

1223 = Val

H1 Arch

1. a.) False, increasing performance usually decreases energy efficiency not the other way around
- b.) True, a system needs all of its parts to function ~~properly~~ properly, so the failure point will always be the weakest link in the chain. This is why designing redundancies are good.
- c.) False, Amdahl's Law is very useful ~~for~~ for finding latency and/or bottleneck points. It can also be used to show speedup in, not only serial programs, but parallel ones as well.
- d.) False, Clock speed is only one aspect of performance. There are many other factors you must take into account, in order to minimize exec time
- e.) True, you can have 1 million cores available but if the software is serial, it won't make much of a difference

2. 1.8) a) $E = \frac{1}{2} \text{Capacitance Load} \times V^2 = \frac{1}{2} C V^2$

$E = E_{\text{exec}} + E_{\text{idle}}$, since computation takes $\frac{1}{2}$ the amount of time to run, the energy would be 50%

$$\frac{E}{2} = E_{\text{exec}} = \boxed{50\%}$$

b.) With Energy, f doesn't matter, so $E = \frac{C V^2}{2}$

$$E_{\text{new}} = \frac{C \left(\frac{V}{2}\right)^2}{2} \rightarrow \text{cont on next page}$$

b.) Cont $\frac{E}{E_{\text{new}}} = \frac{cV^2}{c} \cdot \frac{2}{(1/2)^2} = \frac{V^2}{\frac{V^2}{4}} = V^2 \cdot \frac{4}{V^2} = 4$

$$E_{\text{new}} = \frac{E}{4}, \text{ Saved} = E - E_{\text{new}} = E - \frac{E}{4} = E(1 - \frac{1}{4}) \Rightarrow$$

$$\text{Saved} = \frac{3}{4} E = \boxed{.75 E \text{ or } 75\% \text{ Less energy}}$$

~~1.9 (1.9) $P = CV^2$ = 1.1~~
~~• 6 (ES) = 6.8, 169% Power~~
~~• 6 (20) = 1.1, 12 + 4~~

1.9 PC = Power Consumption, S = number of servers
 M = max power consumption, PS = power savings

a) $PC = 9(m)(s)$

$$PC_{\text{new}} = PC - .9(M)(.6S) = .9(MS) - .54(MS) = .36MS$$

$$PS = 1 - \frac{PC_{new}}{PC} = 1 - \frac{.36ms}{.9ms} = 1 - .4 = .6 = \boxed{60\%}$$

1.9 PC = Power Consumption, M = max PC , S = # servers,
 PS = Power Savings

a.) $PC = .9MS$, $PC_{new} = .9(M)(1-.6)S = .36MS$

$$PS = 1 - \frac{PC_{new}}{PC} = 1 - \frac{.36}{.9} = 1 - .4 = .6 = \boxed{60\%}$$

b.) $PC = .9MS$

$$PC_{new} = .9(M).4(S) + .2(M).6(S) = .36MS + .12MS = .48MS$$

$$PS = 1 - \frac{PC_{new}}{PC} = 1 - \frac{.48MS}{.9MS} = 1 - .53 \approx \boxed{.47}$$

c.) $PC = \frac{CV^2f}{2} = \frac{Ef}{2}$

$$PC_{new} = \frac{C((1-.2)V)^2((1-.4)f)}{2} = \frac{C(.8V)^2(.6f)}{2} = \frac{.384CV^2f}{2} = \frac{.384Ef}{2}$$

$$PS = \frac{PC - PC_n}{PC} = 1 - \frac{.384Ef/2}{Ef/2} = 1 - .384 = \boxed{.616 \approx 62\%}$$

d.) $PC_{new} = .9(M)(1-.6)(S) + .2(M).3(S) = .36MS + .06MS$
 $= .42MS$

$$PS = \frac{PC - PC_n}{PC} = \frac{.9MS - .42MS}{.9MS} = 1 - \frac{.42}{.9} = 1 - .467 \approx \boxed{.53 = 53\%}$$

