

CPSC-406 Report

Your Name
Chapman University

February 11, 2026

Abstract

Contents

1	Introduction	1
2	Week by Week	1
2.1	Week 1	1
3	Synthesis	4
4	Evidence of Participation	4
5	Conclusion	4

1 Introduction

2 Week by Week

2.1 Week 1

Exercise 1

1. Word acceptance table

w	accepted by A_1 ?	accepted by A_2 ?
<i>aaa</i>	No	Yes
<i>aab</i>	Yes	No
<i>aba</i>	No	No
<i>abb</i>	No	No
<i>baa</i>	No	Yes
<i>bab</i>	No	No
<i>bba</i>	No	No
<i>bbb</i>	No	No

2. Description of the languages

Language of A_1 . In A_1 , any word beginning with b immediately goes to a trap state. If the word begins with a , the automaton stays in state 2 while reading a 's, and moves to the accepting state 3 upon reading a single b . Any further symbol leaves the accepting state.

Therefore, a word is accepted if and only if it consists of one or more a 's followed by exactly one b .

$$L(A_1) = \{a^n b \mid n \geq 1\}$$

Equivalently, as a regular expression:

$$L(A_1) = a^+ b$$

Language of A_2 . In A_2 , the only accepting state is 3. The automaton reaches state 3 precisely after reading two consecutive a 's. Any b resets the automaton to state 1.

Thus, a word is accepted if and only if it ends with at least two consecutive a 's.

$$L(A_2) = \{w \in \{a, b\}^* \mid w \text{ ends with } aa\}$$

Equivalently, as a regular expression:

$$L(A_2) = (a|b)^* aa$$

Exercise 2

Alphabet: $\Sigma = \{a, b\}$.

1. DFAs for the given languages

(1) All words that end with ab . Let $M_1 = (Q, \Sigma, \delta, q_0, F)$ where

$$Q = \{q_0, q_1, q_2\}, \quad q_0 \text{ start}, \quad F = \{q_2\}.$$

Transitions:

	a	b
q_0	q_1	q_0
q_1	q_1	q_2
q_2	q_1	q_0

State q_2 represents that the word currently ends in ab .

(2) All words that contain aba. Let $M_2 = (Q, \Sigma, \delta, q_0, F)$ where

$$Q = \{q_0, q_1, q_2, q_3\}, \quad q_0 \text{ start}, \quad F = \{q_3\}.$$

Transitions:

	a	b
q_0	q_1	q_0
q_1	q_1	q_2
q_2	q_3	q_0
q_3	q_3	q_3

State q_3 means the substring **aba** has been seen.

(3) Odd number of a's and odd number of b's. Use four states representing parity:

$$Q = \{(E, E), (E, O), (O, E), (O, O)\}$$

(start state (E, E)). Accepting state: (O, O) .

Reading a toggles the first component; reading b toggles the second component.

(4) Even number of a's and odd number of b's. Same construction as (3).

Start state: (E, E) . Accepting state: (E, O) .

Transitions again toggle parity accordingly.

(5) Any three consecutive characters contain at least one a. This is equivalent to saying the word does *not* contain **bbb**.

Use states counting consecutive b 's:

$$Q = \{q_0, q_1, q_2, q_3\}$$

- q_0 : no recent b
- q_1 : one consecutive b
- q_2 : two consecutive b 's
- q_3 : three consecutive b 's (trap)

Start: q_0 .

Accepting states: $\{q_0, q_1, q_2\}$.

Transitions:

- On a : go to q_0 from any state except q_3 - On b :

$$q_0 \rightarrow q_1, \quad q_1 \rightarrow q_2, \quad q_2 \rightarrow q_3, \quad q_3 \rightarrow q_3$$

(6) All words that contain bbb. Same structure as (5), but now:

Accepting state: $\{q_3\}$ only.

Once q_3 is reached, stay there.

2. Observations

Several patterns appear:

- Languages involving substrings (e.g. aba, bbb) use states that track partial progress toward matching the substring.
- Parity conditions use a product construction (Cartesian product) of two 2-state automata, giving 4 states.
- Conditions about avoiding a pattern (problem 5) are closely related to conditions about containing that pattern (problem 6); they differ mainly in which states are accepting.
- Many DFAs follow a systematic design pattern: track exactly the minimal information necessary to decide acceptance.

3 Synthesis

4 Evidence of Participation

5 Conclusion

References

[BLA] Author, [Title](#), Publisher, Year.