# Principal Component Analysis

# Dataset testDF imputed\$completeObs

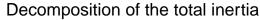
This dataset contains 58 individ	uals and 50 variables.	
1. Study of the outliers		
The analysis of the graphs does	not detect any outlier.	

#### 2. Inertia distribution

The inertia of the first dimensions shows if there are strong relationships between variables and suggests the number of dimensions that should be studied.

The first two dimensions of analyse express 51.61% of the total dataset inertia; that means that 51.61% of the individuals (or variables) cloud total variability is explained by the plane. This percentage is relatively high and thus the first plane well represents the data variability. This value is strongly greater than the reference value that equals 13.88%, the variability explained by this plane is thus highly significant (the reference value is the 0.95-quantile of the inertia percentages distribution obtained by simulating 5856 data tables of equivalent size on the basis of a normal distribution).

From these observations, it should be better to also interpret the dimensions greater or equal to the third one.



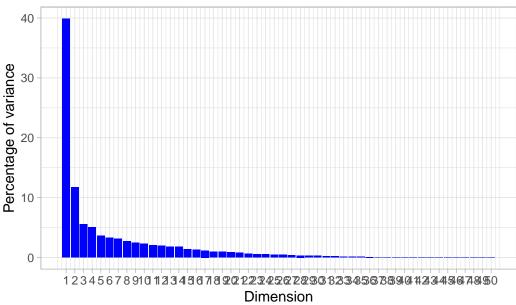


Figure 2 - Decomposition of the total inertia

We can observe that the first 2 axis present an amount of inertia greater than those obtained by the 0.95-quantile of random distributions (51.61% against 13.88%). Thus, a wise decision would be to restrict the description to these only axis. However, we choosed to describe the first 4 axis.

# 3. Description of the plane 1:2

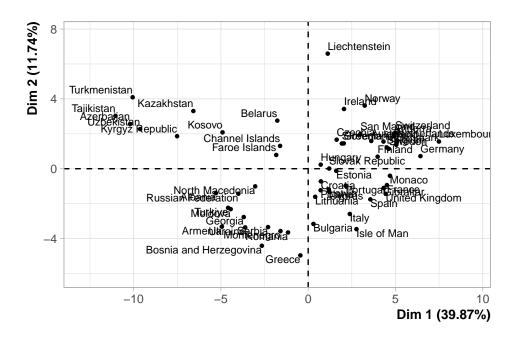


Figure 3.1 - Individuals factor map (PCA) The labeled individuals are those with the higher contribution to the plane construction.

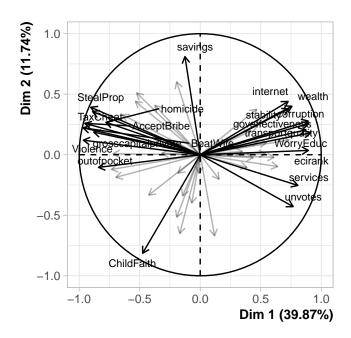


Figure 3.2 - Variables factor map (PCA) The labeled variables are those the best shown on the plane.

The dimension 1 opposes individuals such as Gibraltar, Netherlands, Denmark, Austria, Belgium, Switzerland, Andorra, Monaco, Isle of Man and Finland (to the right of the graph, characterized by a strongly positive coordinate on the axis) to individuals such as Turkmenistan, Kyrgyz Republic, Uzbekistan, Tajikistan, Azerbaijan, Kosovo, Kazakhstan, Armenia, Channel Islands and Georgia (to the left of the graph, characterized by a strongly negative coordinate on the axis).

The group in which the individuals Gibraltar, Netherlands, Denmark, Austria, Belgium, Switzerland, Andorra, Monaco, Isle of Man and Finland stand (characterized by a positive coordinate on the axis) is sharing:

- high values for variables like WorryEduc, transportquality, goveffectiveness, corruption, ecirank, stability, femaleminister, internet, femaleparliament and services (variables are sorted from the strongest).
- low values for variables like Violence, BeatWife, grosscapitalprivate, AcceptBribe, outofpocket, TaxCheat, StealProp, prison, homicide and agriculture (variables are sorted from the weakest).

