

# Algorithmic Human-Robot Interaction

---

Trajectory Optimization  
&  
Project Ideas

# Today: Trajectory Optimization & Project Brainstorming

Making Robots Move (how we want them to)

- Optimizing motion plans

Research Projects

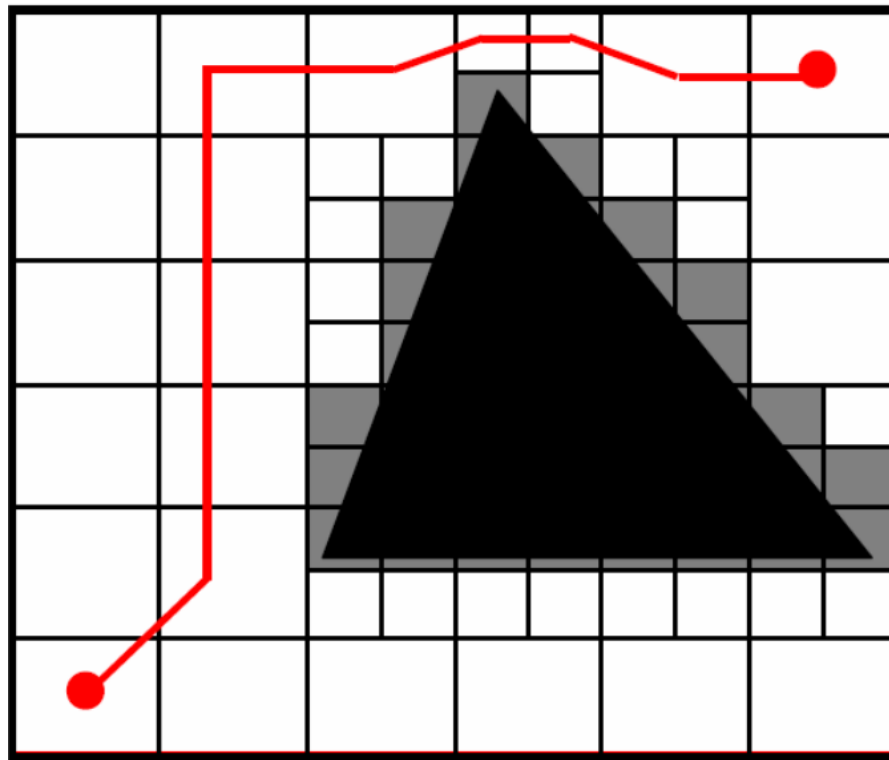
- Broad overview of open HRI problems not covered last time
- Rapid-fire Project Discussions

Last Time...

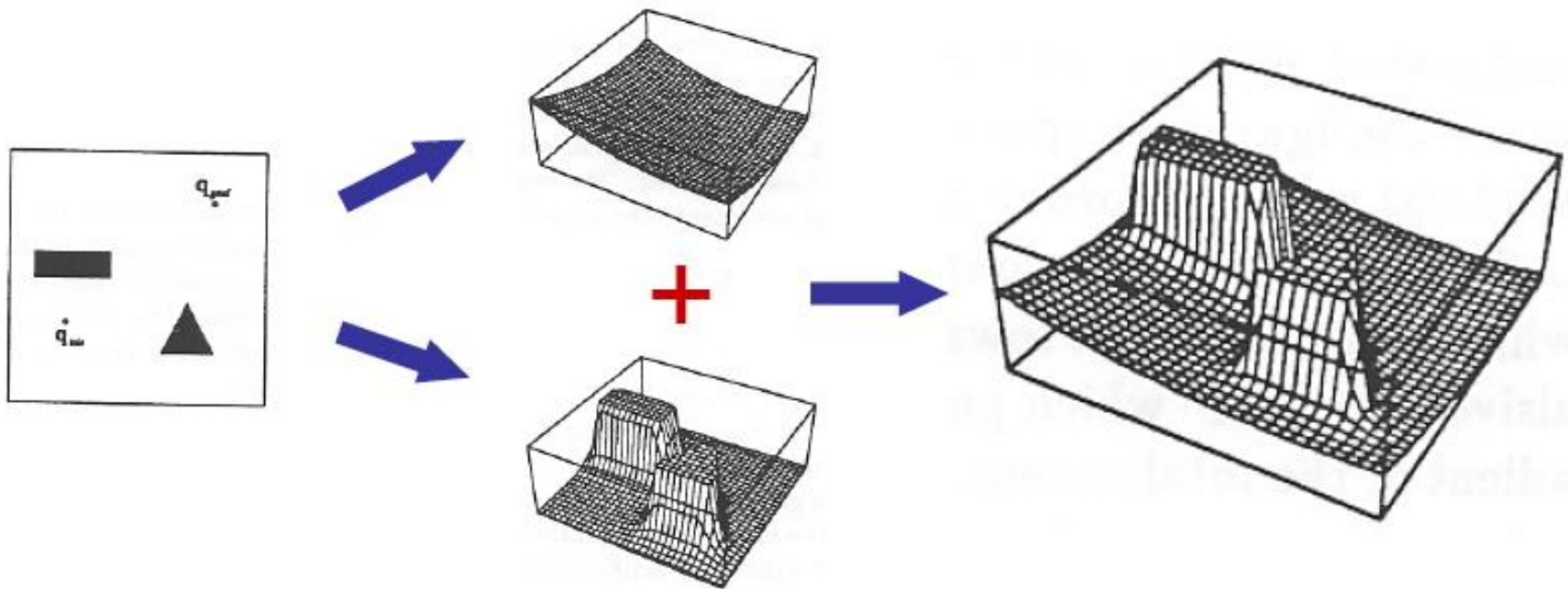
# Cell Decomposition

Not necessarily *complete*

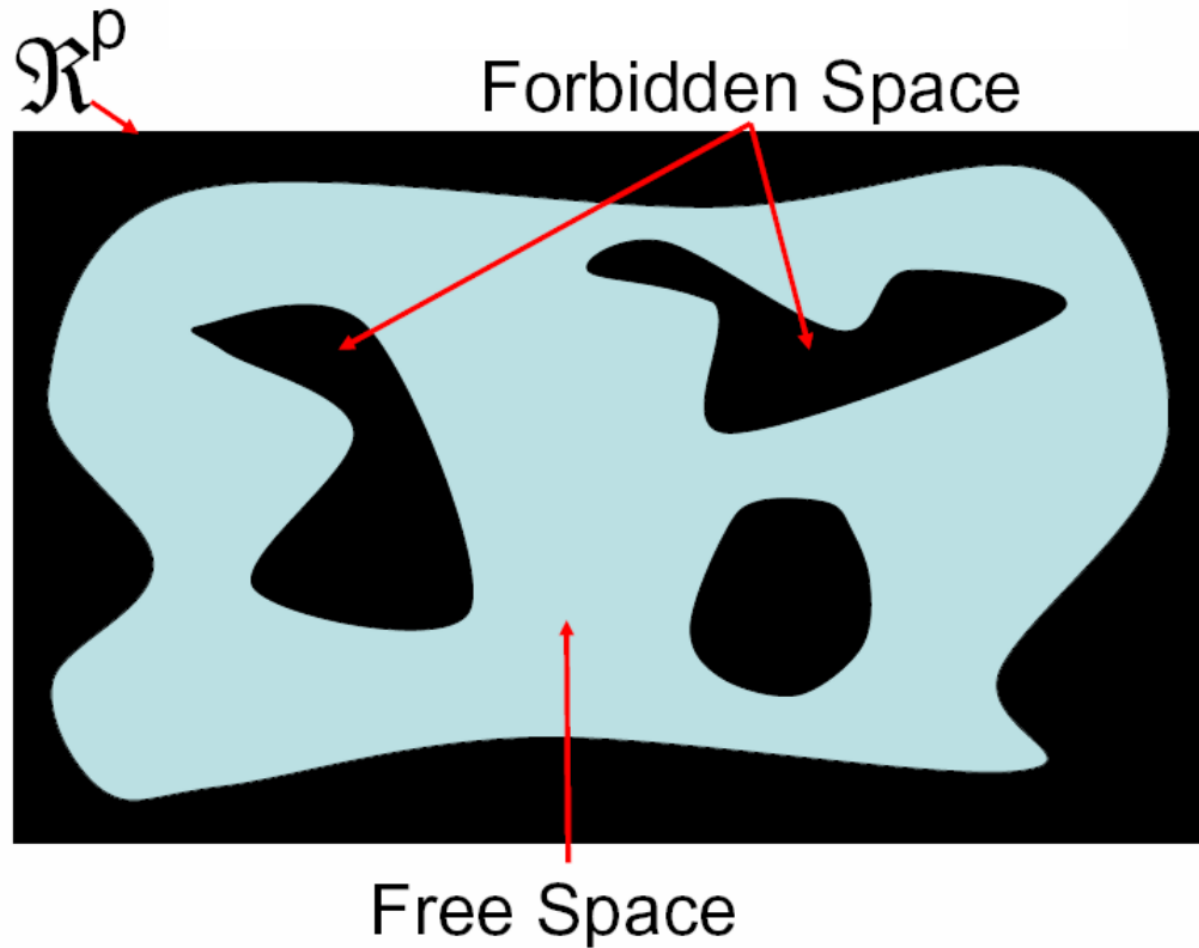
(Complete: If a solution exists, it will eventually be found)



