



TECHNICAL PROJECT

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TRAJECTORY PLANNING

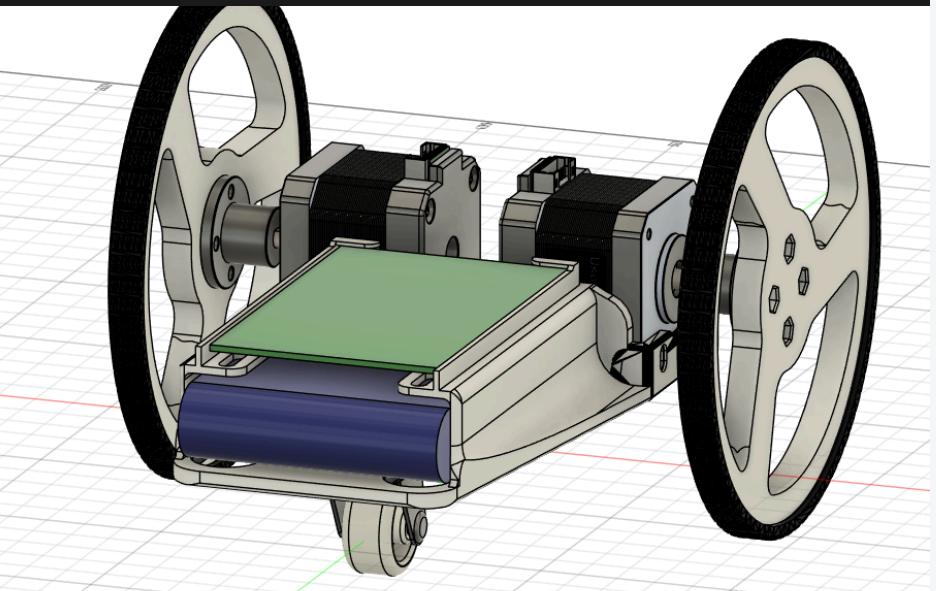
06

FUTURE DEVELOPMENTS



HARDWARE

CAD MODEL

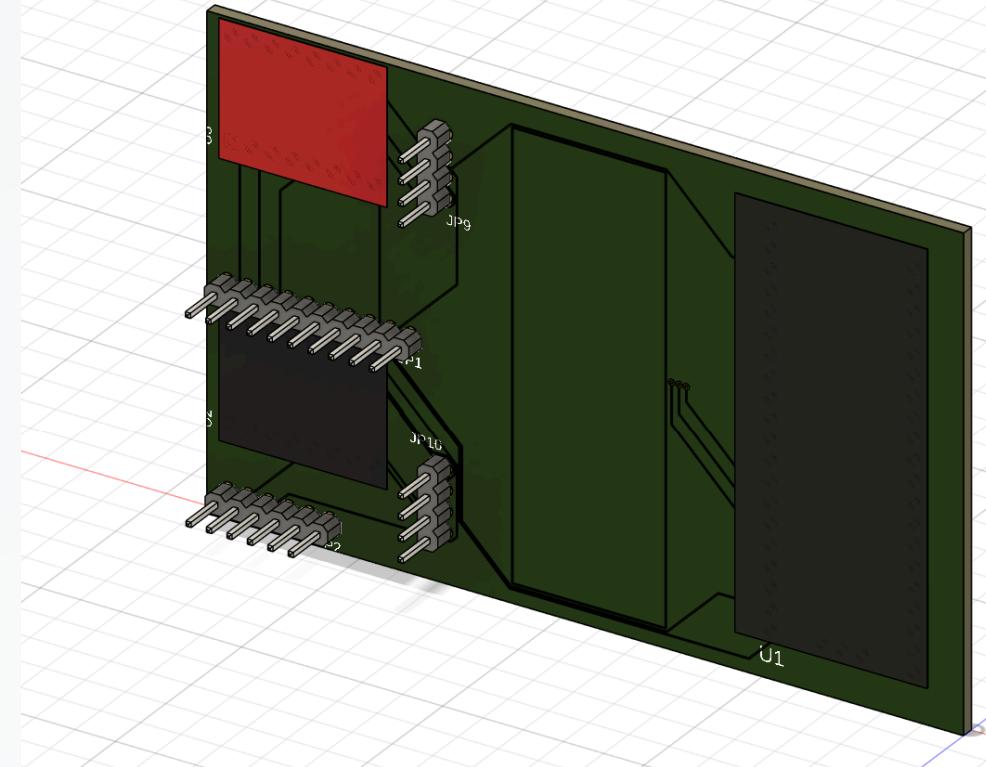


- Designed with Autodesk Fusion 360
- 3D printed and assembled by us

Components on the PCB

- Raspberry pi Pico
- HC 05 Bluetooth Module
- GY-6500 IMU Sensor
- Stepper Motors
- DRV8825 Stepper drivers

PCB



ROBOT SOFTWARE

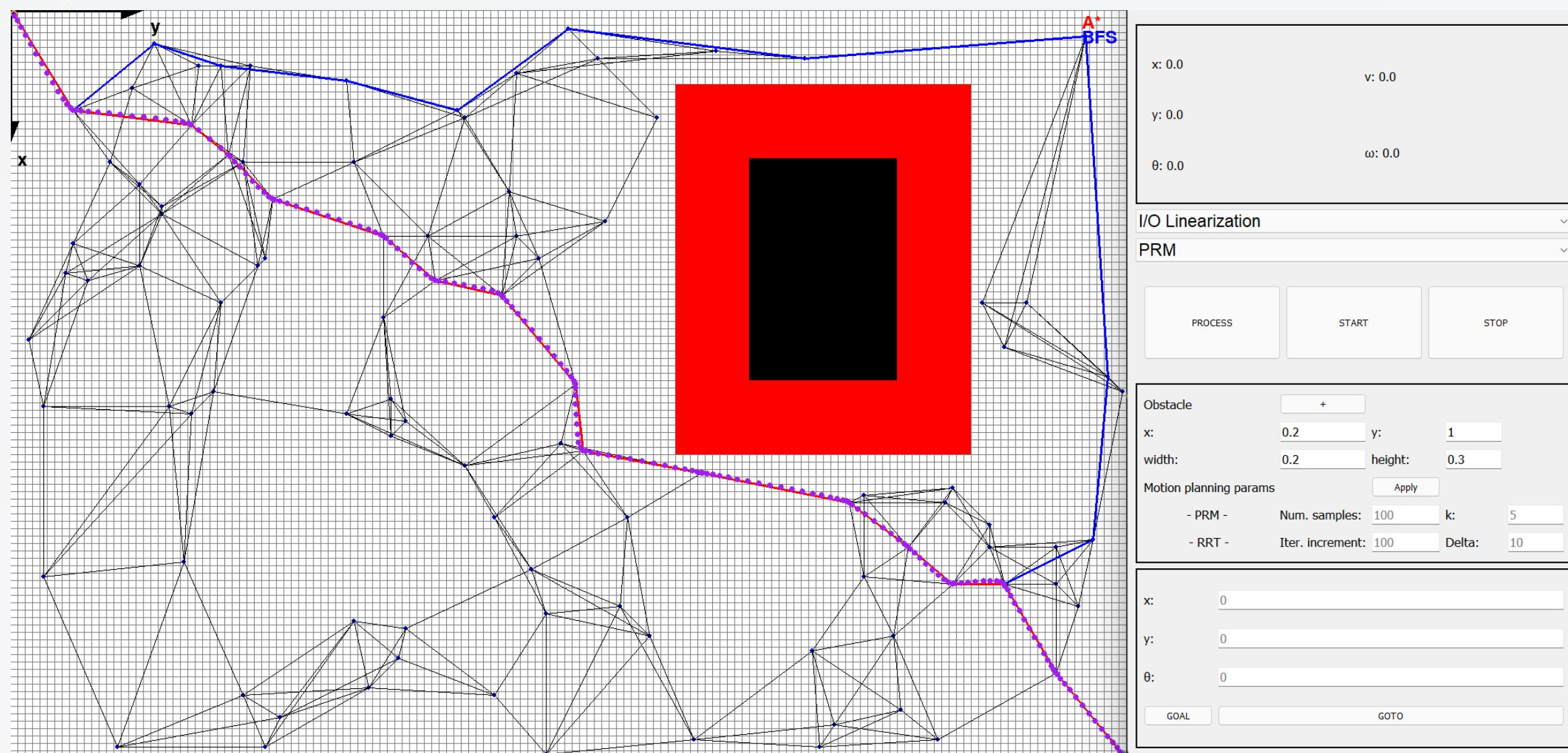
- MicroPython
- OOP (object oriented programming)
- Interruptions no busy wait

- Control: I/O Linearization, Posture Regulation
- IMU: Calibration and reading
- Localization: Euler approximation, Second-order Runge-Kutta
- Wheeled: IK solver

LOW LEVEL CONTROL

-  bluetooth
-  control
-  imu
-  localization
-  main
-  mpu6500
-  stepper
-  ukf
-  utils
-  vect_utils
-  wheeled

GCS SOFTWARE



- Python
- OOP (object oriented programming)
- Show the gridmap
- Handle the communication with DRIFTY (controller, goto, start, stop...)
- Contain Motion planning and trajectory planning modules

