

SBML Model Report

Model name:
“Lei2001_Yeast_Aerobic_Metabolism”



May 6, 2016

1 General Overview

This is a document in SBML Level 2 Version 4 format. This model was created by Lukas Endler¹ at March 25th 2010 at 2:28 a. m. and last time modified at June third 2010 at 10:40 a. m. Table 1 shows an overview of the quantities of all components of this model.

Table 1: Number of components in this model, which are described in the following sections.

| Element | Quantity | Element | Quantity |
|-------------------|----------|----------------------|----------|
| compartment types | 0 | compartments | 2 |
| species types | 0 | species | 11 |
| events | 0 | constraints | 0 |
| reactions | 20 | function definitions | 0 |
| global parameters | 42 | unit definitions | 8 |
| rules | 6 | initial assignments | 0 |

Model Notes

This the model from the article:

A biochemically structured model for *Saccharomyces cerevisiae*.

Lei F, Rotbl M, Jrgensen SB. J Biotechnol. 2001 Jul 12;88(3):205-21. PMID: [11434967](#) ,DOI: [10.1016/S0168-1656\(01\)00269-3](#)

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Abstract:

A biochemically structured model for the aerobic growth of *Saccharomyces cerevisiae* on glucose and ethanol is presented. The model focuses on the pyruvate and acetaldehyde branch points where overflow metabolism occurs when the growth changes from oxidative to oxidoreductive. The model is designed to describe the onset of aerobic alcoholic fermentation during steady-state as well as under dynamical conditions, by triggering an increase in the glycolytic flux using a key signalling component which is assumed to be closely related to acetaldehyde. An investigation of the modelled process dynamics in a continuous cultivation revealed multiple steady states in a region of dilution rates around the transition between oxidative and oxidoreductive growth. A bifurcation analysis using the two external variables, the dilution rate, D , and the inlet concentration of glucose, $S(f)$, as parameters, showed that a fold bifurcation occurs close to the critical dilution rate resulting in multiple steady-states. The region of dilution rates within which multiple steady states may occur depends strongly on the substrate feed concentration. Consequently a single steady state may prevail at low feed concentrations, whereas multiple steady states may occur over a relatively wide range of dilution rates at higher feed concentrations.

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To cite BioModels Database, please use [Le Novre N., Bornstein B., Broicher A., Courtot M., Donizelli M., Dharuri H., Li L., Sauro H., Schilstra M., Shapiro B., Snoep J.L., Hucka M. \(2006\) BioModels Database: A Free, Centralized Database of Curated, Published, Quantitative Kinetic Models of Biochemical and Cellular Systems Nucleic Acids Res., 34: D689-D691.](#)

2 Unit Definitions

This is an overview of ten unit definitions of which two are predefined by SBML and not mentioned in the model.

2.1 Unit substance

Name gram

Definition g

2.2 Unit time

Name hours

Definition 3600 s

2.3 Unit volume

Name liter

Definition 1

2.4 Unit `per_h`

Name per hour

Definition $(3600\text{ s})^{-1}$

2.5 Unit `g_per_l`

Name gram per liter

Definition $\text{g} \cdot \text{l}^{-1}$

2.6 Unit `l_per_g`

Name liter per gram

Definition $\text{g}^{-1} \cdot \text{l}$

2.7 Unit `g_per_l_per_h`

Name gram per liter per hour

Definition $\text{g} \cdot \text{l}^{-1} \cdot (3600\text{ s})^{-1}$

2.8 Unit `mmole_per_g_per_h`

Name mmole per gram BM per hour

Definition $\text{mmol} \cdot (3600\text{ s})^{-1} \cdot \text{g}^{-1}$

2.9 Unit `area`

Notes Square metre is the predefined SBML unit for area since SBML Level 2 Version 1.

Definition m^2

2.10 Unit `length`

Notes Metre is the predefined SBML unit for length since SBML Level 2 Version 1.

Definition m

3 Compartments

This model contains two compartments.

Table 2: Properties of all compartments.

| Id | Name | SBO | Spatial Dimensions | Size | Unit | Constant | Outside |
|------|-------------|---------|-----------------------|------|-------|-------------------------------------|---------|
| env | environment | 0000290 | 3 | 1 | litre | <input checked="" type="checkbox"/> | |
| cell | | 0000290 | 3 | 1 | litre | <input checked="" type="checkbox"/> | |

3.1 Compartment `env`

This is a three dimensional compartment with a constant size of one litre.

Name environment

SBO:0000290 physical compartment

3.2 Compartment `cell`

This is a three dimensional compartment with a constant size of one litre.

SBO:0000290 physical compartment

4 Species

This model contains eleven species. The boundary condition of five of these species is set to `true` so that these species' amount cannot be changed by any reaction. Section 8 provides further details and the derived rates of change of each species.

