

SBML Model Report

Model name: “Gardner2000 - genetic toggle switch in E.coli”



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1 General Overview

This is a document in SBML Level 3 Version 1 format. This model was created by the following two authors: Vijayalakshmi Chelliah¹ and Nicolas Le Novre² at January 19th 2014 at 7:51 p. m. and last time modified at November 26th 2014 at 11:26 a. m. Table 1 shows an overview of the quantities of all components of this model.

Table 1: Number of components in this model, which are described in the following sections.

Element	Quantity	Element	Quantity
compartment types	0	compartments	1
species types	0	species	3
events	0	constraints	0
reactions	4	function definitions	2
global parameters	9	unit definitions	5
rules	1	initial assignments	2

Model Notes

Gardner2000 - genetic toggle switch in E.coli

The behaviour of the genetic toggle switch and the conditions for bistability has been studies using a synthetic, bistable gene circuit.

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This model is described in the article: [Construction of a genetic toggle switch in Escherichia coli](#). Gardner TS, Cantor CR, Collins JJ Nature. 2000 Jan 20;403(6767):339-42.

Abstract:

It has been proposed' that gene-regulatory circuits with virtually any desired property can be constructed from networks of simple regulatory elements. These properties, which include multistability and oscillations, have been found in specialized gene circuits such as the bacteriophage lambda switch and the Cyanobacteria circadian oscillator. However, these behaviours have not been demonstrated in networks of non-specialized regulatory components. Here we present the construction of a genetic toggle switch-a synthetic, bistable gene-regulatory network-in Escherichia coli and provide a simple theory that predicts the conditions necessary for bistability. The toggle is constructed from any two repressible promoters arranged in a mutually inhibitory network. It is flipped between stable states using transient chemical or thermal induction and exhibits a nearly ideal switching threshold. As a practical device, the toggle switch forms a synthetic, addressable cellular memory unit and has implications for biotechnology, biocomputing and gene therapy.

This model is hosted on [BioModels Database](#) and identified by: [BIOMD0000000507](#) .

To cite BioModels Database, please use: [BioModels Database: An enhanced, curated and annotated resource for published quantitative kinetic models](#) .

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2 Unit Definitions

This is an overview of five unit definitions.

2.1 Unit length

Name length

Definition m

2.2 Unit area

Name area

Definition m²

2.3 Unit volume

Name volume

Definition l

2.4 Unit `time`

Name `time`

Definition `s`

2.5 Unit `substance`

Name `substance`

Definition `mol`

3 Compartment

This model contains one compartment.

Table 2: Properties of all compartments.

Id	Name	SBO	Spatial Dimensions	Size	Unit	Constant	Outside
<code>compartment_1</code>	<code>compartment</code>	<code>0000290</code>	<code>3</code>	<code>1</code>		<input checked="" type="checkbox"/>	

3.1 Compartment `compartment_1`

This is a three dimensional compartment with a constant size of one litre.

Name `compartment`

SBO:0000290 `physical compartment`

4 Species

This model contains three species. Section [10](#) provides further details and the derived rates of change of each species.

Table 3: Properties of each species.

Id	Name	Compartment	Derived Unit	Constant	Boundary Condi- tion
species_1	U	compartment_1	$\text{mol} \cdot \text{l}^{-1}$	\square	\square
species_2	V	compartment_1	$\text{mol} \cdot \text{l}^{-1}$	\square	\square
species_3	IPTG	compartment_1	$\text{mol} \cdot \text{l}^{-1}$	\square	\square

5 Parameters

This model contains nine global parameters.

Table 4: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
parameter_1	alpha1		156.250		<input checked="" type="checkbox"/>
parameter_2	alpha2		15.600		<input checked="" type="checkbox"/>
parameter_3	beta		2.500		<input checked="" type="checkbox"/>
parameter_4	gamma		1.000		<input checked="" type="checkbox"/>
parameter_5	K		$2.9618 \cdot 10^{-5}$		<input checked="" type="checkbox"/>
parameter_6	nu		2.002		<input checked="" type="checkbox"/>
parameter_7	Umodif		0.000		<input type="checkbox"/>
ModelValue_4	Initial for K		$2.9618 \cdot 10^{-5}$		<input checked="" type="checkbox"/>
ModelValue_5	Initial for nu		2.002		<input checked="" type="checkbox"/>

6 Initialassignments

This is an overview of two initialassignments.

6.1 Initialassignment ModelValue_4

Derived unit contains undeclared units

Math parameter_5

6.2 Initialassignment ModelValue_5

Derived unit contains undeclared units

Math parameter_6

7 Function definitions

This is an overview of two function definitions.

7.1 Function definition function_1

Name toggle repressor production

SBO:0000393 production

Arguments alpha, X, n

Mathematical Expression

$$\frac{\alpha}{1 + X^n} \quad (1)$$

7.2 Function definition `function_2`**Name** toggle repressor production with induction**SBO:0000393** production**Arguments** alpha, X, n**Mathematical Expression**

$$\frac{\alpha}{1 + X^n} \quad (2)$$

8 Rule

This is an overview of one rule.

8.1 Rule `parameter_7`Rule `parameter_7` is an assignment rule for parameter `parameter_7`:

$$\text{parameter_7} = \frac{[\text{species_1}]}{\left(1 + \frac{[\text{species_3}]}{\text{ModelValue_4}}\right)^{\text{ModelValue_5}}} \quad (3)$$

9 Reactions

This model contains four reactions. All reactions are listed in the following table and are subsequently described in detail. If a reaction is affected by a modifier, the identifier of this species is written above the reaction arrow.