ESTIMATORS



EULERO



RUNGE KUTTA
SECOND ORDER



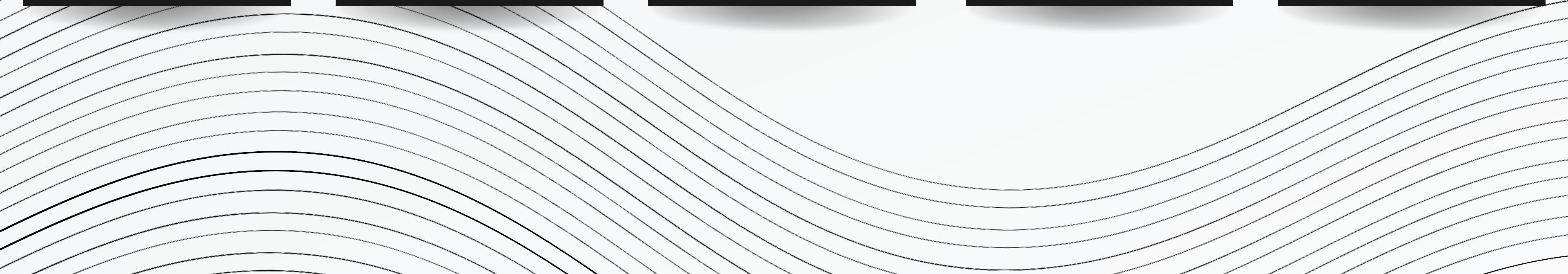
RUNGE KUTTA
FOURTH ORDEN



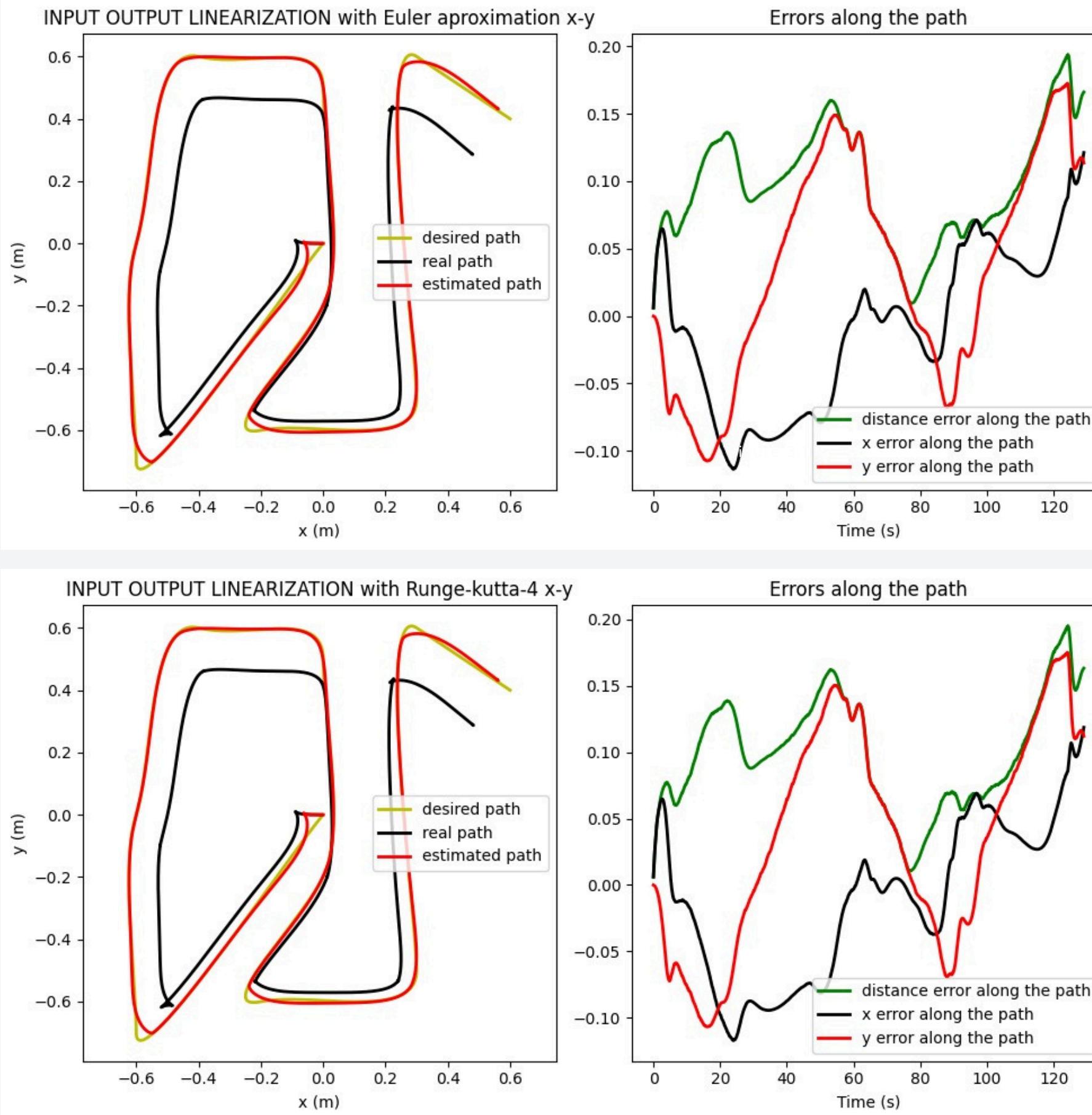
KALMAN FILTER



UNSCENDED
KALMAN FILTER

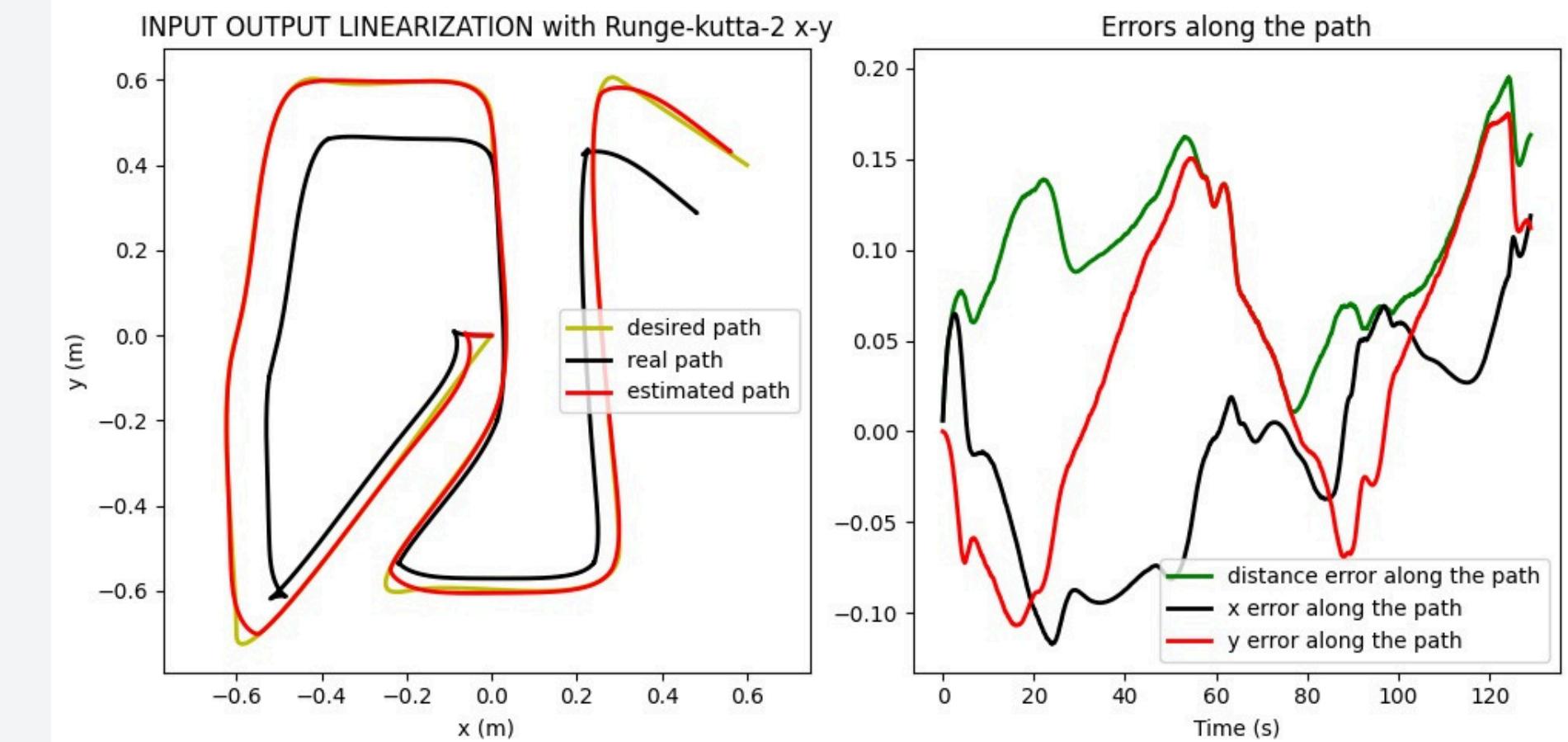


SIMULATIONS

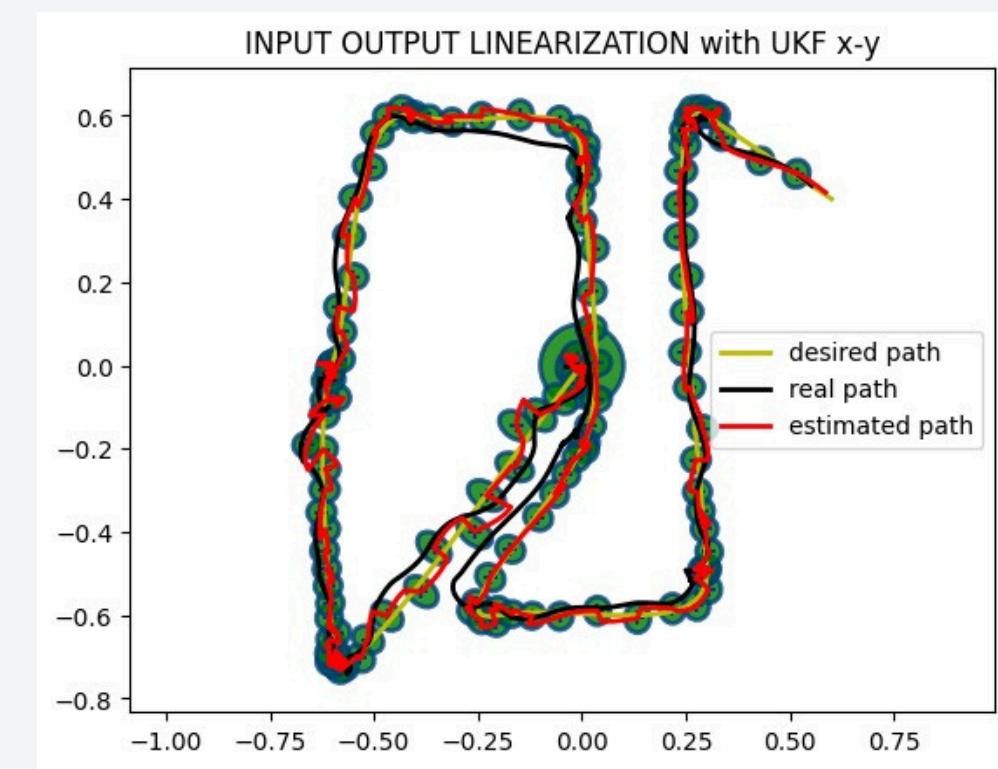
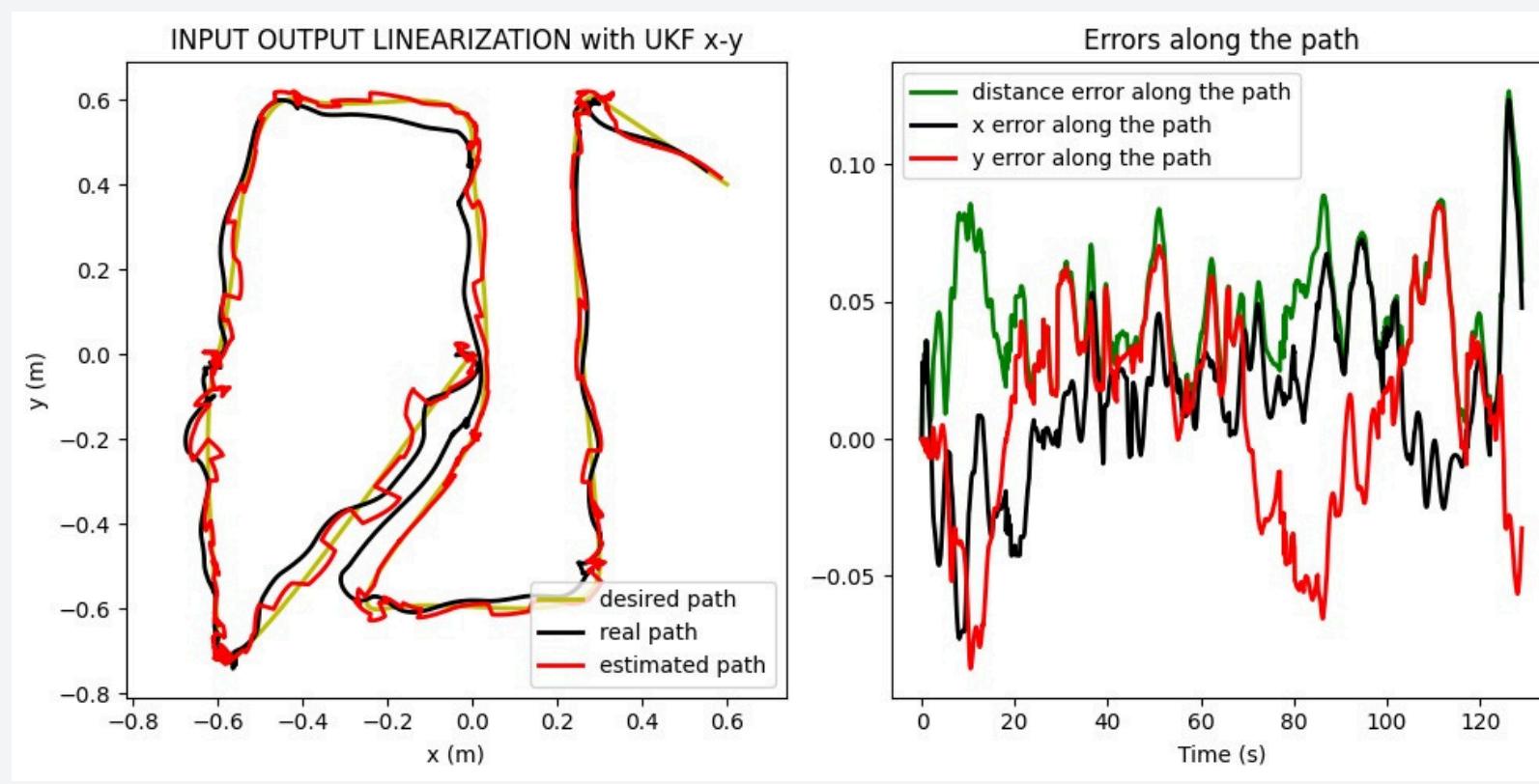
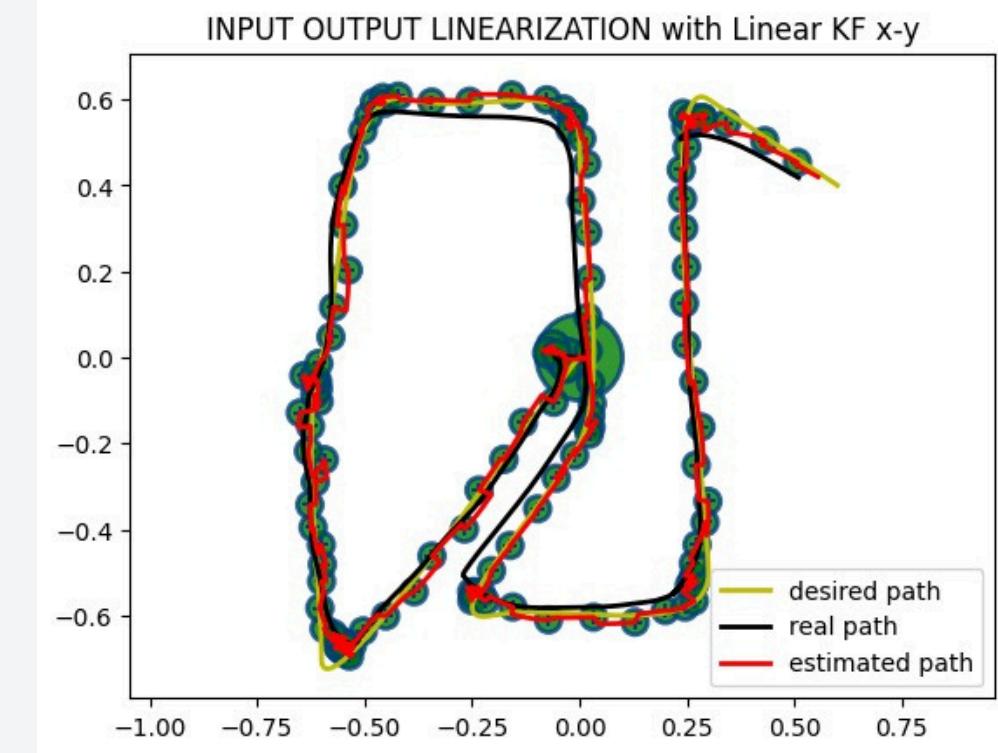
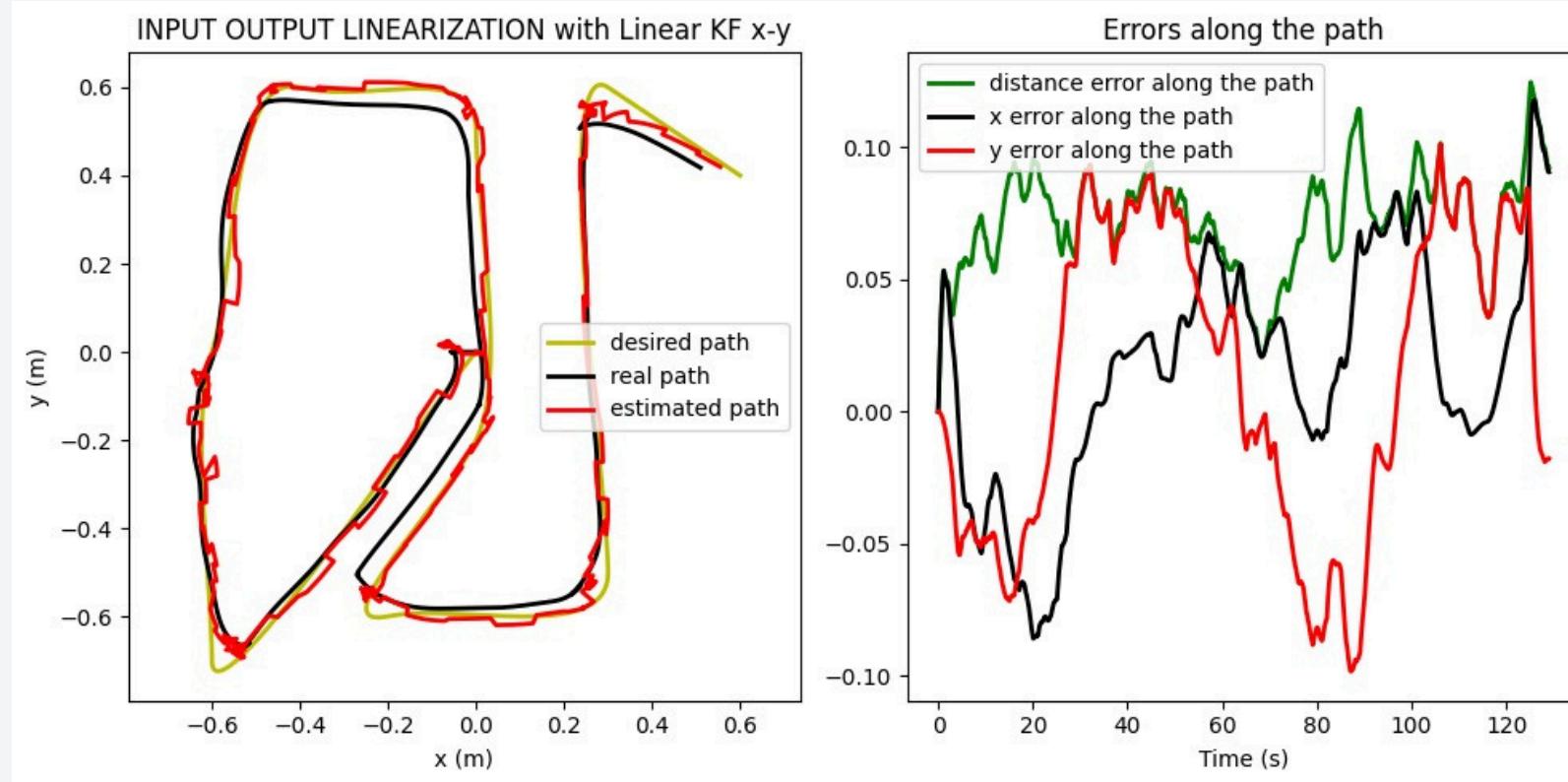


Maximum difference between :

