cdot S1} \cdot \frac{S1 - \frac{P1}{Keq}}{1 + \frac{S1}{K \cdot S1} + 1 + \frac{P1}{K \cdot P1} - 1}$$
(213)

Table 136: Properties of each parameter.

Id	Name	SBO Value Unit	Constant
Vmax	Vmax	0.002	
K_S1	K_S1	0.054	$\square$
Keq	Keq	35.453	$\square$
K_P1	K_P1	0.778	$\square$

## 9.52 Reaction TKL\_1\_astrocytes\_\_R01641

This is an irreversible reaction of two reactants forming two products.

Name TKL-1\_astrocytes (R01641)

SBO:0000176 biochemical reaction

## **Reaction equation**

$$X5P_astrocytes + R5P_astrocytes \longrightarrow species_10 + S7P_astrocytes$$
 (214)

#### **Reactants**

Table 137: Properties of each reactant.

Id	Name	SBO
X5P_astrocytes	X5P	
R5P_astrocytes	R5P	

### **Products**

Table 138: Properties of each product.

Id	Name	SBO
species_10 S7P_astrocytes	GAP S7P	

## **Kinetic Law**

 $\textit{v}_{52} = vol\left(compartment\_3\right) \cdot modular\_rate\_law\_for\_two\_substrates\_\_two\_products\left(Vmax, was a constant and was a constant$ 

$$K\_S1, K\_S2, \frac{X5P\_astrocytes}{vol (compartment\_3)}, \frac{R5P\_astrocytes}{vol (compartment\_3)}, \frac{species\_10}{vol (compartment\_3)}, \frac{S7P\_astrocytes}{vol (compartment\_3)}, Keq, K\_P1, K\_P2 \right) \tag{215}$$

 $modular\_rate\_law\_for\_two\_substrates\_\_two\_products (Vmax, K\_S1,$ 

$$K\_S2,S1,S2,P1,P2,Keq,K\_P1,K\_P2) = Vmax \cdot \frac{1}{K\_S1 \cdot K\_S2}$$

$$S1 \cdot S2 - \frac{P1 \cdot P2}{Keq}$$

$$(216)$$

$$\frac{\left(1 + \frac{S1}{K\_S1}\right) \cdot \left(1 + \frac{S2}{K\_S2}\right) + \left(1 + \frac{P1}{K\_P1}\right) \cdot \left(1 + \frac{P2}{K\_P2}\right) - 1}$$

modular\_rate\_law\_for\_two\_substrates\_\_two\_products (Vmax, K\_S1,

$$\begin{split} \text{K\_S2,S1,S2,P1,P2,Keq,K\_P1,K\_P2)} &= \text{Vmax} \cdot \frac{1}{\text{K\_S1} \cdot \text{K\_S2}} \\ &\cdot \frac{\text{S1} \cdot \text{S2} - \frac{\text{P1} \cdot \text{P2}}{\text{Keq}}}{\left(1 + \frac{\text{S1}}{\text{K\_S1}}\right) \cdot \left(1 + \frac{\text{S2}}{\text{K\_S2}}\right) + \left(1 + \frac{\text{P1}}{\text{K\_P1}}\right) \cdot \left(1 + \frac{\text{P2}}{\text{K\_P2}}\right) - 1} \end{split} \tag{217}$$

Table 139: Properties of each parameter.

	1401	• 10 3 . 1 1 op • 1 1 1 0 2	or care para		
Id	Name	SBO	Value	Unit	Constant
Vmax	Vmax	2	2.44278 · 10-	4	$\overline{Z}$
$K_S1$	K_S1	1	$1.73625 \cdot 10^{-6}$	4	
$K_S2$	$K_{-}S2$	4	$5.85387 \cdot 10^{-6}$	4	$   \overline{\mathscr{L}} $
Keq	Keq		1652870.000	)	$   \overline{\mathscr{L}} $
K_P1	K_P1		0.168	}	
K_P2	K_P2		0.193	<b>;</b>	$\overline{\checkmark}$

## 9.53 Reaction TKL\_1\_neurons\_\_R01641

This is an irreversible reaction of two reactants forming two products.

Name TKL-1\_neurons (R01641)

SBO:0000176 biochemical reaction

## **Reaction equation**

$$X5P_neurons + R5P_neurons \longrightarrow species_9 + S7P_neurons$$
 (218)

### **Reactants**

Table 140: Properties of each reactant.

Id	Name	SBO
X5P_neurons	X5P	
$R5P\_neurons$	R5P	

#### **Products**

Table 141: Properties of each product.

AP P

#### **Kinetic Law**

#### Derived unit contains undeclared units

$$v_{53} = vol \\ (compartment\_2) \\ \cdot modular\_rate\_law\_for\_two\_substrates\_two\_products \\ \left( Vmax, K\_S1, K\_S2, \frac{X5P\_neurons}{vol \\ (compartment\_2)}, \frac{R5P\_neurons}{vol \\ (compartment\_2)}, \frac{species\_9}{vol \\ (compartment\_2)}, \frac{S7P\_neurons}{vol \\ (compartment\_2)}, Keq, K\_P1, K\_P2 \right) \\ (219)$$

 $modular\_rate\_law\_for\_two\_substrates\_\_two\_products (Vmax, K\_S1,$ 

$$K\_S2, S1, S2, P1, P2, Keq, K\_P1, K\_P2) = V max \cdot \frac{1}{K\_S1 \cdot K\_S2}$$

$$\cdot \frac{S1 \cdot S2 - \frac{P1 \cdot P2}{Keq}}{\left(1 + \frac{S1}{K\_S1}\right) \cdot \left(1 + \frac{S2}{K\_S2}\right) + \left(1 + \frac{P1}{K\_P1}\right) \cdot \left(1 + \frac{P2}{K\_P2}\right) - 1}$$
(220)

 $modular\_rate\_law\_for\_two\_substrates\_\_two\_products (Vmax, K\_S1,$ 

$$K\_S2,S1,S2,P1,P2,Keq,K\_P1,K\_P2) = Vmax \cdot \frac{1}{K\_S1 \cdot K\_S2}$$

$$S1 \cdot S2 - \frac{P1 \cdot P2}{Keq}$$

$$\cdot \frac{(221)}{(1 + \frac{S1}{K\_S1}) \cdot (1 + \frac{S2}{K\_S2}) + (1 + \frac{P1}{K\_P1}) \cdot (1 + \frac{P2}{K\_P2}) - 1}$$

Table 142: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
Vmax	Vmax		$4.93027 \cdot 10^{-2}$		$ \overline{\checkmark} $
$K_S1$	K_S1	1	$1.73625 \cdot 10^{-2}$	1	
$K_S2$	K_S2	5	$5.85387 \cdot 10^{-2}$	1	
Keq	Keq		1652870.000		
$K_{-}P1$	K_P1		0.168		
K_P2	K_P2		0.193		

## **9.54 Reaction** TAL\_astrocytes\_\_R01827

This is a reversible reaction of two reactants forming two products.

