

Full Adder			
Input			Output
A	B	C-in	Sum C-out
0	0	0	0 0
0	0	1	1 0
0	1	0	1 0
0	1	1	0 1
1	0	0	1 0
1	0	1	0 1
1	1	0	0 1
1	1	1	1 1

Sum

$$\begin{aligned}
 \text{Sum} &= \overline{A}\overline{B}C_{\text{in}} + \overline{A}B\overline{C_{\text{in}}} + A\overline{B}\overline{C_{\text{in}}} + ABC_{\text{in}} \\
 &= \overline{A}(\overline{B}C_{\text{in}} + B\overline{C_{\text{in}}}) + A(\overline{B}\overline{C_{\text{in}}} + BC_{\text{in}}) \\
 &= \overline{A}(B \text{ xor } C_{\text{in}}) + A(\overline{B \text{ xor } C_{\text{in}}}) \\
 &= A \text{ xor } (B \text{ xor } C_{\text{in}})
 \end{aligned}$$

$$\begin{aligned}
 C_{\text{out}} &= \overline{A}B C_{\text{in}} + A\overline{B} C_{\text{in}} + AB\overline{C_{\text{in}}} + ABC_{\text{in}} \\
 &= AB + C_{\text{in}}(\overline{A}B + A\overline{B}) \\
 &= AB + C_{\text{in}}(A \text{ xor } B)
 \end{aligned}$$