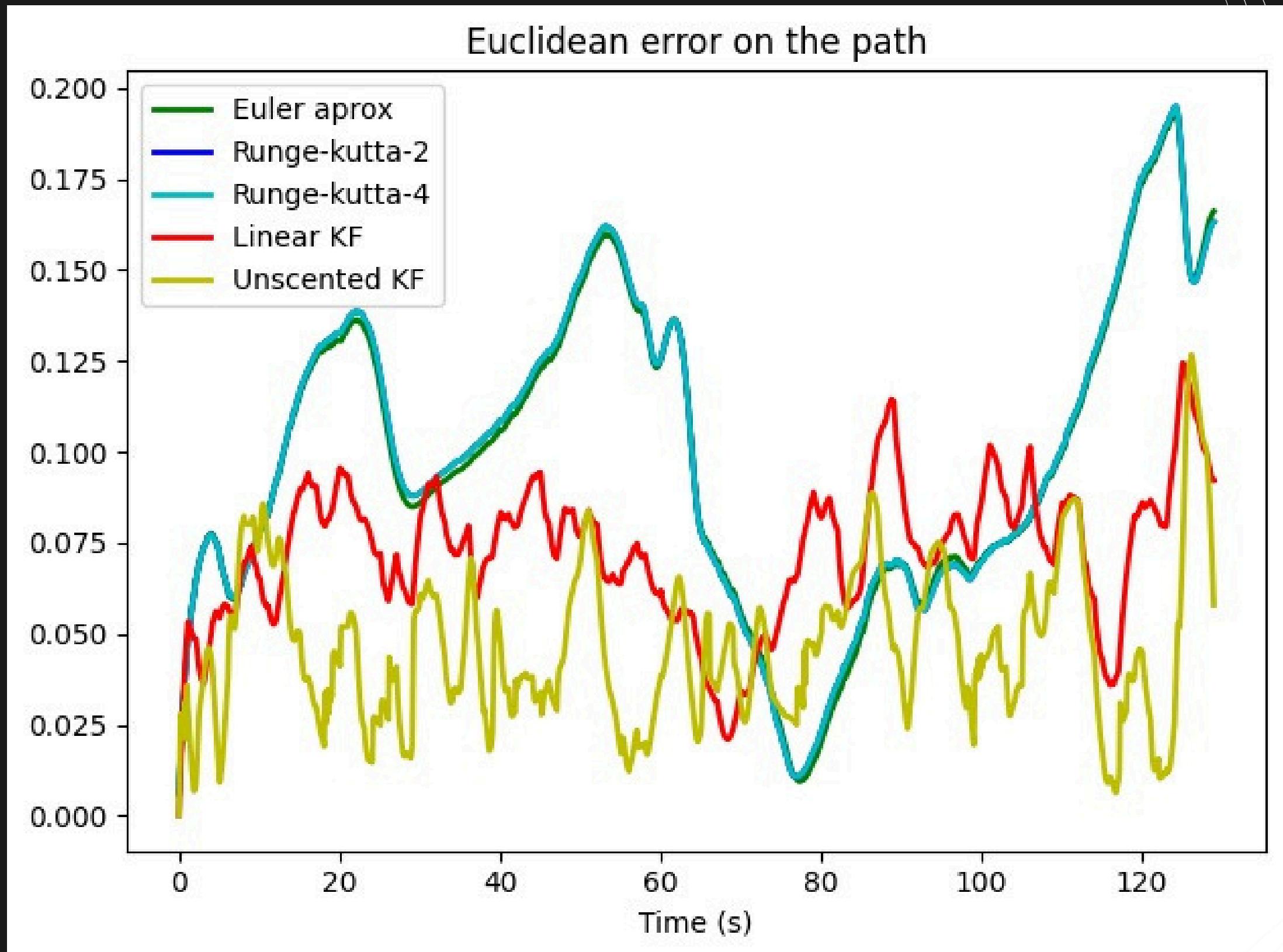
- RK-2 and Euler 0.00353
- RK-4 and Euler: 0.00353
- RK-4 and RK-2: 1.60478 e-05



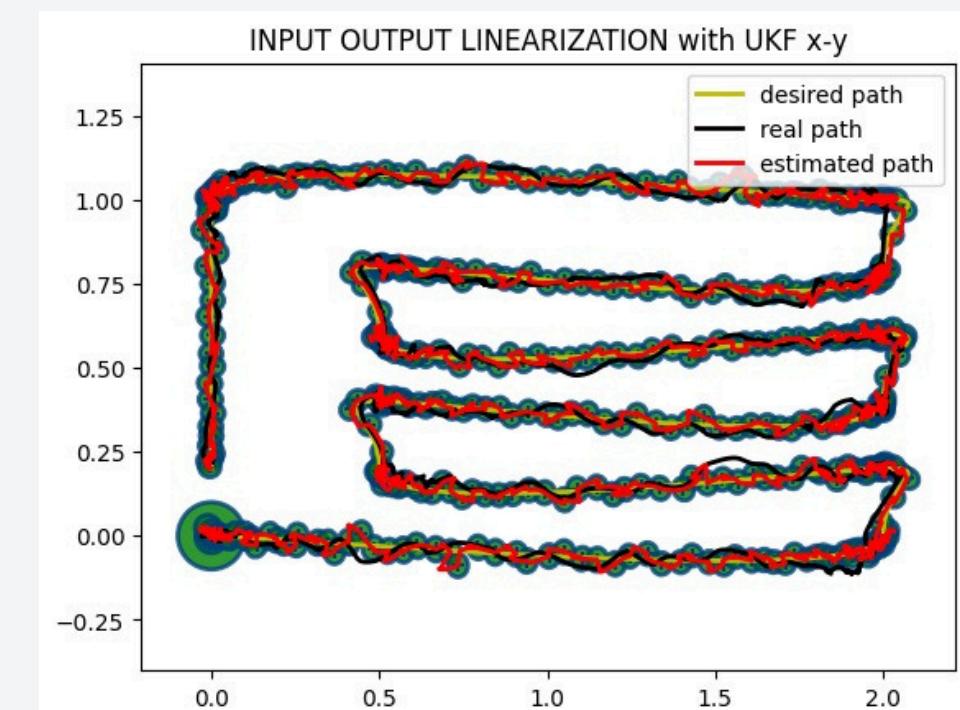
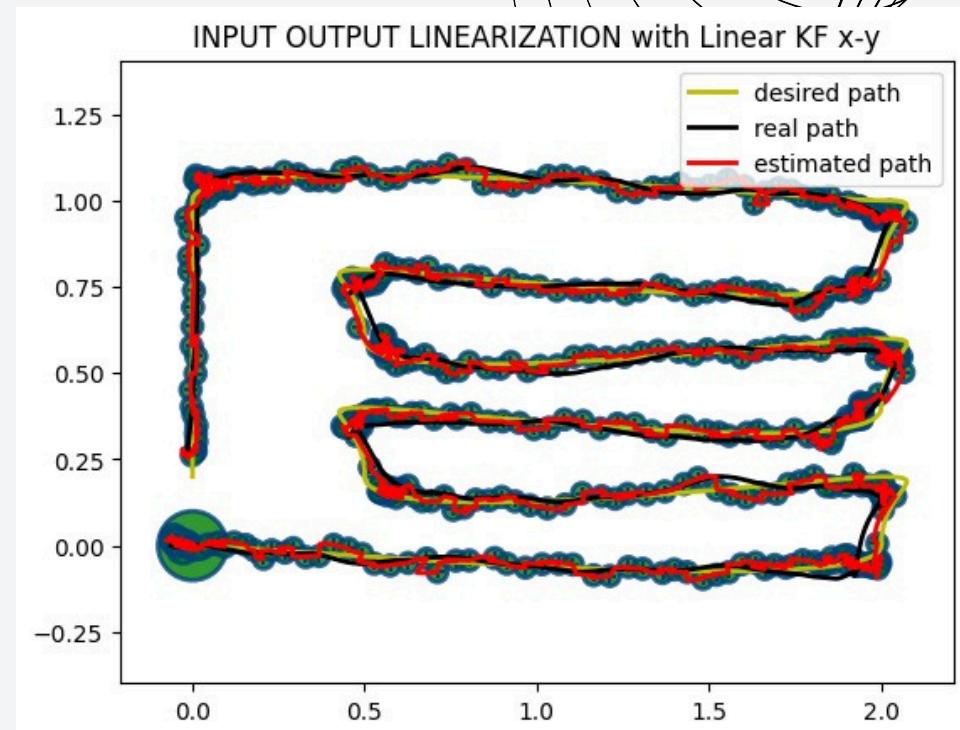
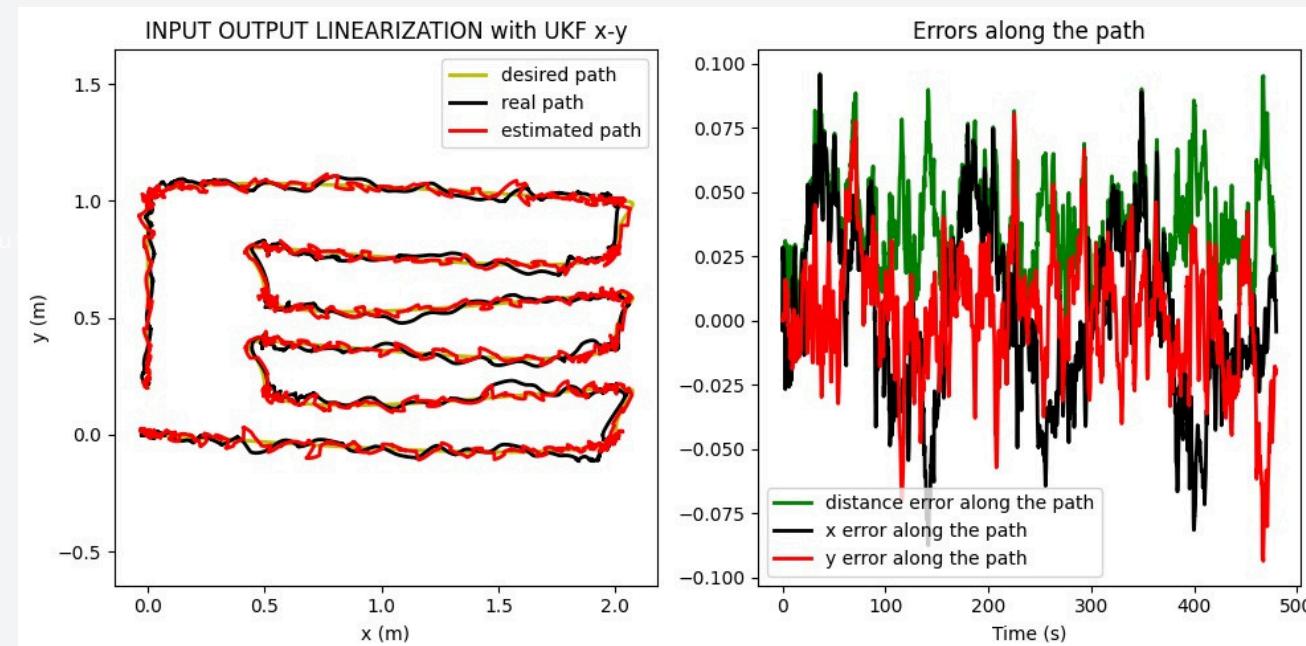
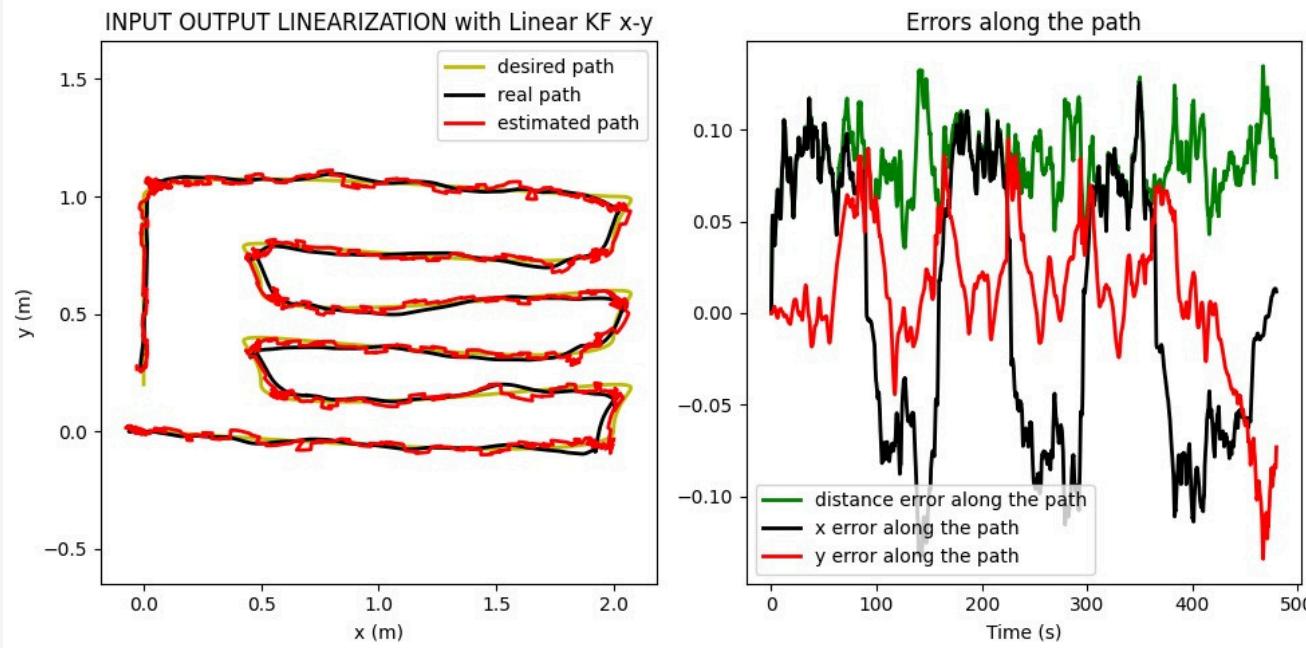
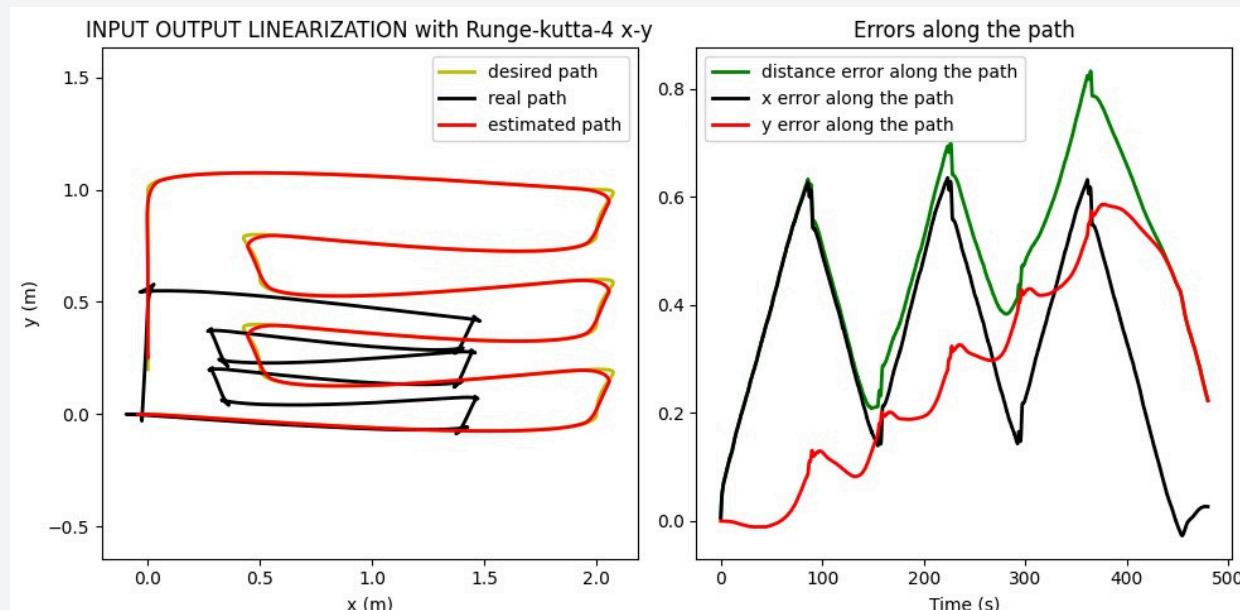
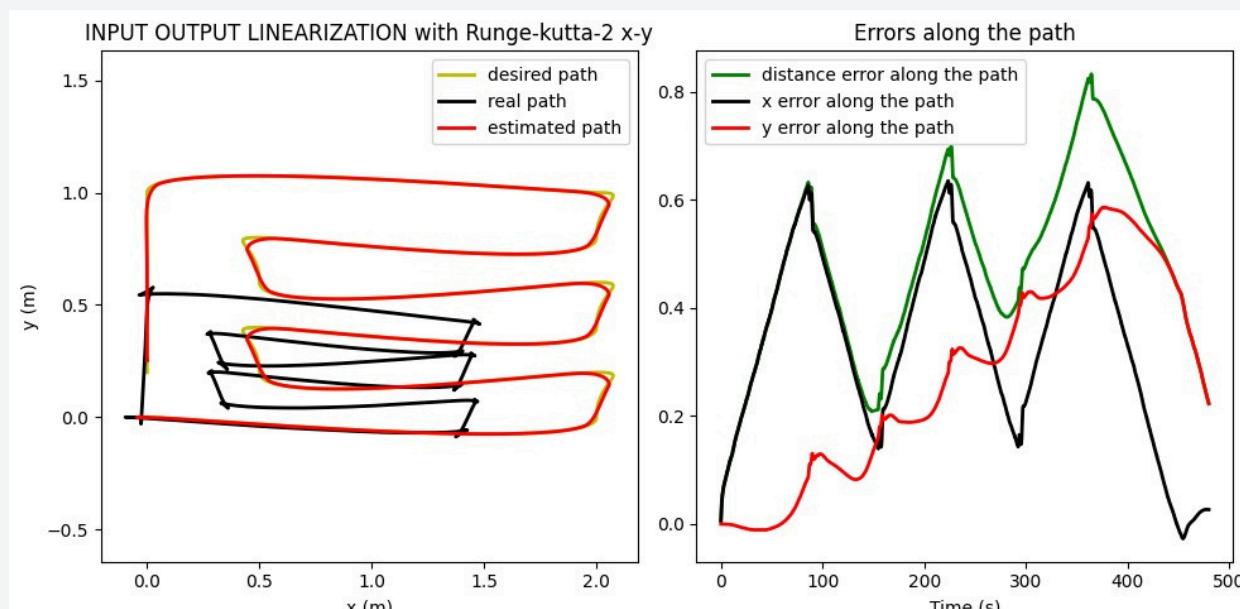
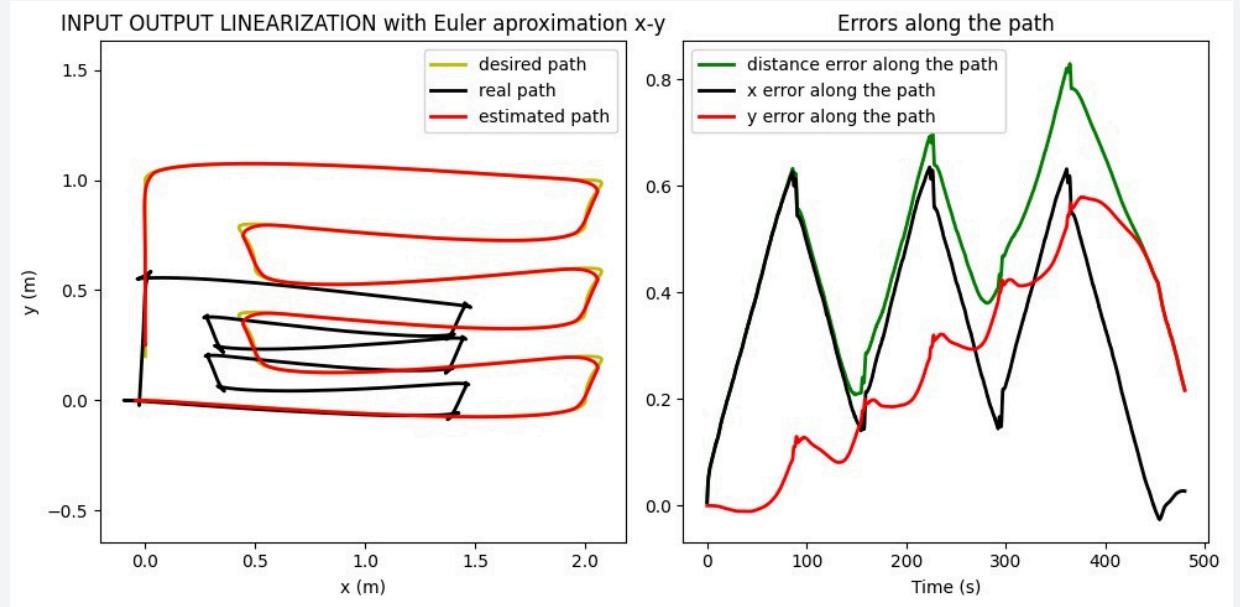
SIMULATIONS