Name TAL\_astrocytes (R01827)

SBO:0000176 biochemical reaction

## **Reaction equation**

$$species_10 + S7P_astrocytes \Longrightarrow species_8 + E4P_astrocytes$$
 (222)

### **Reactants**

Table 143: Properties of each reactant.

Id	Name	
species_10	GAP	
$S7P_astrocytes$	S7P	

## **Products**

Table 144: Properties of each product.

Id	Name	SBO
species_8	F6P	
${ t E4P_astrocytes}$	E4P	

#### **Kinetic Law**

$$\textit{v}_{54} = vol\left(compartment\_3\right) \cdot modular\_rate\_law\_for\_two\_substrates\_\_two\_products\left(Vmax, was a constant and was a constant$$

$$K\_S1, K\_S2, \frac{species\_10}{vol (compartment\_3)}, \frac{S7P\_astrocytes}{vol (compartment\_3)}, \frac{species\_8}{vol (compartment\_3)}, \frac{E4P\_astrocytes}{vol (compartment\_3)}, Keq, K\_P1, K\_P2 \right) \tag{223}$$

 $modular\_rate\_law\_for\_two\_substrates\_\_two\_products (Vmax, K\_S1,$ 

$$K\_S2,S1,S2,P1,P2,Keq,K\_P1,K\_P2) = Vmax \cdot \frac{1}{K\_S1 \cdot K\_S2}$$

$$S1 \cdot S2 - \frac{P1 \cdot P2}{Keq}$$

$$(224)$$

$$\frac{(1 + \frac{S1}{K\_S1}) \cdot (1 + \frac{S2}{K\_S2}) + (1 + \frac{P1}{K\_P1}) \cdot (1 + \frac{P2}{K\_P2}) - 1}{(1 + \frac{P2}{K\_P2}) \cdot (1 + \frac{P2}{K\_P2}) - 1}$$

modular\_rate\_law\_for\_two\_substrates\_\_two\_products (Vmax, K\_S1,

$$\begin{split} \text{K\_S2,S1,S2,P1,P2,Keq,K\_P1,K\_P2)} &= \text{Vmax} \cdot \frac{1}{\text{K\_S1} \cdot \text{K\_S2}} \\ &\cdot \frac{\text{S1} \cdot \text{S2} - \frac{\text{P1} \cdot \text{P2}}{\text{Keq}}}{\left(1 + \frac{\text{S1}}{\text{K\_S1}}\right) \cdot \left(1 + \frac{\text{S2}}{\text{K\_S2}}\right) + \left(1 + \frac{\text{P1}}{\text{K\_P1}}\right) \cdot \left(1 + \frac{\text{P2}}{\text{K\_P2}}\right) - 1} \end{split} \tag{225}$$

Table 145: Properties of each parameter.

Id	Name	SBO Value Unit	Constant
Vmax	Vmax	0.008	Ø
K_S1	K_S1	0.168	
$K_S2$	K_S2	0.193	
Keq	Keq	0.324	
K_P1	K_P1	0.080	
K_P2	K_P2	0.110	$\checkmark$

#### 9.55 Reaction TAL\_neurons\_\_R01827

This is a reversible reaction of two reactants forming two products.

Name TAL\_neurons (R01827)

SBO:0000176 biochemical reaction

### **Reaction equation**

$$species_9 + S7P_neurons \Longrightarrow species_7 + E4P_neurons$$
 (226)

### **Reactants**

Table 146: Properties of each reactant.

Id	Name	SBO
species_9	GAP	
S7P_neurons	S7P	

#### **Products**

Table 147: Properties of each product.

Id	Name	SBO
species_7	F6P	
E4P_neurons	E4P	

#### **Kinetic Law**

#### Derived unit contains undeclared units

$$v_{55} = vol (compartment\_2) \cdot modular\_rate\_law\_for\_two\_substrates\_\_two\_products \left(Vmax, K\_S1, K\_S2, \frac{species\_9}{vol (compartment\_2)}, \frac{S7P\_neurons}{vol (compartment\_2)}, \frac{species\_7}{vol (compartment\_2)}, \frac{E4P\_neurons}{vol (compartment\_2)}, Keq, K\_P1, K\_P2\right)$$

 $modular\_rate\_law\_for\_two\_substrates\_\_two\_products (Vmax, K\_S1,$ 

$$K\_S2, S1, S2, P1, P2, Keq, K\_P1, K\_P2) = V max \cdot \frac{1}{K\_S1 \cdot K\_S2}$$

$$\cdot \frac{S1 \cdot S2 - \frac{P1 \cdot P2}{Keq}}{\left(1 + \frac{S1}{K\_S1}\right) \cdot \left(1 + \frac{S2}{K\_S2}\right) + \left(1 + \frac{P1}{K\_P1}\right) \cdot \left(1 + \frac{P2}{K\_P2}\right) - 1}$$
(228)

 $modular\_rate\_law\_for\_two\_substrates\_\_two\_products (Vmax, K\_S1,$ 

$$K\_S2, S1, S2, P1, P2, Keq, K\_P1, K\_P2) = Vmax \cdot \frac{1}{K\_S1 \cdot K\_S2}$$

$$S1 \cdot S2 - \frac{P1 \cdot P2}{Keq}$$

$$(229)$$

$$\frac{(1 + \frac{S1}{K\_S1}) \cdot (1 + \frac{S2}{K\_S2}) + (1 + \frac{P1}{K\_P1}) \cdot (1 + \frac{P2}{K\_P2}) - 1}{(1 + \frac{P2}{K\_P2}) \cdot (1 + \frac{P2}{K\_P2}) - 1}$$

Table 148: Properties of each parameter.

Id	Name	SBO Value Unit	Constant
Vmax	Vmax	0.016	$\overline{Z}$
K_S1	K_S1	0.168	
$K_S2$	$K_S2$	0.193	
Keq	Keq	0.324	
K_P1	K_P1	0.080	
K_P2	K_P2	0.110	$\overline{\mathbf{Z}}$

## **9.56 Reaction** TKL\_2\_astrocytes\_\_R01830

This is an irreversible reaction of two reactants forming two products.

Name TKL-2\_astrocytes (R01830)

SBO:0000176 biochemical reaction

## **Reaction equation**

$$species_8 + species_10 \longrightarrow X5P_astrocytes + E4P_astrocytes$$
 (230)

### **Reactants**

Table 149: Properties of each reactant.

Id	Name	SBO
species_8	F6P GAP	
species_10	GAP	

## **Products**

Table 150: Properties of each product.

