

# Assignment 6

Sayak Ghorai || BT21GCS004 || B2 || Design and Analysis of Algorithm

**Q:** Write an algo for Quick sort and Merge sort for an array of integers.

**Code for Quick Sort:**

```
QuickSort.java x MergeSort.java x
1 import java.util.*;
2 public class QuickSort {
3     static int Count;
4     public static void main(String[] args) {
5         int[] Arr1 = CreateArr();
6         System.out.println("Original Array1: " + Arrays.toString(Arr1));
7         int[] Sorted1=myQuickSort(Arr1, start: 0, end: Arr1.length-1);
8         System.out.println("Sorted Arr is: " + Arrays.toString(Sorted1));
9         System.out.println("Checking pivot element: "+Count);
10    }
11    static int[] CreateArr(){
12        Scanner sc=new Scanner(System.in);
13        System.out.println("Size of Arr?");
14        int N=sc.nextInt();
15        int[] Arr= new int[N];
16        for(int i=0;i<N;i++){
17            System.out.print("Enter "+(i+1)+"'th Element: ");
18            Arr[i]=sc.nextInt();
19        }
20        return Arr;
21    }
22    static int getPartitionIndex (int[] arr, int start, int end){
23        int pivot = arr[end];
24        int i = (start - 1);
25        for (int j = start; j <= end - 1; j++){
26            if (arr[j] < pivot){
27                i++;
28                int t = arr[i];
29                arr[i] = arr[j];
30                arr[j] = t;
31            }
32            else
33                Count++;
34        }
35        int temp = arr[i+1];
36        arr[i+1] = arr[end];
37        arr[end] = temp;
38        Count++;
39        return (i + 1);
40    }
41    static int[] myQuickSort(int[] Arr,int start, int end) {
42        if (start < end)
43        {
44            int p = getPartitionIndex(Arr, start, end);
45            myQuickSort(Arr, start, end: p - 1);
46            myQuickSort(Arr, start: p + 1, end);
47        }
48        return Arr;
49    }
50 }
```

## Output of Quick Sort:

Worst Case: Takes  $N^2$  Steps »  $O(N^2)$

```
- ↺ Size of Arr?  
⇩ 9  
🖨 Enter 1'th Element: 9  
🗑 Enter 2'th Element: 8  
Enter 3'th Element: 7  
Enter 4'th Element: 6  
Enter 5'th Element: 5  
Enter 6'th Element: 4  
Enter 7'th Element: 3  
Enter 8'th Element: 2  
Enter 9'th Element: 1  
Original Array1: [9, 8, 7, 6, 5, 4, 3, 2, 1]  
Sorted Arr is: [1, 2, 3, 4, 5, 6, 7, 8, 9]  
Checking pivot element: 28
```

Best Case: Takes  $N \times \log(N)$  Steps »  $O(N \times \log(N))$

```
- ↺ Size of Arr?  
⇩ 9  
🖨 Enter 1'th Element: 1  
🗑 Enter 2'th Element: 2  
Enter 3'th Element: 3  
Enter 4'th Element: 4  
Enter 5'th Element: 5  
Enter 6'th Element: 6  
Enter 7'th Element: 7  
Enter 8'th Element: 8  
Enter 9'th Element: 9  
Original Array1: [1, 2, 3, 4, 5, 6, 7, 8, 9]  
Sorted Arr is: [1, 2, 3, 4, 5, 6, 7, 8, 9]  
Checking pivot element: 8
```

Average Case:Takes  $N \times \log(N)$  Steps »  $O(N \times \log(N))$

```
- ↩ Size of Arr?  
⇩ 9  
🖨 Enter 1'th Element: 1  
🗑 Enter 2'th Element: 2  
Enter 3'th Element: 3  
Enter 4'th Element: 4  
Enter 5'th Element: 5  
Enter 6'th Element: 9  
Enter 7'th Element: 8  
Enter 8'th Element: 7  
Enter 9'th Element: 6  
Original Array1: [1, 2, 3, 4, 5, 9, 8, 7, 6]  
Sorted Arr is: [1, 2, 3, 4, 5, 6, 7, 8, 9]  
Checking pivot element: 11
```