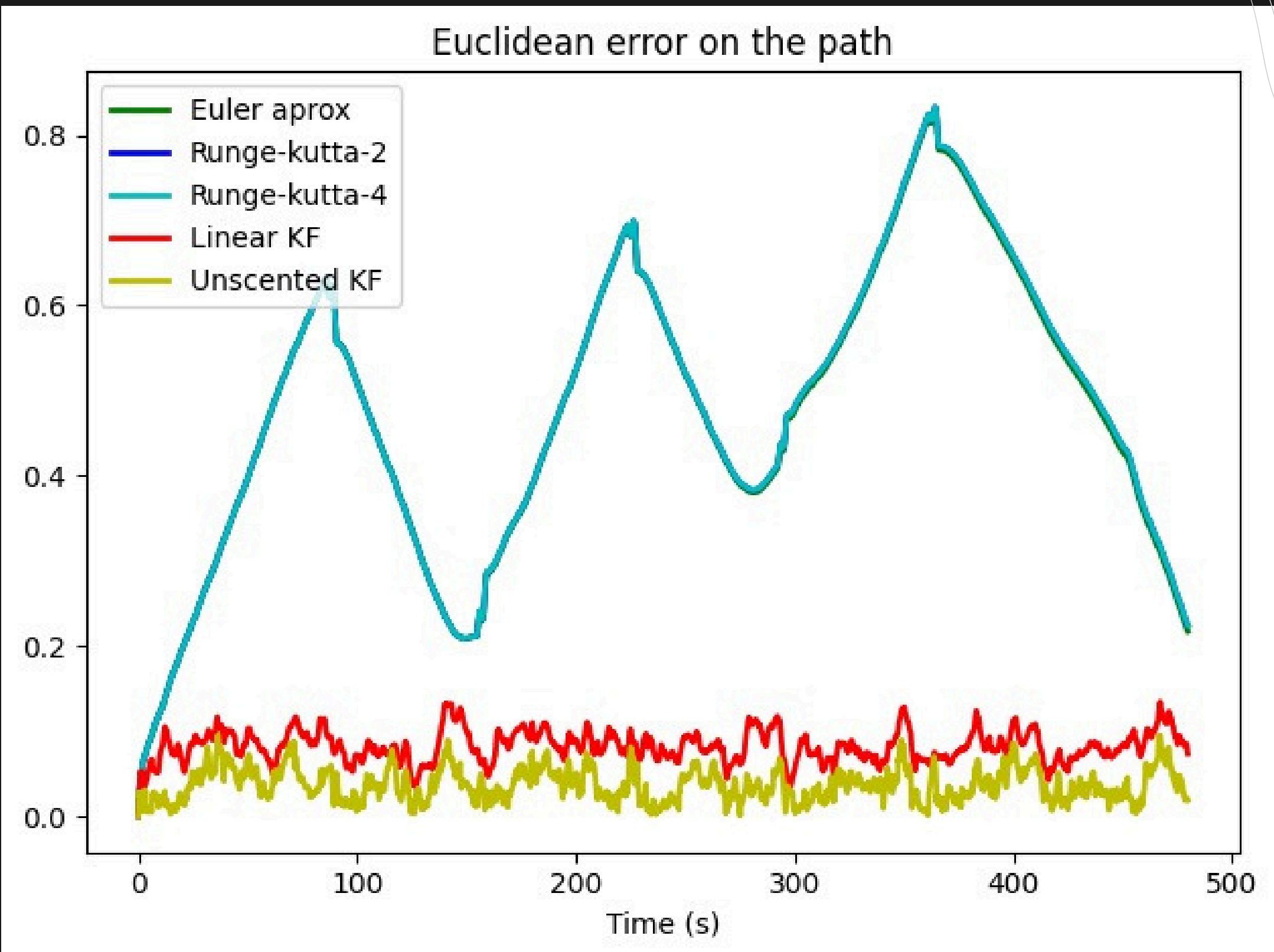
SIMULATIONS



SIMULATIONS



SIMULATIONS



CONTROL STRATEGIES

I/O Linearization

- Linearization of the system through feedback.
- A point B at a distance $|b|$ from the center of the wheel is chosen along the sagittal axis
- Orientation uncontrolled
- Outputs:

$$y_1 = x + b \cos \theta$$

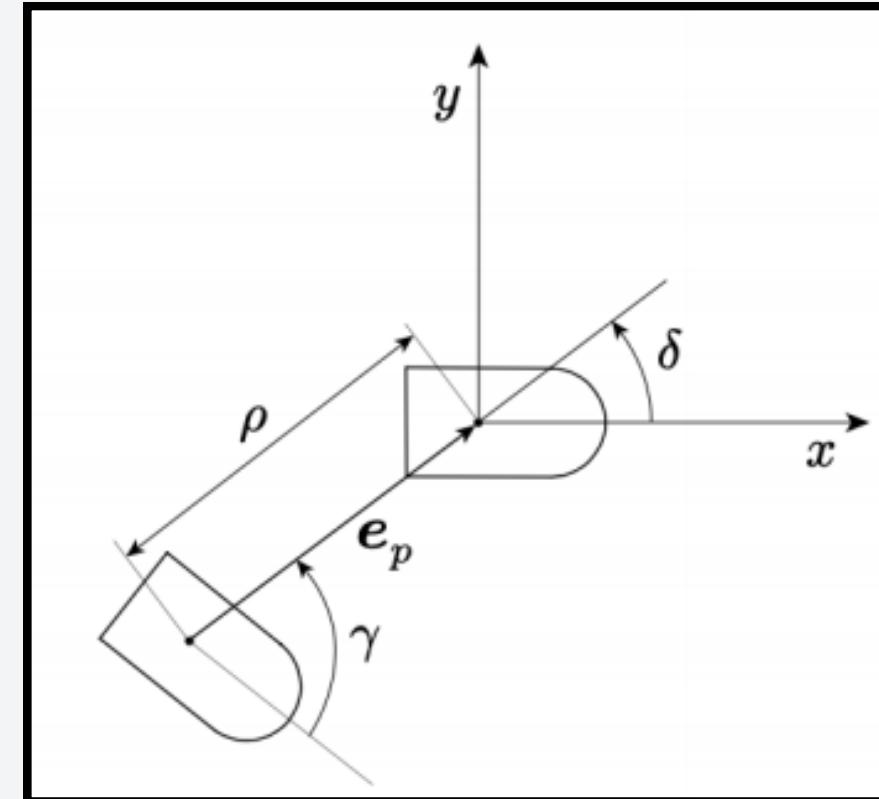
$$y_2 = y + b \sin \theta$$

- We can design

$$u_1 = \dot{y}_{1,d} + k_1(y_{1,d} - y_1)$$

$$u_2 = \dot{y}_{2,d} + k_2(y_{2,d} - y_2)$$

$$\begin{bmatrix} v \\ \omega \end{bmatrix} = T(\theta)^{-1} \begin{bmatrix} u_1 \\ u_2 \end{bmatrix}$$



Posture Regulation

- We use $q_d = [0 \ 0 \ 0]^T$
- Expressing the problem in polar coordinates

$$\rho = \sqrt{x^2 + y^2}$$

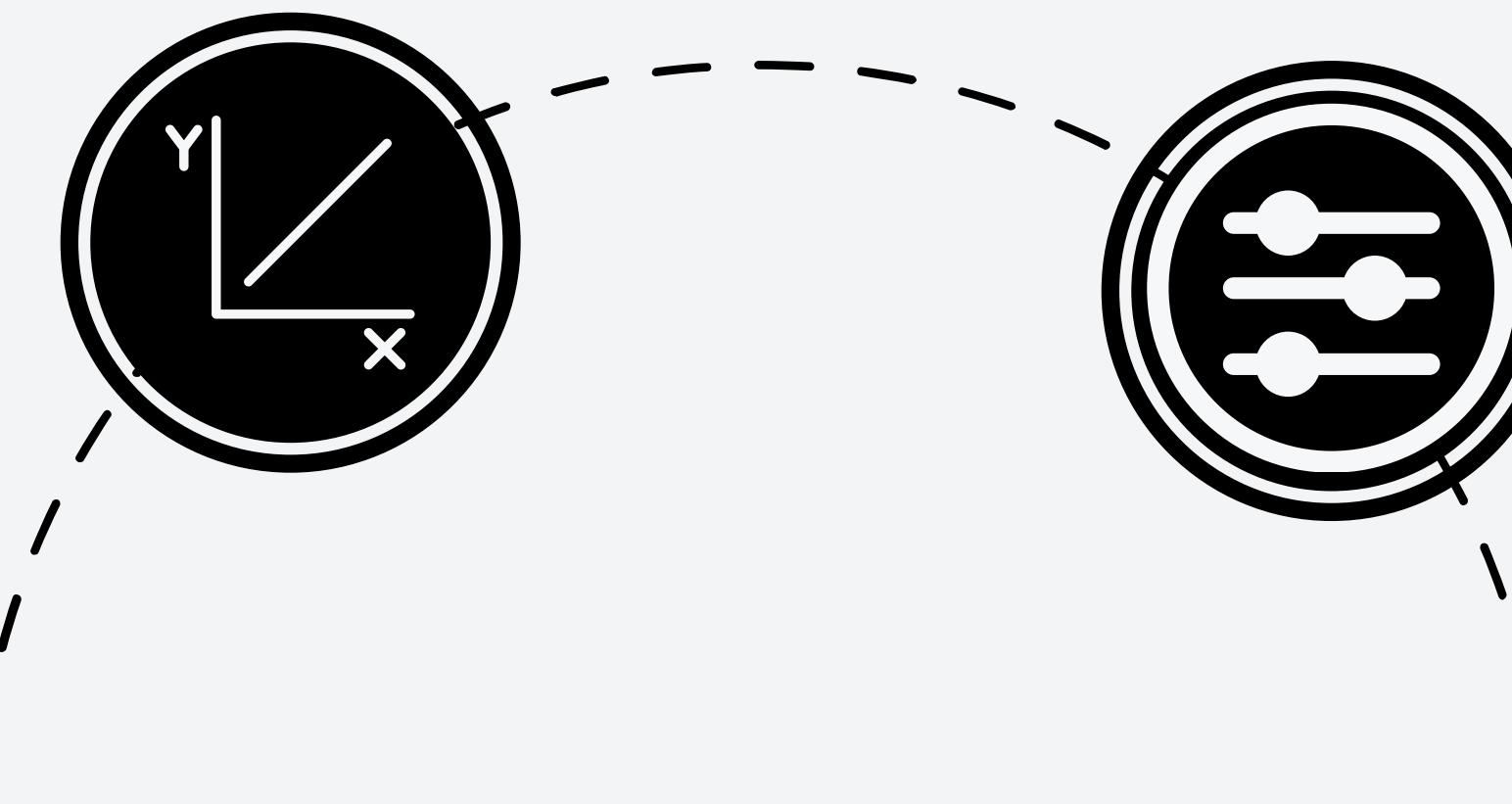
$$\gamma = \text{atan } 2(y, x) - \theta + \pi$$

$$\delta = \gamma + \theta$$

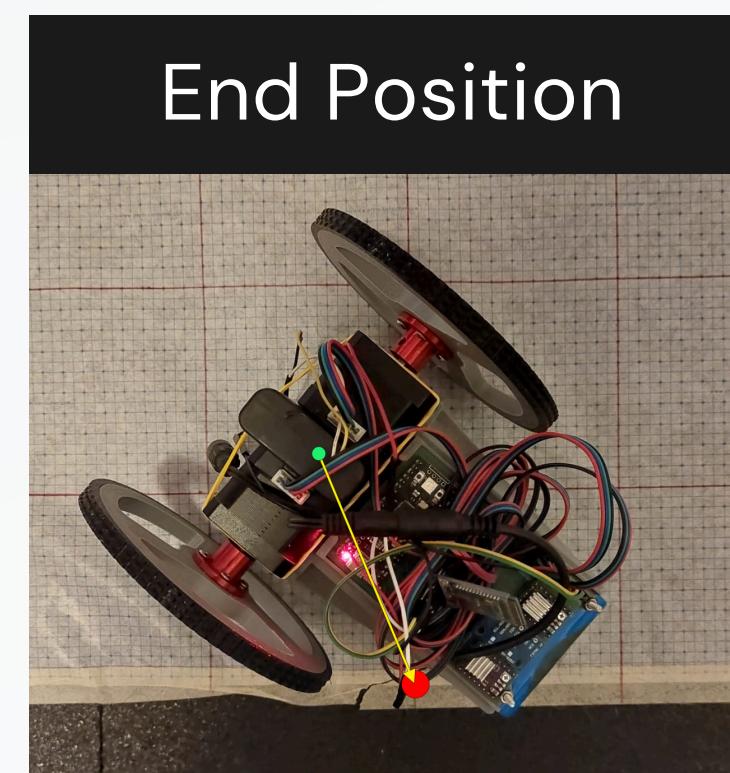
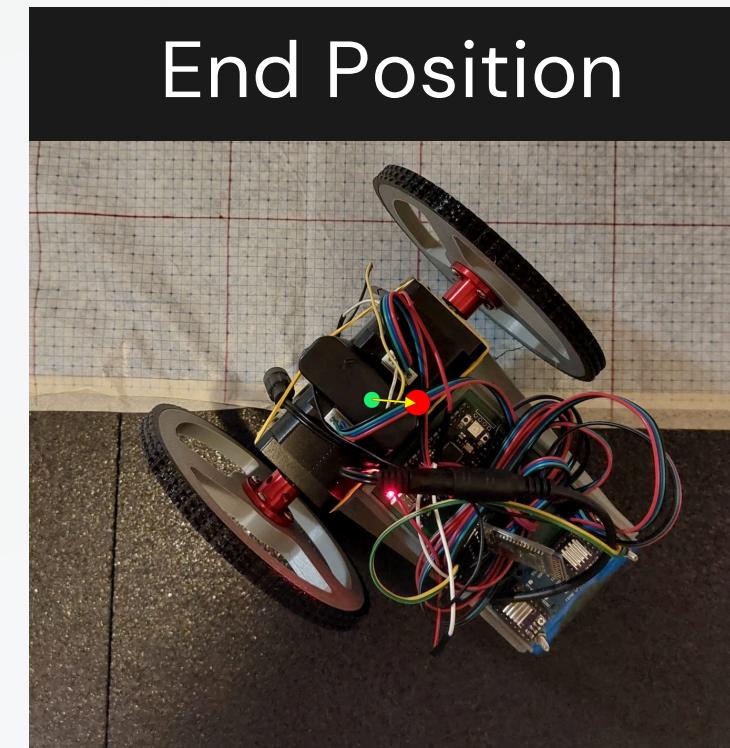
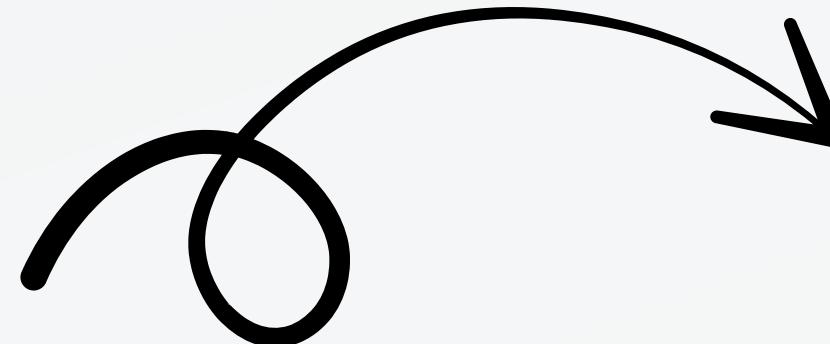
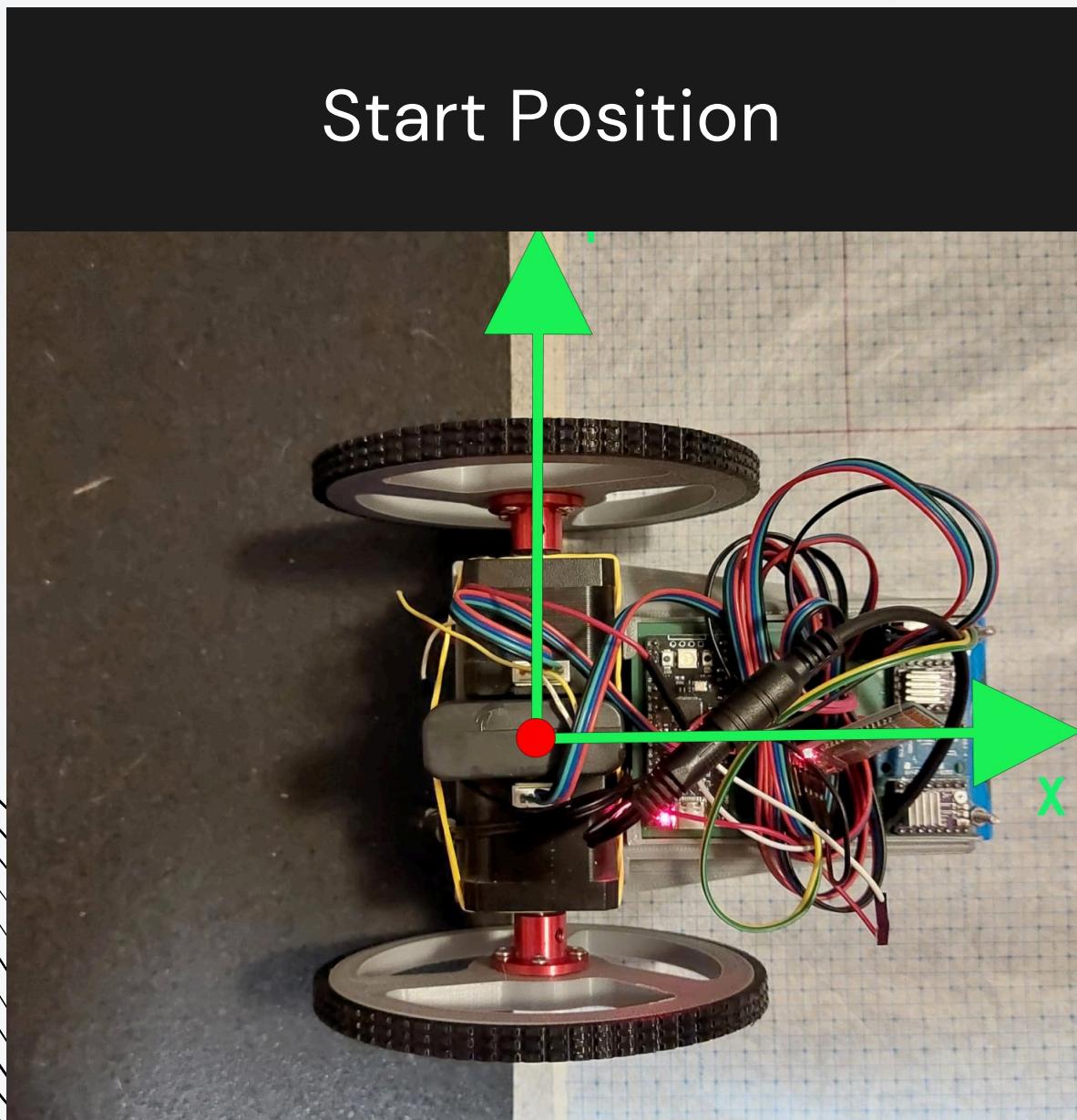
- We can design the following feedback controller