Id	Name	SBO
X5P_astrocytes		
E4P_astrocytes	E4P	

#### **Kinetic Law**

$$v_{56} = \text{vol}\left(\text{compartment\_3}\right) \cdot \text{modular\_rate\_law\_for\_two\_substrates\_\_two\_products}\left(\text{Vmax}, \frac{\text{species\_8}}{\text{vol}\left(\text{compartment\_3}\right)}, \frac{\text{species\_10}}{\text{vol}\left(\text{compartment\_3}\right)}, \frac{\text{X5P\_astrocytes}}{\text{vol}\left(\text{compartment\_3}\right)}, \frac{\text{E4P\_astrocytes}}{\text{vol}\left(\text{compartment\_3}\right)}, \text{Keq}, \text{K\_P1}, \text{K\_P2}\right)$$

$$(231)$$

 $modular\_rate\_law\_for\_two\_substrates\_\_two\_products (Vmax, K\_S1,$ 

$$K\_S2,S1,S2,P1,P2,Keq,K\_P1,K\_P2) = Vmax \cdot \frac{1}{K\_S1 \cdot K\_S2}$$

$$S1 \cdot S2 - \frac{P1 \cdot P2}{Keq}$$

$$(232)$$

$$\frac{(1 + \frac{S1}{K\_S1}) \cdot (1 + \frac{S2}{K\_S2}) + (1 + \frac{P1}{K\_P1}) \cdot (1 + \frac{P2}{K\_P2}) - 1}{(1 + \frac{P2}{K\_P2}) \cdot (1 + \frac{P2}{K\_P2}) - 1}$$

modular\_rate\_law\_for\_two\_substrates\_\_two\_products (Vmax, K\_S1,

$$\begin{split} \text{K\_S2,S1,S2,P1,P2,Keq,K\_P1,K\_P2)} &= \text{Vmax} \cdot \frac{1}{\text{K\_S1} \cdot \text{K\_S2}} \\ &\cdot \frac{\text{S1} \cdot \text{S2} - \frac{\text{P1} \cdot \text{P2}}{\text{Keq}}}{\left(1 + \frac{\text{S1}}{\text{K\_S1}}\right) \cdot \left(1 + \frac{\text{S2}}{\text{K\_S2}}\right) + \left(1 + \frac{\text{P1}}{\text{K\_P1}}\right) \cdot \left(1 + \frac{\text{P2}}{\text{K\_P2}}\right) - 1} \end{split} \tag{233}$$

Table 151: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
Vmax	Vmax	1.	$37124 \cdot 10^{-2}$	4	lacksquare
K_S1	K_S1		0.080		
$K_S2$	K_S2		0.168		
Keq	Keq		0.078		
K_P1	K_P1		0.603		
K_P2	K_P2		0.110		$\overline{\mathbf{Z}}$

#### 9.57 Reaction TKL\_2\_neurons\_\_R01830

This is an irreversible reaction of two reactants forming two products.

Name TKL-2\_neurons (R01830)

SBO:0000176 biochemical reaction

#### **Reaction equation**

$$species_7 + species_9 \longrightarrow X5P_neurons + E4P_neurons$$
 (234)

## Reactants

Table 152: Properties of each reactant.

Id	Name	SBO
species_7 species_9	F6P GAP	

#### **Products**

Table 153: Properties of each product.

Id	Name	SBO
X5P_neurons	X5P	
${\tt E4P\_neurons}$	E4P	

#### **Kinetic Law**

#### Derived unit contains undeclared units

$$v_{57} = vol \\ (compartment\_2) \\ \cdot \\ modular\_rate\_law\_for\_two\_substrates\_two\_products \\ \left( \\ Vmax, \\ K\_S1, K\_S2, \\ \frac{species\_7}{vol \\ (compartment\_2)}, \\ \frac{species\_9}{vol \\ (compartment\_2)}, \\ \frac{E4P\_neurons}{vol \\ (compartment\_2)}, \\ Keq, K\_P1, K\_P2 \right) \\ (235)$$

 $modular\_rate\_law\_for\_two\_substrates\_\_two\_products (Vmax, K\_S1,$ 

$$K\_S2, S1, S2, P1, P2, Keq, K\_P1, K\_P2) = V max \cdot \frac{1}{K\_S1 \cdot K\_S2}$$

$$\cdot \frac{S1 \cdot S2 - \frac{P1 \cdot P2}{Keq}}{\left(1 + \frac{S1}{K\_S1}\right) \cdot \left(1 + \frac{S2}{K\_S2}\right) + \left(1 + \frac{P1}{K\_P1}\right) \cdot \left(1 + \frac{P2}{K\_P2}\right) - 1}$$
(236)

 $modular\_rate\_law\_for\_two\_substrates\_\_two\_products (Vmax, K\_S1,$ 

$$K_{-}S2, S1, S2, P1, P2, Keq, K_{-}P1, K_{-}P2) = V \max \cdot \frac{1}{K_{-}S1 \cdot K_{-}S2}$$

$$\cdot \frac{S1 \cdot S2 - \frac{P1 \cdot P2}{Keq}}{\left(1 + \frac{S1}{K_{-}S1}\right) \cdot \left(1 + \frac{S2}{K_{-}S2}\right) + \left(1 + \frac{P1}{K_{-}P1}\right) \cdot \left(1 + \frac{P2}{K_{-}P2}\right) - 1}$$
(237)

Table 154: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
Vmax	Vmax	2	.76758 · 10	4	
K_S1	K_S1		0.080		
K_S2	K_S2		0.168		
Keq	Keq		0.078		
K_P1	K_P1		0.603		
K_P2	K_P2		0.110		$\overline{\mathbf{Z}}$

### 9.58 Reaction NADPH\_oxidase\_neurons\_\_R07172

This is an irreversible reaction of one reactant forming one product.

Name NADPH oxidase neurons (R07172)

SBO:0000631 pseudoreaction

## **Reaction equation**

$$NADPH_neurons \longrightarrow NADP_neurons$$
 (238)

### Reactant

Table 155: Properties of each reactant.

Id	Name	SBO
NADPH_neurons	NADPH	

#### **Product**

Table 156: Properties of each product.

Id	Name	SBO
NADP_neurons	NADP	

### **Kinetic Law**

$$v_{58} = k1 \cdot NADPH\_neurons$$
 (239)

Table 157: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
k1	k1	2	4.23283 · 10-	4	$ \mathbf{Z} $

## 9.59 Reaction NADPH\_oxidase\_astrocytes\_\_R07172

This is an irreversible reaction of one reactant forming one product.