Table 3: Properties of each species.

| Id | Name | Compartment | Derived Unit | Constant | Boundary Condi- tion |
|-----------|------------------|-------------|--------------------------------|--------------------------|-------------------------------------|
| s_glu | Glucose | env | $\text{g} \cdot \text{l}^{-1}$ | <input type="checkbox"/> | <input type="checkbox"/> |
| s_pyr | Pyruvate | env | $\text{g} \cdot \text{l}^{-1}$ | <input type="checkbox"/> | <input type="checkbox"/> |
| s_acetate | Acetate | env | $\text{g} \cdot \text{l}^{-1}$ | <input type="checkbox"/> | <input type="checkbox"/> |
| s_acetald | Acetaldehyde | env | $\text{g} \cdot \text{l}^{-1}$ | <input type="checkbox"/> | <input type="checkbox"/> |
| s_EtOH | EtOH | env | $\text{g} \cdot \text{l}^{-1}$ | <input type="checkbox"/> | <input type="checkbox"/> |
| x | BM | env | $\text{g} \cdot \text{l}^{-1}$ | <input type="checkbox"/> | <input type="checkbox"/> |
| a | BM(active) | env | $\text{g} \cdot \text{l}^{-1}$ | <input type="checkbox"/> | <input checked="" type="checkbox"/> |
| AcDH | BM(AcDH) | env | $\text{g} \cdot \text{l}^{-1}$ | <input type="checkbox"/> | <input checked="" type="checkbox"/> |
| CO2 | CO2 | env | $\text{g} \cdot \text{l}^{-1}$ | <input type="checkbox"/> | <input checked="" type="checkbox"/> |
| Red | Red. Equ. (NADH) | env | $\text{g} \cdot \text{l}^{-1}$ | <input type="checkbox"/> | <input checked="" type="checkbox"/> |
| S_f | Glucose(feed) | env | $\text{g} \cdot \text{l}^{-1}$ | <input type="checkbox"/> | <input checked="" type="checkbox"/> |

5 Parameters

This model contains 42 global parameters.

Table 4: Properties of each parameter.

| Id | Name | SBO | Value | Unit | Constant |
|--------|--------|-----|----------------------|--|-------------------------------------|
| q02 | | | 0.000 | $\text{mmol} \cdot (\text{3600 s})^{-1} \cdot \text{g}^{-1}$ | <input type="checkbox"/> |
| qC02 | | | 0.000 | $\text{mmol} \cdot (\text{3600 s})^{-1} \cdot \text{g}^{-1}$ | <input type="checkbox"/> |
| X_a | X_a | | 0.100 | dimensionless | <input type="checkbox"/> |
| X_AcDH | X_AcDH | | 0.008 | dimensionless | <input type="checkbox"/> |
| k_1h | | | 0.584 | $\text{g} \cdot \text{l}^{-1} \cdot (\text{3600 s})^{-1}$ | <input checked="" type="checkbox"/> |
| K_1h | | | 0.012 | $\text{g} \cdot \text{l}^{-1}$ | <input checked="" type="checkbox"/> |
| k_1l | | | 1.430 | $\text{g} \cdot \text{l}^{-1} \cdot (\text{3600 s})^{-1}$ | <input checked="" type="checkbox"/> |
| K_1l | | | 0.940 | $\text{g} \cdot \text{l}^{-1}$ | <input checked="" type="checkbox"/> |
| k_1e | | | 47.100 | $\text{g} \cdot \text{l}^{-1} \cdot (\text{3600 s})^{-1}$ | <input checked="" type="checkbox"/> |
| K_1e | | | 0.120 | $\text{g} \cdot \text{l}^{-1}$ | <input checked="" type="checkbox"/> |
| K_1i | | | 14.200 | $\text{g}^{-1} \cdot \text{l}$ | <input checked="" type="checkbox"/> |
| k_2 | | | 0.501 | $\text{g} \cdot \text{l}^{-1} \cdot (\text{3600 s})^{-1}$ | <input checked="" type="checkbox"/> |
| K_2 | | | $2 \cdot 10^{-5}$ | $\text{g} \cdot \text{l}^{-1}$ | <input checked="" type="checkbox"/> |
| K_2i | | | 0.101 | $\text{g}^{-1} \cdot \text{l}$ | <input checked="" type="checkbox"/> |
| k_3 | | | 5.810 | $\text{g} \cdot \text{l}^{-1} \cdot (\text{3600 s})^{-1}$ | <input checked="" type="checkbox"/> |
| K_3 | | | $5 \cdot 10^{-7}$ | $\text{g} \cdot \text{l}^{-1}$ | <input checked="" type="checkbox"/> |
| k_4 | | | 4.800 | $\text{g} \cdot \text{l}^{-1} \cdot (\text{3600 s})^{-1}$ | <input checked="" type="checkbox"/> |
| K_4 | | | $2.64 \cdot 10^{-4}$ | $\text{g} \cdot \text{l}^{-1}$ | <input checked="" type="checkbox"/> |
| k_5 | | | 0.010 | $\text{g} \cdot \text{l}^{-1} \cdot (\text{3600 s})^{-1}$ | <input checked="" type="checkbox"/> |
| K_5 | | | 0.010 | $\text{g} \cdot \text{l}^{-1}$ | <input checked="" type="checkbox"/> |
| k_5e | | | 0.775 | $\text{g} \cdot \text{l}^{-1} \cdot (\text{3600 s})^{-1}$ | <input checked="" type="checkbox"/> |
| K_5e | | | 0.100 | $\text{g} \cdot \text{l}^{-1}$ | <input checked="" type="checkbox"/> |
| K_5i | | | 440.000 | $\text{g}^{-1} \cdot \text{l}$ | <input checked="" type="checkbox"/> |
| k_6 | | | 2.820 | $\text{g} \cdot \text{l}^{-1} \cdot (\text{3600 s})^{-1}$ | <input checked="" type="checkbox"/> |
| K_6 | | | 0.034 | $\text{g} \cdot \text{l}^{-1}$ | <input checked="" type="checkbox"/> |
| k_6r | | | 0.013 | dimensionless | <input checked="" type="checkbox"/> |
| K_6e | | | 0.057 | $\text{g} \cdot \text{l}^{-1}$ | <input checked="" type="checkbox"/> |
| k_7 | | | 1.203 | $\text{g} \cdot \text{l}^{-1} \cdot (\text{3600 s})^{-1}$ | <input checked="" type="checkbox"/> |
| K_7 | | | 0.010 | $\text{g} \cdot \text{l}^{-1}$ | <input checked="" type="checkbox"/> |
| k_8 | | | 0.589 | $\text{g} \cdot \text{l}^{-1} \cdot (\text{3600 s})^{-1}$ | <input checked="" type="checkbox"/> |
| k_9 | | | 0.008 | $\text{g} \cdot \text{l}^{-1} \cdot (\text{3600 s})^{-1}$ | <input checked="" type="checkbox"/> |
| K_9 | | | 10^{-6} | $\text{g} \cdot \text{l}^{-1}$ | <input checked="" type="checkbox"/> |
| k_9e | | | 0.075 | $\text{g} \cdot \text{l}^{-1} \cdot (\text{3600 s})^{-1}$ | <input checked="" type="checkbox"/> |