The group in which the individuals Turkmenistan, Kyrgyz Republic, Uzbekistan, Tajikistan, Azerbaijan and Kazakhstan stand (characterized by a negative coordinate on the axis) is sharing:

- high values for variables like StealProp, TaxCheat, AcceptBribe, BeatWife, Violence, homicide, resourcements, prison, grosscapitalprivate and industry (variables are sorted from the strongest).
- low values for variables like unvotes, ecirank, corruption, WorryEduc, goveffectiveness, femaleminister, services, transportquality, wageworker and cleanfuel (variables are sorted from the weakest).

The group in which the individuals Kosovo, Armenia, Channel Islands, Georgia and Ukraine stand (characterized by a negative coordinate on the axis) is sharing:

- high values for the variables *ChildFaith*, *unemployed*, *outofschool* and *outofpocket* (variables are sorted from the strongest).
- low values for the variables stability, femaleparliament, transportquality, wealth, WorryEduc and goverfectiveness (variables are sorted from the weakest).

Note that the variables *AcceptBribe*, *Violence* and *BeatWife* are highly correlated with this dimension (respective correlation of 0.91, 0.93, 0.94). These variables could therefore summarize themselve the dimension 1

The dimension 2 opposes individuals such as *Turkmenistan*, *Kyrgyz Republic*, *Uzbekistan*, *Tajikistan*, *Azerbaijan* and *Kazakhstan* (to the top of the graph, characterized by a strongly positive coordinate on the axis) to individuals such as *Kosovo*, *Armenia*, *Channel Islands*, *Georgia* and *Ukraine* (to the bottom of the graph, characterized by a strongly negative coordinate on the axis).

The group in which the individuals *Turkmenistan*, *Kyrgyz Republic*, *Uzbekistan*, *Tajikistan*, *Azerbaijan* and *Kazakhstan* stand (characterized by a positive coordinate on the axis) is sharing:

- high values for variables like StealProp, TaxCheat, AcceptBribe, BeatWife, Violence, homicide, resourcements, prison, grosscapitalprivate and industry (variables are sorted from the strongest).
- low values for variables like unvotes, ecirank, corruption, WorryEduc, goveffectiveness, femaleminister, services, transportquality, wageworker and cleanfuel (variables are sorted from the weakest).

The group in which the individuals Kosovo, Armenia, Channel Islands, Georgia and Ukraine stand (characterized by a negative coordinate on the axis) is sharing:

- high values for the variables *ChildFaith*, *unemployed*, *outofschool* and *outofpocket* (variables are sorted from the strongest).
- low values for the variables stability, femaleparliament, transportquality, wealth, WorryEduc and goverfiectiveness (variables are sorted from the weakest).

### 4. Description of the plane 3:4

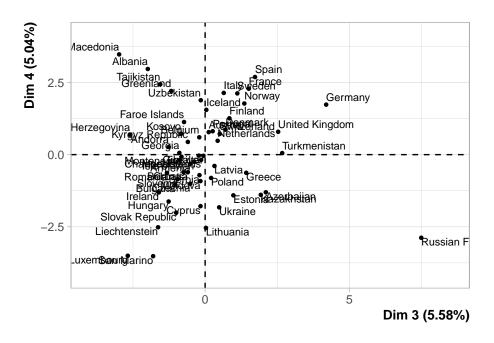


Figure 4.1 - Individuals factor map (PCA) The labeled individuals are those with the higher contribution to the plane construction.

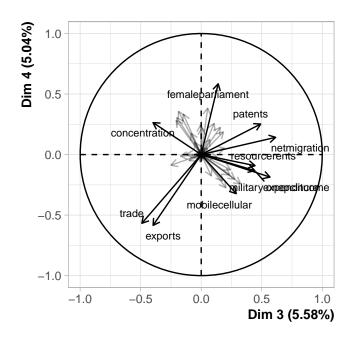


Figure 4.2 - Variables factor map (PCA) The labeled variables are those the best shown on the plane.