Name NADPH oxidase astrocytes (R07172)

SBO:0000631 pseudoreaction

## **Reaction equation**

 $NADPH\_astrocytes \longrightarrow NADP\_astrocytes \qquad (240)$ 

#### Reactant

Table 158: Properties of each reactant.

Id	Name	SBO
NADPH_astrocytes	NADPH	

## **Product**

Table 159: Properties of each product.

	1	
Id	Name	SBO
${\tt NADP\_astrocytes}$	NADP	

#### **Kinetic Law**

$$v_{59} = k1 \cdot NADPH$$
\_astrocytes (241)

Table 160: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
k1	k1	2	2.09722 · 10-	4	$lue{2}$

## 9.60 Reaction R5P\_sink\_astrocytes\_\_n\_a\_

This is an irreversible reaction of one reactant forming no product.

Name R5P sink\_astrocytes (n.a.)

SBO:0000631 pseudoreaction

## **Reaction equation**

R5P\_astrocytes 
$$\longrightarrow \emptyset$$
 (242)

### Reactant

Table 161: Properties of each reactant.

Id	Name	SBO
R5P_astrocytes	R5P	

### **Kinetic Law**

**Derived unit** contains undeclared units

$$v_{60} = \text{NULL} \cdot \text{R5P\_astrocytes}$$
 (243)

### 9.61 Reaction R5P\_sink\_neurons\_\_n\_a\_

This is an irreversible reaction of one reactant forming no product.

Name R5P sink\_neurons (n.a.)

SBO:0000631 pseudoreaction

## **Reaction equation**

$$R5P\_neurons \longrightarrow \emptyset$$
 (244)

#### Reactant

Table 162: Properties of each reactant.

Id	Name	SBO
R5P_neurons	R5P	

### **Kinetic Law**

**Derived unit** contains undeclared units

$$v_{61} = k1 \cdot R5P\_neurons \tag{245}$$

Table 163: Properties of each parameter.

Id	Name	SBO Value Unit	Constant
k1	k1	0.0	$\checkmark$

## **9.62 Reaction** PGI\_astrocytes\_\_R02740\_\_\_HS

This is a reversible reaction of one reactant forming one product.

Name PGI\_astrocytes (R02740) (HS)

### **Reaction equation**

$$species_6 \Longrightarrow species_8$$
 (246)

### Reactant

Table 164: Properties of each reactant.

Id	Name	SBO
species_6	G6P	

#### **Product**

Table 165: Properties of each product.

Id	Name	SBO
species_8	F6P	

#### **Kinetic Law**

$$v_{62} = \text{vol} \left( \text{compartment\_3} \right) \cdot \left( \text{k1} \cdot \frac{\text{species\_6}}{\text{vol} \left( \text{compartment\_3} \right)} - \text{k2} \cdot \frac{\text{species\_8}}{\text{vol} \left( \text{compartment\_3} \right)} \right)$$
 (247)

Table 166: Properties of each parameter.

Id	Name	SBO Value Unit	Constant
k1	k1	931.69	
k2	k2	2273.32	

### 9.63 Reaction HK\_neurons\_R01786\_\_HeinrichSchuster

This is an irreversible reaction of two reactants forming two products influenced by one modifier.

Name HK\_neurons (R01786) (HeinrichSchuster)

SBO:0000176 biochemical reaction

## **Reaction equation**

species\_3 + species\_1 
$$\xrightarrow{\text{species}\_2}$$
 species\_2 + ADP\_neurons (248)

#### **Reactants**

Table 167: Properties of each reactant.

Id	Name	SBO
species_3	ATP	
${ t species\_1}$	GLC	

#### Modifier

Table 168: Properties of each modifier.

Id	Name	SBO
species_2	G6P	

#### **Products**

Table 169: Properties of each product.

Id	Name	SBO
species_2 ADP_neurons	G6P ADP	

#### **Kinetic Law**

**Derived unit** contains undeclared units

$$v_{63} = \text{vol (compartment\_2)} \\ \cdot \text{vHK\_HS}\left(\text{k\_HK}, \frac{\text{species\_3}}{\text{vol (compartment\_2)}}, \frac{\text{species\_2}}{\text{vol (compartment\_2)}}, \text{K\_I\_G6P}\right)$$
(249)

$$vHK\_HS\left(k\_HK,ATP,G6P,K\_I\_G6P\right) = k\_HK \cdot ATP \cdot \left(1 + \frac{G6P}{K\_I\_G6P}\right)^{l} \tag{250}$$

$$vHK\_HS\left(k\_HK,ATP,G6P,K\_I\_G6P\right) = k\_HK\cdot ATP\cdot \left(1 + \frac{G6P}{K\_I\_G6P}\right)^{\!1} \tag{251}$$

Table 170: Properties of each parameter.

Id	Name	SBO Value Unit	Constant
k_HK	k_HK	0.022	$\square$
$K_{-}I_{-}G6P$	K_I_G6P	0.020	$\square$

### 9.64 Reaction PGI\_neurons\_R02740\_\_\_HS

This is a reversible reaction of one reactant forming one product.

Name PGI\_neurons (R02740) (HS)

#### **Reaction equation**

$$species_2 \rightleftharpoons species_7$$
 (252)

#### Reactant

Table 171: Properties of each reactant.

Id	Name	SBO
species_2	G6P	

#### **Product**

Table 172: Properties of each product.

Id	Name	SBO
species_7	F6P	

#### **Kinetic Law**

**Derived unit** contains undeclared units

$$v_{64} = \text{vol} \left( \text{compartment\_2} \right) \cdot \left( \text{k1} \cdot \frac{\text{species\_2}}{\text{vol} \left( \text{compartment\_2} \right)} - \text{k2} \cdot \frac{\text{species\_7}}{\text{vol} \left( \text{compartment\_2} \right)} \right)$$
 (253)

Table 173: Properties of each parameter.

Id	Name	SBO Value Unit	Constant
k1	k1	931.69	
k2	k2	2273.32	

## 10 Derived Rate Equations

When interpreted as an ordinary differential equation framework, this model implies the following set of equations for the rates of change of each species.

Identifiers for kinetic laws highlighted in gray cannot be verified to evaluate to units of SBML substance per time. As a result, some SBML interpreters may not be able to verify the consistency of the units on quantities in the model. Please check if

- parameters without an unit definition are involved or
- volume correction is necessary because the hasOnlySubstanceUnits flag may be set to false and spacialDimensions > 0 for certain species.