| Id | Name | SBO | Value | Unit | Constant |
|-------|--------------|-----|--------|--|-------------------------------------|
| K_9e | | | 13.000 | $\text{g} \cdot \text{l}^{-1}$ | <input checked="" type="checkbox"/> |
| K_9i | | | 25.000 | $\text{g}^{-1} \cdot \text{l}$ | <input checked="" type="checkbox"/> |
| k_9c | | | 0.004 | $\text{g} \cdot \text{l}^{-1} \cdot (\text{s})^{-1}$ | <input checked="" type="checkbox"/> |
| k_10 | | | 0.392 | $\text{g} \cdot \text{l}^{-1} \cdot (\text{s})^{-1}$ | <input checked="" type="checkbox"/> |
| K_10 | | | 0.002 | $\text{g} \cdot \text{l}^{-1}$ | <input checked="" type="checkbox"/> |
| k_10e | | | 0.003 | $\text{g} \cdot \text{l}^{-1} \cdot (\text{s})^{-1}$ | <input checked="" type="checkbox"/> |
| K_10e | | | 0.002 | $\text{g} \cdot \text{l}^{-1}$ | <input checked="" type="checkbox"/> |
| k_11 | | | 0.020 | $\text{g} \cdot \text{l}^{-1} \cdot (\text{s})^{-1}$ | <input checked="" type="checkbox"/> |
| D | Dilutionrate | | 0.100 | $(\text{s})^{-1}$ | <input checked="" type="checkbox"/> |

6 Rules

This is an overview of six rules.

6.1 Rule a

Rule a is an assignment rule for species a:

$$a = [x] \cdot X_a \quad (1)$$

Derived unit $\text{g} \cdot \text{l}^{-1}$

6.2 Rule AcDH

Rule AcDH is an assignment rule for species AcDH:

$$\text{AcDH} = [x] \cdot X_{\text{AcDH}} \quad (2)$$

Derived unit $\text{g} \cdot \text{l}^{-1}$

6.3 Rule X_a

Rule X_a is a rate rule for parameter X_a:

$$\frac{d}{dt}X_a = \frac{(0.732 \cdot r7 + 0.619 \cdot r8) \cdot (1 - X_a) - r9 - r10}{[x] \cdot \text{vol}(\text{env})} \quad (3)$$

6.4 Rule X_AcDH

Rule X_AcDH is a rate rule for parameter X_AcDH:

$$\frac{d}{dt}X_{\text{AcDH}} = \frac{r9 - r11 - (0.732 \cdot r7 + 0.619 \cdot r8) \cdot X_{\text{AcDH}}}{[x] \cdot \text{vol}(\text{env})} \quad (4)$$

6.5 Rule q02

Rule q02 is an assignment rule for parameter q02:

$$\begin{aligned} qO2 & \\ = & \frac{\frac{1000}{32} \cdot (0.178 \cdot r1 + 0.908 \cdot r2 + 0.363 \cdot r4 + 1.066 \cdot r5 - 0.363 \cdot r6 + 0.063 \cdot r7 + 0.214 \cdot r8)}{[x] \cdot \text{vol}(\text{env})} \end{aligned} \quad (5)$$

6.6 Rule qC02

Rule qC02 is an assignment rule for parameter qC02:

$$qCO2 = \frac{\frac{1000}{44.01} \cdot (1.499 \cdot r2 + 0.5 \cdot r3 + 1.466 \cdot r5 + 0.127 \cdot r7 + 0.325 \cdot r8)}{[x] \cdot \text{vol}(\text{env})} \quad (6)$$

7 Reactions

This model contains 20 reactions. All reactions are listed in the following table and are subsequently described in detail. If a reaction is affected by a modifier, the identifier of this species is written above the reaction arrow.