$$v = k_1 \rho \cos \gamma$$

$$\omega = k_2 \gamma + k_1 \sin \gamma \cos \gamma \left(1 + k_3 \frac{\delta}{\gamma} \right)$$



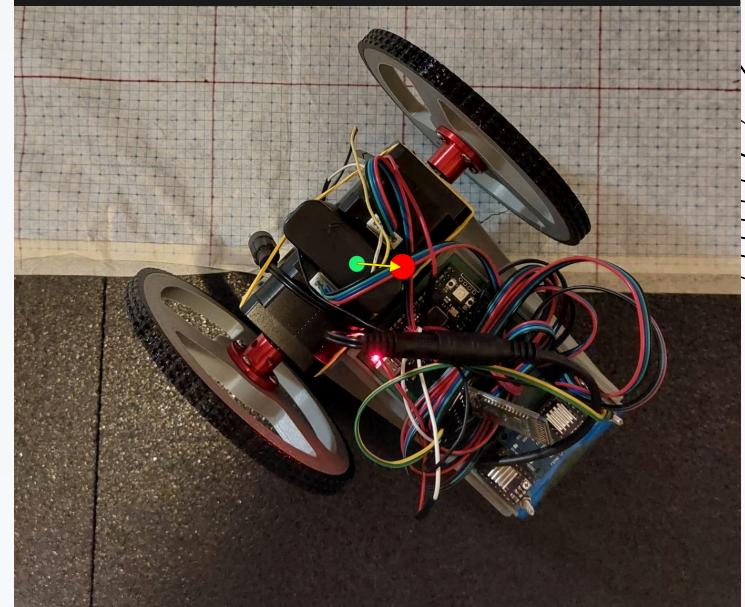
I/O LINEARIZATION



I/O LINEARIZATION



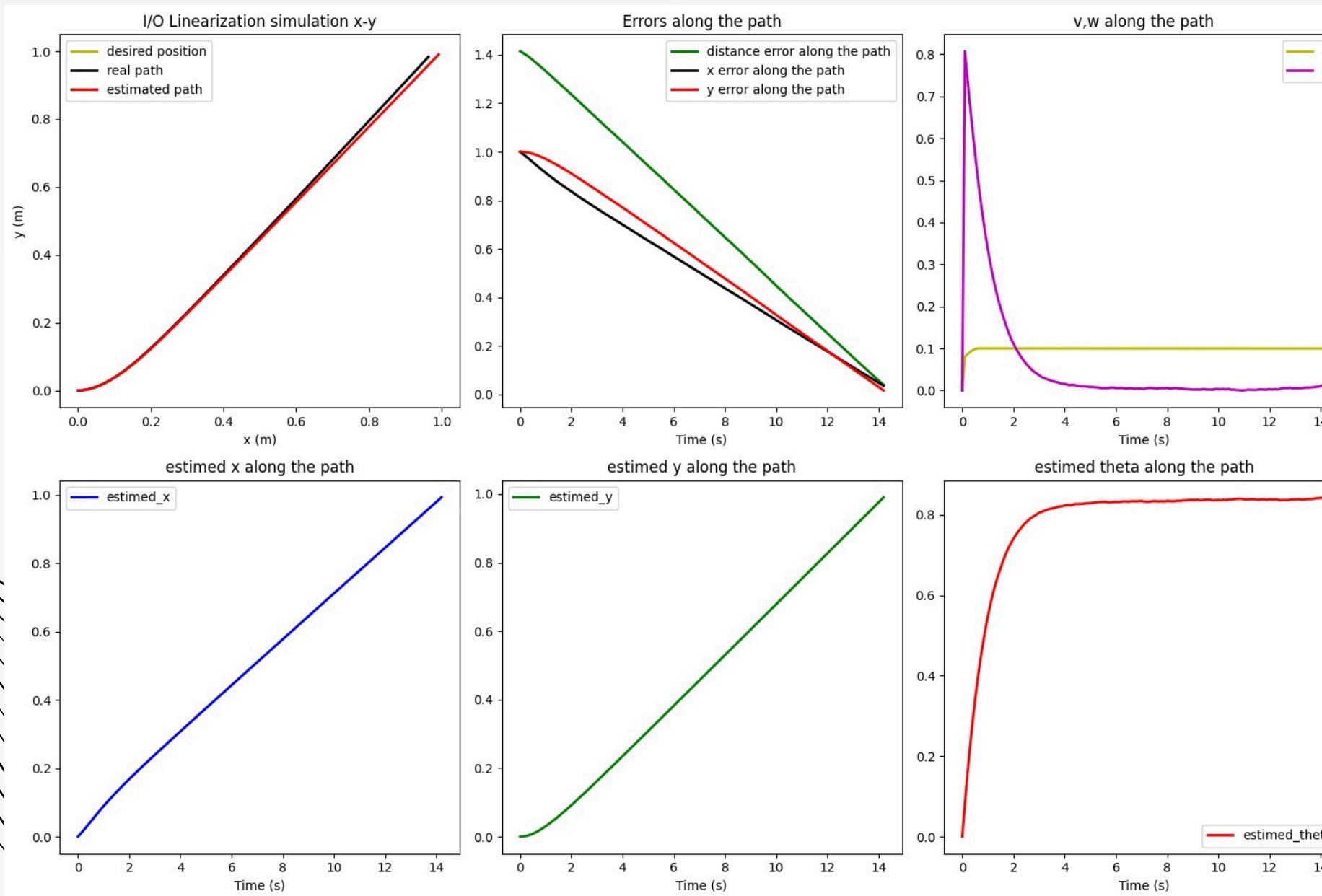
End Position



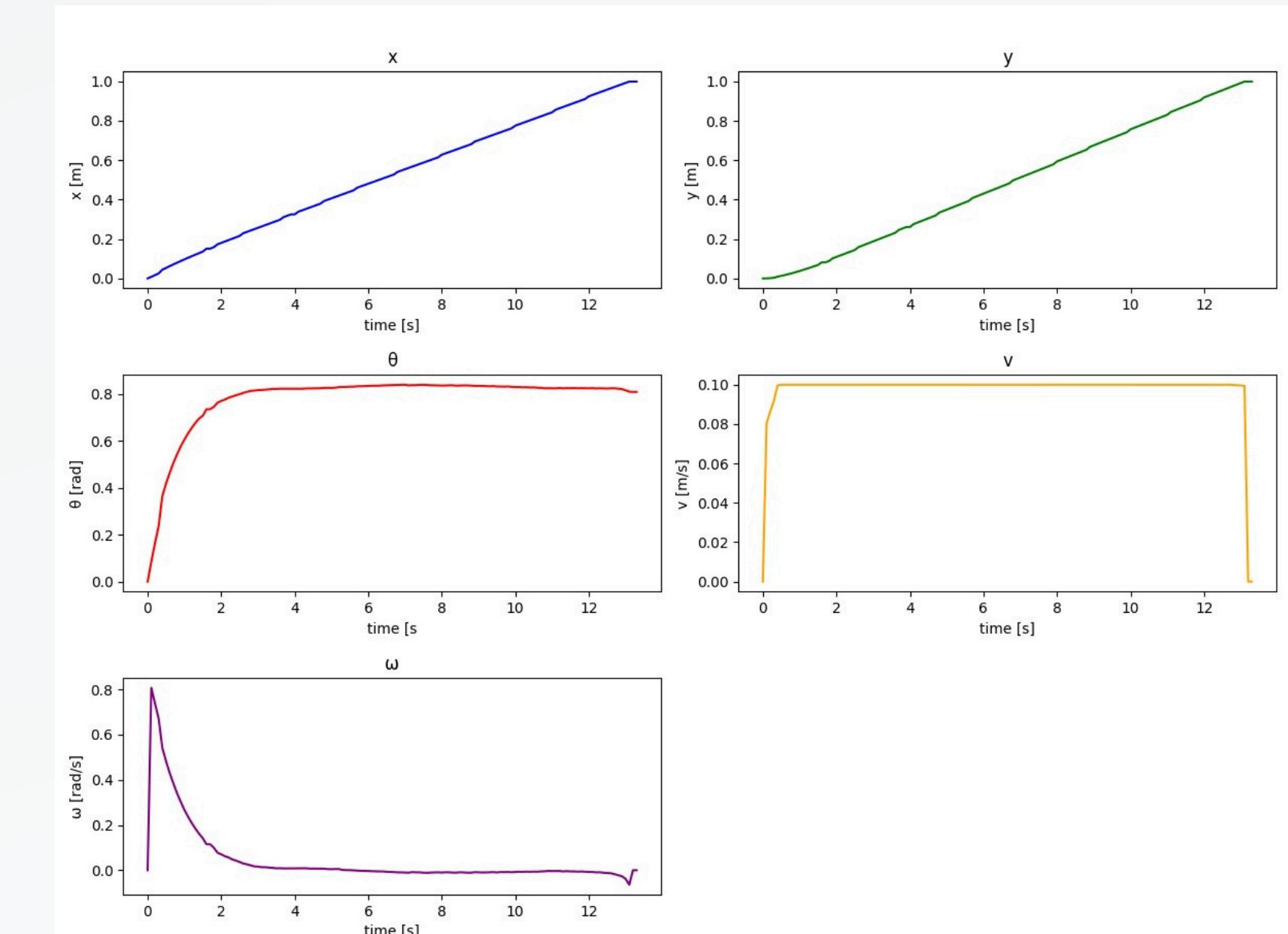
K1=0.01 K2=0.01

I/O LINEARIZATION

K1=0.01 K2=0.01

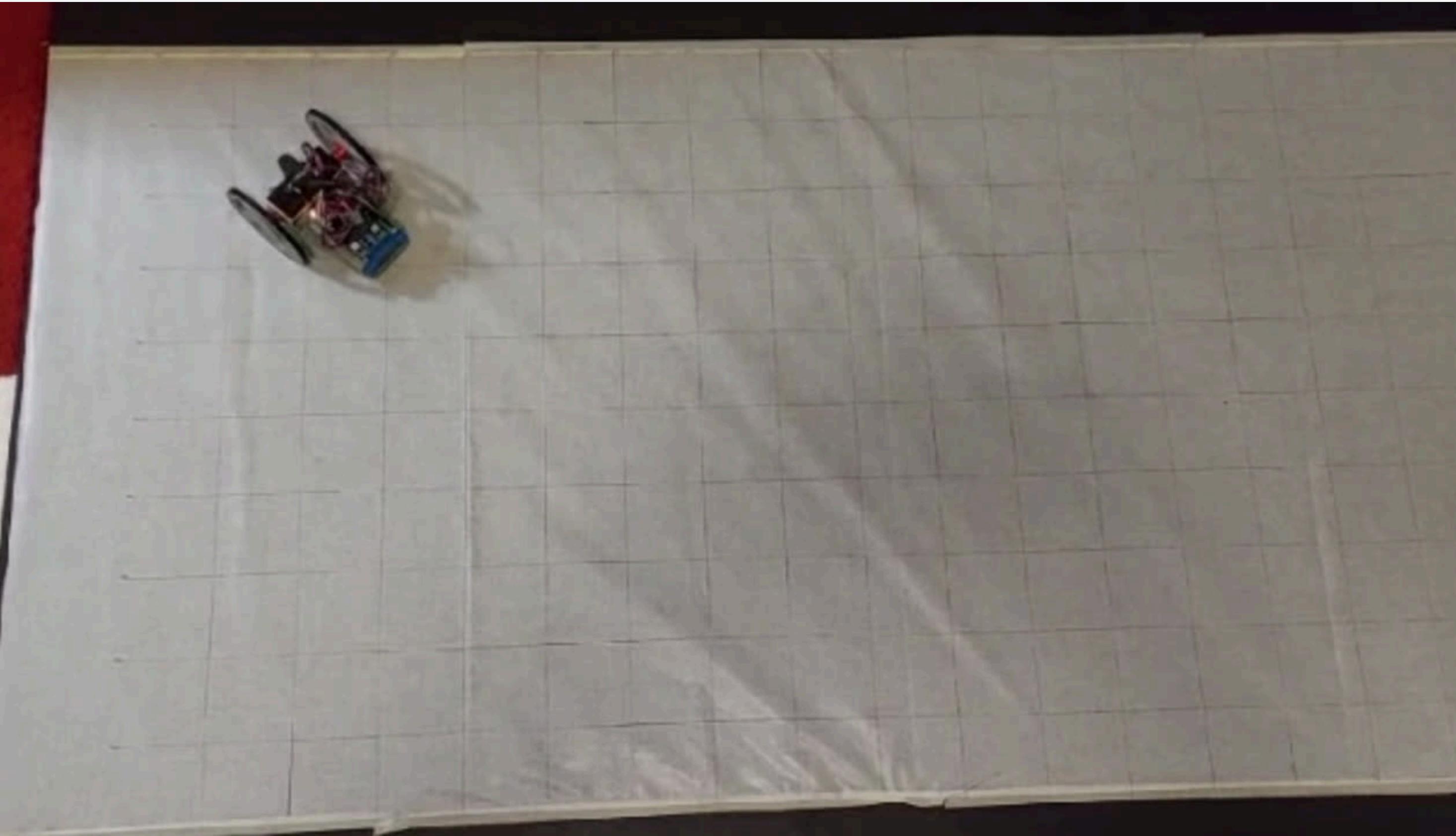


SIMULATION

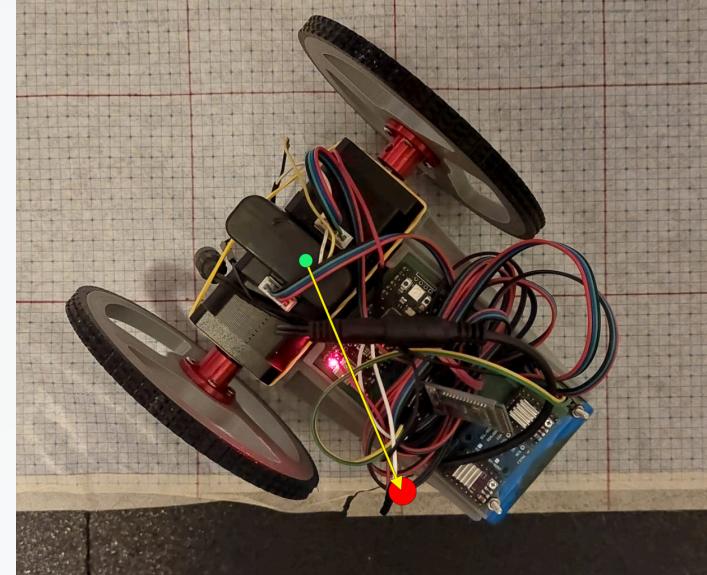


TEST

I/O LINEARIZATION



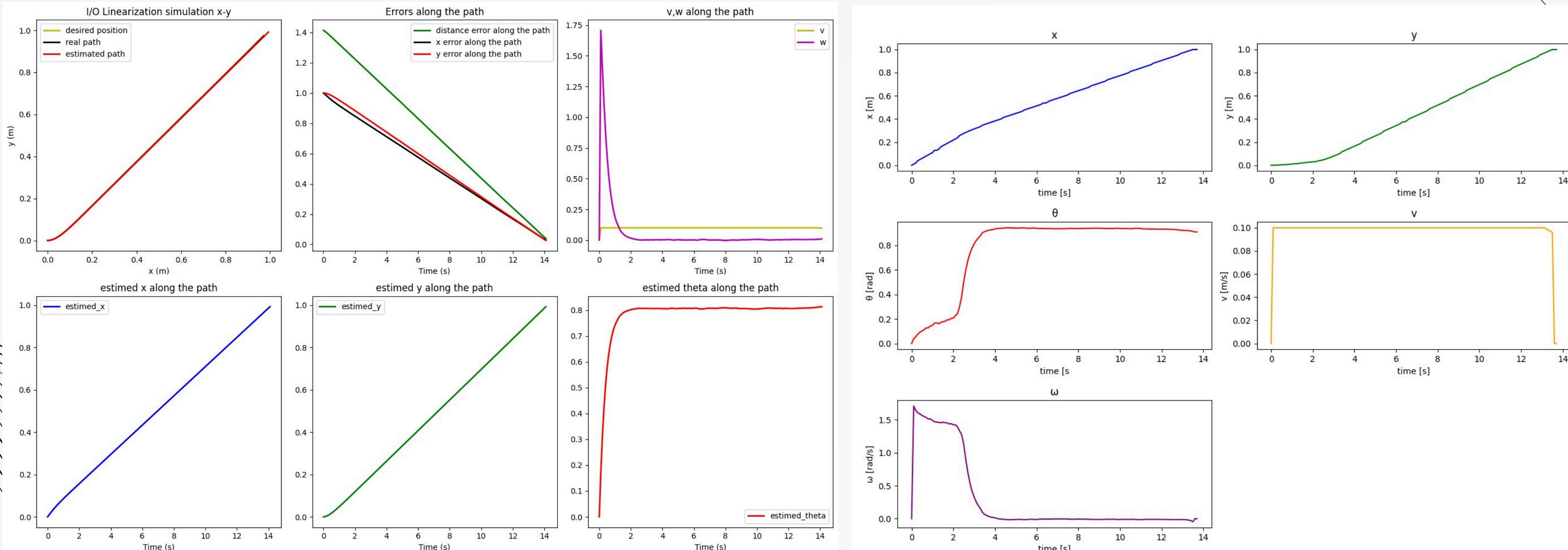
End Position



K1=0.1 K2=0.1

I/O LINEARIZATION

K1=0.1 K2=0.1



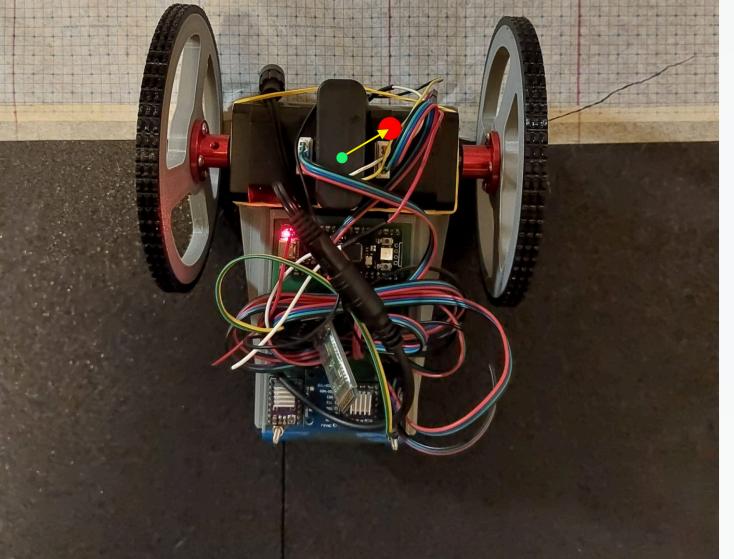
SIMULATION

TEST

POSTURE REGULATION



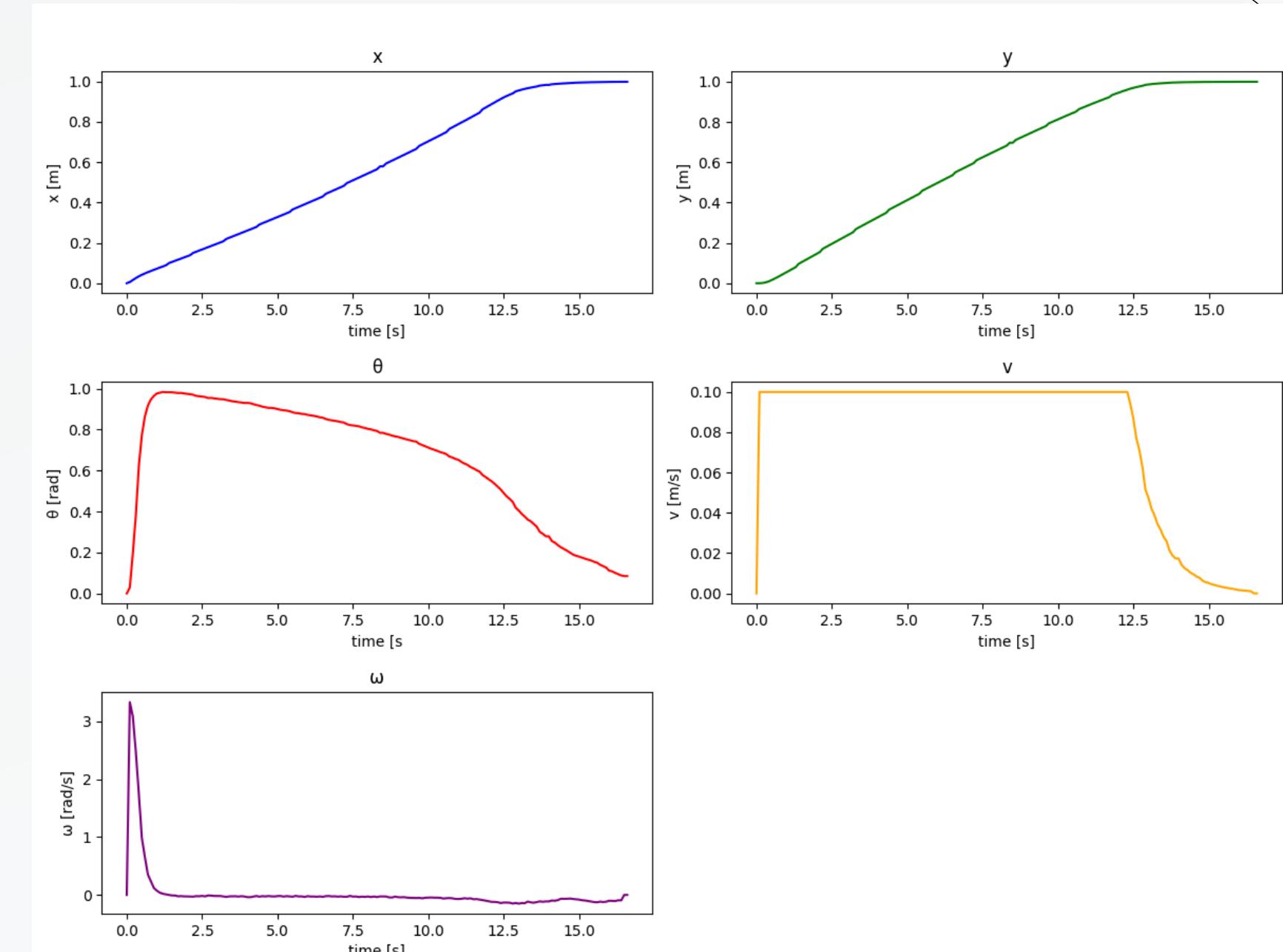
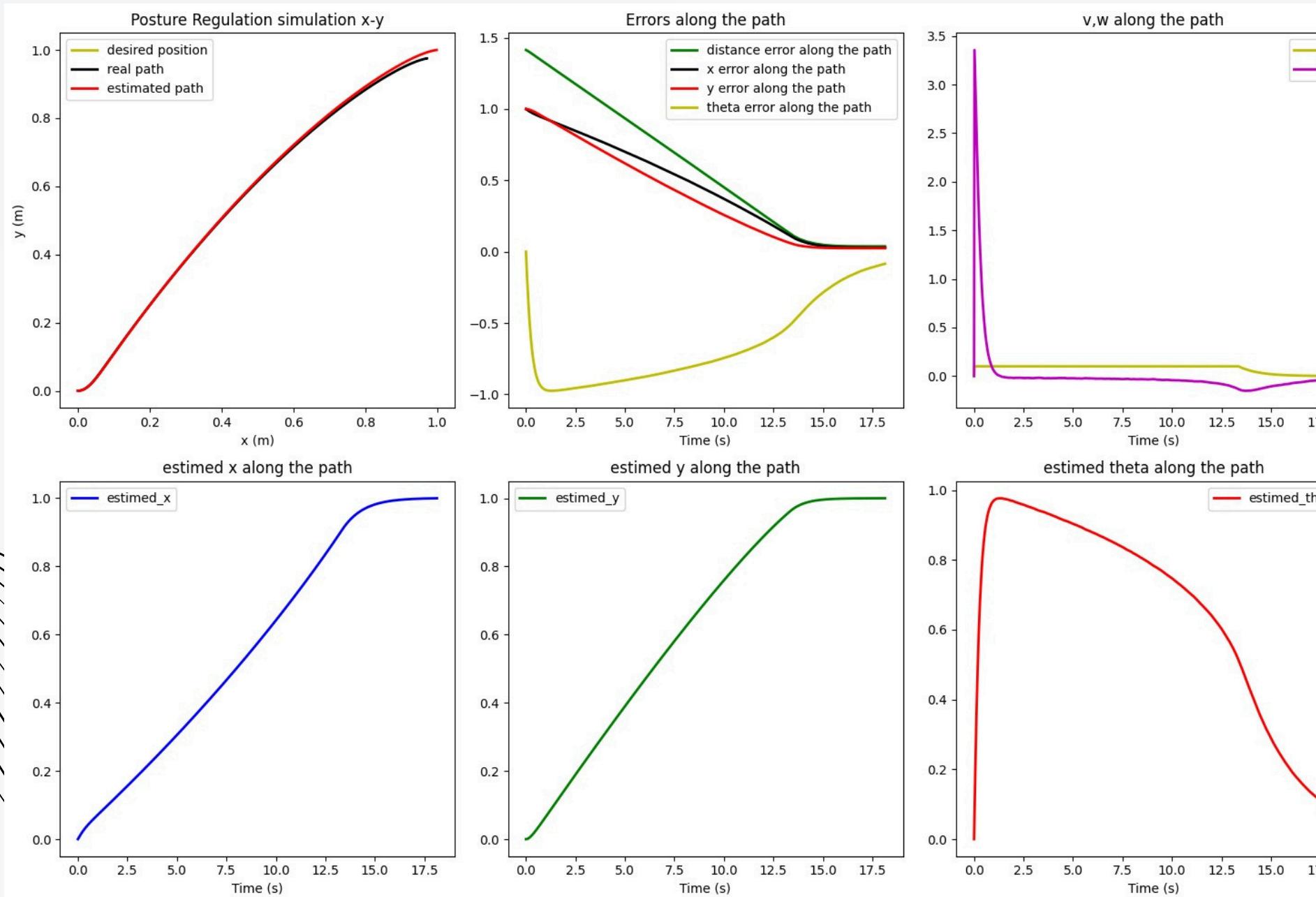
End Position
(0,0,0)



K1=1 K2=3 K3=1

POSTURE REGULATION

K1=1 K2=3 K3=1



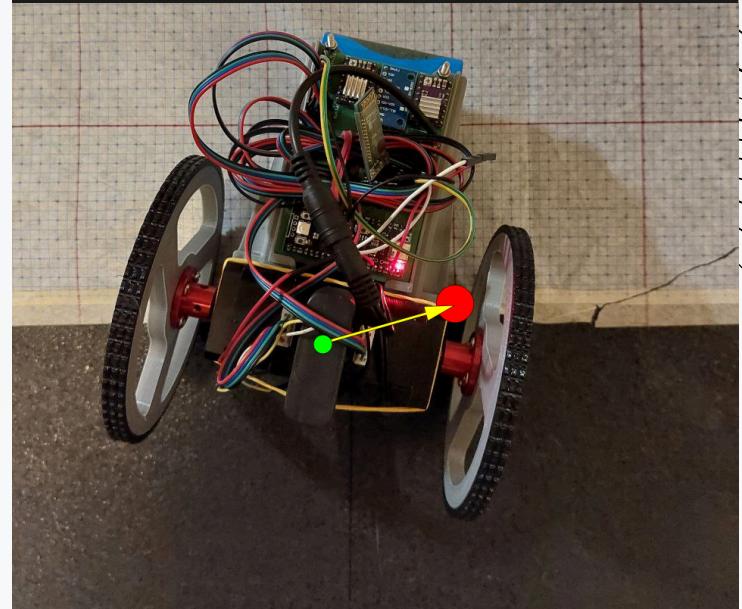
SIMULATION

TEST

POSTURE REGULATION



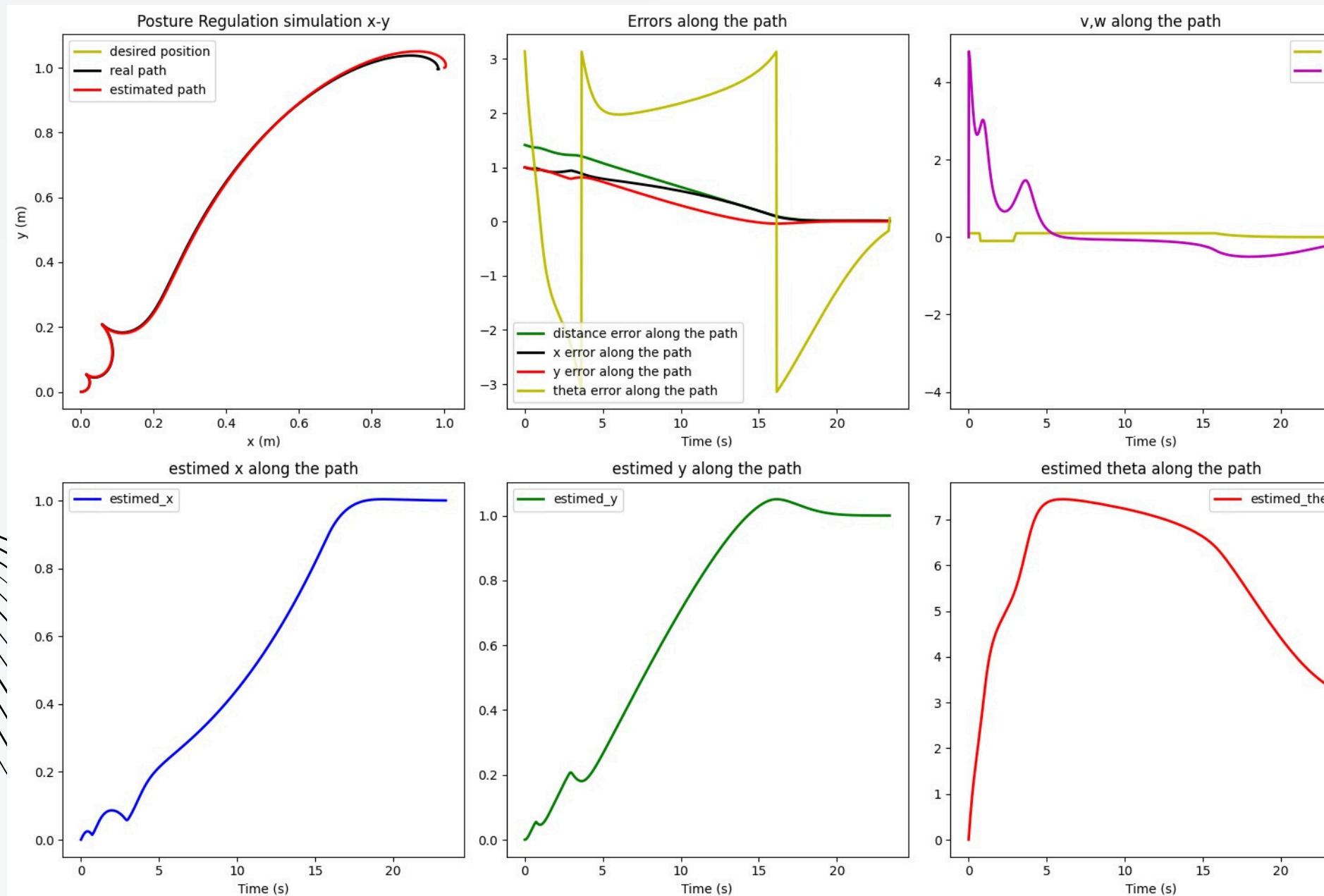
End Position
(0,0,pi)



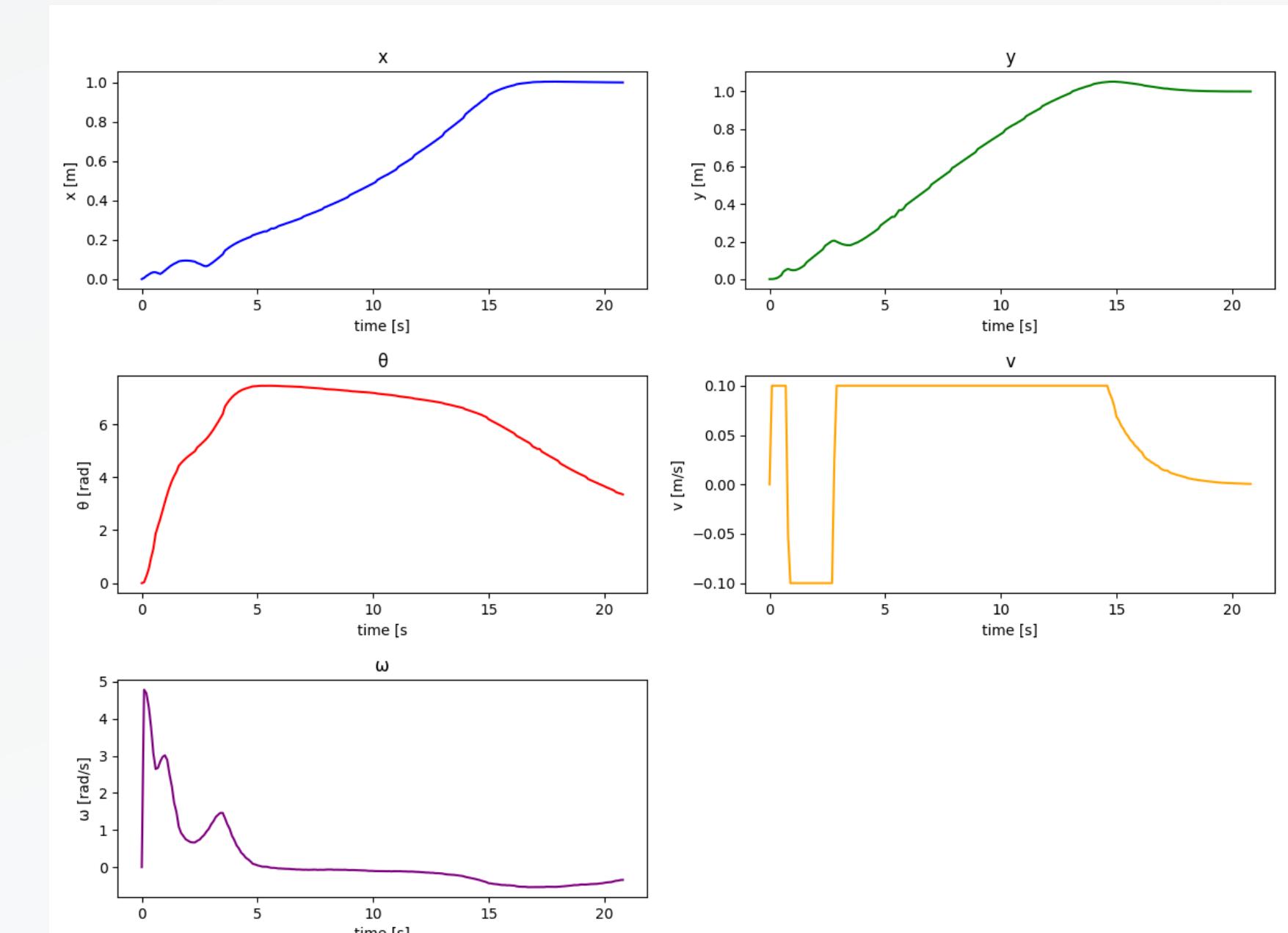
K1=1 K2=0.6 K3=0.2

POSTURE REGULATION

K1=1 K2=0.6 K3=0.2 WITH FINAL CONFIGURATIO (0,0,PI)