### 10.1 Species species\_23

### Name O2

Initial amount 0.040323291746644 mmol

This species takes part in four reactions (as a reactant in O2\_exchange\_capillary\_neurons, O2\_exchange\_capillary\_astrocytes and as a product in Blood\_flow\_contribution\_to\_capillary\_O2 and as a modifier in inflow\_of\_dHb).

$$\frac{d}{dt} \text{species} 23 = |v_{20}| - |v_{18}| - |v_{19}|$$
 (254)

### 10.2 Species species\_24

Name CO2

**Initial amount** 0.0121467082533562 mmol

This species takes part in three reactions (as a reactant in Flow\_of\_CO2\_between\_capillary\_and\_vessel\_artery\_ and as a product in reaction\_13, reaction\_14).

$$\frac{d}{dt} \text{species.} 24 = 3 v_8 + 3 v_9 - v_{23}$$
 (255)

## 10.3 Species species\_25

Name GLC

**Initial amount** 0.0253903826849856 mmol

This species takes part in three reactions (as a reactant in reaction\_19, reaction\_20 and as a product in Blood\_flow\_contribution\_to\_capillary\_GLC).

$$\frac{d}{dt} \text{species}_{25} = |v_{21}| - |v_{12}| - |v_{13}| \tag{256}$$

## 10.4 Species species\_26

Name LAC

**Initial amount** 0.00188912996259375 mmol

This species takes part in three reactions (as a reactant in Blood\_flow\_contribution\_to-capillary\_LAC and as a product in reaction\_21, reaction\_24).

$$\frac{d}{dt} \text{species}_{26} = |v_{14}| + |v_{17}| - |v_{22}| \tag{257}$$

### 10.5 Species dHb

Name dHb

Initial amount  $2.62913971209081 \cdot 10^{-4} \text{ mmol}$ 

This species takes part in two reactions (as a reactant in outflow\_of\_dHb and as a product in inflow\_of\_dHb).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{dHb} = v_{32} - v_{33} \tag{258}$$

### 10.6 Species species\_1

Name GLC

Initial amount 0.513125204430911 mmol

This species takes part in two reactions (as a reactant in HK\_neurons\_R01786\_\_\_HeinrichSchuster and as a product in reaction\_17).

$$\frac{d}{dt}$$
 species\_1 =  $|v_{10}| - |v_{63}|$  (259)

### **10.7 Species** species\_2

Name G6P

Initial amount 0.0506867341754652 mmol

This species takes part in four reactions (as a reactant in ZWF\_neurons\_R02736, PGI\_neurons\_R02740\_\_HS and as a product in HK\_neurons\_R01786\_\_HeinrichSchuster and as a modifier in HK\_neurons\_R01786\_\_HeinrichSchuster).

$$\frac{d}{dt} \text{species} 2 = |v_{63}| - |v_{43}| - |v_{64}| \tag{260}$$

### 10.8 Species species\_3

Name ATP

Initial amount 1.01756735100076 mmol

This species takes part in nine reactions (as a reactant in reaction\_5, vPUMP\_neurons, ATPase\_neurons, HK\_neurons\_R01786\_\_HeinrichSchuster and as a product in reaction\_7, reaction\_9, reaction\_13, AK\_neurons, CK\_neurons\_forward\_R01881).

$$\frac{d}{dt} \text{species}_{3} = v_{4} + v_{6} + 15 v_{8} + v_{36} + v_{39} - v_{2} - v_{24} - v_{34} - v_{63}$$
 (261)

### **10.9 Species** species\_7

Name F6P

Initial amount 0.0207718119329183 mmol

This species takes part in four reactions (as a reactant in reaction\_5, TKL\_2\_neurons\_\_R01830 and as a product in TAL\_neurons\_\_R01827, PGI\_neurons\_\_R02740\_\_HS).

$$\frac{d}{dt} \text{species}_{7} = |v_{55}| + |v_{64}| - |v_{2}| - |v_{57}|$$
(262)

### 10.10 Species species\_9

Name GAP

Initial amount  $4.84856903277021 \cdot 10^{-4} \text{ mmol}$ 

This species takes part in five reactions (as a reactant in reaction\_7, TAL\_neurons\_R01827, TKL\_2\_neurons\_R01830 and as a product in reaction\_5, TKL\_1\_neurons\_R01641).

$$\frac{d}{dt} \text{species}_{9} = 2 v_{2} + v_{53} - v_{4} - v_{55} - v_{57}$$
 (263)

## **10.11 Species** species\_11

Name NADH

**Initial amount** 0.00736369051750214 mmol

This species takes part in three reactions (as a reactant in reaction\_13, LDH\_neurons\_forward\_\_\_R00703 and as a product in reaction\_7).

$$\frac{d}{dt} \text{species}_{-}11 = |v_4| - |v_8| - |v_{41}| \tag{264}$$

## **10.12 Species** species\_12

Name PEP

Initial amount 0.00137130155845014 mmol

This species takes part in two reactions (as a reactant in reaction\_9 and as a product in reaction\_7).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{species}_{12} = |v_4| - |v_6| \tag{265}$$

### 10.13 Species species\_15

Name PYR

**Initial amount** 0.05894677979576 mmol

This species takes part in three reactions (as a reactant in reaction\_13, LDH\_neurons\_forward\_\_\_R00703 and as a product in reaction\_9).

$$\frac{d}{dt} \text{species}_{-}15 = |v_6| - |v_8| - |v_{41}| \tag{266}$$

# 10.14 Species species\_18

Name LAC

**Initial amount** 0.631465311475557 mmol

This species takes part in two reactions (as a product in reaction\_22, LDH\_neurons\_forward\_\_\_R00703).

$$\frac{d}{dt} \text{species}_{-}18 = |v_{15}| + |v_{41}| \tag{267}$$

# 10.15 Species species\_16

Name O2

Initial amount 0.0134379352275963 mmol

This species takes part in two reactions (as a reactant in reaction\_13 and as a product in 02-\_exchange\_capillary\_neurons).

$$\frac{d}{dt} \text{species}_{-16} = |v_{18}| - 3 v_8 \tag{268}$$

# 10.16 Species species\_21

Name PCr

Notes Phosphocreatine

**Initial amount** 0.648285185366582 mmol

This species takes part in one reaction (as a reactant in CK\_neurons\_forward\_R01881).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{species}_{21} = -v_{39} \tag{269}$$

# 10.17 Species Na\_neurons

Name Na+

**Initial amount** 6.98905574867159 mmol

This species takes part in three reactions (as a reactant in vPUMP\_neurons and as a product in vLEAK\_Na\_neurons, vSTIM).

$$\frac{d}{dt} \text{Na\_neurons} = |v_{26}| + |v_{28}| - 3|v_{24}|$$
 (270)

# 10.18 Species GLU\_neurons

Name GLU

Initial amount 1.35000000000001 mmol

This species takes part in two reactions (as a reactant in vGLU\_ne and as a product in vGLU\_gn).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{GLU\_neurons} = v_{31} - v_{29} \tag{271}$$