Table 5: Overview of all reactions

| Nº | Id | Name | Reaction Equation | SBO |
|----|---------------|------------------------|---|---------|
| 1 | r1 | glycolysis | $s_glu \xrightarrow{s_acetald, x} 0 \cdot 978 s_pyr + 0 \cdot 178 \text{ Red}$ | 0000205 |
| 2 | r2 | TCA (pyruvate) | $s_pyr \xrightarrow{x, s_glu} 1 \cdot 499 \text{ CO}_2 + 0 \cdot 908 \text{ Red}$ | 0000205 |
| 3 | r3 | Pyruvate Dehydrogenase | $s_pyr \xrightarrow{x} 0 \cdot 5 s_acetald + 0 \cdot 33 \text{ CO}_2$ | 0000200 |
| 4 | r4 | Acetald. dehydrogenase | $s_acetald \xrightarrow{x, s_EtOH} 1 \cdot 363 s_acetate + 0 \cdot 363 \text{ Red}$ | 0000200 |
| 5 | r5 | TCA (acetate) | $s_acetate \xrightarrow{x, s_glu} 1 \cdot 446 \text{ CO}_2 + 1 \cdot 066 \text{ Red}$ | 0000205 |
| 6 | r6 | ADH | $s_acetald + 0 \cdot 363 \text{ Red} \xrightleftharpoons{x} 1 \cdot 045 s_EtOH$ | 0000200 |
| 7 | r7 | BM growth (gluc) | $s_glu \xrightarrow{x} 0 \cdot 732 x + 0 \cdot 127 \text{ CO}_2 + 0 \cdot 063 \text{ Red}$ | 0000205 |
| 8 | r8 | BM growth (acetate) | $s_acetate \xrightarrow{x, s_glu} 0 \cdot 619 x + 0 \cdot 325 \text{ CO}_2 + 0 \cdot 214 \text{ Red}$ | 0000205 |
| 9 | r9 | Acdh production | $a \xrightarrow{x, s_glu, s_EtOH} \text{AcDH}$ | 0000184 |
| 10 | r10 | active BM degradation | $a \xrightarrow{x, s_glu, s_EtOH} \emptyset$ | 0000179 |
| 11 | r11 | Acdh degradation | $\text{AcDH} \xrightarrow{x} \emptyset$ | 0000179 |
| 12 | s_glu_in | Glucose inflow | $S_f \longrightarrow s_glu$ | 0000185 |
| 13 | s_glu_out | Glucose outflow | $s_glu \longrightarrow \emptyset$ | 0000185 |
| 14 | s_pyr_out | Pyruvate outflow | $s_pyr \longrightarrow \emptyset$ | 0000185 |
| 15 | s_acetate_out | Acetate outflow | $s_acetate \longrightarrow \emptyset$ | 0000185 |
| 16 | s_acetald_out | Acetaldehyde outflow | $s_acetald \longrightarrow \emptyset$ | 0000185 |
| 17 | s_EtOH_out | EtOH outflow | $s_EtOH \longrightarrow \emptyset$ | 0000185 |
| 18 | a_out | active BM outflow | $a \longrightarrow \emptyset$ | 0000185 |

| Nº | Id | Name | Reaction Equation | SBO |
|----|----------|-----------------|---|---------|
| 19 | x_out | BM outflow | $x \longrightarrow \emptyset$ | 0000185 |
| 20 | AcDH_out | AcDH BM outflow | $\text{AcDH} \longrightarrow \emptyset$ | 0000185 |

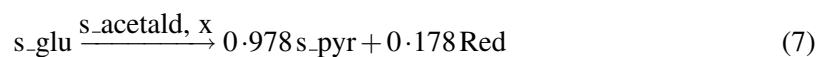
7.1 Reaction r1

This is an irreversible reaction of one reactant forming two products influenced by two modifiers.

Name glycolysis

SBO:0000205 composite biochemical process

Reaction equation



Reactant

Table 6: Properties of each reactant.

| Id | Name | SBO |
|-------|---------|-----|
| s_glu | Glucose | |

Modifiers

Table 7: Properties of each modifier.

| Id | Name | SBO |
|-----------|--------------|-----|
| s_acetald | Acetaldehyde | |
| x | BM | |

Products

Table 8: Properties of each product.

| Id | Name | SBO |
|-------|------------------|-----|
| s_pyr | Pyruvate | |
| Red | Red. Equ. (NADH) | |

Kinetic Law

Derived unit contains undeclared units

$$v_1 = \left(\frac{k_{1l} \cdot [s_glu]}{[s_glu] + K_{1l}} + \frac{k_{1h} \cdot [s_glu]}{[s_glu] + K_{1h}} + \frac{k_{1e} \cdot [s_acetald] \cdot [s_glu]}{[s_glu] \cdot (K_{1i} \cdot [s_acetald] + 1) + K_{1e}} \right) \cdot [x] \cdot X_a \cdot vol(env) \quad (8)$$

7.2 Reaction r2

This is an irreversible reaction of one reactant forming two products influenced by two modifiers.

Name TCA (pyruvate)

SBO:0000205 composite biochemical process

Reaction equation



Reactant

Table 9: Properties of each reactant.

| Id | Name | SBO |
|-------|----------|-----|
| s_pyr | Pyruvate | |

Modifiers

Table 10: Properties of each modifier.

| Id | Name | SBO |
|-------|---------|-----|
| x | BM | |
| s_glu | Glucose | |

Products

Table 11: Properties of each product.

| Id | Name | SBO |
|-----|------------------|-----|
| CO2 | CO2 | |
| Red | Red. Equ. (NADH) | |

Kinetic Law

Derived unit contains undeclared units

$$v_2 = \frac{k_2 \cdot [\text{s_pyr}]}{([\text{s_pyr}] + K_2) \cdot (K_{2i} \cdot [\text{s_glu}] + 1)} \cdot [\text{x}] \cdot X_a \cdot \text{vol}(\text{env}) \quad (10)$$

7.3 Reaction r3

This is an irreversible reaction of one reactant forming two products influenced by one modifier.

