

## Standard Deviation

Consider a population of size  $N$  and a sample (subset) of the population of size  $n < N$ . We draw the values for a feature of the entire population (or we sample) for an attribute, say age.

Now, the standard deviation is as follows for the **population**. Given  $a_i, i \in [1, N]$  is the set of  $N$  ages, first find the average  $\bar{a}_i$

$$\bar{a}_i = \sum_{i=1}^N a_i / N \quad (1)$$

Then *stdev* is

$$stdev = \sqrt{\frac{\sum_{i=1}^N (a_i - \bar{a}_i)^2}{N}} \quad (2)$$

Now, if I **sample**  $n$  examples from  $N$ , the *stdev* is calculated as:

$$\bar{a}_i = \sum_{i=1}^n a_i / n \quad (3)$$

Then *stdev* is

$$stdev = \sqrt{\frac{\sum_{i=1}^n (a_i - \bar{a}_i)^2}{n - 1}} \quad (4)$$

What is different?

What is the effect of dividing by  $n - 1$ ? Why might this be reasonable?

The effect is you get a higher standard deviation. It is reasonable because you only have a sample or subset of the data which may not be enough to get a tight estimate of the true standard deviation.