SIMULATION



TEST

MOTION PLANNING

NODE
GENERATION

SEARCH
ALGORITHMS

RTT

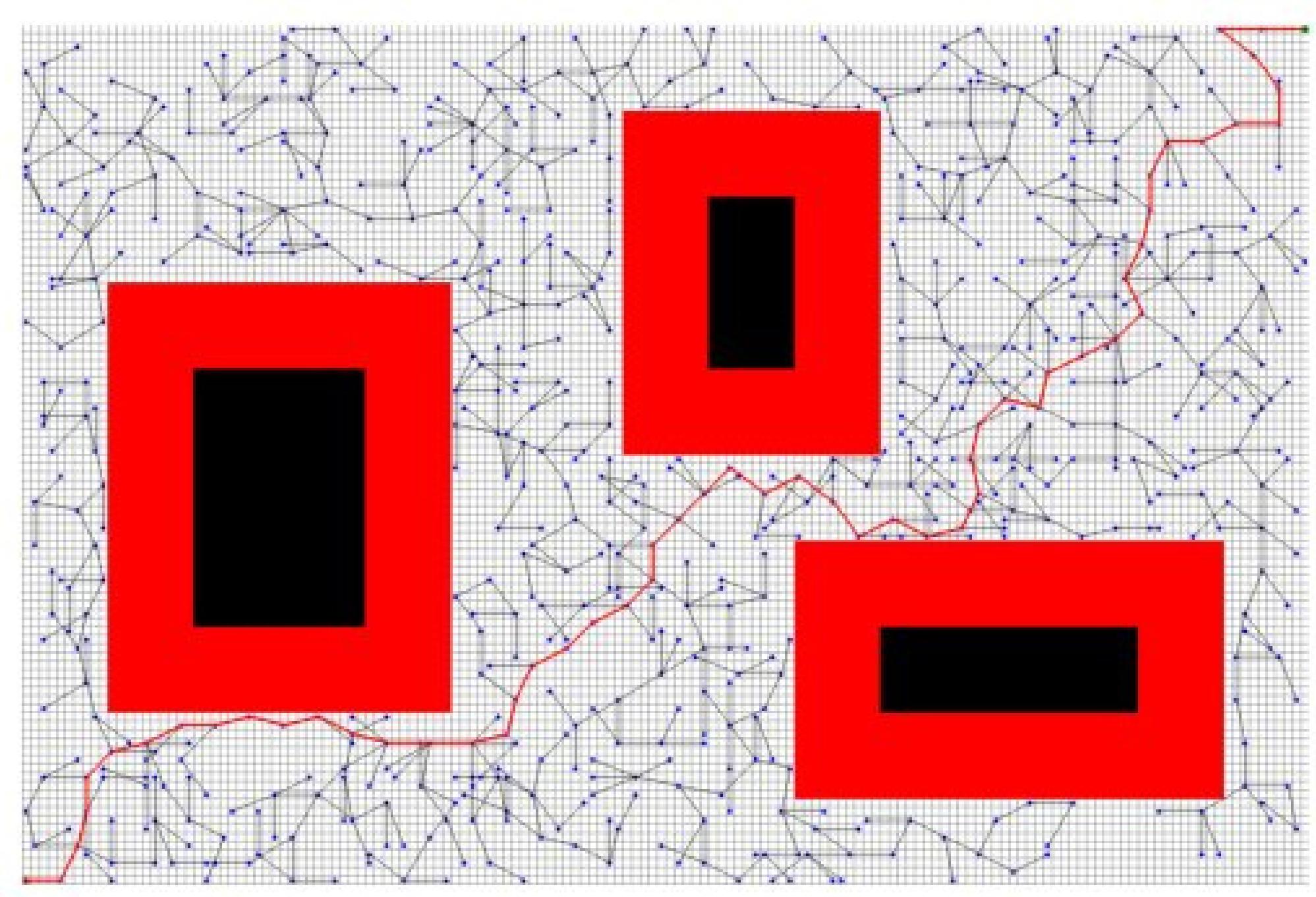
PRM

A*

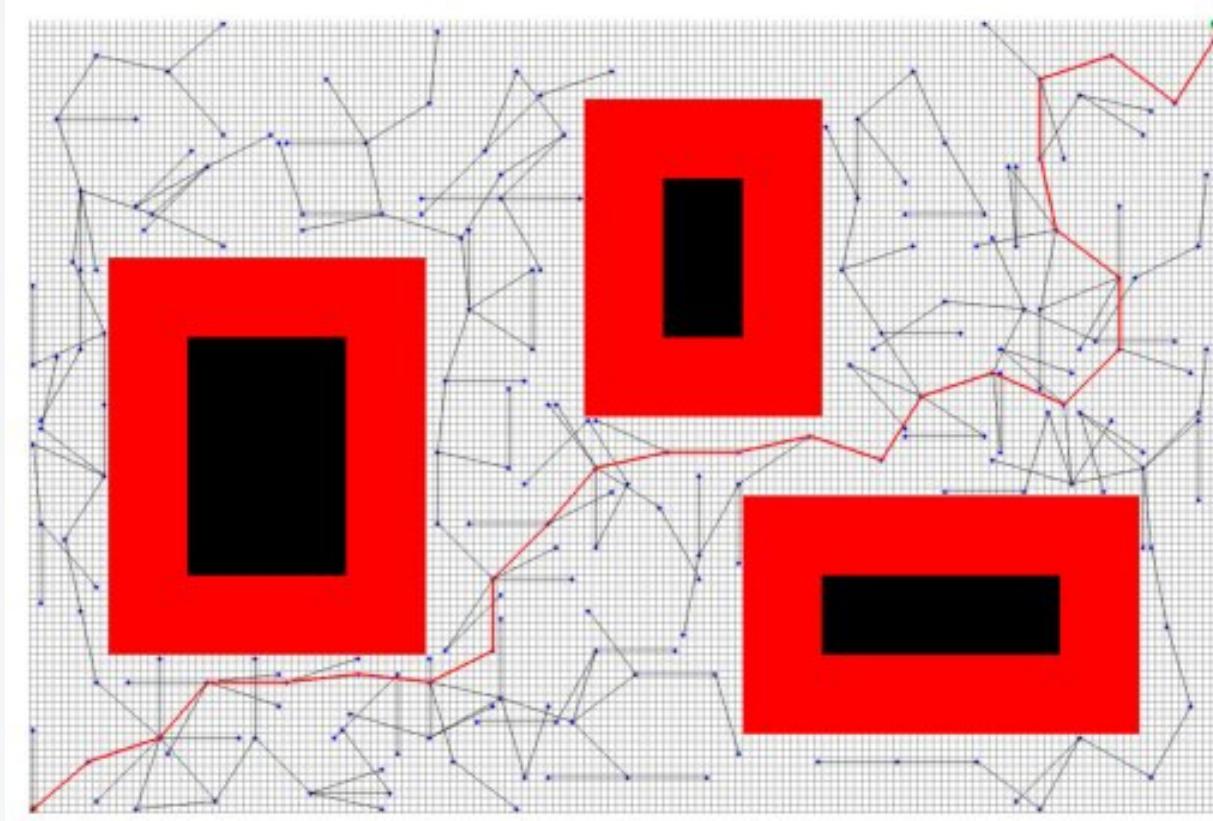
BFS



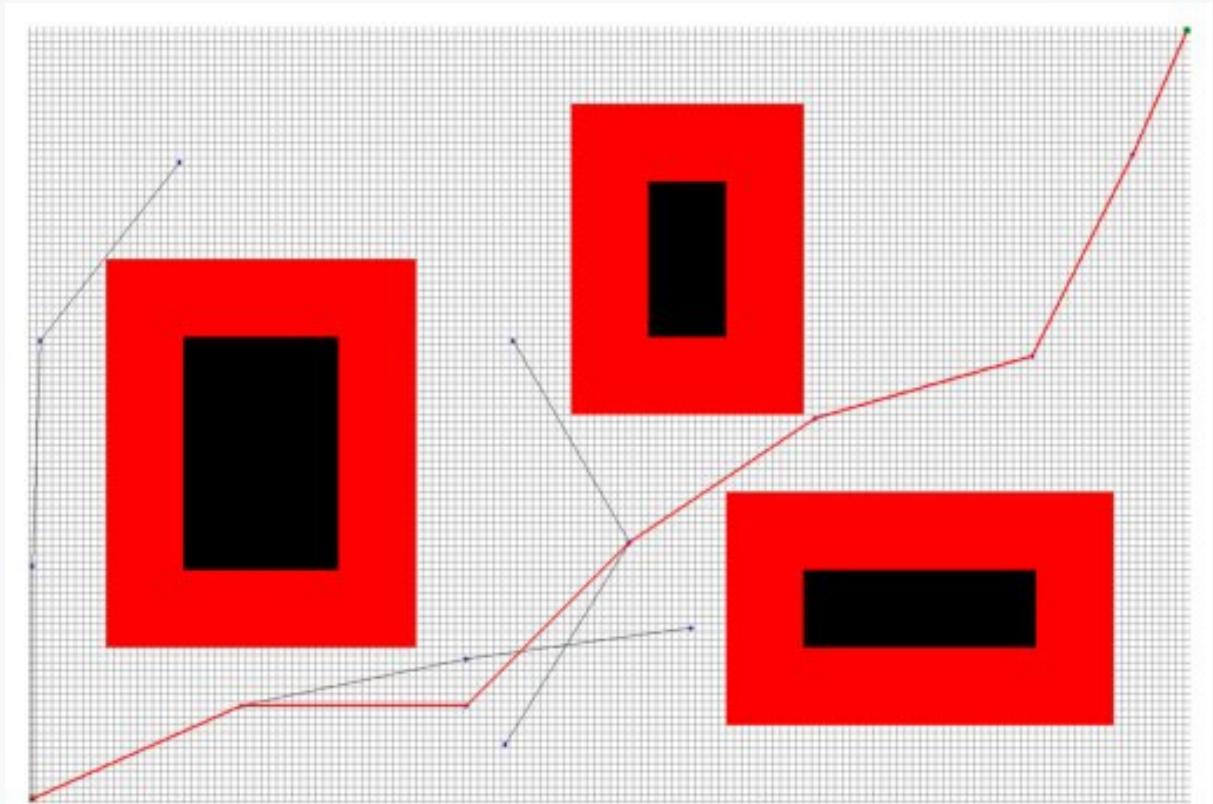
RRT



DELTA=5

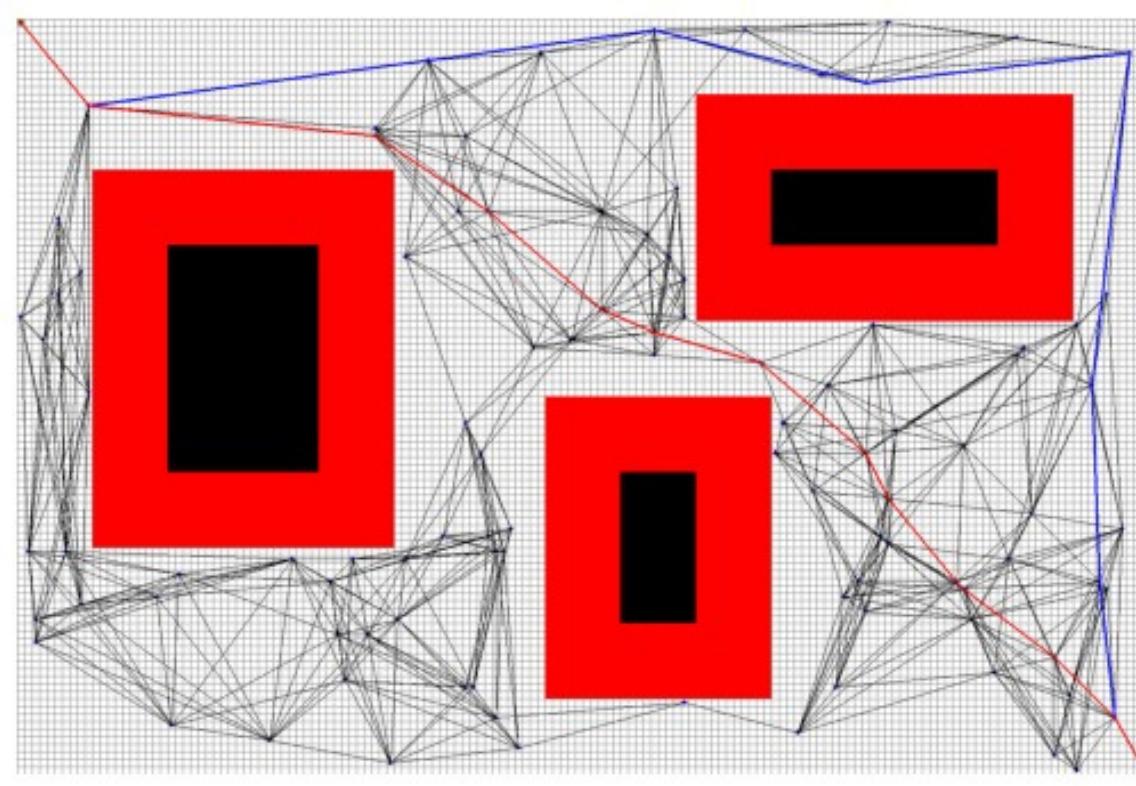


DELTA=10



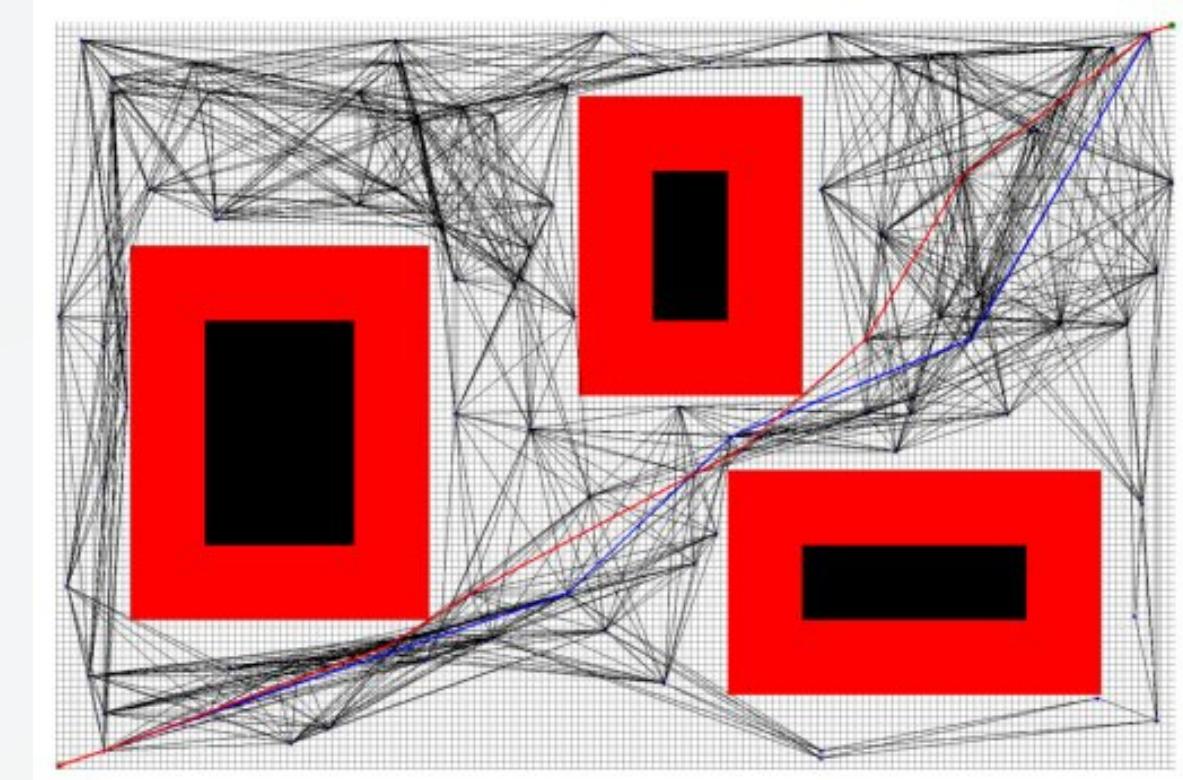
DELTA=30

PRM

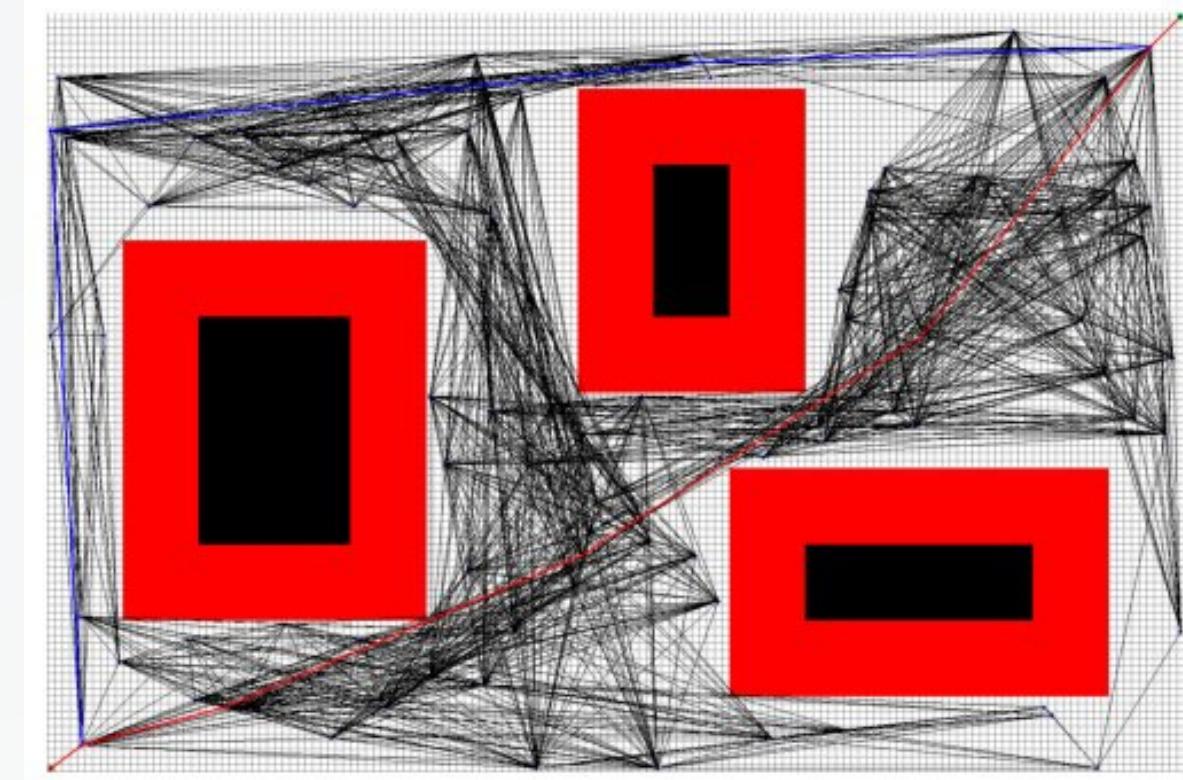


K=5

- A* algorithm: lenght 1876 with 14 points (RED)
- BFS algorithm: lenght 2504 with 10 points (BLUE)