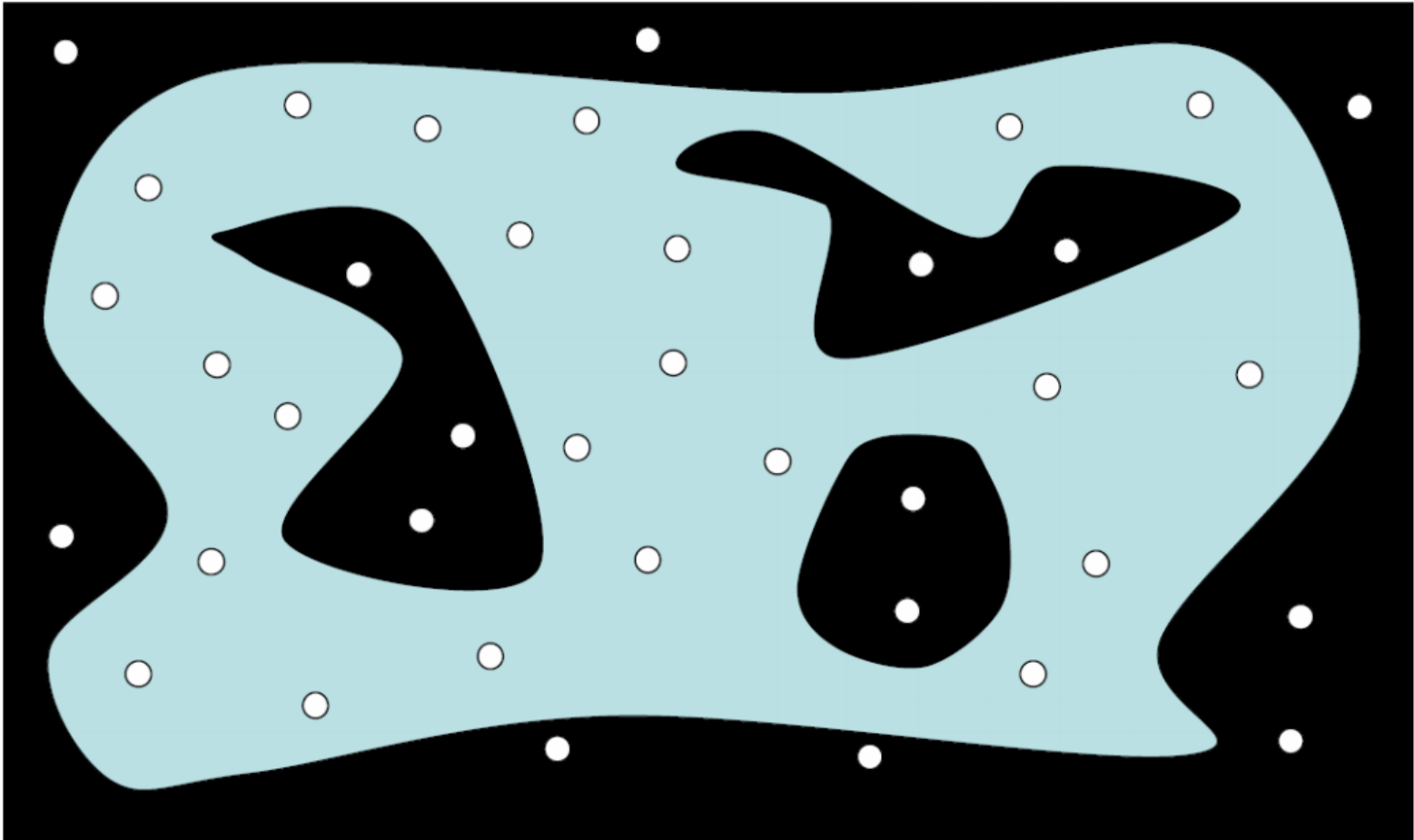
# How Does It Work?



# Probabilistic Road Map (PRM)

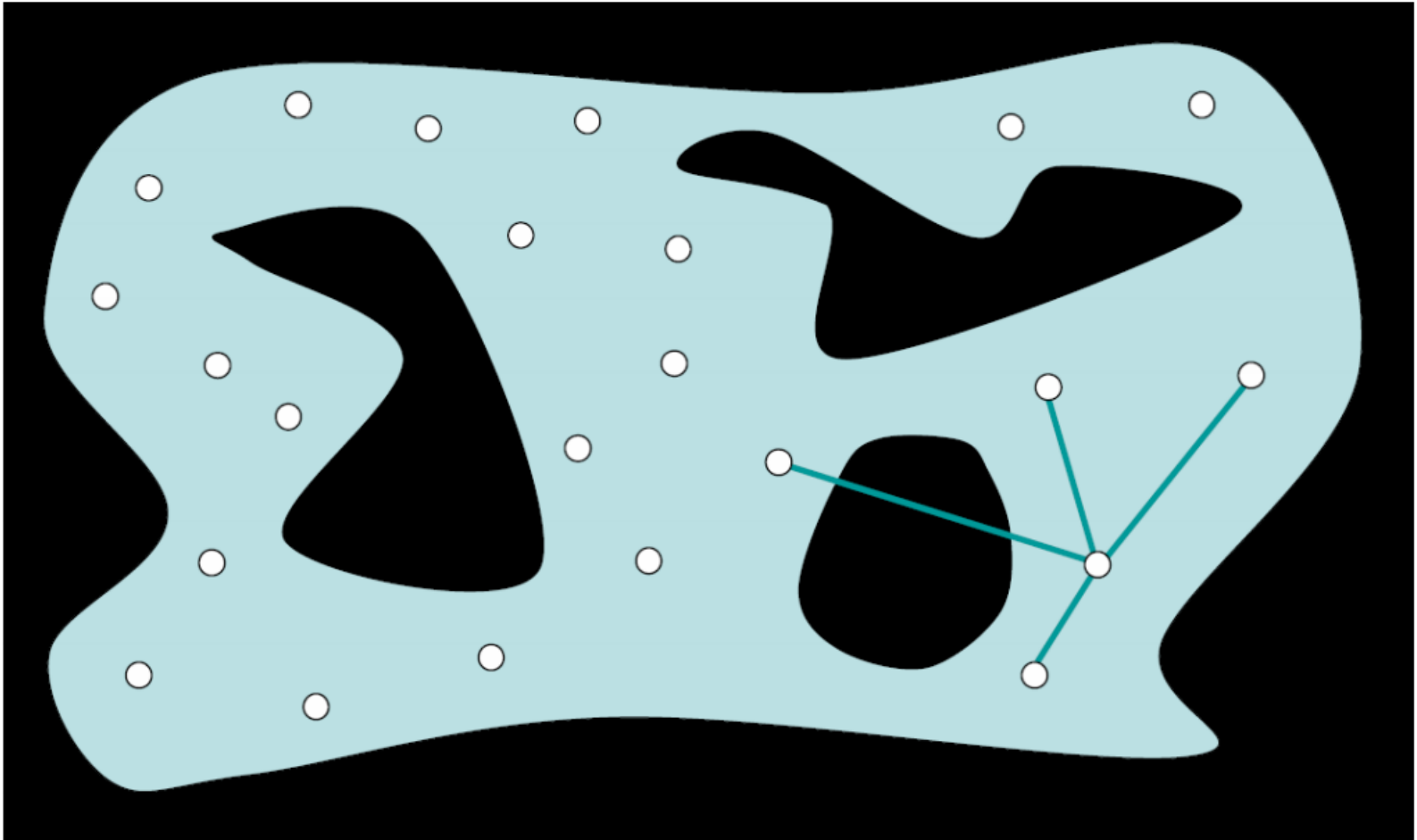


# Probabilistic Road Map (PRM)



Sample random locations!

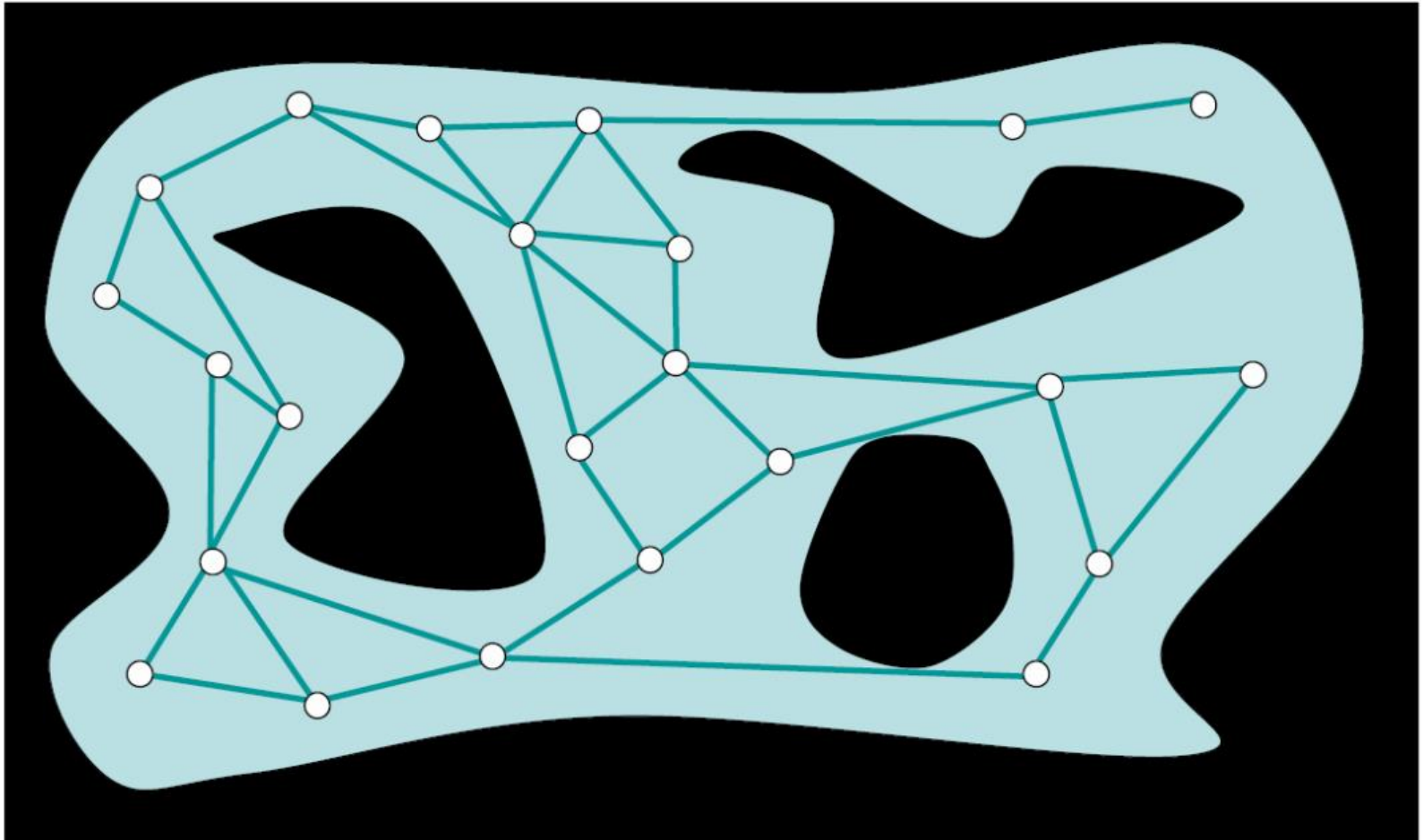
# Probabilistic Road Map (PRM)