Name Pyruvate Dehydrogenase

SBO:0000200 redox reaction

Reaction equation



Reactant

Table 12: Properties of each reactant.

| Id | Name | SBO |
|-------|----------|-----|
| s_pyr | Pyruvate | |

Modifier

Table 13: Properties of each modifier.

| Id | Name | SBO |
|----|------|-----|
| x | BM | |

Products

Table 14: Properties of each product.

| Id | Name | SBO |
|-----------|--------------|-----|
| s_acetald | Acetaldehyde | |
| CO2 | CO2 | |

Kinetic Law

Derived unit $\text{g}^2 \cdot \text{l}^{-1} \cdot (3600 \text{ s})^{-1}$

$$v_3 = \frac{k_3 \cdot [\text{s_pyr}]^4}{[\text{s_pyr}]^4 + K_3} \cdot [x] \cdot X_a \cdot \text{vol}(\text{env}) \quad (12)$$

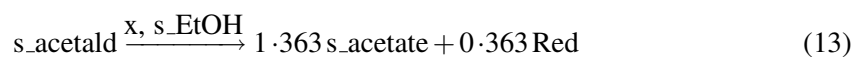
7.4 Reaction r4

This is an irreversible reaction of one reactant forming two products influenced by two modifiers.

Name Acetald. dehydrogenase

SBO:0000200 redox reaction

Reaction equation



Reactant

Table 15: Properties of each reactant.

| Id | Name | SBO |
|-----------|--------------|-----|
| s_acetald | Acetaldehyde | |

Modifiers

Table 16: Properties of each modifier.

| Id | Name | SBO |
|--------|------|-----|
| x | BM | |
| s_EtOH | EtOH | |

Products

Table 17: Properties of each product.

| Id | Name | SBO |
|-----------|------------------|-----|
| s_acetate | Acetate | |
| Red | Red. Equ. (NADH) | |

Kinetic Law

Derived unit $g^2 \cdot l^{-1} \cdot (3600 s)^{-1}$

$$v_4 = \frac{k_4 \cdot [s_acetald]}{[s_acetald] + K_4} \cdot [x] \cdot X_a \cdot X_{AcDH} \cdot vol(env) \quad (14)$$

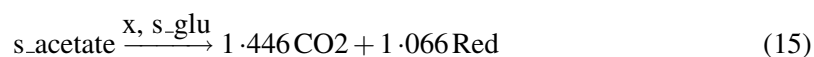
7.5 Reaction r5

This is an irreversible reaction of one reactant forming two products influenced by two modifiers.

Name TCA (acetate)

SBO:0000205 composite biochemical process

Reaction equation



Reactant

Table 18: Properties of each reactant.

| Id | Name | SBO |
|-----------|---------|-----|
| s_acetate | Acetate | |

Modifiers

Table 19: Properties of each modifier.

| Id | Name | SBO |
|-------|---------|-----|
| x | BM | |
| s_glu | Glucose | |

Products

Table 20: Properties of each product.

| Id | Name | SBO |
|-----|------------------|-----|
| CO2 | CO2 | |
| Red | Red. Equ. (NADH) | |

Kinetic Law

Derived unit contains undeclared units

$$v_5 = \left(\frac{k_5 \cdot [s_acetate]}{[s_acetate] + K_5} + \frac{k_{5e} \cdot [s_acetate]}{([s_acetate] + K_{5e}) \cdot (1 + K_{5i} \cdot [s_glu])} \right) \cdot [x] \cdot X_a \cdot vol(env) \quad (16)$$

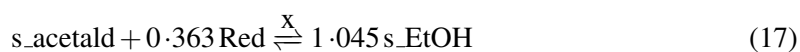
7.6 Reaction r6

This is a reversible reaction of two reactants forming one product influenced by one modifier.

Name ADH

SBO:0000200 redox reaction

Reaction equation



Reactants

Table 21: Properties of each reactant.

| Id | Name | SBO |
|-----------|------------------|-----|
| s_acetald | Acetaldehyde | |
| Red | Red. Equ. (NADH) | |

Modifier

Table 22: Properties of each modifier.

| Id | Name | SBO |
|----|------|-----|
| x | BM | |

Product

Table 23: Properties of each product.

| Id | Name | SBO |
|--------|------|-----|
| s_EtOH | EtOH | |

Kinetic Law

Derived unit $\text{g}^2 \cdot \text{l}^{-1} \cdot (3600 \text{ s})^{-1}$

$$v_6 = \frac{k_6 \cdot ([s_acetald] - k_{6r} \cdot [s_EtOH])}{[s_acetald] + K_6 + K_{6e} \cdot [s_EtOH]} \cdot [x] \cdot X_a \cdot \text{vol}(\text{env}) \quad (18)$$

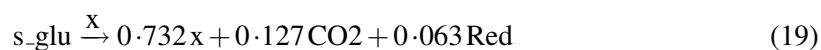
7.7 Reaction r_7

This is an irreversible reaction of one reactant forming three products influenced by one modifier.