#### 10.19 Species ADP\_neurons

Name ADP

Initial amount 0.0502819665719672 mmol

This species takes part in nine reactions (as a reactant in reaction\_7, reaction\_9, reaction\_13, AK\_neurons, CK\_neurons\_forward\_R01881 and as a product in reaction\_5, vPUMP-neurons, ATPase\_neurons, HK\_neurons\_R01786\_\_HeinrichSchuster).

$$\frac{d}{dt}ADP\_neurons = v_2 + v_{24} + v_{34} + v_{63} - v_4 - v_6 - 15v_8 - 2v_{36} - v_{39}$$
 (272)

# 10.20 Species AMP\_neurons

Name AMP

**Initial amount** 0.00270068242727579 mmol

Initial assignment AMP\_neurons

This species takes part in one reaction (as a product in AK\_neurons).

$$\frac{\mathrm{d}}{\mathrm{d}t} AMP\_neurons = v_{36}$$
 (273)

# 10.21 Species Cr\_neurons

Name Cr

Initial amount 1.60171481463342 mmol

Initial assignment Cr\_neurons

This species takes part in one reaction (as a product in CK\_neurons\_forward\_R01881).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{Cr}_{-\mathrm{neurons}} = v_{39} \tag{274}$$

# 10.22 Species NAD\_neurons

Name NAD

Initial amount 0.0916363094824979 mmol

Initial assignment NAD\_neurons

This species takes part in three reactions (as a reactant in reaction\_7 and as a product in reaction\_13, LDH\_neurons\_forward\_R00703).

$$\frac{\mathrm{d}}{\mathrm{d}t} \mathrm{NAD\_neurons} = v_8 + v_{41} - v_4 \tag{275}$$

# 10.23 Species G6L\_neurons

Name G6L

Initial amount  $1.35054620762897 \cdot 10^{-6}$  mmol

This species takes part in two reactions (as a reactant in SOL\_neurons\_R02035 and as a product in ZWF\_neurons\_R02736).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{G6L\_neurons} = v_{43} - v_{44} \tag{276}$$

#### **10.24 Species P6G\_neurons**

Name P6G

**Initial amount** 0.00129746785673949 mmol

This species takes part in two reactions (as a reactant in GND\_neurons\_\_\_R01528 and as a product in SOL\_neurons\_\_R02035).

$$\frac{d}{dt}$$
P6G\_neurons =  $|v_{44}| - |v_{46}|$  (277)

# 10.25 Species Ru5P\_neurons

Name Ru5P

Initial amount  $3.03470299804797 \cdot 10^{-4} \text{ mmol}$ 

This species takes part in three reactions (as a reactant in RPE\_neurons\_\_R01529, RKI\_neurons\_\_R01056 and as a product in GND\_neurons\_\_R01528).

$$\frac{d}{dt} Ru5P_{neurons} = |v_{46}| - |v_{48}| - |v_{51}|$$
 (278)

# 10.26 Species X5P\_neurons

Name X5P

**Initial amount** 0.00930686571830458 mmol

This species takes part in three reactions (as a reactant in TKL\_1\_neurons\_R01641 and as a product in RPE\_neurons\_R01529, TKL\_2\_neurons\_R01830).

$$\frac{d}{dt}X5P_{neurons} = v_{48} + v_{57} - v_{53}$$
 (279)

# 10.27 Species R5P\_neurons

Name R5P

Initial amount  $1.21527766162824 \cdot 10^{-5} \text{ mmol}$ 

This species takes part in three reactions (as a reactant in TKL\_1\_neurons\_\_R01641, R5P\_sink\_neurons\_\_n\_a\_ and as a product in RKI\_neurons\_\_R01056).

$$\frac{d}{dt}R5P_{neurons} = |v_{51}| - |v_{53}| - |v_{61}|$$
 (280)

# 10.28 Species S7P\_neurons

Name S7P

**Initial amount** 0.519857938505835 mmol

This species takes part in two reactions (as a reactant in TAL\_neurons\_R01827 and as a product in TKL\_1\_neurons\_R01641).

$$\frac{\mathrm{d}}{\mathrm{d}t} S7P_{\text{neurons}} = |v_{53}| - |v_{55}| \tag{281}$$

# 10.29 Species E4P\_neurons

Name E4P

**Initial amount** 0.00293045545188872 mmol

This species takes part in two reactions (as a product in TAL\_neurons\_\_R01827, TKL\_2\_neurons\_\_R01830).

$$\frac{\mathrm{d}}{\mathrm{d}t} \text{E4P\_neurons} = |v_{55}| + |v_{57}| \tag{282}$$

# 10.30 Species NADPH\_neurons

Name NADPH

**Initial amount** 0.13105170046902 mmol

This species takes part in three reactions (as a reactant in NADPH\_oxidase\_neurons\_\_R07172 and as a product in ZWF\_neurons\_\_R02736, GND\_neurons\_\_R01528).

$$\frac{d}{dt} NADPH\_neurons = |v_{43}| + |v_{46}| - |v_{58}|$$
 (283)

# 10.31 Species NADP\_neurons

Name NADP

Initial amount  $9.96586007623714 \cdot 10^{-10} \text{ mmol}$ 

This species takes part in three reactions (as a reactant in ZWF\_neurons\_\_R02736, GND\_neurons\_\_R01528 and as a product in NADPH\_oxidase\_neurons\_\_R07172).

$$\frac{d}{dt} NADP_neurons = |v_{58}| - |v_{43}| - v_{46}$$
 (284)

# **10.32 Species** species\_4

Name GLC

**Initial amount** 0.28506553827656 mmol

This species takes part in three reactions (as a reactant in reaction\_2 and as a product in reaction\_18, reaction\_20).

$$\frac{d}{dt} \text{species}_{4} = |v_{11}| + |v_{13}| - |v_{1}| \tag{285}$$

#### 10.33 Species species\_5

Name ATP

Initial amount 0.453875749582273 mmol

This species takes part in ten reactions (as a reactant in reaction\_2, reaction\_6, vPUMP\_astrocytes, vGLU\_gn, ATPase\_astrocytes and as a product in reaction\_8, reaction\_10, reaction\_14, AK\_astrocytes, CK\_astrocytes\_forward\_R01881).

$$\frac{d}{dt} \text{species\_5} = v_5 + |v_7| + 15 |v_9| + |v_{37}| + |v_{38}| - |v_1| - |v_3| - |v_{25}| - |v_{31}| - |v_{35}|$$
(286)

# 10.34 Species species\_6

Name G6P

**Initial amount** 0.0170326696107673 mmol

This species takes part in four reactions (as a reactant in ZWF\_astrocytes\_R02736, PGI\_astrocytes\_R02740\_HS and as a product in reaction\_2 and as a modifier in reaction\_2).

