# Statistic recalls

#### 1. Overview

### Spectral Theorem

Let M be a symmetric matrix with real coefficients. Then it exists U orthogonal and D diagonal with real coefficients such that  $M = UDU^T$ .

#### Central Limit Theorem

Let  $(X_n)_{n\geq 1}$  be a real and independent sequence with same law such that  $\mu=\mathbb{E}[X_1]$  and  $\mathbb{V}[X_1]=\sigma^2$  are defined  $(\mathbb{V}[X_1]\leq +\infty)$ . Noting  $\bar{X}_n=\frac{1}{n}(X_1+\ldots+X_n)$ , we have:

$$\sqrt{n} \frac{(\bar{X}_n - \mu)}{\sigma} \sim_{n \to \infty} \mathcal{N}(0, 1)$$

## Estimation

#### Likelihood method

This method consists on finding the parameter that maximizes the likelihood:  $L(\theta|X) = f(X|\theta) = \prod_{i=1}^{n} f_{\theta}(x_i;\theta)$  which is the product of densities across all samples.

Intuitively, we want to find the  $\theta$  that maximizes a certain event, that is, obtaining some data X (which is why we have  $X|\theta$ ).

We often use the log in order to get rid of power coefficients appearing with the product. likelihood equation:  $\frac{d}{d\theta}ln(L(\theta|X)) = 0$