Name BM growth (gluc)

SBO:0000205 composite biochemical process

Reaction equation



Reactant

Table 24: Properties of each reactant.

| Id | Name | SBO |
|-------|---------|-----|
| s_glu | Glucose | |

Modifier

Table 25: Properties of each modifier.

| Id | Name | SBO |
|----|------|-----|
| x | BM | |

Products

Table 26: Properties of each product.

| Id | Name | SBO |
|-----------------|------------------|-----|
| x | BM | |
| CO ₂ | CO ₂ | |
| Red | Red. Equ. (NADH) | |

Kinetic Law

Derived unit $g^2 \cdot l^{-1} \cdot (3600\text{ s})^{-1}$

$$v_7 = \frac{k_7 \cdot [s_glu]}{[s_glu] + K_7} \cdot [x] \cdot X_a \cdot vol(env) \quad (20)$$

7.8 Reaction r8

This is an irreversible reaction of one reactant forming three products influenced by two modifiers.

Name BM growth (acetate)

SBO:0000205 composite biochemical process

Reaction equation



Reactant

Table 27: Properties of each reactant.

| Id | Name | SBO |
|-----------|---------|-----|
| s_acetate | Acetate | |

Modifiers

Table 28: Properties of each modifier.

| Id | Name | SBO |
|-------|---------|-----|
| x | BM | |
| s_glu | Glucose | |

Products

Table 29: Properties of each product.

| Id | Name | SBO |
|-----|------------------|-----|
| x | BM | |
| CO2 | CO2 | |
| Red | Red. Equ. (NADH) | |

Kinetic Law

Derived unit contains undeclared units

$$v_8 = \frac{k_8 \cdot [s_acetate]}{([s_acetate] + K_{5e}) \cdot (1 + K_{5i} \cdot [s_glu])} \cdot [x] \cdot X_a \cdot vol(env) \quad (22)$$

7.9 Reaction r9

This is an irreversible reaction of one reactant forming one product influenced by three modifiers.

Name Acdh production

SBO:0000184 translation

Reaction equation



Reactant

Table 30: Properties of each reactant.

| Id | Name | SBO |
|----|------------|-----|
| a | BM(active) | |

Modifiers

Table 31: Properties of each modifier.

| Id | Name | SBO |
|--------|---------|-----|
| x | BM | |
| s_glu | Glucose | |
| s_EtOH | EtOH | |

Product

Table 32: Properties of each product.

| Id | Name | SBO |
|------|----------|-----|
| AcDH | BM(AcDH) | |

Kinetic Law

Derived unit contains undeclared units

$$v_9 = \left(\frac{k_{-9} \cdot [s_glu]}{[s_glu] + K_{-9}} + \frac{k_{-9c} \cdot [s_EtOH]}{[s_EtOH] + K_{-9c}} + \frac{k_{-9c} \cdot [s_glu]}{[s_glu] + K_{-9}} \right) \cdot X_a \cdot [x] \cdot vol(env) \quad (24)$$

7.10 Reaction r10

This is an irreversible reaction of one reactant forming no product influenced by three modifiers.

Name active BM degradation

SBO:0000179 degradation

Reaction equation



Reactant

Table 33: Properties of each reactant.

| Id | Name | SBO |
|----|------------|-----|
| a | BM(active) | |

Modifiers

Table 34: Properties of each modifier.

| Id | Name | SBO |
|--------|---------|-----|
| x | BM | |
| s_glu | Glucose | |
| s_EtOH | EtOH | |

Kinetic Law

Derived unit $\text{g}^2 \cdot \text{l}^{-1} \cdot (3600 \text{ s})^{-1}$

$$v_{10} = \left(\frac{k_{10} \cdot [s_glu]}{[s_glu] + K_{10}} + \frac{k_{10e} \cdot [s_EtOH]}{[s_EtOH] + K_{10e}} \right) \cdot X_a \cdot [x] \cdot \text{vol}(\text{env}) \quad (26)$$

7.11 Reaction r11

This is an irreversible reaction of one reactant forming no product influenced by one modifier.

Name Acdh degradation

SBO:0000179 degradation

Reaction equation



Reactant

Table 35: Properties of each reactant.

| Id | Name | SBO |
|------|----------|-----|
| AcDH | BM(AcDH) | |

Modifier

Table 36: Properties of each modifier.

| Id | Name | SBO |
|----|------|-----|
| x | BM | |

Kinetic Law

Derived unit $\text{g}^2 \cdot \text{l}^{-1} \cdot (3600 \text{ s})^{-1}$

$$v_{11} = k_{11} \cdot X_{\text{AcDH}} \cdot [x] \cdot \text{vol}(\text{env}) \quad (28)$$

7.12 Reaction `s_glu_in`

This is an irreversible reaction of one reactant forming one product.

Name Glucose inflow

SBO:0000185 transport reaction

Reaction equation



Reactant

Table 37: Properties of each reactant.

| Id | Name | SBO |
|-----|---------------|-----|
| S_f | Glucose(feed) | |

Product

Table 38: Properties of each product.

| Id | Name | SBO |
|-------|---------|-----|
| s_glu | Glucose | |

Kinetic Law

Derived unit $\text{g} \cdot (3600 \text{ s})^{-1}$

$$v_{12} = [\text{S}_f] \cdot D \cdot \text{vol}(\text{env}) \quad (30)$$

7.13 Reaction s_glu_out

This is an irreversible reaction of one reactant forming no product.