The dimension 3 opposes individuals such as Russian Federation, Spain, Germany, France, United Kingdom, Sweden, Norway and Italy (to the right of the graph, characterized by a strongly positive coordinate on the axis) to individuals such as San Marino, Slovak Republic, Lithuania, North Macedonia, Hungary, Albania, Luxembourg, Cyprus, Ireland and Estonia (to the left of the graph, characterized by a strongly negative coordinate on the axis).

The group in which the individuals *Spain*, *Germany*, *France*, *United Kingdom*, *Sweden*, *Norway* and *Italy* stand (characterized by a positive coordinate on the axis) is sharing:

- high values for the variables transportquality, femaleparliament, patents, femaleminister, WorryEduc, wealthincome, netmigration, corruption and goveffectiveness (variables are sorted from the strongest).
- low values for the variables StealProp, TaxCheat, AcceptBribe, BeatWife, grosscapitalprivate, Violence, trade, exports, outofpocket and homicide (variables are sorted from the weakest).

The group in which the individual Russian Federation stands (characterized by a positive coordinate on the axis) is sharing:

- high values for the variables onepcincome, resourcements, military expenditure, prison, homicide, female income, mobile cellular and net migration (variables are sorted from the strongest).
- low values for the variable unvotes.

The group in which the individuals *North Macedonia*, *Albania*, *Greenland*, *Faroe Islands* and *Bosnia and Herzegovina* stand (characterized by a negative coordinate on the axis) is sharing:

- high values for variables like agriculture, concentration, selfemployed, Violence, BeatWife, AcceptBribe, TaxCheat, grosscapitalprivate, unemployed and StealProp (variables are sorted from the strongest).
- low values for variables like cleanfuel, wageworker, goveffectiveness, WorryEduc, mobilecellular, transportguality, internet, services, urbanlevel and ecirank (variables are sorted from the weakest).

The group in which the individuals San Marino, Slovak Republic, Lithuania, Hungary, Luxembourg, Cyprus, Ireland and Estonia stand (characterized by a negative coordinate on the axis) is sharing:

- high values for the variables *trade* and *exports* (variables are sorted from the strongest).
- low values for the variable femaleparliament.

The dimension 4 opposes individuals such as North Macedonia, Spain, Germany, France, Albania, United Kingdom, Sweden, Norway, Greenland and Faroe Islands (to the top of the graph, characterized by a strongly positive coordinate on the axis) to individuals such as San Marino, Slovak Republic, Lithuania, Hungary, Luxembourg, Cyprus, Ireland and Estonia (to the bottom of the graph, characterized by a strongly negative coordinate on the axis).

The group in which the individuals *North Macedonia*, *Albania*, *Greenland*, *Faroe Islands* and *Bosnia and Herzegovina* stand (characterized by a positive coordinate on the axis) is sharing:

- high values for variables like agriculture, concentration, selfemployed, Violence, BeatWife, AcceptBribe, TaxCheat, grosscapitalprivate, unemployed and StealProp (variables are sorted from the strongest).
- low values for variables like cleanfuel, wageworker, goveffectiveness, WorryEduc, mobilecellular, transportguality, internet, services, urbanlevel and ecirank (variables are sorted from the weakest).

The group in which the individuals *Spain*, *Germany*, *France*, *United Kingdom*, *Sweden*, *Norway* and *Italy* stand (characterized by a positive coordinate on the axis) is sharing:

- high values for the variables transportquality, femaleparliament, patents, femaleminister, WorryEduc, wealthincome, netmigration, corruption and goveffectiveness (variables are sorted from the strongest).
- low values for the variables StealProp, TaxCheat, AcceptBribe, BeatWife, grosscapitalprivate, Violence, trade, exports, outofpocket and homicide (variables are sorted from the weakest).

The group in which the individuals San Marino, Slovak Republic, Lithuania, Hungary, Luxembourg, Cyprus, Ireland and Estonia stand (characterized by a negative coordinate on the axis) is sharing:

- high values for the variables *trade* and *exports* (variables are sorted from the strongest).
- low values for the variable femaleparliament.

