



University of Colorado
Boulder

Human-Robot Interaction

Choosing a Test, Contingency Analysis, & Correlations

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Choosing a Statistical Test

Things to consider

What do you want to do?

- Look for differences between conditions (i.e., test hypotheses)

- Compare frequency (counts)

- Correlate variables

- Reduce data

Things to consider

How many factors and levels (conditions)

How many dependent variables

What type of variables are they?

E.g., nominal, ordinal, ratio, etc.

Things to consider

Paired or unpaired data?

Independent samples – *unpaired*

Used in most controlled laboratory experiments

Dependent samples – *paired*

Used in observational studies, field experiments, in the presence of confounding factors, etc.

Example:

Unpaired data: weight loss between two populations, one given new drug and the other given a placebo

Paired data: Weight before and after drug in one population

Paired or Matched Data

Variable	Test
Nominal	McNemar's Test
Ordinal (ordered categories)	Wilcoxon
Quantitative (discrete or non-normal)	Wilcoxon
Quantitative (normal)	Paired t-test

Some Summaries

www.maths.dur.ac.uk/mathlab/resources/whichtest.html

Choosing a statistical test				
What do you want to do?	Number of variables and conditions	Design	Parametric / Nonparametric	Statistical Test
Look for differences between conditions	One independent variable: two conditions. One dependent variable	Independent measures (unrelated)	Parametric	Independent <i>t</i> test
		Independent measures (unrelated)	Nonparametric	Mann–Whitney <i>U</i> test
		Repeated measures (related)	Parametric	Related <i>t</i> test
		Repeated measures (related)	Nonparametric	Wilcoxon signed-ranks test
	One independent variable: more than two conditions. One dependent variable	Independent measures	Parametric	One factor independent measures ANOVA
		Independent measures	Nonparametric	Kruskal–Wallis test
		Repeated measures	Parametric	One factor repeated measures ANOVA
		Repeated measures	Nonparametric	Friedman test
	Two independent variables. One dependent variable	Independent measures on both variables	Parametric	Two factor independent measures ANOVA
		Repeated measures on both variables	Parametric	Two factor repeated measures ANOVA
		One independent measures factor and one repeated measures factor	Parametric	Two factor mixed design ANOVA
	One independent variable. More than one dependent variable	Independent measures. Multivariate design	Parametric	One factor independent measures MANOVA
Compare frequency counts (in categories)	One or more variables	Association	Nonparametric	Chi-square test
Correlate variables	Two variables	Correlational	Parametric	Pearson's <i>r</i>
	Two variables	Correlational	Nonparametric	Spearman's <i>r</i>
	More than two variables	Correlational	Parametric	Multiple correlation
Reduce data	Many variables	Correlational	Parametric	Factor analysis

Summary Table of Statistical Tests

Level of Measurement	Sample Characteristics					Correlation	
	1 Sample	2 Sample		K Sample (i.e., >2)			
		Independent	Dependent	Independent	Dependent		
Categorical or Nominal	X ² or bi-nomial	X ²	Macnarmar's X ²	X ²	Cochran's Q		
Rank or Ordinal		Mann Whitney U	Wilcoxin Matched Pairs Signed Ranks	Kruskal Wallis H	Friedman's ANOVA	Spearman's rho	
Parametric (Interval & Ratio)	z test or t test	t test between groups	t test within groups	1 way ANOVA between groups	1 way ANOVA (within or repeated measure)	Pearson's r	
		Factorial (2 way) ANOVA					

(Plonskey, 2001)

Output Variable

Input Variable

	Nominal	Categorical (>2 categories)	Ordinal	Quantitative Discrete	Quantitative Non-Normal	Quantitative Normal
Nominal	χ^2 or Fisher's	χ^2	χ^2 trend or Mann-Whitney	Mann-Whitney	Mann-Whitney or log-rank (a)	Student's t-test
Categorical (>2 categories)	χ^2	χ^2	Kruskal-Wallis (b)	Kruskal-Wallis (b)	Kruskal-Wallis (b)	Analysis of variance (c)
Ordinal	χ^2 trend or Mann-Whitney	(e)	Spearman rank	Spearman rank	Spearman rank	Spearman rank or linear regression (d)
Quantitative Discrete	Logistic regression	(e)	(e)	Spearman rank	Spearman rank	Spearman rank or linear regression (d)
Quantitative Non-Normal	Logistic regression	(e)	(e)	(e)	Plot data and Pearson or Spearman rank	Plot data and Pearson or Spearman rank and linear regression
Quantitative Normal	Logistic regression	(e)	(e)	(e)	Linear regression (d)	Pearson and linear regression