Name Glucose outflow

SBO:0000185 transport reaction

Reaction equation



Reactant

Table 39: Properties of each reactant.

| Id | Name | SBO |
|-------|---------|-----|
| s_glu | Glucose | |

Kinetic Law

Derived unit $\text{g} \cdot (3600 \text{ s})^{-1}$

$$v_{13} = [\text{s_glu}] \cdot D \cdot \text{vol}(\text{env}) \quad (32)$$

7.14 Reaction s_pyr_out

This is an irreversible reaction of one reactant forming no product.

Name Pyruvate outflow

SBO:0000185 transport reaction

Reaction equation



Reactant

Table 40: Properties of each reactant.

| Id | Name | SBO |
|-------|----------|-----|
| s_pyr | Pyruvate | |

Kinetic Law

Derived unit $\text{g} \cdot (3600 \text{ s})^{-1}$

$$v_{14} = [\text{s_pyr}] \cdot D \cdot \text{vol}(\text{env}) \quad (34)$$

7.15 Reaction s_acetate_out

This is an irreversible reaction of one reactant forming no product.

Name Acetate outflow

SBO:0000185 transport reaction

Reaction equation



Reactant

Table 41: Properties of each reactant.

| Id | Name | SBO |
|-----------|---------|-----|
| s_acetate | Acetate | |

Kinetic Law

Derived unit $\text{g} \cdot (3600 \text{ s})^{-1}$

$$v_{15} = [\text{s_acetate}] \cdot D \cdot \text{vol}(\text{env}) \quad (36)$$

7.16 Reaction `s_acetald_out`

This is an irreversible reaction of one reactant forming no product.

Name Acetaldehyde outflow

SBO:0000185 transport reaction

Reaction equation



Reactant

Table 42: Properties of each reactant.

| Id | Name | SBO |
|------------------------|--------------|-----|
| <code>s_acetald</code> | Acetaldehyde | |

Kinetic Law

Derived unit $\text{g} \cdot (3600 \text{ s})^{-1}$

$$v_{16} = [\text{s_acetald}] \cdot D \cdot \text{vol}(\text{env}) \quad (38)$$

7.17 Reaction `s_EtOH_out`

This is an irreversible reaction of one reactant forming no product.

Name EtOH outflow

SBO:0000185 transport reaction

Reaction equation



Reactant

Table 43: Properties of each reactant.

| Id | Name | SBO |
|---------------------|------|-----|
| <code>s_EtOH</code> | EtOH | |

Kinetic Law

Derived unit $\text{g} \cdot (3600 \text{ s})^{-1}$

$$v_{17} = [\text{s_EtOH}] \cdot D \cdot \text{vol}(\text{env}) \quad (40)$$

7.18 Reaction `a_out`

This is an irreversible reaction of one reactant forming no product.

Name active BM outflow

SBO:0000185 transport reaction

Reaction equation



Reactant

Table 44: Properties of each reactant.

| Id | Name | SBO |
|----|------------|-----|
| a | BM(active) | |

Kinetic Law

Derived unit $\text{g} \cdot (3600 \text{ s})^{-1}$

$$v_{18} = [a] \cdot D \cdot \text{vol}(\text{env}) \quad (42)$$

7.19 Reaction `x_out`

This is an irreversible reaction of one reactant forming no product.

Name BM outflow

SBO:0000185 transport reaction

Reaction equation



Reactant

Table 45: Properties of each reactant.

| Id | Name | SBO |
|----|------|-----|
| x | BM | |

Kinetic Law

Derived unit $\text{g} \cdot (3600 \text{ s})^{-1}$

$$v_{19} = [\text{x}] \cdot D \cdot \text{vol}(\text{env}) \quad (44)$$

7.20 Reaction AcDH_out

This is an irreversible reaction of one reactant forming no product.

Name AcDH BM outflow

SBO:0000185 transport reaction

Reaction equation



Reactant

Table 46: Properties of each reactant.

| Id | Name | SBO |
|------|----------|-----|
| AcDH | BM(AcDH) | |

Kinetic Law

Derived unit $\text{g} \cdot (3600 \text{ s})^{-1}$

$$v_{20} = [\text{AcDH}] \cdot D \cdot \text{vol}(\text{env}) \quad (46)$$

8 Derived Rate Equations

When interpreted as an ordinary differential equation framework, this model implies the following set of equations for the rates of change of each species.

Identifiers for kinetic laws highlighted in gray cannot be verified to evaluate to units of SBML substance per time. As a result, some SBML interpreters may not be able to verify the consistency of the units on quantities in the model. Please check if

- parameters without an unit definition are involved or
- volume correction is necessary because the `hasOnlySubstanceUnits` flag may be set to `false` and `spacialDimensions > 0` for certain species.