Table 5: Overview of all reactions

Nº	Id	Name	Reaction Equation	SBO
1	reaction_1	production of U	$\emptyset \xrightarrow{\text{species_2, species_2}} \text{species_1}$	0000393
2	reaction_2	degradation of U	$\text{species_1} \xrightarrow{\text{species_1}} \emptyset$	0000179
3	reaction_3	production of V	$\emptyset \longrightarrow \text{species_2}$	0000393
4	reaction_4	degration of V	$\text{species_2} \xrightarrow{\text{species_2}} \emptyset$	0000179

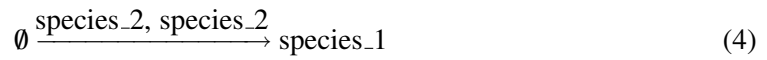
9.1 Reaction `reaction_1`

This is an irreversible reaction of no reactant forming one product influenced by two modifiers.

Name production of U

SBO:0000393 production

Reaction equation



Modifiers

Table 6: Properties of each modifier.

Id	Name	SBO
species_2	V	
species_2	V	

Product

Table 7: Properties of each product.

Id	Name	SBO
species_1	U	

Kinetic Law

Derived unit contains undeclared units

$$v_1 = \text{vol}(\text{compartment_1}) \cdot \text{function_1}(\text{parameter_1}, [\text{species_2}], \text{parameter_3}) \quad (5)$$

$$\text{function_1}(\alpha, X, n) = \frac{\alpha}{1 + X^n} \quad (6)$$

$$\text{function_1}(\alpha, X, n) = \frac{\alpha}{1 + X^n} \quad (7)$$

9.2 Reaction `reaction_2`

This is an irreversible reaction of one reactant forming no product influenced by one modifier.

Name degradation of U

SBO:0000179 degradation

Reaction equation



Reactant

Table 8: Properties of each reactant.

Id	Name	SBO
species_1	U	

Modifier

Table 9: Properties of each modifier.

Id	Name	SBO
species_1	U	

Kinetic Law

Derived unit mol

$$v_2 = \text{vol}(\text{compartment_1}) \cdot k_1 \cdot [\text{species_1}] \quad (9)$$

9.3 Reaction reaction_3

This is an irreversible reaction of no reactant forming one product.

Name production of V

SBO:0000393 production

Reaction equation



Product

Table 10: Properties of each product.

Id	Name	SBO
species_2	V	

Kinetic Law

Derived unit contains undeclared units

$$v_3 = \text{vol}(\text{compartment_1}) \cdot \text{function_2}(\text{parameter_2}, \text{parameter_7}, \text{parameter_4}) \quad (11)$$

$$\text{function_2}(\alpha, X, n) = \frac{\alpha}{1 + X^n} \quad (12)$$

$$\text{function_2}(\alpha, X, n) = \frac{\alpha}{1 + X^n} \quad (13)$$

9.4 Reaction `reaction_4`

This is an irreversible reaction of one reactant forming no product influenced by one modifier.

Name degradation of V

SBO:0000179 degradation

Reaction equation



Reactant

Table 11: Properties of each reactant.

Id	Name	SBO
<code>species_2</code>	V	

Modifier

Table 12: Properties of each modifier.

Id	Name	SBO
<code>species_2</code>	V	

Kinetic Law

Derived unit mol

$$v_4 = \text{vol}(\text{compartment_1}) \cdot k_1 \cdot [\text{species_2}] \quad (15)$$

10 Derived Rate Equations

When interpreted as an ordinary differential equation framework, this model implies the following set of equations for the rates of change of each species.

Identifiers for kinetic laws highlighted in gray cannot be verified to evaluate to units of SBML substance per time. As a result, some SBML interpreters may not be able to verify the consistency of the units on quantities in the model. Please check if

- parameters without an unit definition are involved or
- volume correction is necessary because the `hasOnlySubstanceUnits` flag may be set to `false` and `spacialDimensions` > 0 for certain species.

10.1 Species `species_1`

Name U

Notes concentration of repressor 1

Initial concentration $0 \text{ mol} \cdot \text{l}^{-1}$

This species takes part in three reactions (as a reactant in [reaction_2](#) and as a product in [reaction_1](#) and as a modifier in [reaction_2](#)).

$$\frac{d}{dt}\text{species}_1 = v_1 - v_2 \quad (16)$$

10.2 Species `species_2`

Name V

Notes concentration of repressor 2

Initial concentration $0 \text{ mol} \cdot \text{l}^{-1}$

This species takes part in five reactions (as a reactant in [reaction_4](#) and as a product in [reaction_3](#) and as a modifier in [reaction_1](#), [reaction_1](#), [reaction_4](#)).

$$\frac{d}{dt}\text{species}_2 = v_3 - v_4 \quad (17)$$

10.3 Species `species_3`

Name IPTG

Initial concentration $0 \text{ mol} \cdot \text{l}^{-1}$

This species does not take part in any reactions. Its quantity does hence not change over time:

$$\frac{d}{dt}\text{species}_3 = 0 \quad (18)$$

A Glossary of Systems Biology Ontology Terms

SBO:0000179 degradation: Complete disappearance of a physical entity

SBO:0000290 physical compartment: Specific location of space, that can be bounded or not.
A physical compartment can have 1, 2 or 3 dimensions

SBO:0000393 production: Generation of a material or conceptual entity.

SBML²TeX was developed by Andreas Dräger^a, Hannes Planatscher^a, Dieudonné M Wouamba^a, Adrian Schröder^a, Michael Hucka^b, Lukas Endler^c, Martin Golebiewski^d and Andreas Zell^a. Please see <http://www.ra.cs.uni-tuebingen.de/software/SBML2LaTeX> for more information.

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