#### 5. Classification

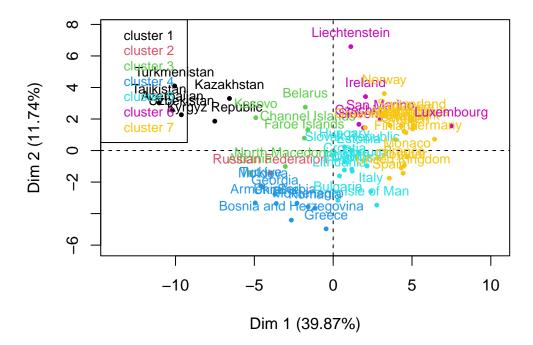


Figure 5 - Ascending Hierarchical Classification of the individuals. The classification made on individuals reveals 7 clusters.

The **cluster 1** is made of individuals such as Azerbaijan, Kazakhstan, Kyrgyz Republic, Tajikistan, Turkmenistan and Uzbekistan. This group is characterized by:

- high values for variables like TaxCheat, StealProp, resourcerents, AcceptBribe, BeatWife, Violence, homicide, grosscapitalprivate, outofpocket and selfemployed (variables are sorted from the strongest).
- low values for variables like unvotes, ecirank, services, wageworker, WorryEduc, goveffectiveness, corruption, femaleminister, transportguality and govern (variables are sorted from the weakest).

The cluster 2 is made of individuals such as Russian Federation. This group is characterized by:

• high values for the variables onepcincome, prison, netmigration, femaleincome, military expenditure, mobile cellular, resourcements and homicide (variables are sorted from the strongest).

The **cluster 3** is made of individuals such as *Albania*, *Belarus*, *Channel Islands*, *Faroe Islands*, *North Macedonia* and *Kosovo*. This group is characterized by :

- high values for the variables concentration, agriculture, grosscapital, grosscapitalprivate and onepcwealth (variables are sorted from the strongest).
- low values for the variables services and transportquality (variables are sorted from the weakest).

The **cluster 4** is made of individuals such as *Armenia*, *Bosnia and Herzegovina*, *Georgia*, *Greece*, *Moldova*, *Montenegro*, *Romania*, *Serbia*, *Turkiye* and *Ukraine*. This group is characterized by :

- high values for the variables *ChildFaith*, unemployed, outofschool, femaleincome, gini, selfemployed, militaryexpenditure and outofpocket (variables are sorted from the strongest).
- low values for variables like savings, stability, internet, cleanfuel, wealth, goveffectiveness, WorryEduc, transportquality, urbanrate and wealthincome (variables are sorted from the weakest).

The **cluster 5** is made of individuals such as *Bulgaria*, *Cyprus*, *Estonia*, *Croatia*, *Hungary*, *Isle of Man*, *Italy*, *Lithuania*, *Latvia* and *Poland*. This group is characterized by :

- high values for the variable unvotes.
- low values for the variables *urbanrate*, *concentration* and *grosscapital* (variables are sorted from the weakest).

The **cluster 6** is made of individuals such as *Czechia*, *Ireland*, *Liechtenstein*, *Luxembourg*, *San Marino* and *Slovenia*. This group is characterized by:

- high values for the variables exports, trade, stability, wealth, ecirank, goveffectiveness, corruption and industry (variables are sorted from the strongest).
- low values for the variables fdi, ChildFaith, militaryexpenditure, outofpocket and unemployed (variables are sorted from the weakest).

The **cluster 7** is made of individuals such as *Andorra*, *Austria*, *Belgium*, *Switzerland*, *Germany*, *Denmark*, *Spain*, *Finland*, *France* and *United Kingdom*. This group is characterized by :

- high values for variables like transportquality, femaleparliament, corruption, goveffectiveness, urbanlevel, WorryEduc, internet, wealth, femaleminister and govexp (variables are sorted from the strongest).
- low values for variables like Violence, BeatWife, AcceptBribe, prison, grosscapitalprivate, TaxCheat, outofpocket, StealProp, ChildFaith and homicide (variables are sorted from the weakest).

## Annexes