Remove points in forbidden areas  
Link each point to its K nearest neighbors



# Probabilistic Road Map (PRM)



Remove edges crossing forbidden areas

# Rapidly-exploring Random Trees

## Algorithm BuildRRT

Input: Initial configuration  $q_{init}$ , number of vertices in RRT  $K$ , incremental distance  $\Delta q$

Output: RRT graph  $G$

$G.init(q_{init})$

**for**  $k = 1$  **to**  $K$

$q_{rand} \leftarrow \text{RAND\_CONF}()$

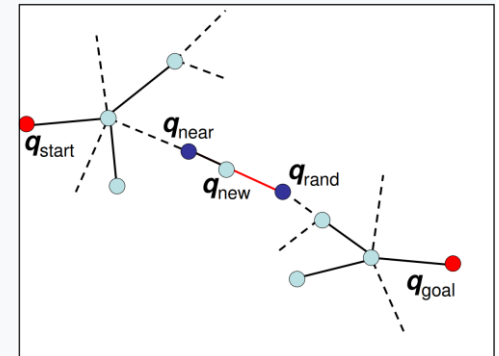
$q_{near} \leftarrow \text{NEAREST\_VERTEX}(q_{rand}, G)$

$q_{new} \leftarrow \text{NEW\_CONF}(q_{near}, q_{rand}, \Delta q)$

$G.add\_vertex(q_{new})$

$G.add\_edge(q_{near}, q_{new})$

**return**  $G$



# RRT: Limitations

- RRT fails to converge to optimal solutions
  - Early solutions end up constraining the search
- RRT\* guarantees asymptotic optimality (convergence to optimal solutions)
- RRT and RRT\* require the same (asymptotic) computational resources