$$\frac{d}{dt} \text{species}_{6} = |v_{1}| - |v_{42}| - |v_{62}| \tag{287}$$

# 10.35 Species species\_8

Name F6P

Initial amount 0.00698016362763041 mmol

This species takes part in four reactions (as a reactant in reaction\_6, TKL\_2\_astrocytes\_-R01830 and as a product in TAL\_astrocytes\_\_R01827, PGI\_astrocytes\_\_R02740\_\_HS).

$$\frac{d}{dt} \text{species}_{8} = |v_{54}| + |v_{62}| - |v_{3}| - |v_{56}| \tag{288}$$

#### **10.36 Species** species\_10

Name GAP

Initial amount  $5.51039449892962 \cdot 10^{-4} \text{ mmol}$ 

This species takes part in five reactions (as a reactant in reaction\_8, TAL\_astrocytes\_\_R01827, TKL\_2\_astrocytes\_\_R01830 and as a product in reaction\_6, TKL\_1\_astrocytes\_\_R01641).

$$\frac{d}{dt} \text{species}_{10} = 2 v_3 + v_{52} - v_5 - v_{54} - v_{56}$$
 (289)

# **10.37 Species** species\_13

Name NADH

**Initial amount** 0.014484722086168 mmol

This species takes part in three reactions (as a reactant in reaction\_14, LDH\_astrocytes\_forward\_R00703 and as a product in reaction\_8).

$$\frac{d}{dt} \text{species}_{-13} = |v_5| - |v_9| - |v_{40}| \tag{290}$$

# 10.38 Species species\_14

Name PEP

Initial amount  $2.31197219260613 \cdot 10^{-4} \text{ mmol}$ 

This species takes part in two reactions (as a reactant in reaction\_10 and as a product in reaction\_8).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{species}_{-}14 = v_5 - v_7 \tag{291}$$

# 10.39 Species species\_17

Name PYR

**Initial amount** 0.0391626309395164 mmol

This species takes part in three reactions (as a reactant in reaction\_14, LDH\_astrocytes\_forward\_R00703 and as a product in reaction\_10).

$$\frac{d}{dt} \text{species}_{17} = |v_7| - |v_9| - |v_{40}| \tag{292}$$

# 10.40 Species species\_19

Name LAC

**Initial amount** 0.341202758724066 mmol

This species takes part in three reactions (as a reactant in reaction\_23, reaction\_24 and as a product in LDH\_astrocytes\_forward\_\_R00703).

$$\frac{d}{dt} \text{species}_{-}19 = |v_{40}| - |v_{16}| - |v_{17}| \tag{293}$$

# **10.41 Species** species\_20

Name O2

Initial amount 0.0114703177351059 mmol

This species takes part in two reactions (as a reactant in reaction\_14 and as a product in 02-\_exchange\_capillary\_astrocytes).

$$\frac{d}{dt} \text{species}.20 = |v_{19}| - 3 |v_{9}| \tag{294}$$

# 10.42 Species species\_22

Name PCr

Notes Phosphocreatine

**Initial amount** 0.0943080249454476 mmol

This species takes part in one reaction (as a reactant in CK\_astrocytes\_forward\_\_R01881).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{species}_{22} = -\nu_{38} \tag{295}$$

# 10.43 Species Na\_astrocytes

Name Na+

**Initial amount** 4.00737645868716 mmol

This species takes part in three reactions (as a reactant in vPUMP\_astrocytes and as a product in vLEAK\_Na\_astrocytes, vGLU\_eg).

$$\frac{d}{dt}$$
Na\_astrocytes =  $|v_{27}| + |v_{30}| - 3|v_{25}|$  (296)

# 10.44 Species GLU\_astrocytes

Name GLU

Initial amount 0 mmol

This species takes part in two reactions (as a reactant in vGLU\_gn and as a product in vGLU\_eg).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{GLU}_{-\mathrm{astrocytes}} = |v_{30}| - |v_{31}| \tag{297}$$

# 10.45 Species ADP\_astrocytes

Name ADP

**Initial amount** 0.111239857216292 mmol

This species takes part in ten reactions (as a reactant in reaction\_8, reaction\_10, reaction\_14, AK\_astrocytes, CK\_astrocytes\_forward\_R01881 and as a product in reaction\_2, reaction\_6, vPUMP\_astrocytes, vGLU\_gn, ATPase\_astrocytes).

$$\frac{d}{dt}ADP_{astrocytes} = v_1 + v_3 + v_{25} + v_{31} + v_{35} - v_5 - v_7 - 15 v_9 - 2 v_{37} - v_{38}$$
 (298)

# 10.46 Species AMP\_astrocytes

Name AMP

**Initial amount** 0.0296343932014343 mmol

Initial assignment AMP\_astrocytes

This species takes part in one reaction (as a product in AK\_astrocytes).

$$\frac{\mathrm{d}}{\mathrm{d}t} AMP_{-} astrocytes = v_{37}$$
 (299)

#### 10.47 Species Cr\_astrocytes

Name Cr

**Initial amount** 1.15569197505455 mmol

Initial assignment Cr\_astrocytes

This species takes part in one reaction (as a product in CK\_astrocytes\_forward\_R01881).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{Cr\_astrocytes} = v_{38} \tag{300}$$

# 10.48 Species NAD\_astrocytes

Name NAD

**Initial amount** 0.040515277913832 mmol

Initial assignment NAD\_astrocytes

This species takes part in three reactions (as a reactant in reaction\_8 and as a product in reaction\_14, LDH\_astrocytes\_forward\_\_R00703).

$$\frac{d}{dt}NAD_{astrocytes} = |v_9| + |v_{40}| - |v_5|$$
(301)

# 10.49 Species G6L\_astrocytes

Name G6L

Initial amount  $7.49440003798258 \cdot 10^{-7} \text{ mmol}$ 

This species takes part in two reactions (as a reactant in SOL\_astrocytes\_R02035 and as a product in ZWF\_astrocytes\_R02736).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{G6L\_astrocytes} = |v_{42}| - |v_{45}| \tag{302}$$

# 10.50 Species P6G\_astrocytes

Name P6G

Initial amount  $4.50905835212361 \cdot 10^{-4} \text{ mmol}$ 

This species takes part in two reactions (as a reactant in GND\_astrocytes\_R01528 and as a product in SOL\_astrocytes\_R02035).

$$\frac{d}{dt}P6G_{astrocytes} = v_{45} - v_{47}$$
 (303)

# 10.51 Species Ru5P\_astrocytes

Name Ru5P

Initial amount  $1.68586812670336 \cdot 10^{-4} \text{ mmol}$ 

This species takes part in three reactions (as a reactant in RPE\_astrocytes\_R01529, RKI-astrocytes\_R01056 and as a product in GND\_astrocytes\_R01528).