Contingency Analysis

Comparing Frequencies (counts)

Example

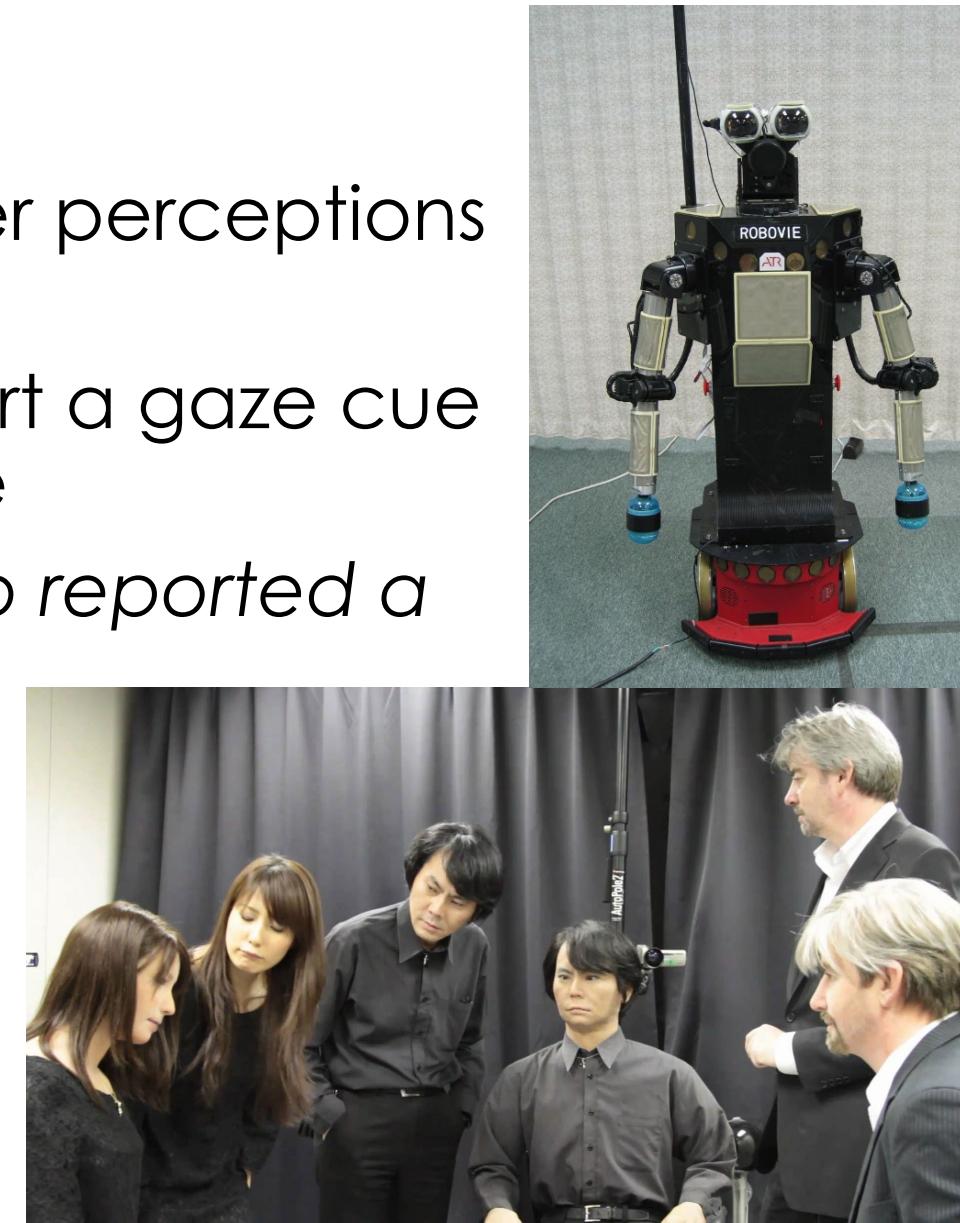
RQ: Does robot morphology affect user perceptions of gaze cues?

Measure: number of people who report a gaze cue from a Gemenoid and from a Robovie

Question: *is the number of people who reported a gaze cue different when the cue comes from a Gemenoid or Robovie?*

What are my IVs, DVs, factors, and levels?

What type of variables are they?