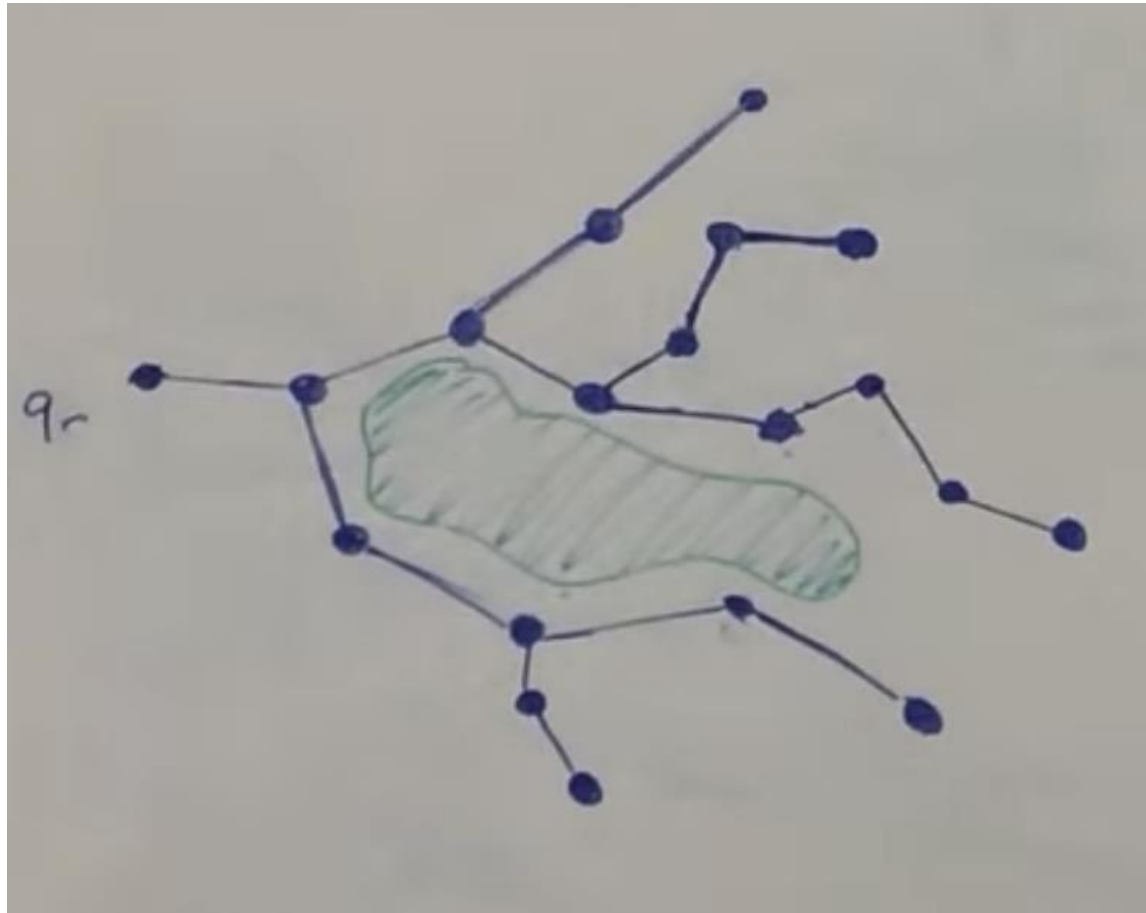
**RRT**



**RRT\***

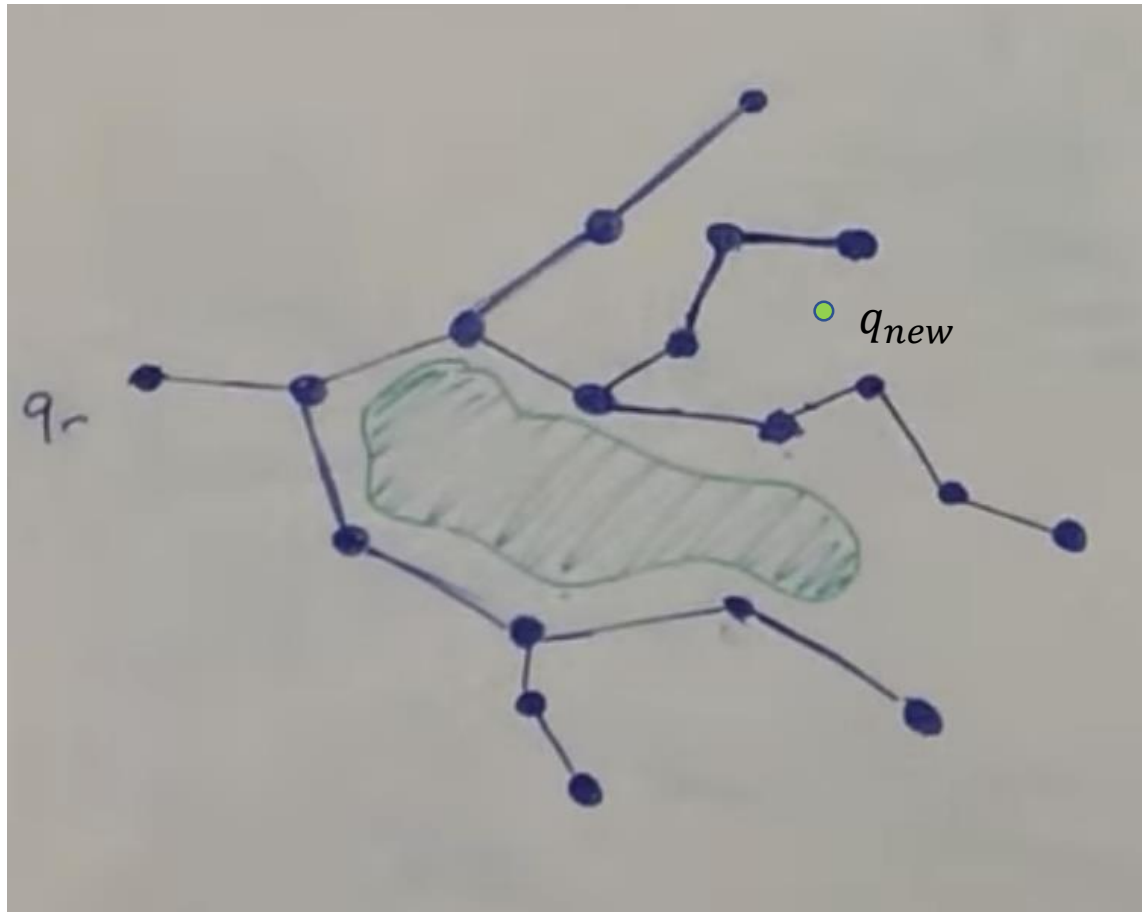


# RRT\*



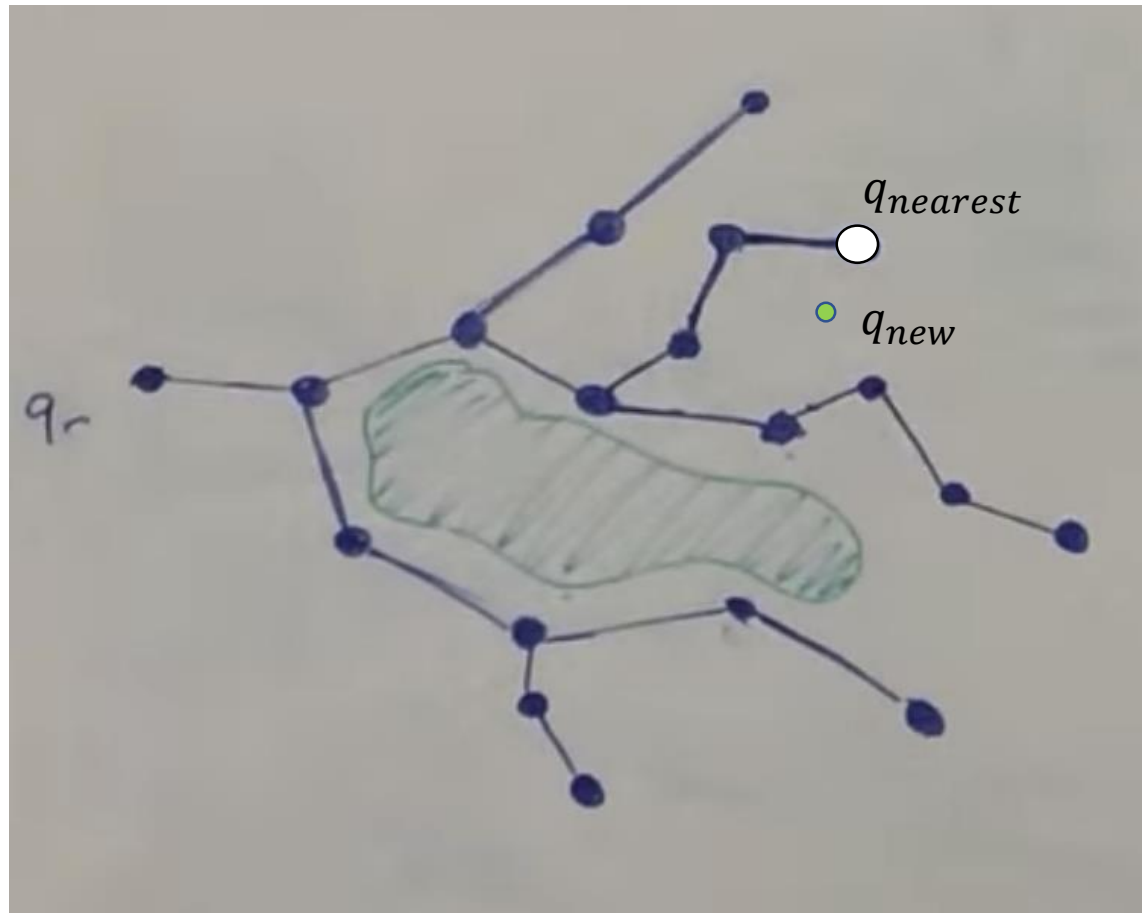
<https://www.youtube.com/watch?v=JM7kmWE8Gtc>

# RRT\*: Sample



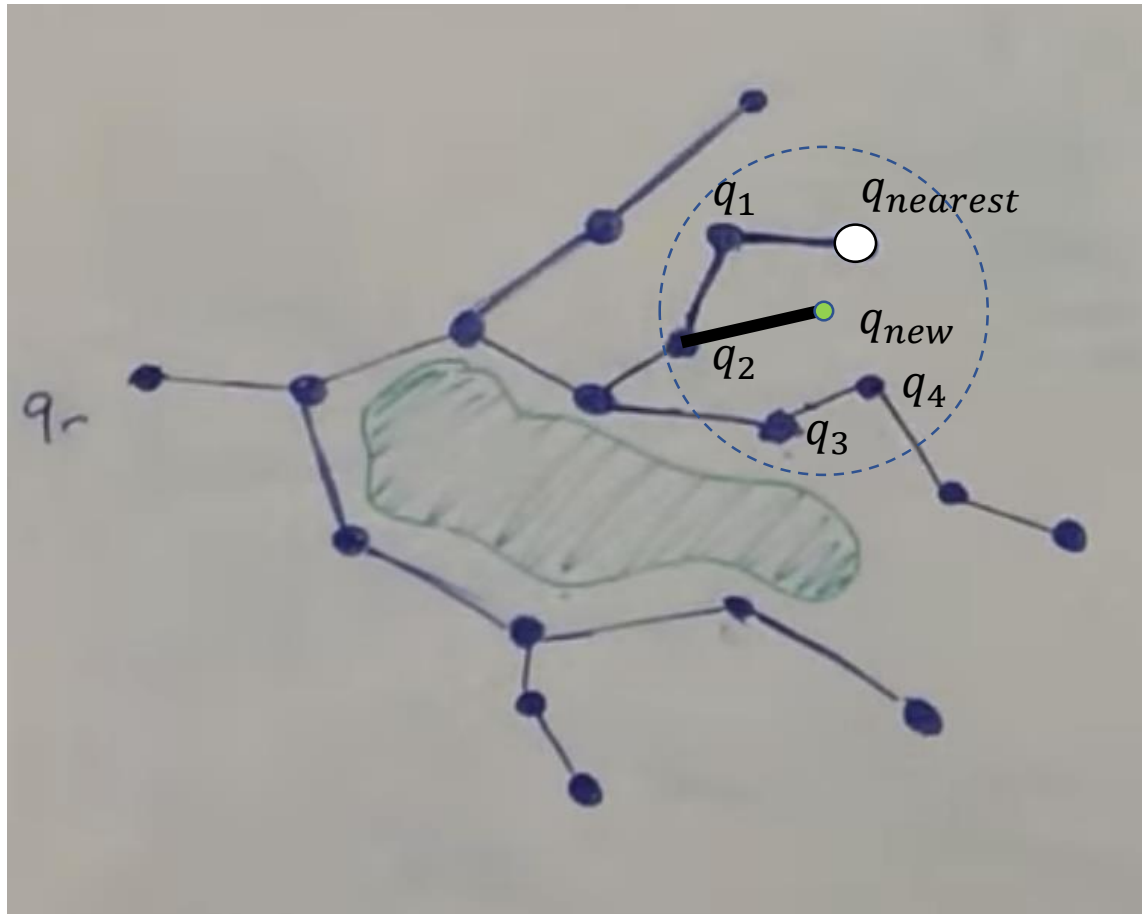
<https://www.youtube.com/watch?v=JM7kmWE8Gtc>