$$\frac{\mathrm{d}}{\mathrm{d}t} \mathrm{Ru}5\mathrm{P\_astrocytes} = |v_{47}| - |v_{49}| - |v_{50}| \tag{304}$$

# 10.52 Species X5P\_astrocytes

Name X5P

**Initial amount** 0.00517018155675064 mmol

This species takes part in three reactions (as a reactant in TKL\_1\_astrocytes\_\_R01641 and as a product in RPE\_astrocytes\_\_R01529, TKL\_2\_astrocytes\_\_R01830).

$$\frac{\mathrm{d}}{\mathrm{d}t} X5 P_{\text{astrocytes}} = |v_{49}| + |v_{56}| - |v_{52}| \tag{305}$$

# 10.53 Species R5P\_astrocytes

Name R5P

**Initial amount**  $6.5024908937442 \cdot 10^{-6}$  mmol

This species takes part in three reactions (as a reactant in TKL\_1\_astrocytes\_R01641, R5P-\_sink\_astrocytes\_n\_a\_ and as a product in RKI\_astrocytes\_R01056).

$$\frac{\mathrm{d}}{\mathrm{d}t} R5P_{\text{astrocytes}} = |v_{50}| - |v_{52}| - |v_{60}| \tag{306}$$

# 10.54 Species S7P\_astrocytes

Name S7P

**Initial amount** 0.0691726529321511 mmol

This species takes part in two reactions (as a reactant in TAL\_astrocytes\_\_R01827 and as a product in TKL\_1\_astrocytes\_\_R01641).

$$\frac{\mathrm{d}}{\mathrm{d}t} S7P_{-} \text{astrocytes} = |v_{52}| - |v_{54}| \tag{307}$$

# 10.55 Species E4P\_astrocytes

Name E4P

**Initial amount** 0.00142484578792443 mmol

This species takes part in two reactions (as a product in TAL\_astrocytes\_R01827, TKL\_2-astrocytes\_R01830).

$$\frac{\mathrm{d}}{\mathrm{d}t} \text{E4P\_astrocytes} = |v_{54}| + |v_{56}| \tag{308}$$

# 10.56 Species NADP\_astrocytes

Name NADP

Initial amount  $6.89248119909569 \cdot 10^{-10} \text{ mmol}$ 

This species takes part in three reactions (as a reactant in ZWF\_astrocytes\_R02736, GND-astrocytes\_R01528 and as a product in NADPH\_oxidase\_astrocytes\_R07172).

$$\frac{\mathrm{d}}{\mathrm{d}t} \text{NADP\_astrocytes} = |v_{59}| - |v_{42}| - |v_{47}| \tag{309}$$

# 10.57 Species NADPH\_astrocytes

Name NADPH

**Initial amount** 0.0728065001051474 mmol

This species takes part in three reactions (as a reactant in NADPH\_oxidase\_astrocytes\_-R07172 and as a product in ZWF\_astrocytes\_\_R02736, GND\_astrocytes\_\_R01528).

$$\frac{\mathrm{d}}{\mathrm{d}t} \text{NADPH\_astrocytes} = |v_{42}| + |v_{47}| - |v_{59}| \tag{310}$$

# 10.58 Species species\_27

Name GLC

**Initial amount** 0.228060016230605 mmol

This species takes part in three reactions (as a reactant in reaction\_17, reaction\_18 and as a product in reaction\_19).

$$\frac{d}{dt} \text{species.} 27 = |v_{12}| - |v_{10}| - |v_{11}| \tag{311}$$

# 10.59 Species species\_28

Name LAC

**Initial amount** 0.269553776630414 mmol

This species takes part in three reactions (as a reactant in reaction\_21, reaction\_22 and as a product in reaction\_23).

$$\frac{d}{dt} \text{species} 28 = |v_{16}| - |v_{14}| - |v_{15}| \tag{312}$$

# 10.60 Species GLU\_extracellular\_space

Name GLU

**Initial amount** 0 mmol

This species takes part in two reactions (as a reactant in vGLU\_eg and as a product in vGLU\_ne).

$$\frac{d}{dt}GLU_{extracellular\_space} = v_{29} - v_{30}$$
 (313)

# 10.61 Species Na\_extracellular\_space

Name Na+

Initial amount 30 mmol

This species takes part in three reactions (as a reactant in vLEAK\_Na\_neurons, vLEAK\_Na\_astrocytes, vSTIM), which do not influence its rate of change because this constant species is on the boundary of the reaction system:

$$\frac{\mathrm{d}}{\mathrm{d}t} \mathrm{Na\_extracellular\_space} = 0 \tag{314}$$

# 10.62 Species 02\_artery

Name O2

#### Initial amount 0.0458700000000001 mmol

This species takes part in two reactions (as a reactant in Blood\_flow\_contribution\_to-capillary\_02 and as a modifier in inflow\_of\_dHb), which do not influence its rate of change because this constant species is on the boundary of the reaction system:

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{O}2_{-}\mathrm{artery} = 0 \tag{315}$$

# 10.63 Species CO2\_artery

Name CO2

Initial amount 0.006600000000000000 mmol

This species takes part in one reaction (as a product in Flow\_of\_CO2\_between\_capillary\_and\_vessel\_artery\_), which does not influence its rate of change because this constant species is on the boundary of the reaction system:

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{CO2\_artery} = 0 \tag{316}$$

#### 10.64 Species GLC\_artery

Name GLC

Initial amount 0.0264000000000000 mmol

This species takes part in one reaction (as a reactant in Blood\_flow\_contribution\_to\_capillary\_GLC), which does not influence its rate of change because this constant species is on the boundary of the reaction system:

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{GLC\_artery} = 0 \tag{317}$$

#### **10.65 Species** LAC\_artery

Name LAC

Initial amount 0.0017215 mmol

This species takes part in one reaction (as a product in Blood\_flow\_contribution\_to\_capillary\_LAC), which does not influence its rate of change because this constant species is on the boundary of the reaction system:

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{LAC\_artery} = 0 \tag{318}$$

# A Glossary of Systems Biology Ontology Terms

- **SBO:0000176 biochemical reaction:** An event involving one or more chemical entities that modifies the electrochemical structure of at least one of the participants.
- **SBO:0000185 transport reaction:** Movement of a physical entity without modification of the structure of the entity
- **SBO:0000290 physical compartment:** Specific location of space, that can be bounded or not. A physical compartment can have 1, 2 or 3 dimensions
- **SBO:0000395 encapsulating process:** An aggregation of interactions and entities into a single process
- **SBO:0000631 pseudoreaction:** A conceptual process used for modeling purposes, often created solely to complete model structure, with respect to providing inflow or outflow of matter or material. Unlike other reactions, pseudoreactions are not usually subjected to mass balance considerations

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