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PREFACE

This volume contains work on the decision problem done in Kazan(Russia), Tallinn (Estonia) and Vienna (Austria). The authors met several times to discuss and exchange their results and finally decided to write a monograph together. Besides a unified treatment of previously published results there are many new results first presented in this volume. We thank Grigori Mints for enlighting discussions and valuable hints. We are also grateful to Mrs. Franziska Gusel for typing the manuscript.

February 1993 C. Fermüller, A. Leitsch, T. Tammet, N. Zamov

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