# RRT\*

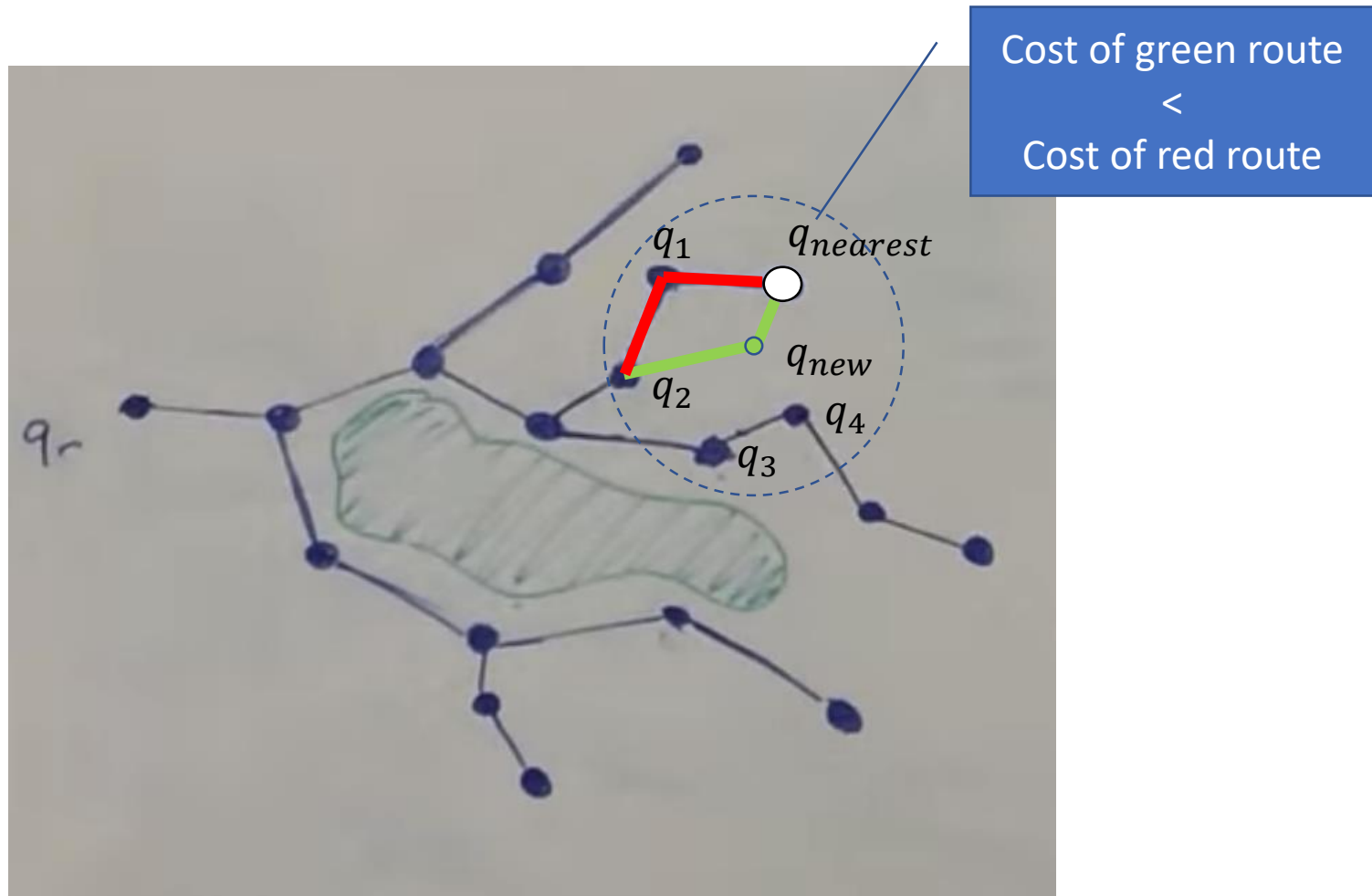


<https://www.youtube.com/watch?v=JM7kmWE8Gtc>

# RRT\*: Connect cheapest path

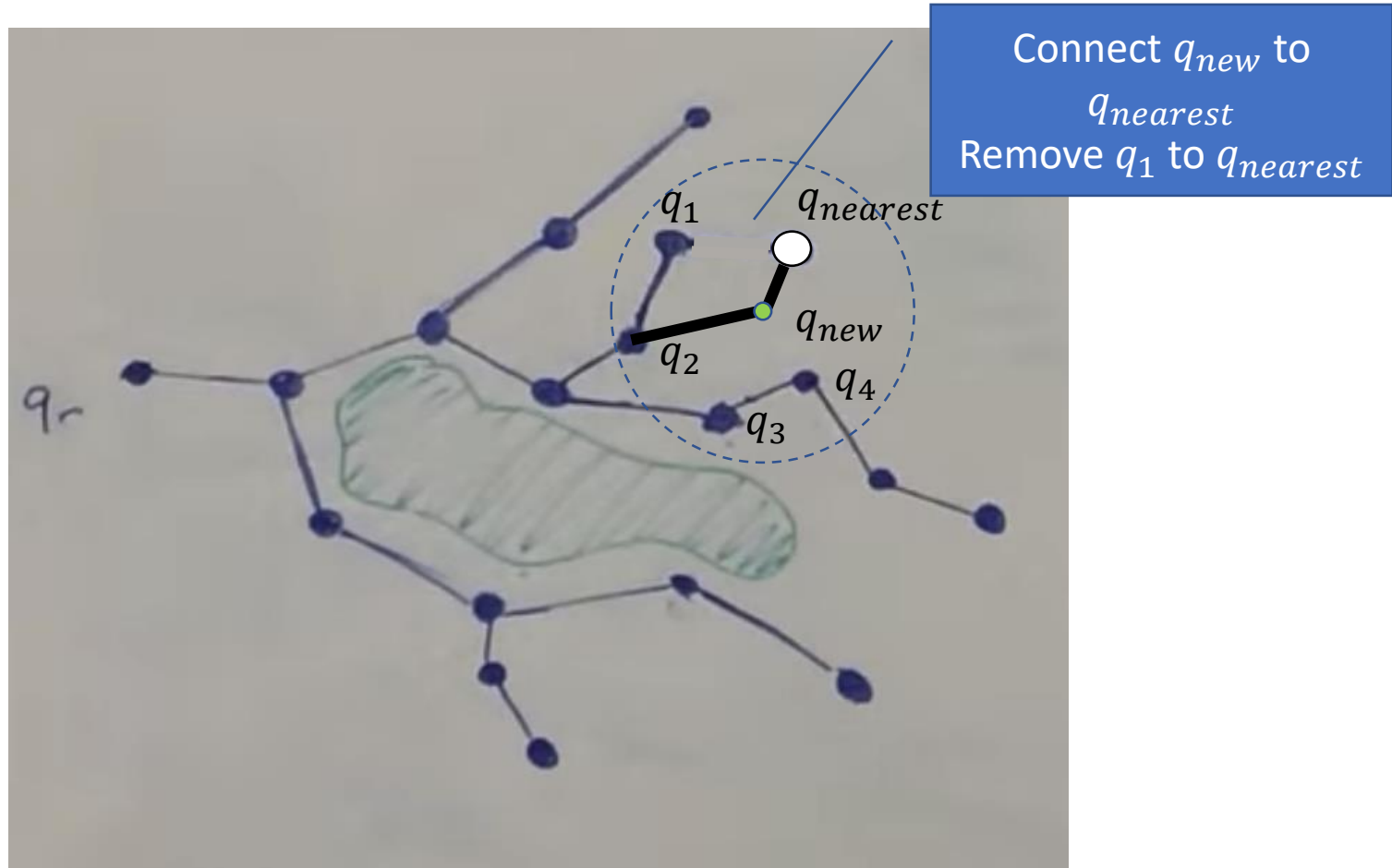


# RRT\*: Re-wire Graph

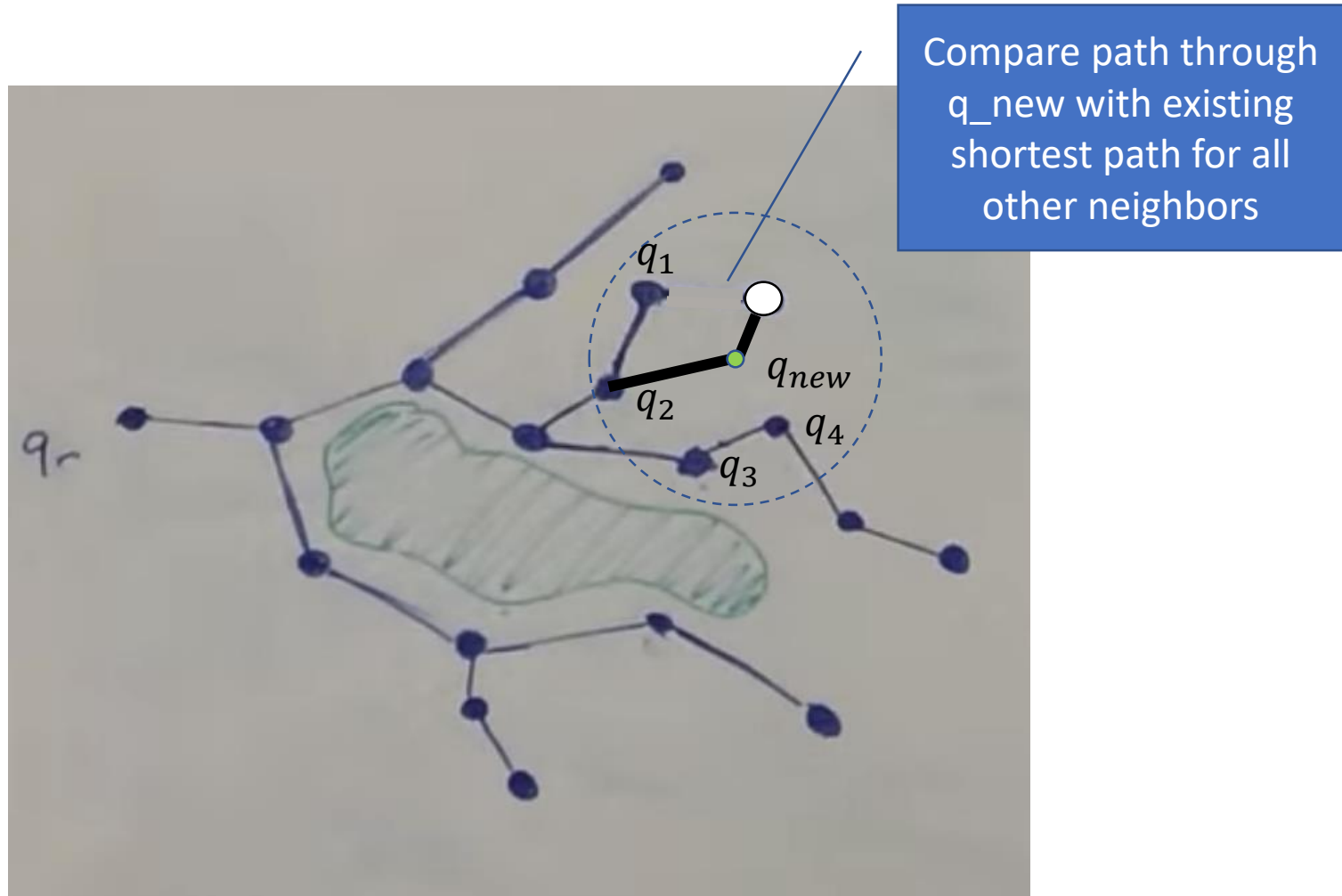




# RRT\*: Re-wire Graph



# RRT\*: Re-wire Graph

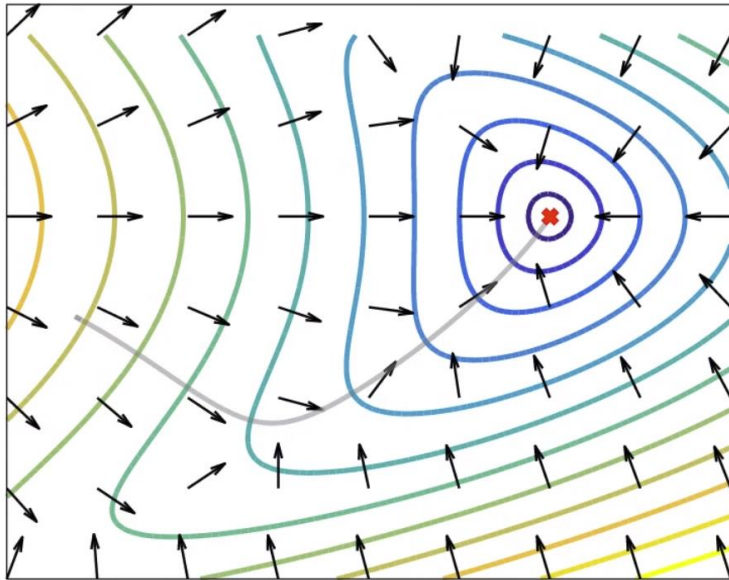


Today

# Optimal Control

**Optimal Control:** Finding the best control policy for a desired goal

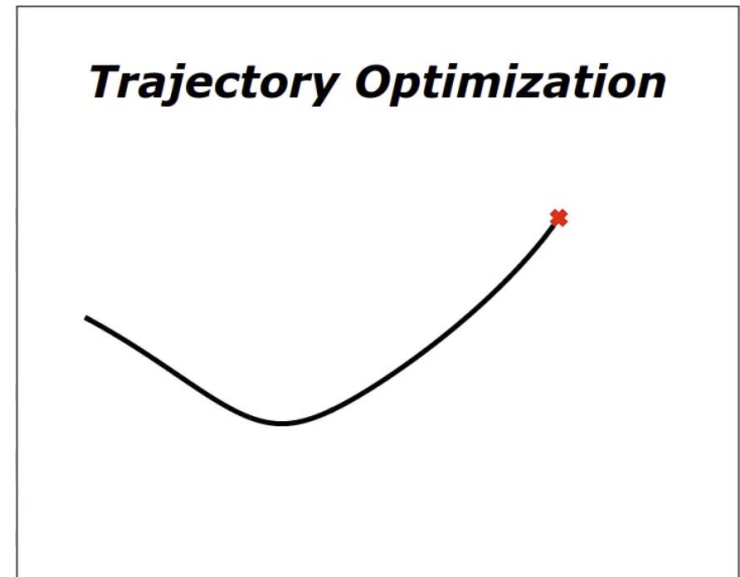
## Closed-Loop Solutions



$$u = u(x)$$

“Global Method”: Gives action at all states  
Very expensive to compute

## Open-Loop Solution



$$u = u(t)$$

“Local Method”: Gives action at relevant states  
Usable in high dimensions

# Trajectory Optimization:

## Problem Statement

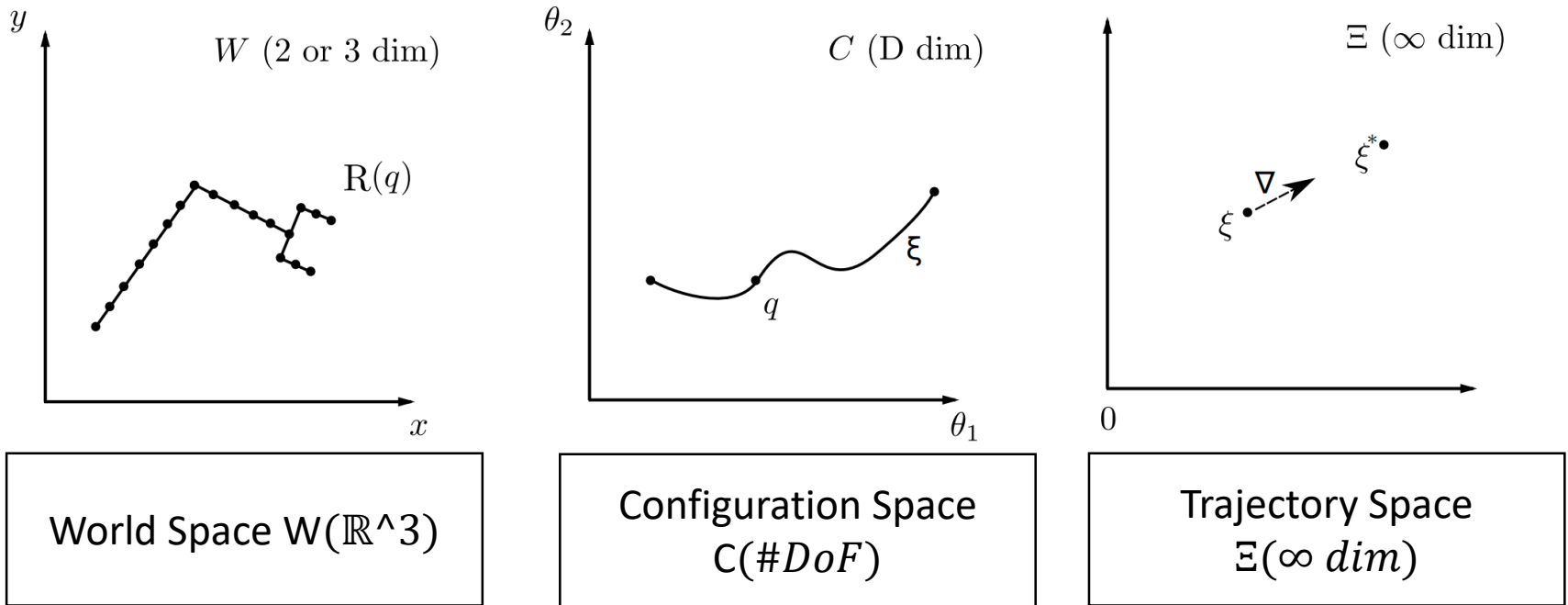
- Trajectory  $\xi: t \in [0, T] \rightarrow \mathcal{C}$  *Maps time to configurations*