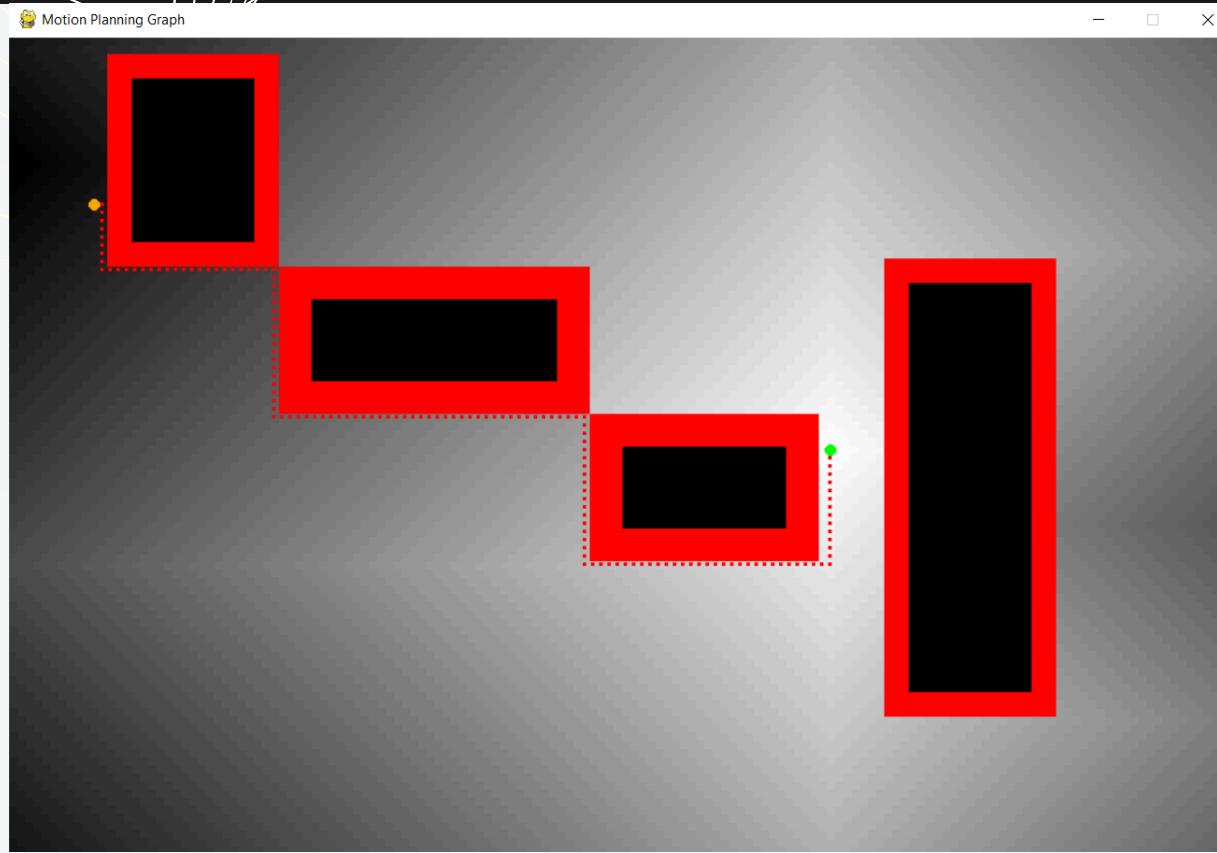


K=20

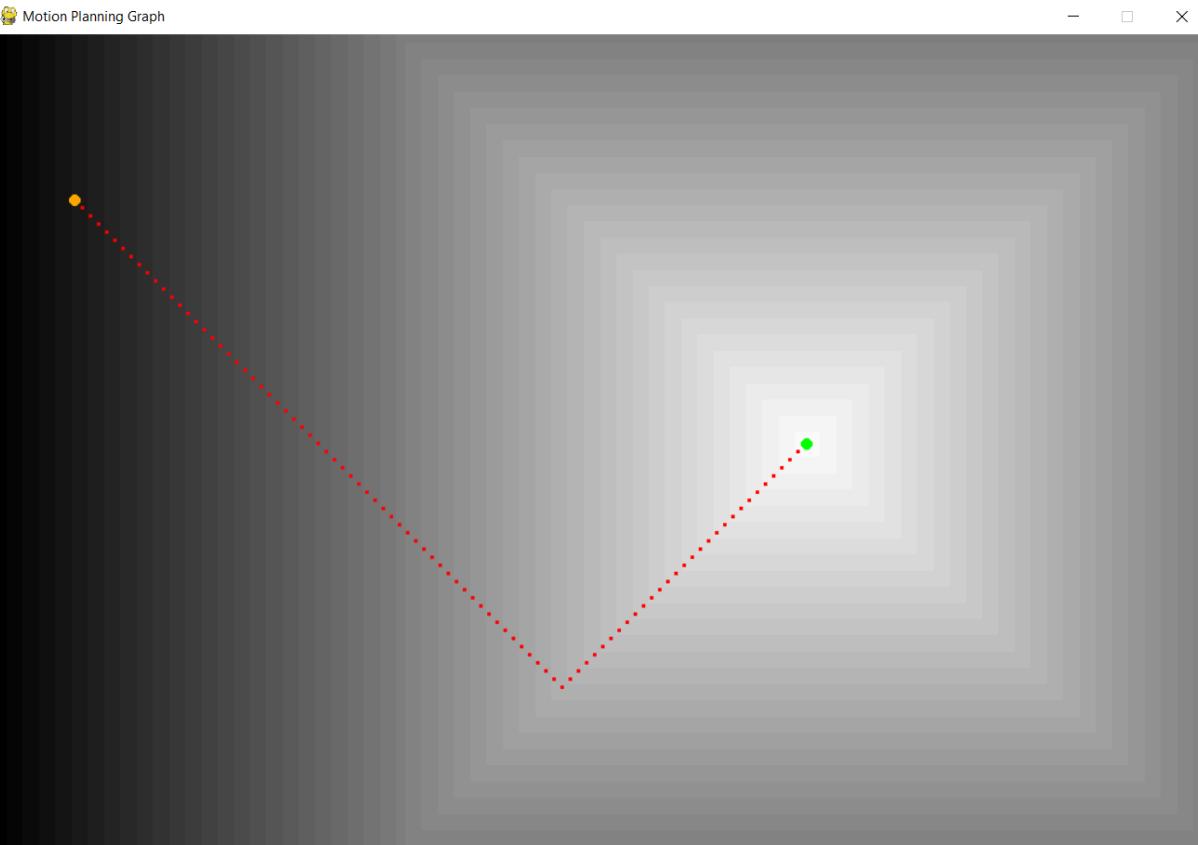


K=50

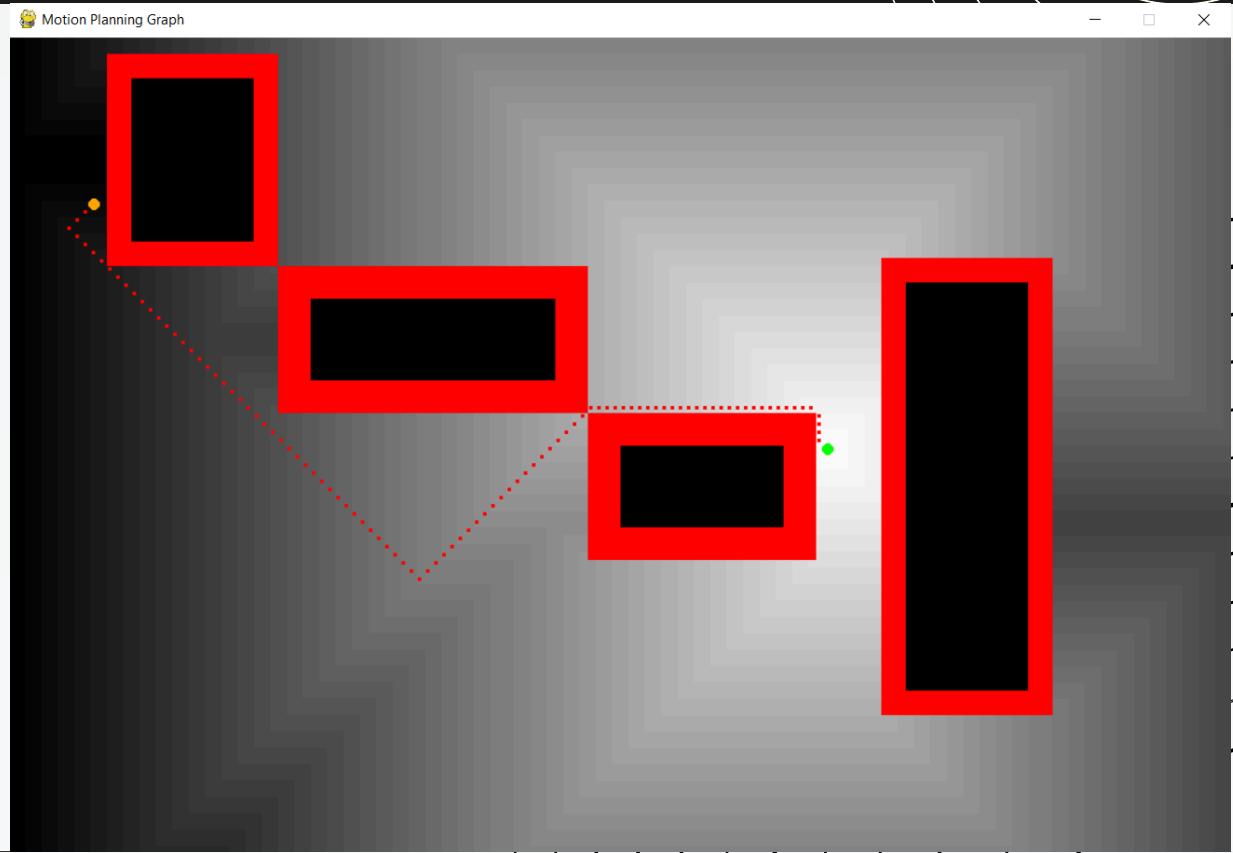
NAVIGATION FUNCTION



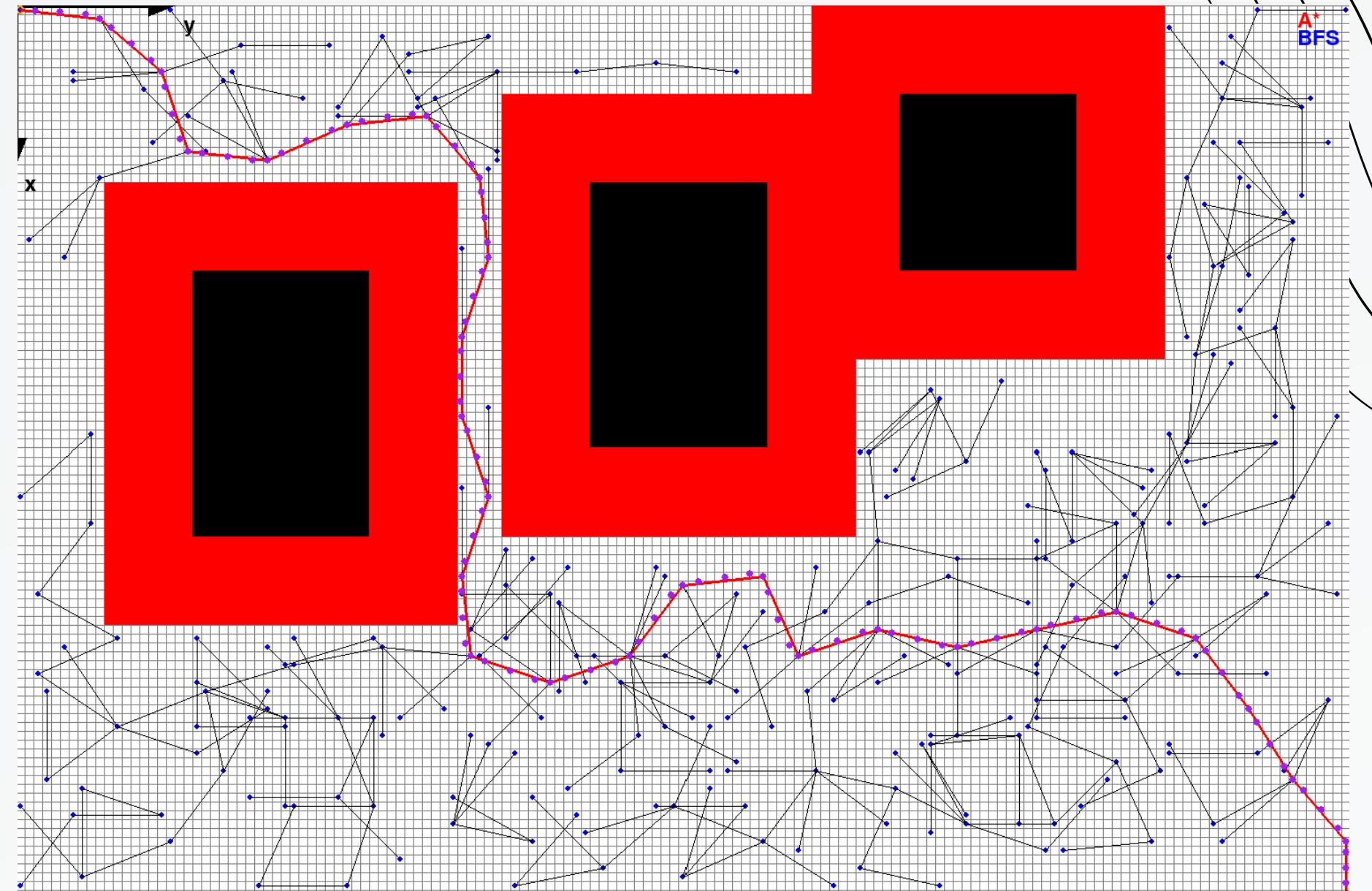
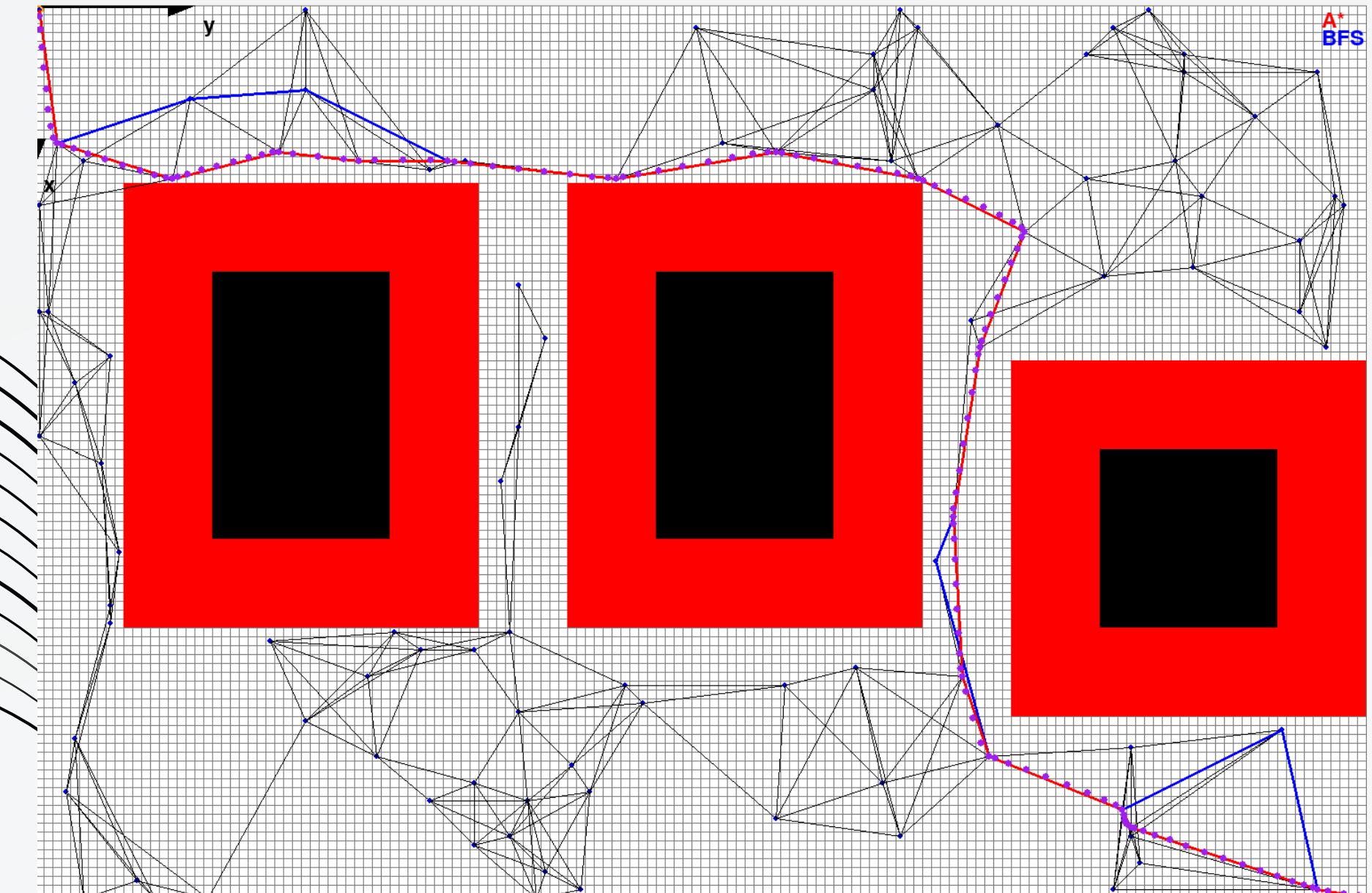
FREE SPACE



WITH OBSTACLE



PRM VS RRT





TRAJECTORY PLANNING

- Input: A* Path generated by Motion Planning
- Cartesian polynomials trajectories

$$x(t) = s(t)^3 x_f - (s(t) - 1)^3 x_i + \alpha_x s(t)^2 (s(t) - 1) + \beta_x s(t) (s(t) - 1)^2$$

$$y(t) = s(t)^3 y_f - (s(t) - 1)^3 y_i + \alpha_y s(t)^2 (s(t) - 1) + \beta_y s(t) (s(t) - 1)^2$$

$$\alpha_x = k \cos \theta_f - 3x_f$$

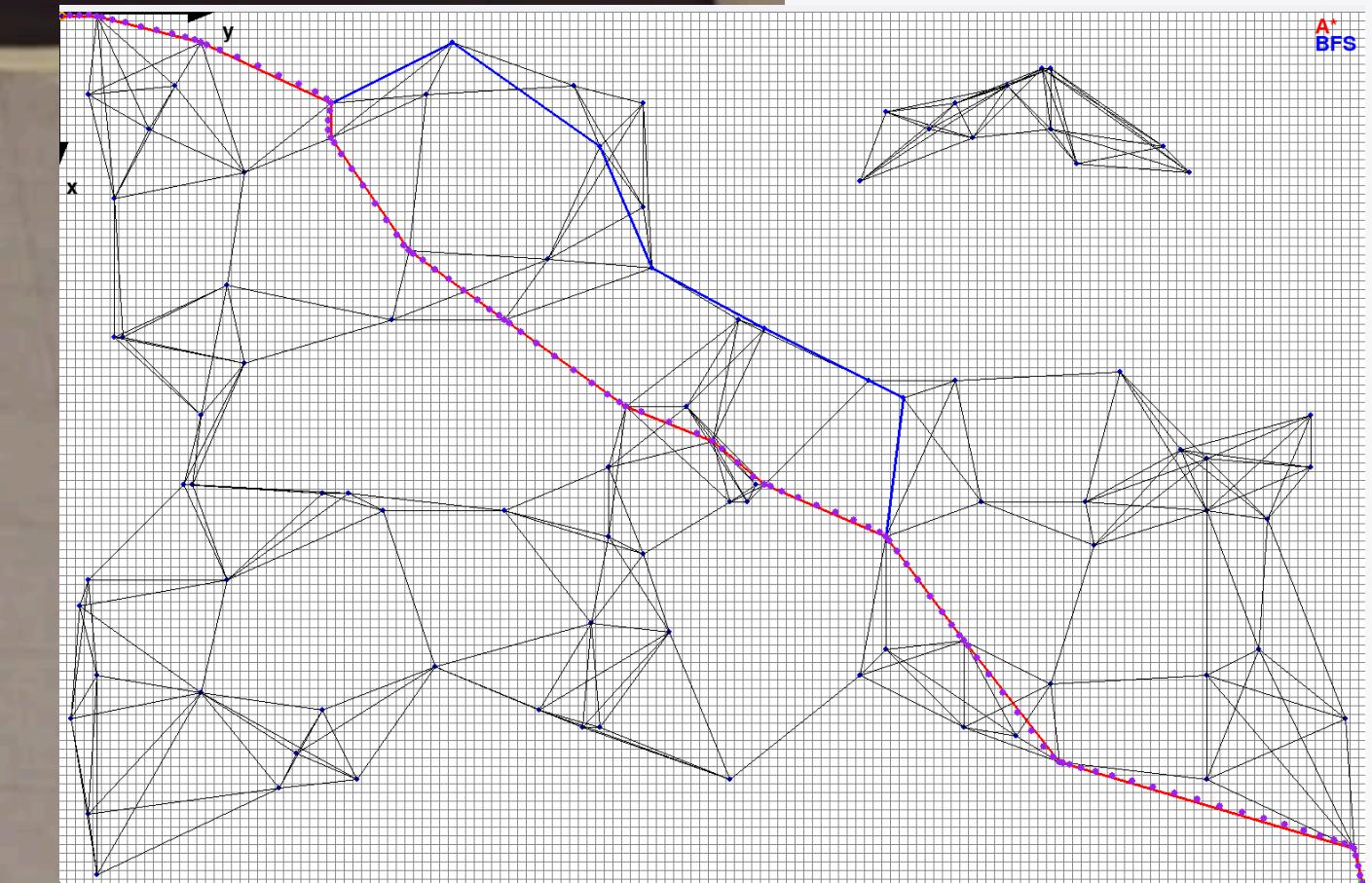
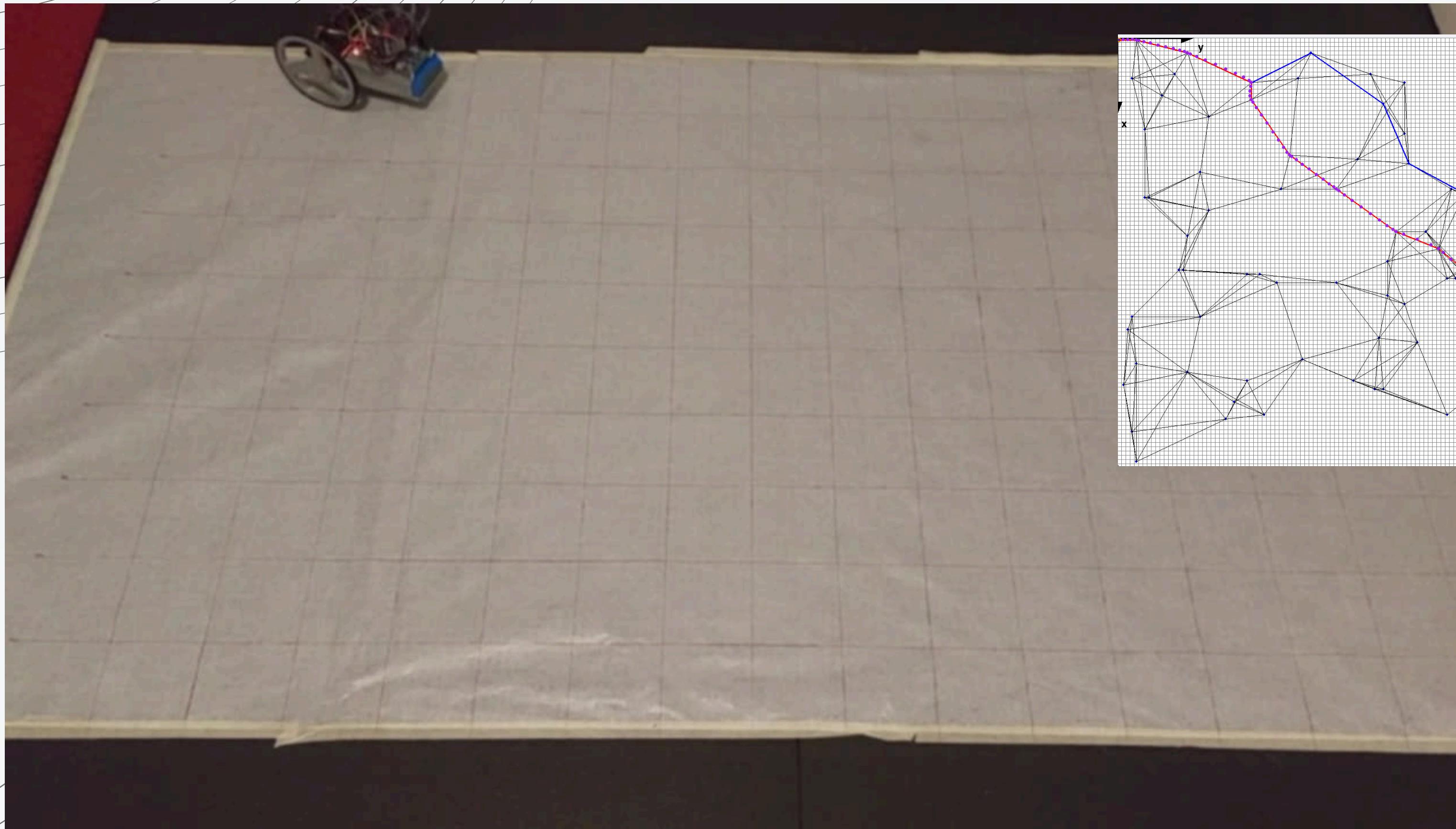
$$\alpha_y = k \sin \theta_f - 3y_f$$

$$\beta_x = k \cos \theta_i + 3x_i$$

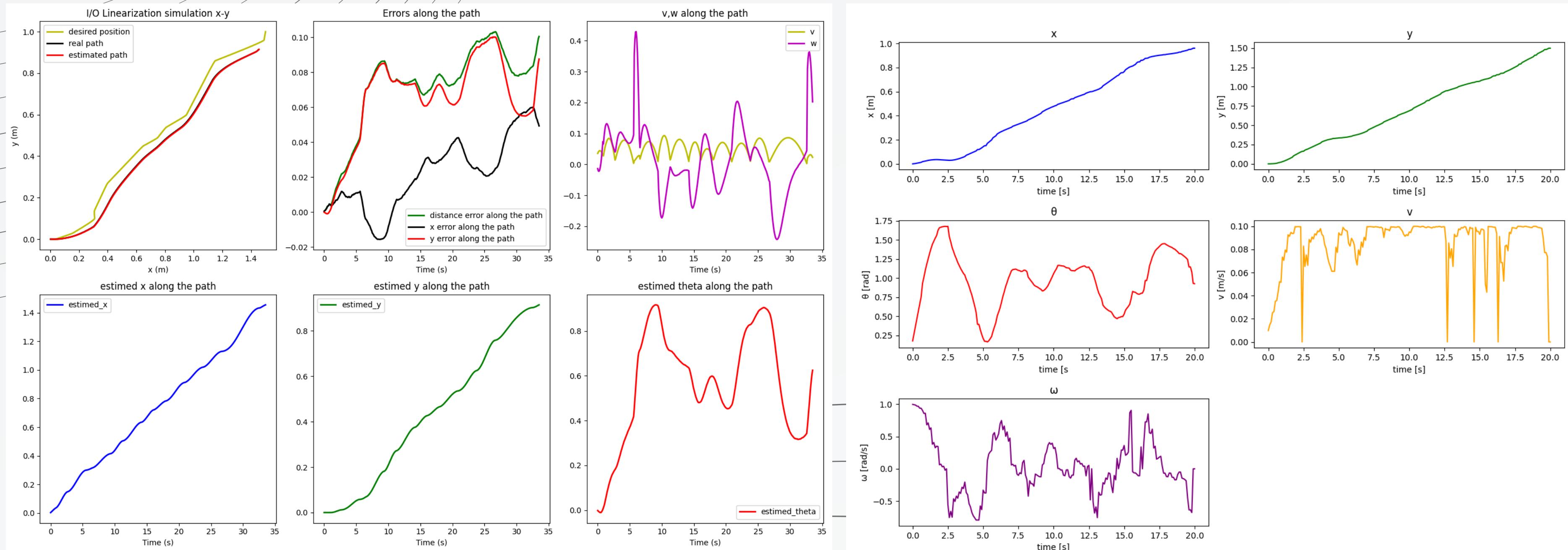
$$\beta_y = k \sin \theta_i + 3y_i$$

- Tuning k parameter
- Abscissa for each segment:
 - Linear profile (const. velocity)
 - Trapezoidal velocity profile
 - Cubic profile
- Trajectory scaling to respect motors saturation [linear, cubic]