$$\text{Amdahl} = \frac{E_{\text{ec old}}}{E_{\text{ec new}}}$$

$$1.12 \quad b.) \quad Z = \frac{E_{\text{ec old}}}{E_{\text{ec new}}} = \frac{1}{(1-F) + \frac{F}{20}} \Rightarrow$$

$$(1-F) + \frac{F}{20} = \frac{1}{2} \Rightarrow 20 - 20F + F = 10$$

$$\Rightarrow 10 = 20F - F = 19F, \quad \boxed{F = \frac{10}{19} \approx 53\%}$$

$$c.) \quad E_{\text{ec new}} = E_0 \left(\frac{10}{19} \right) \left(\frac{10}{20} \right)$$

$$E_n = \frac{E_0}{20} \quad \frac{E_0}{20} = E_0 \left(\frac{9}{19} + \frac{10}{19(20)} \right)$$

$$E_0 = 20E_0 \left(\frac{9}{19} \right) + 20E_0 \left(\frac{10}{19(20)} \right) =$$

$$0 = \frac{180E_0}{19} + \frac{10E_0}{19} - E_0 = \frac{190E_0}{19} - E_0 = 10E_0 - E_0$$

$$= 9E_0 = 0$$

$$E_0 = \frac{0}{9}$$

$$c.) \quad S_2 = \frac{1}{(1 - 0.9(1/2)) + \frac{0.9(1/2)}{2}} = \frac{1}{0.55 + 0.225} = \frac{1}{0.775}$$

$$\boxed{\approx 1.29}$$

$$c.) S_4 = \frac{1}{.55 + \frac{.45}{4}} = \frac{1}{.55 + .1125} = \frac{1}{.6625} =$$

$$\boxed{\approx 1.51}$$

$$1.14 \quad a.) S = \frac{1}{(1-.2) + \frac{.2}{2}} = \frac{1}{.8 + \frac{1}{10}} = \frac{1}{.9} \approx \boxed{1.11}$$

$$b.) S = \frac{1}{(1-.1) + \frac{.1}{2/3} + \frac{.2}{2}} =$$

$$\frac{1}{.7 + .1 \frac{.3}{2}} = \frac{1}{.95} \boxed{\approx 1.05}$$

$S = \text{Speedup from b.)}$

$$c.) F\% = \frac{0.2}{2} S = \frac{0.2}{2} \times 1.05 = \boxed{0.105} = \boxed{10.5\%}$$

$$\text{Cache \%} = \frac{0.1}{2/3} S = \frac{0.3}{2} \times 1.05 = \boxed{0.1575} = \boxed{15.75\%}$$

$$1.16 \quad a.) \quad S = \frac{1}{(1-0.8) + \frac{0.8}{N}} = \frac{1}{0.2 + \frac{0.8}{N}}$$

$$\frac{\frac{N \cdot 2}{N} + \frac{0.8}{N}}{N} = \frac{0.2N + 0.8}{N} = \frac{N}{0.2N + 0.8}$$

$$\frac{1}{(1-0.8) + \frac{0.8}{N}} = \frac{1}{0.2 + \frac{0.8}{N}}$$

$$0.2 \left(1 + \frac{0.4}{N} \right) = \frac{1}{(1-4/5) + \frac{4}{5N}} = \frac{1}{\frac{1}{5} + \frac{4}{5N}}$$

$$= \frac{1}{\frac{N}{5N} + \frac{4}{5N}} = \frac{N+4}{5N} = \boxed{\frac{5N}{N+4}}$$

1.1b ~~b.) $\frac{SN}{N+4} + .005N$~~

b.) ~~$\frac{.008}{8+4} + \frac{.005}{12} + .005(8)$~~

$$\frac{1}{(1 - \frac{4}{5}) + \frac{\frac{4}{5}}{8} + .005(8)} = \frac{1}{\frac{1}{5} + \frac{4}{40} + .04}$$

$$= \frac{1}{.2 + .1 + .04} = \frac{1}{.34} \approx 2.94$$