- Objective Functional  $U: \mathcal{E} \rightarrow \mathbb{R}^+$  *Maps trajectories to scalars*
- The objective  $U$  encodes traits we want our path to have
  - Path length
  - Efficiency
  - Obstacle avoidance
  - Legibility
  - Uncertainty reduction
  - Human comfort



Set of possible  
trajectories

**Goal:** Leverage the benefits of randomized sampling with asymptotic optimality

# Problem Specification: Spaces



Robot pose in World Space (set of points)



Single point in Configuration Space

Trajectory through Configuration Space (set of points)



Single point in Trajectory Space

# Problem Specification: Optimization

*Trajectory Optimization* seeks to find an optimal trajectory  $\xi^*$ :

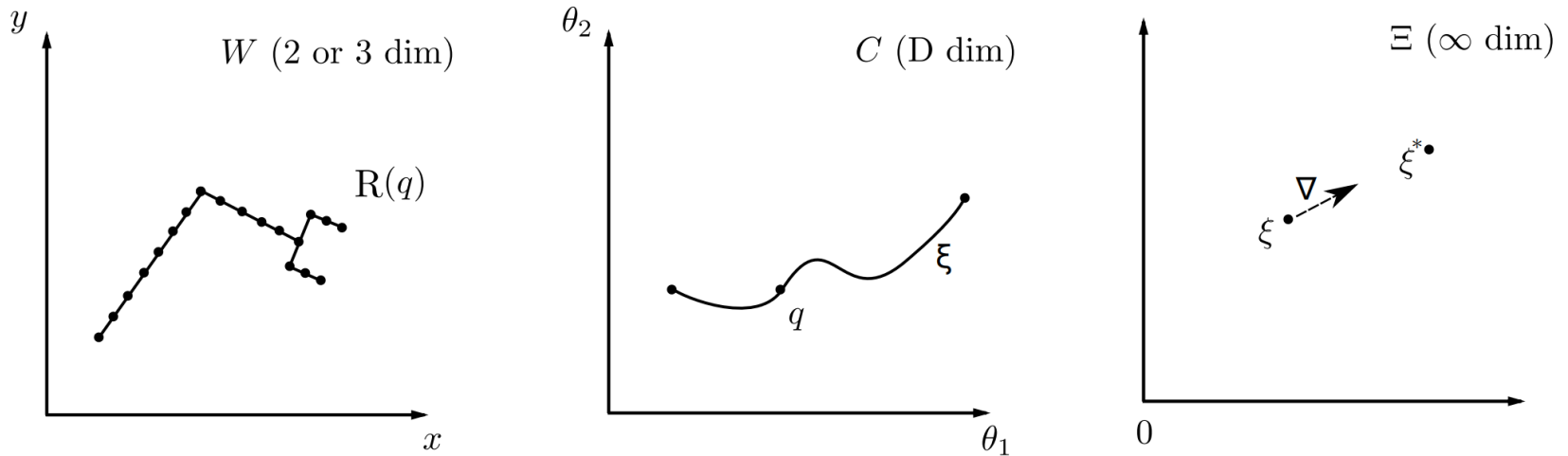
$$\xi^* = \operatorname{argmin}_{\{\xi \in \Xi\}} U[\xi]$$

$$\text{s.t.} \quad \xi(0) = q_s$$

$$\xi(T) = q_g$$

...(any other constraints we want)