TRAJECTORY PLANNING - LINEAR PROFILE



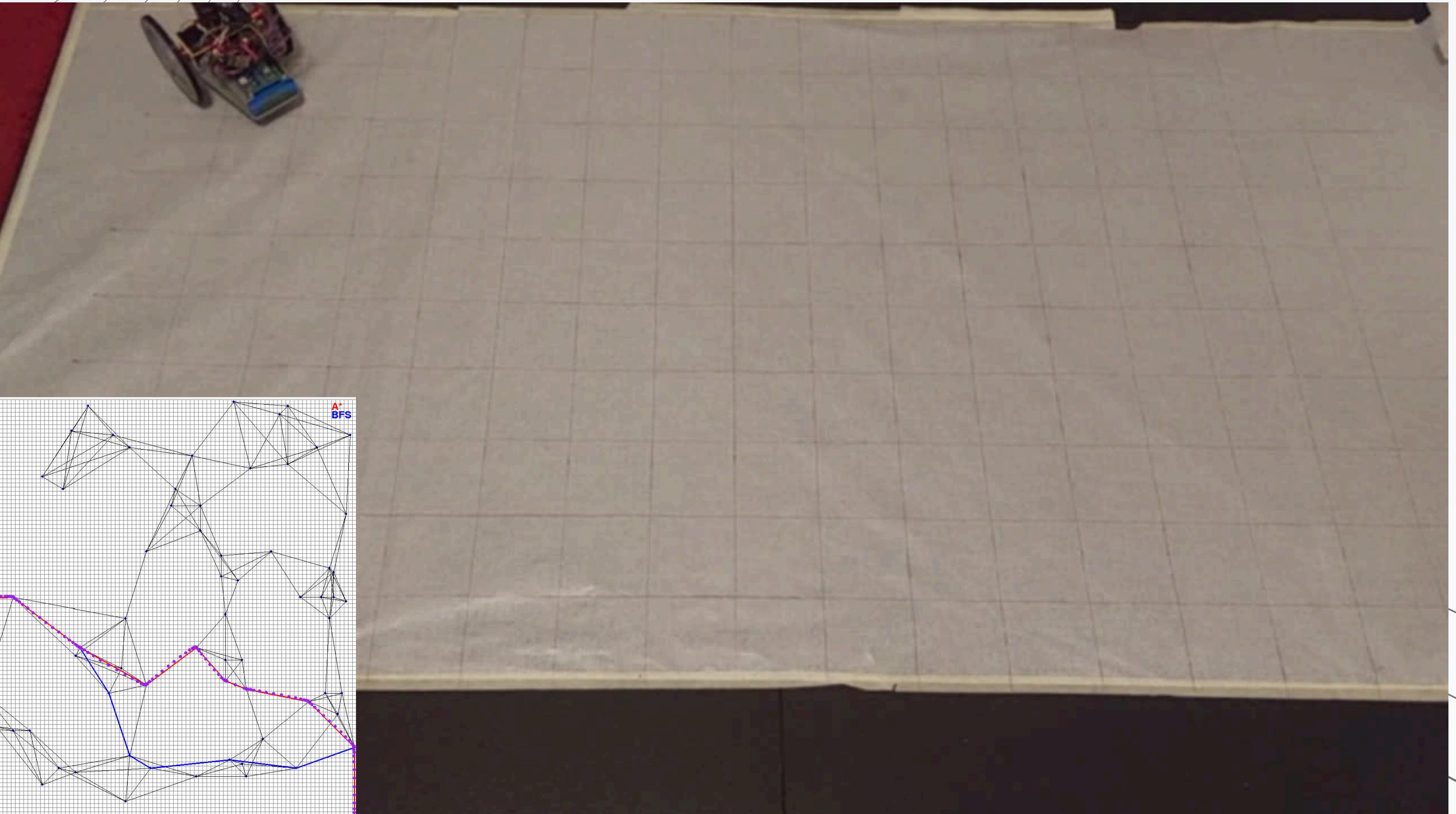
TRAJECTORY PLANNING - LINEAR PROFILE



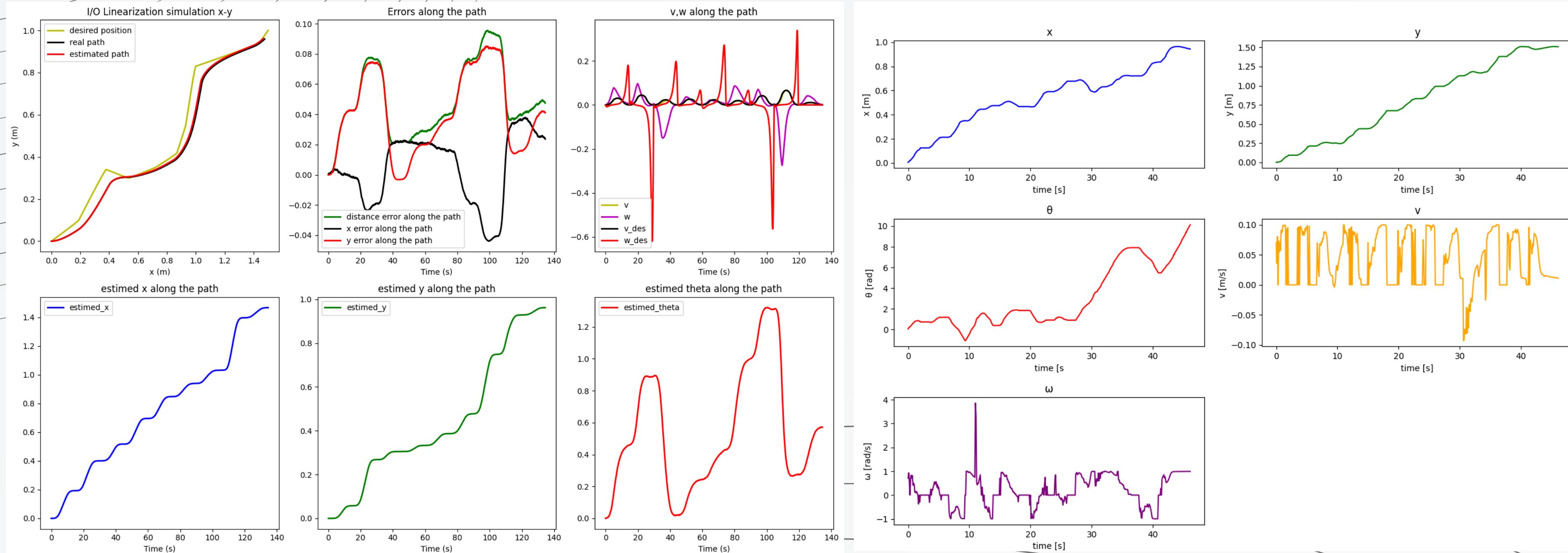
SIMULATION

TEST

TRAJECTORY PLANNING - TRAPEZOIDAL PROFILE



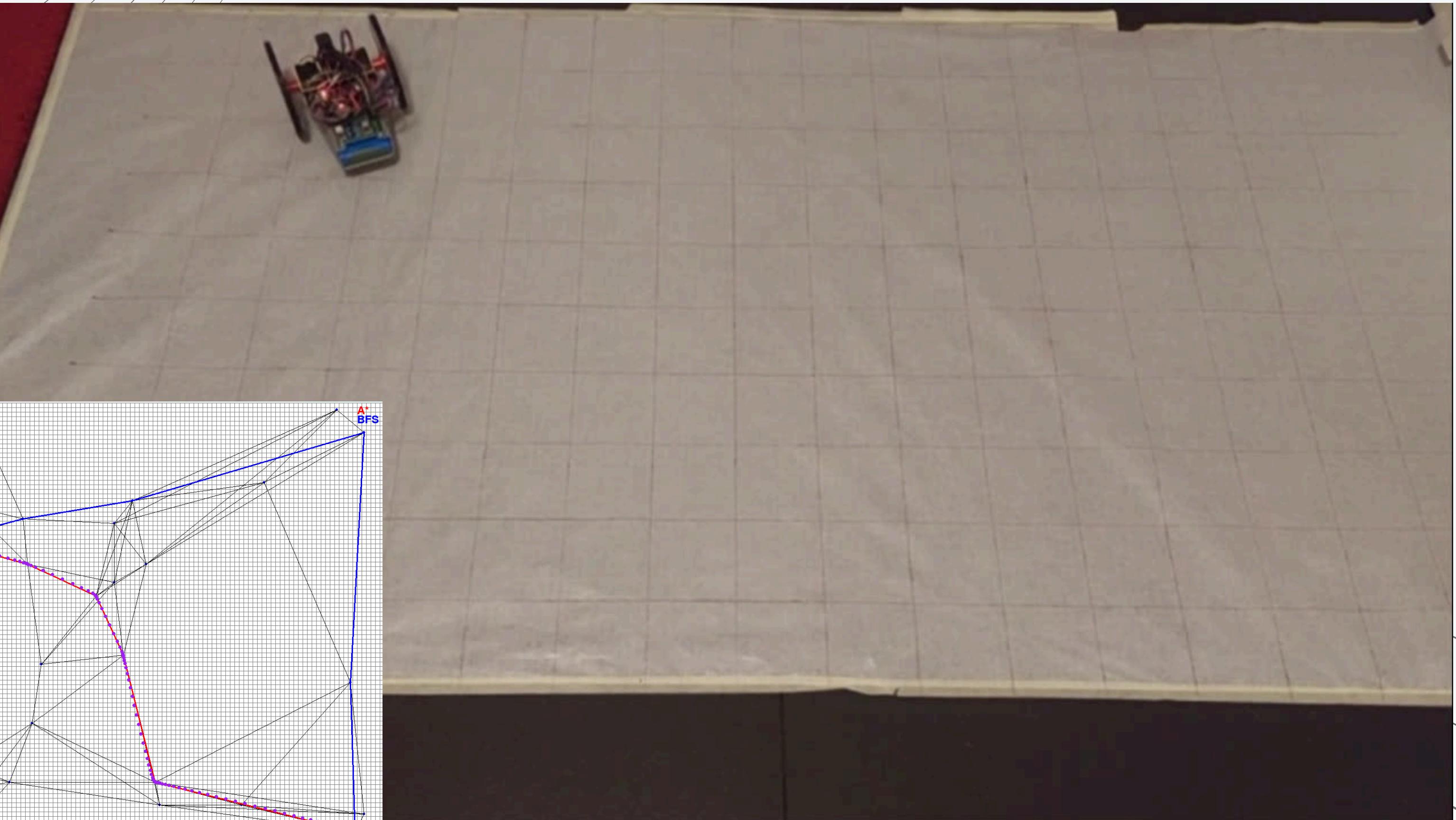
TRAJECTORY PLANNING - TRAPEZOIDAL PROFILE



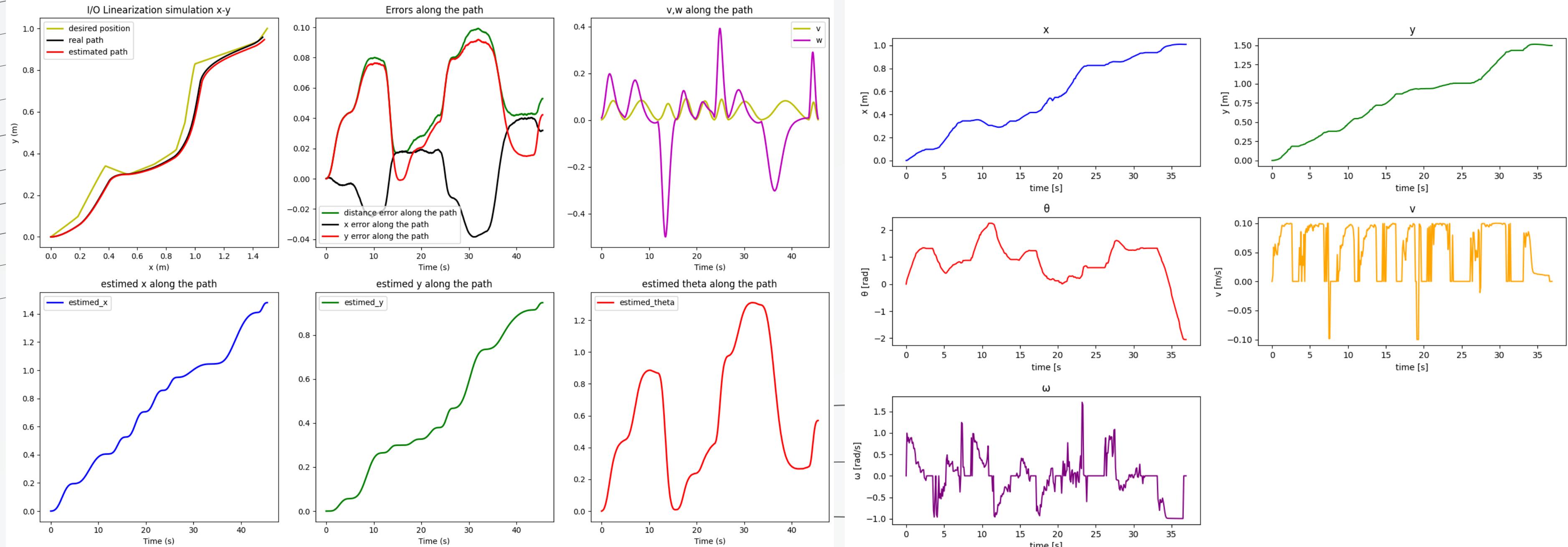
SIMULATION

TEST

TRAJECTORY PLANNING - CUBIC PROFILE



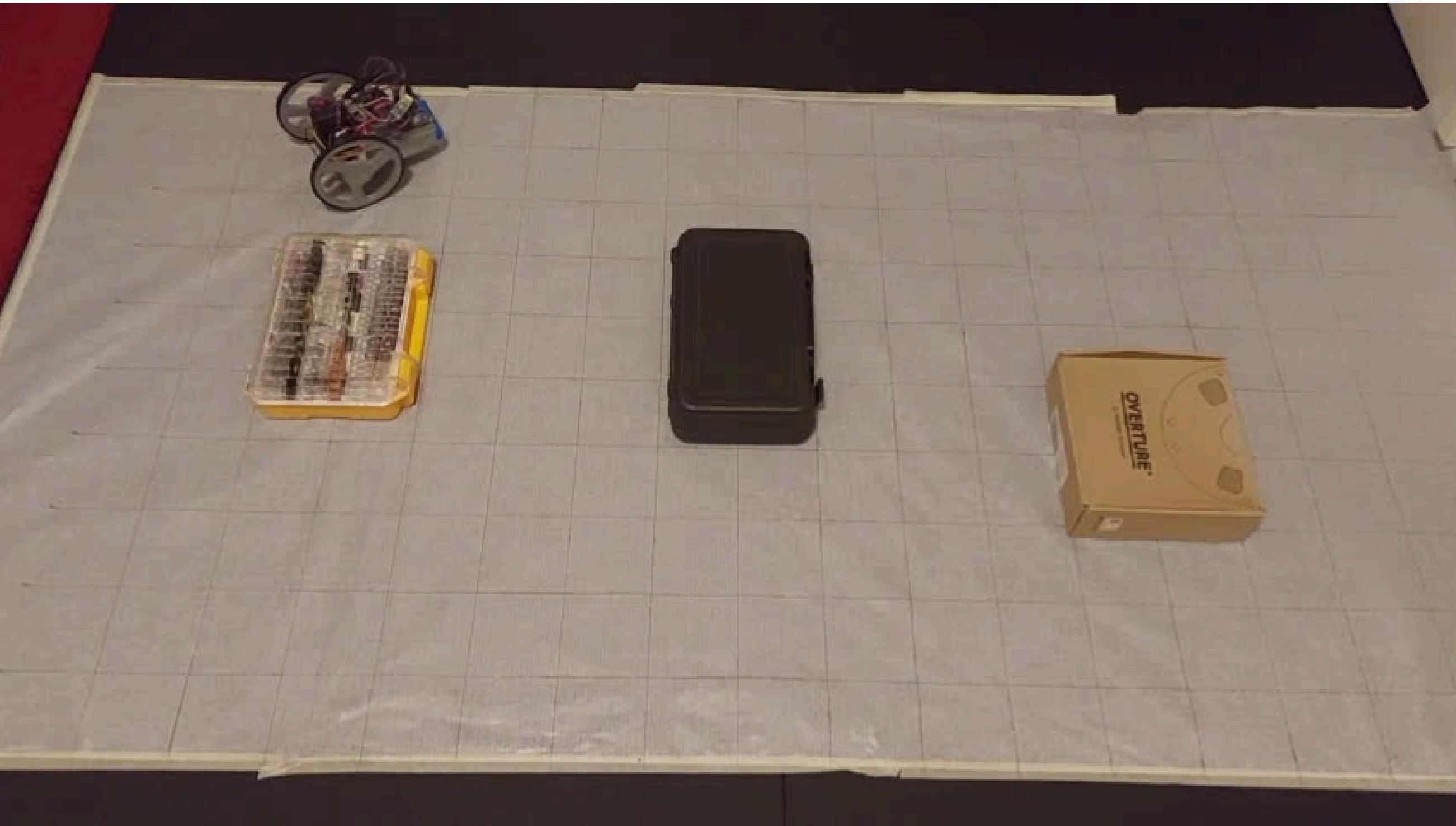
TRAJECTORY PLANNING - CUBIC PROFILE



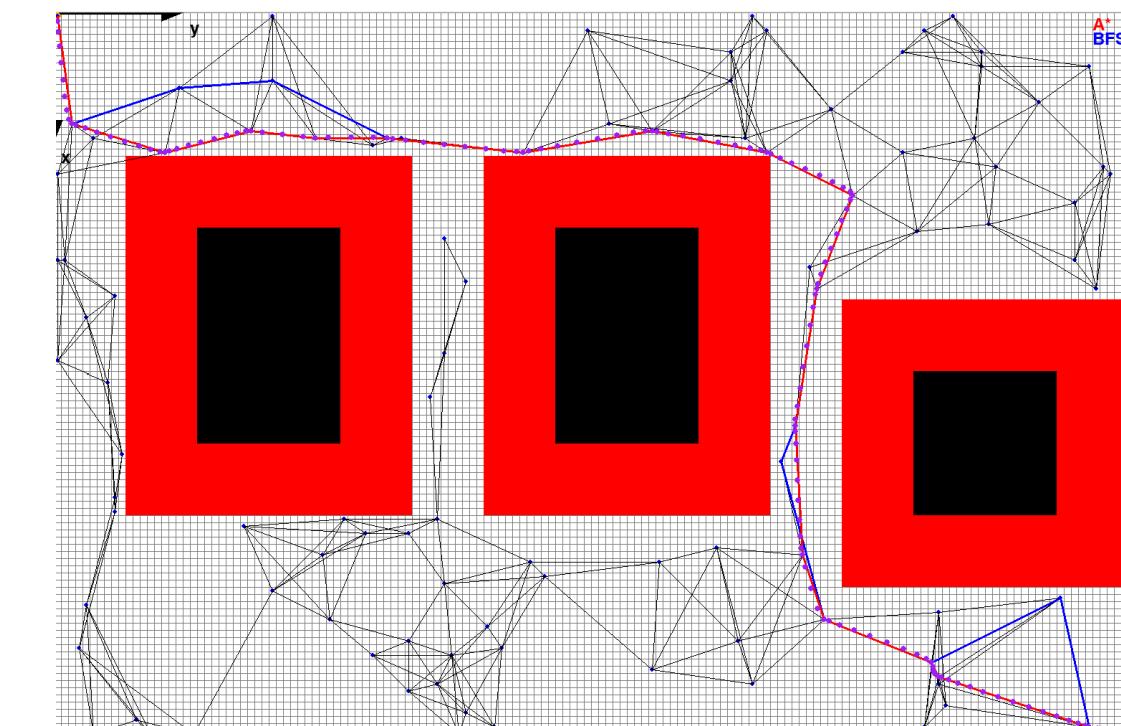
SIMULATION

TEST

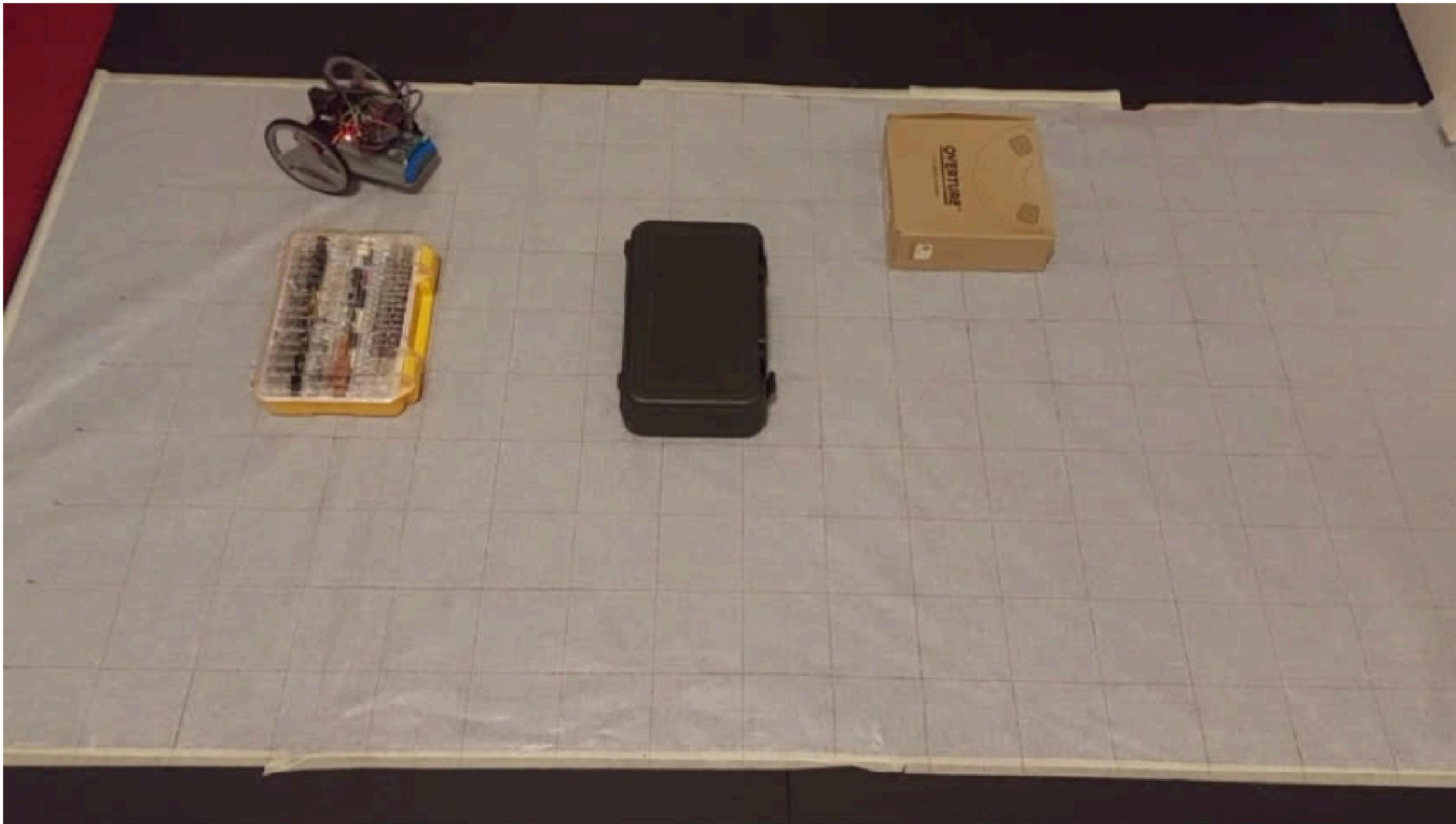
OBSTACLE AVOIDANCE



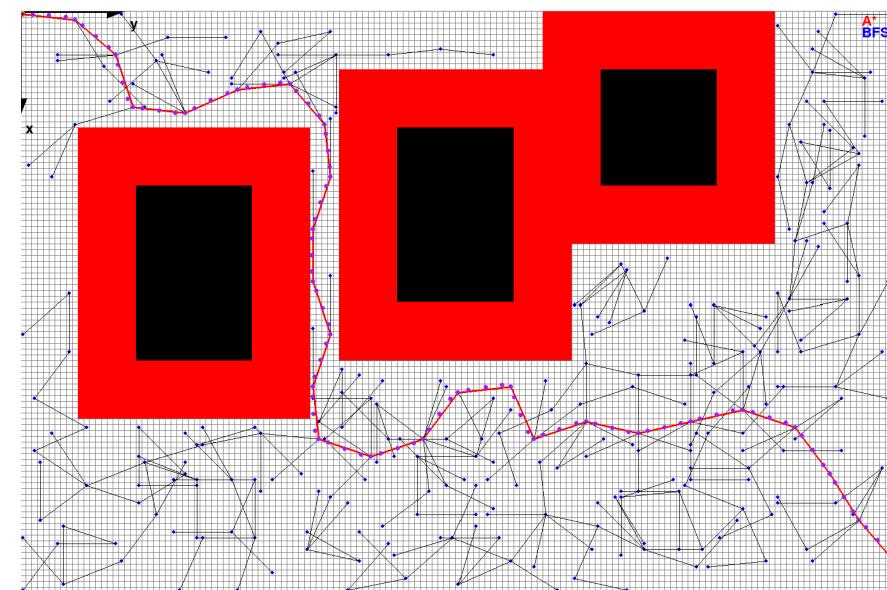
- Nodes: PRM, RRT
- Trajectory: Cartesian polynomial with linear profile



OBSTACLE AVOIDANCE



- Narrow corridor:
Difficult to generate feasible trajectories with PRM



FUTURE DEVELOPMENTS

- UKF onboard with camera or LIDAR
- Spline
- Car body
- Add features GCS (parameters Trajectory planning, live visualization)
- DC motors with incremental encoders