8.1 Species `s_glu`

Name Glucose

SBO:0000247 simple chemical

Initial concentration $15 \text{ g} \cdot \text{l}^{-1}$

This species takes part in nine reactions (as a reactant in `r1`, `r7`, `s_glu_out` and as a product in `s_glu_in` and as a modifier in `r2`, `r5`, `r8`, `r9`, `r10`).

$$\frac{d}{dt}s_{\text{glu}} = v_{12} - v_1 - v_7 - v_{13} \quad (47)$$

8.2 Species `s_pyr`

Name Pyruvate

SBO:0000247 simple chemical

Initial concentration $0 \text{ g} \cdot \text{l}^{-1}$

This species takes part in four reactions (as a reactant in `r2`, `r3`, `s_pyr_out` and as a product in `r1`).

$$\frac{d}{dt}s_{\text{pyr}} = 0.978 v_1 - v_2 - v_3 - v_{14} \quad (48)$$

8.3 Species `s_acetate`

Name Acetate

SBO:0000247 simple chemical

Initial concentration $0 \text{ g} \cdot \text{l}^{-1}$

This species takes part in four reactions (as a reactant in `r5`, `r8`, `s_acetate_out` and as a product in `r4`).

$$\frac{d}{dt}s_{\text{acetate}} = 1.363 v_4 - v_5 - v_8 - v_{15} \quad (49)$$

8.4 Species `s_acetald`

Name Acetaldehyde

SBO:0000247 simple chemical

Initial concentration $0 \text{ g} \cdot \text{l}^{-1}$

This species takes part in five reactions (as a reactant in `r4`, `r6`, `s_acetald_out` and as a product in `r3` and as a modifier in `r1`).

$$\frac{d}{dt}s_acetald = 0.5 v_3 - v_4 - v_6 - v_{16} \quad (50)$$

8.5 Species `s_EtOH`

Name EtOH

SBO:0000247 simple chemical

Initial concentration $0 \text{ g} \cdot \text{l}^{-1}$

This species takes part in five reactions (as a reactant in `s_EtOH_out` and as a product in `r6` and as a modifier in `r4`, `r9`, `r10`).

$$\frac{d}{dt}s_EtOH = 1.045 v_6 - v_{17} \quad (51)$$

8.6 Species `x`

Name BM

SBO:0000240 material entity

Initial concentration $0.0020 \text{ g} \cdot \text{l}^{-1}$

This species takes part in 14 reactions (as a reactant in `x_out` and as a product in `r7`, `r8` and as a modifier in `r1`, `r2`, `r3`, `r4`, `r5`, `r6`, `r7`, `r8`, `r9`, `r10`, `r11`).

$$\frac{d}{dt}x = 0.732 v_7 + 0.619 v_8 - v_{19} \quad (52)$$

8.7 Species `a`

Name BM(active)

SBO:0000241 functional entity

Initial concentration $0 \text{ g} \cdot \text{l}^{-1}$

Involved in rule `a`

This species takes part in three reactions (as a reactant in `r9`, `r10`, `a_out`). Not these but one rule determines the species' quantity because this species is on the boundary of the reaction system.

8.8 Species [AcDH](#)

Name BM(AcDH)

SBO:0000241 functional entity

Initial concentration $0 \text{ g} \cdot \text{l}^{-1}$

Involved in rule [AcDH](#)

This species takes part in three reactions (as a reactant in [r11](#), [AcDH_out](#) and as a product in [r9](#)). Not these but one rule determines the species' quantity because this species is on the boundary of the reaction system.

8.9 Species [CO2](#)

Name CO2

SBO:0000247 simple chemical

Initial concentration $0 \text{ g} \cdot \text{l}^{-1}$

This species takes part in five reactions (as a product in [r2](#), [r3](#), [r5](#), [r7](#), [r8](#)), which do not influence its rate of change because this species is on the boundary of the reaction system:

$$\frac{d}{dt} \text{CO}_2 = 0 \quad (53)$$

8.10 Species [Red](#)

Name Red. Equ. (NADH)

SBO:0000247 simple chemical

Initial concentration $0 \text{ g} \cdot \text{l}^{-1}$

This species takes part in seven reactions (as a reactant in [r6](#) and as a product in [r1](#), [r2](#), [r4](#), [r5](#), [r7](#), [r8](#)), which do not influence its rate of change because this species is on the boundary of the reaction system:

$$\frac{d}{dt} \text{Red} = 0 \quad (54)$$

8.11 Species [S_f](#)

Name Glucose(feed)

SBO:0000247 simple chemical

Initial concentration $15 \text{ g} \cdot \text{l}^{-1}$

This species takes part in one reaction (as a reactant in `s_glu_in`), which does not influence its rate of change because this species is on the boundary of the reaction system:

$$\frac{d}{dt}S_f = 0 \quad (55)$$

A Glossary of Systems Biology Ontology Terms

SBO:0000179 degradation: Complete disappearance of a physical entity

SBO:0000184 translation: Process in which a polypeptide chain is produced from a messenger RNA

SBO:0000185 transport reaction: Movement of a physical entity without modification of the structure of the entity

SBO:0000200 redox reaction: Chemical process in which atoms have their oxidation number (oxidation state) changed

SBO:0000205 composite biochemical process: Process that involves the participation of chemical or biological entities and is composed of several elementary steps or reactions.

SBO:0000240 material entity: A real thing that is defined by its physico-chemical structure.

SBO:0000241 functional entity: A real thing, defined by its properties or the actions it performs, rather than its physico-chemical structure

SBO:0000247 simple chemical: Simple, non-repetitive chemical entity

SBO:0000290 physical compartment: Specific location of space, that can be bounded or not. A physical compartment can have 1, 2 or 3 dimensions

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