## Code for Merge Sort:

```
QuickSort.java x MergeSort.java x
1  import java.util.Arrays;
2  import java.util.Scanner;
3
4  class MergeSort {
5      7 usages
6      static int Count;
7      public static void main(String[] args){
8          int[] arr = CreateArr();
9          System.out.println("Original Array: ");
10         System.out.println(Arrays.toString(arr));
11         myMergeSort(arr, l: 0, r: arr.length - 1);
12         System.out.println("Sorted Array: ");
13         System.out.println(Arrays.toString(arr));
14         System.out.println("Steps Required: "+Count);
15     }
16     //#####
17     1 usage
18     @ static int[] CreateArr(){
19         Scanner sc=new Scanner(System.in);
20         System.out.println("Size of Arr?");
21         int N=sc.nextInt();
22         int[] Arr= new int[N];
23         for(int i=0;i<N;i++){
24             System.out.print("Enter "+(i+1)+"'th Element: ");
25             Arr[i]=sc.nextInt();
26         }
27         return Arr;
28     }
29
30     static void merge(int[] arr, int l, int m, int r){
31         int n1=m-l+1;
32         int n2=r-m;
33         int[] L = new int[n1];
34         int[] R = new int[n2];
35         for(int i = 0; i < n1; ++i) {
36             L[i] = arr[l + i];
37             Count++;
38         }
39         for(int j = 0; j < n2; ++j) {
40             R[j] = arr[m + 1 + j];
41             Count++;
42         }
43         int i = 0;
44         int j = 0;
45         int k = l;
46         while (i < n1 && j < n2){
47             if (L[i] <= R[j]){
48                 arr[k] = L[i];
49                 i++;
50             }
51             else{
52                 arr[k] = R[j];
53                 j++;
54             }
55             k++;
56             Count++;
57         }
58     }
59 }
```

```

55         while (i < n1){
56             arr[k] = L[i];
57             i++;
58             k++;
59             Count++;
60         }
61         while (j < n2){
62             arr[k] = R[j];
63             j++;
64             k++;
65             Count++;
66         }
67     }
68     3 usages
69     static void myMergeSort(int[] arr, int l, int r){
70         if (l < r) {
71             int m = l + (r - l) / 2;
72             Count++;
73             myMergeSort(arr, l, m);
74             myMergeSort(arr, l: m + 1, r);
75             merge(arr, l, m, r);
76         }
77     }

```

## Output for Merge Sort:

Best Case:Takes  $N \log(N)$  Steps »  $O(N \log(N))$

```

Size of Arr?
6
Enter 1'th Element: 1
Enter 2'th Element: 2
Enter 3'th Element: 3
Enter 4'th Element: 4
Enter 5'th Element: 5
Enter 6'th Element: 6
Original Array:
[1, 2, 3, 4, 5, 6]
Sorted Array:
[1, 2, 3, 4, 5, 6]
Steps Required: 37

```

Average Case:Takes  $N \log(N)$  Steps »  $O(N \log(N))$

```

Size of Arr?
6
Enter 1'th Element: 3
Enter 2'th Element: 2
Enter 3'th Element: 5
Enter 4'th Element: 1
Enter 5'th Element: 4
Enter 6'th Element: 6
Original Array:
[3, 2, 5, 1, 4, 6]
Sorted Array:
[1, 2, 3, 4, 5, 6]
Steps Required: 37

```

Worst Case:Takes  $N \times \log(N)$  Steps  $\gg O(N \times \log(N))$

```
Size of Arr?  
6  
Enter 1'th Element: 6  
Enter 2'th Element: 5  
Enter 3'th Element: 4  
Enter 4'th Element: 3  
Enter 5'th Element: 2  
Enter 6'th Element: 1  
Original Array:  
[6, 5, 4, 3, 2, 1]  
Sorted Array:  
[1, 2, 3, 4, 5, 6]  
Steps Required: 37
```

### Analysis:

As we can see,  
in Quick sort, Worst case is  $O(N^2)$  and in Merge sort, it is  $O(N \times \log(N))$ .  
So for large number of unsorted inputs, Merge sort is better than Quick sort as  $(N^2 \gg N \times \log(N))$ ;

In Quick sort, the Best case is  $O(N \times \log(N))$ , same as Merge sort. So it doesn't affect.

In Quick sort, the Average case is  $O(N \times \log(N))$ , same as Merge sort. So it doesn't affect.

So, for small unsorted inputs, both performs well. But in case of large inputs, Merge sort is a better choice.