

Let $A_n = [0, \frac{1}{n})$. As we know $\cap_{n=1}^{\infty} (0, \frac{1}{n}) = \emptyset$. But for A_n greatest lower bound is 0, so $\forall n [0 \in A_n]$. That satisfy given properties.
QED.