# Problem Specification: Optimization



Want to optimize  $\xi$  to a global minimum of our objective  $U$

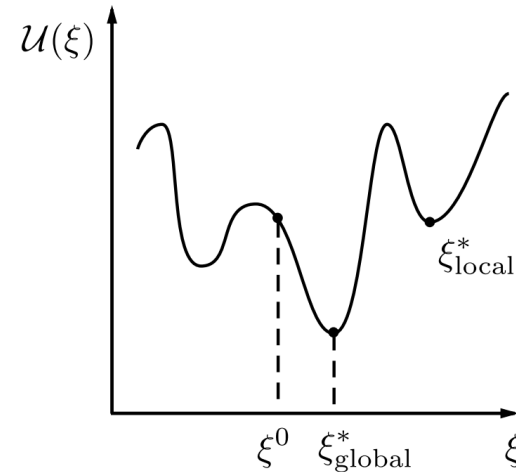
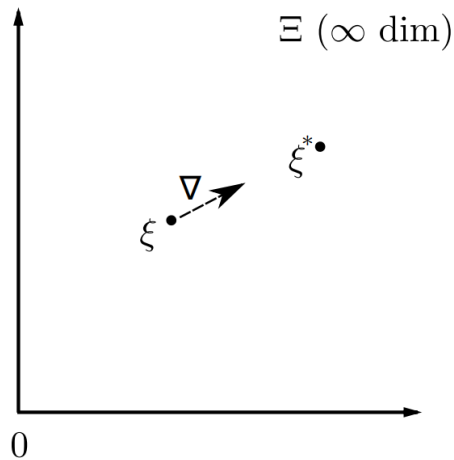
**=> Usually too hard!**

Instead, optimize  $\xi$  to a local minimum of our objective  $U$

**=> If the solution is bad, resample  $\xi$  and try again**



# Problem Specification: Optimization



**Gradient Descent** is a popular technique for finding local minima

Points in the direction of greatest ascent for  $\xi$

$$\xi_{t+1} = \xi_t - \frac{1}{\alpha} \nabla_{\xi} U(\xi_t)$$

# Functional Gradient Descent

To compute the derivatives of a functional, some trickery is required:

$\Xi$  is a Hilbert space with Euclidean inner product

$$U[\xi] = \int_0^T F(t, \xi(t), \xi'(t)) dt$$

$$\nabla_{\xi} U(t) = \frac{\delta F}{\delta \xi(t)}(t) - \frac{d}{dt} \frac{\delta F}{\delta \xi'(t)}(t)$$

$$\nabla_{\xi} U(t) \in \Xi$$

# Functional Gradient Descent

Example: Cost function to minimize magnitude of velocity

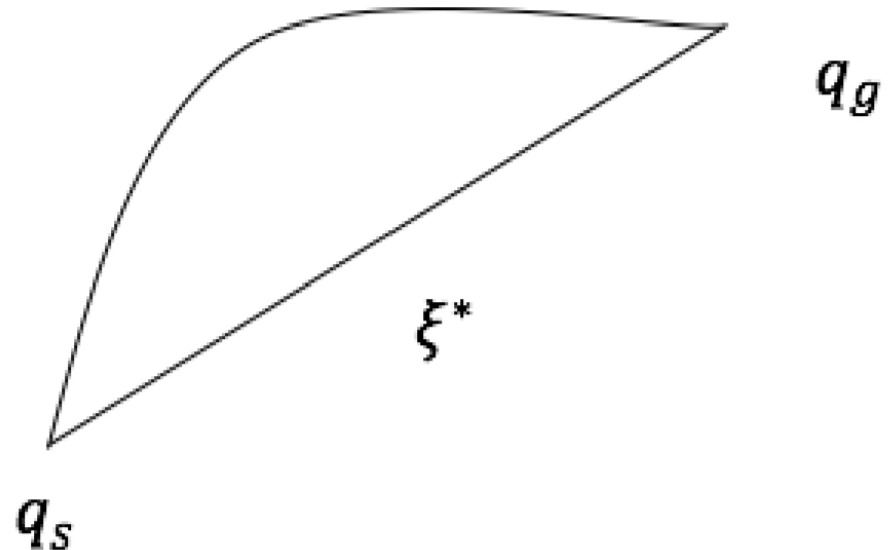
$$\text{Given } U[\xi] = \frac{1}{2} \int_0^T \|\xi'(t)\|^2 dt$$

An optimal trajectory will have the following properties:

**Shape:** Linear.

(Traveling less distance will require less velocity over the time interval.)

**Timing:** Constant velocity



# Making Trajectory Optimization Useful

Need to provide a good choice for  $U[\xi]$ .

## CHOMP: Covariant Hamiltonian Optimization for Motion Planning

Uses a cost function  $U[\xi] = U_{smooth}[\xi] + \lambda U_{obs}[\xi]$

Smoothness cost:  $U_{smooth}[\xi] = \frac{1}{2} \int_0^T ||\xi'(t)||^2 dt$

Obstacle cost:  $U_{obs}[\xi] = \int_t \int_u c(\phi_u(\xi(t))) * \left\| \frac{d}{dt} \phi_u(\xi(t)) \right\| du dt$

Cost function that  
computes distance to  
closest obstacle

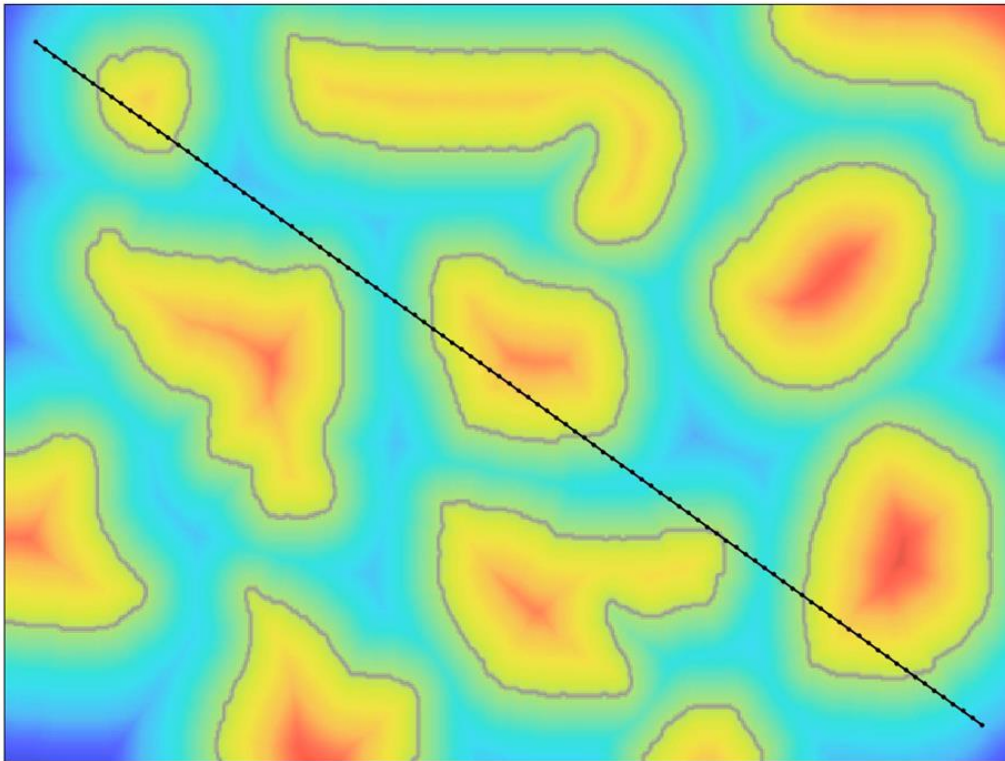
Forward Kinematics  
function that computes  
location of robot body  
point  $u$  at time  $t$  in  $\xi$

Norm of the velocity  
for body point  $u$  at  
time  $t$  in  $\xi$

# Making Trajectory Optimization Useful

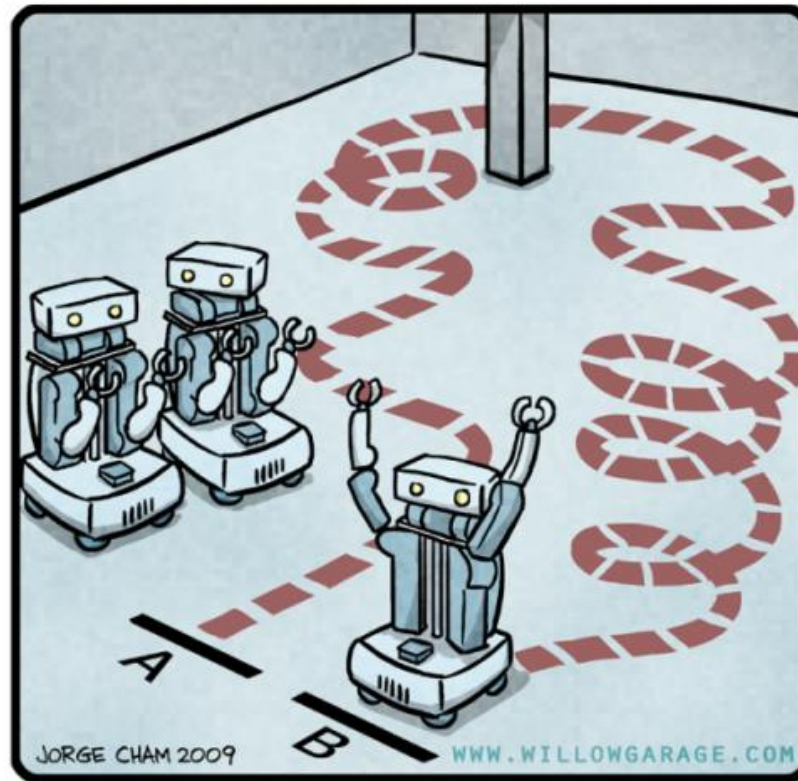
CHOMP: Covariant Hamiltonian Optimization for Motion Planning

Uses a cost function  $U[\xi] = U_{smooth}[\xi] + \lambda U_{obs}[\xi]$



# A-HRI: More Open Problems

R.O.B.O.T. Comics



"HIS PATH-PLANNING MAY BE  
SUB-OPTIMAL, BUT IT'S GOT FLAIR."

# Robots Asking for Help

## Asking for Help Using Inverse Semantics

Stefanie Tellex, Ross A. Knepper

Adrian Li, Thomas M. Howard, Daniela Rus, Nicholas Roy

Supported in part by the Boeing Company, and in part by the U.S Army Research Laboratory under the Robotics Collaborative Technology Alliance.



# Learning by Demonstration

## Learning Robot Objectives from Physical Human Interaction

Andrea Bajcsy\*, Dylan P. Losey\*,  
Marcia K. O'Malley, and Anca D. Dragan





# Parsing Natural Language Instruction



# Reviewing Papers

# Be Compassionate

A silhouette of a woman with long hair and a dog, possibly a Weimaraner, standing in a field at sunset. The woman is on the right, looking down at her hand, and the dog is on the left, looking up at her. The background is a warm, orange glow from the setting sun.

Invert your position and ask yourself how you'd feel if you received your review. If it makes your blood boil, take a break, and revise your review.

# Be Constructive

Every paper has a best paper award hidden in it. Your role is to guide the author to reveal it.





# Be Scholarly

- Cite your sources
- Don't make claims unsubstantiated by evidence  
("I do not feel this is true": Back it up!)
- Do not hawk your viewpoint
- No ad hominem attacks

# Re-Express

You should attempt to re-express  
your target's position so clearly,  
vividly, and fairly that your target says,

“Thanks, I wish I'd thought of putting  
it that way.”

-Daniel Dennett

# Summary

- Re-express target's position clearly, vividly, and fairly
- List any points of agreements
- Mention anything you have learned from the target
- Professionally introduce rebuttal or critique



# Presenting Papers

- Identify key insights
- Identify corner cases
- Identify scaling issues
- Identify unrealistic application constraints
- Avoid being procedural



# Presenting a Paper

1. Bigger picture
2. Motivation
3. Problem Statement
4. Why is this hard
5. Key insight
6. Details
7. Results
8. Broader picture
9. Restate the key insight that addressed the problem

# Papers for Thursday 1/31:

Need 1 PRO (10m) and 1 CON (5m) speaker each

E-mail [Bradley.Hayes@Colorado.edu](mailto:Bradley.Hayes@Colorado.edu) to sign up

## Trajectories and Keyframes for Kinesthetic Teaching: A Human-Robot Interaction Perspective

Baris Akgun et al.

## Planning human-aware motions using a sampling-based costmap planner

Jim Mainprice et al.

# Project Brainstorming!

# Platforms



KINOVA

MOVO<sup>BETA</sup>

A MOBILE  
MANIPULATOR  
PLATFORM

[kinovaMOVO.com](http://kinovaMOVO.com)



# Project Brainstorming

**Form small groups**

A few minutes per topic:

Discuss a capability or system and application scenario that would address the topic

Write down your ideas (brief summaries please)

# Project Brainstorming

Projects can involve either

building an autonomous system

or

testing some aspect of a hypothetical  
autonomous system



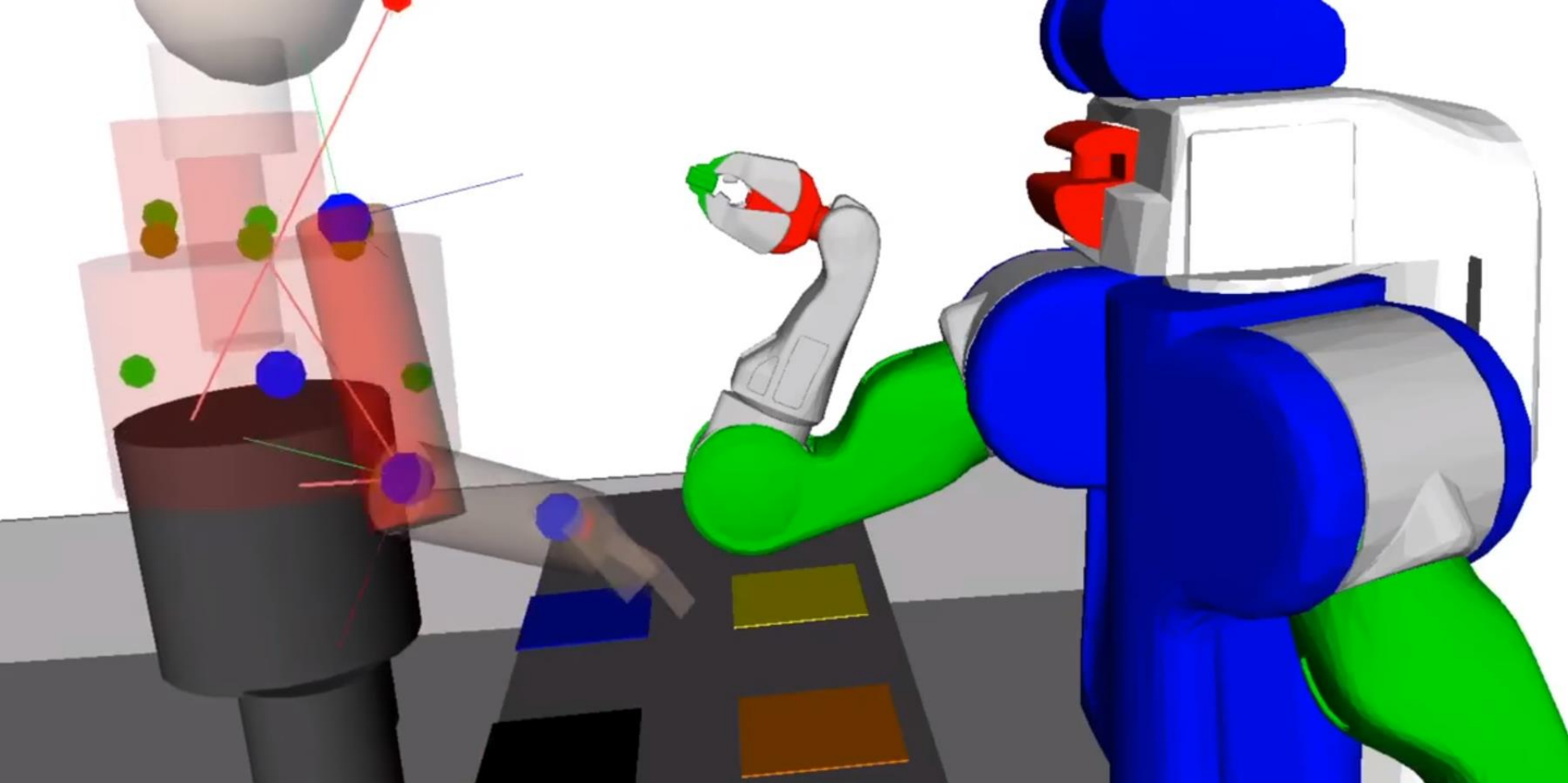
				3		1	3		2
	2	3	3	3	7	4	3	6	2
3									
2									
6									
3									
1									
7									
3									
3									
3									
2									

# Topic: Personalized Robot Tutoring

---

- Language Learning
- Training for Manufacturing (IKEA)
- Nonograms / Games
- Etc.





# Safe Human-Aware Motion Planning

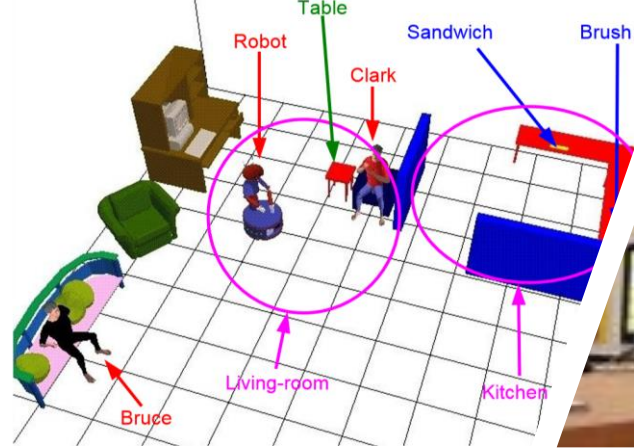
Topic:

Safety systems for mixed human-robot environments

Visualizations for communicating intent

Motion planning cost functions incorporating human activity





## Topic: Reducing Human's Uncertainty During Collaboration

Modeling which objects in scene the human is likely to (not) know the locations of  
Communicating the robot's plan through pantomime or speech