Contingency Table

Displays the multivariate frequency distributions of variables in a matrix format

Also called “cross-tabulation”

	Reported Gaze Cue	Did Not Report Gaze Cue	<i>Totals</i>
Geminoid	10	4	14
Robovie	3	11	14
<i>Totals</i>	13	15	28

Output Variable

Input Variable

	Nominal Categorical (>2 categories)	Ordinal	Quantitative Discrete	Quantitative Non-Normal	Quantitative Normal	
Nominal	X² or Fisher's	X²	X² trend or Mann-Whitney	Mann-Whitney	Mann-Whitney or log-rank (a)	Student's t-test
Categorical (>2 categories)	X²	X²	Kruskal-Wallis (b)	Kruskal-Wallis (b)	Kruskal-Wallis (b)	Analysis of variance (c)
Ordinal	X² trend or Mann-Whitney	(e)	Spearman rank	Spearman rank	Spearman rank	Spearman rank or linear regression (d)
Quantitative Discrete	Logistic regression	(e)	(e)	Spearman rank	Spearman rank	Spearman rank or linear regression (d)
Quantitative Non-Normal	Logistic regression	(e)	(e)	(e)	Plot data and Pearson or Spearman rank	Plot data and Pearson or Spearman rank and linear regression
Quantitative Normal	Logistic regression	(e)	(e)	(e)	Linear regression (d)	Pearson and linear regression

IV: Categorical | DV: Categorical

Compare the frequency distributions across categorical variables

Pearson's Chi-squared Test

$$\chi^2 = \sum_{i=1}^n \frac{(O_i - E_i)^2}{E_i}$$

Number of cells in table

Observed Frequency

Pearson's Test Statistic

Expected Frequency

The diagram illustrates the formula for Pearson's Chi-squared Test statistic. It shows the summation symbol with a superscript n and a subscript i=1. Three arrows point to different parts of the formula: one arrow points from 'Number of cells in table' to the summation symbol; another arrow points from 'Observed Frequency' to the term O_i; and a third arrow points from 'Expected Frequency' to the term E_i.

Pearson's Chi-squared Test

To calculate expected values:
 $(\text{RowTotal} * \text{ColTotal}) / \text{GridTotal}$

	Reported Gaze Cue	Did Not Report Gaze Cue	Totals
Geminoid	10 ($14 * 13 / 29 = 6.28$)	4 (7.72)	14
Robovie	3 (6.72)	12 (8.28)	15
Totals	13	16	29

Pearson's Chi-squared Test

$$\chi^2 = \sum_{i=1}^n \frac{(O_i - E_i)^2}{E_i} = \frac{(10 - 6.28)^2}{6.28} + \frac{(3 - 6.72)^2}{6.72} + \frac{(4 - 7.72)^2}{7.72} + \frac{(12 - 8.28)^2}{8.28}$$

$$\chi^2 = 7.73$$

	Reported Gaze Cue	Did Not Report Gaze Cue	Totals
Geminoid	10 (14*13/29 = 6.28)	4 (7.72)	14
Robovie	3 (6.72)	12 (8.28)	15
Totals	13	16	29

Degrees of Freedom

$df = (\text{Number of rows} - 1) * (\text{Number of columns} - 1)$

$$df = (2 - 1) * (2 - 1) = 1$$

	Reported Gaze Cue	Did Not Report Gaze Cue	<i>Totals</i>
Geminoid	10 $(14*13/29 = \mathbf{6.28})$	4 (7.72)	14
Robovie	3 (6.72)	12 (8.28)	15
<i>Totals</i>	13	16	29

What are degrees of freedom?

Number of values in the final calculation that are “free to vary”

Example: estimate mean from dataset X with 5 values

If I tell you $\mu_x = 3.5$ what values can x_1, x_2, x_3, x_4, x_5 take?

What if I tell you $x_1 = 7$?

And if I tell you $x_2 = 2.5$?

...

How many values $x_1 \dots x_5$ can take on any value given the mean?

General: for mean estimation with n values, we have $(n - 1)$ degrees of freedom

Degrees of Freedom

$df = (\text{Number of rows} - 1) * (\text{Number of columns} - 1)$

$$df = (2 - 1) * (2 - 1) = 1$$

	Reported Gaze Cue	Did Not Report Gaze Cue	<i>Totals</i>
Geminoid	10 $(14*13/29 = \mathbf{6.28})$	4 (7.72)	14
Robovie	3 (6.72)	12 (8.28)	15
<i>Totals</i>	13	16	29

Pearson's Chi-squared Test

$$\chi^2 = 7.73$$

$$df = (2 - 1) * (2 - 1) = 1$$

$| | Reported Gaze Cue | Did Not Report Gaze Cue | Totals |
|----------|-------------------------|-------------------------|--------|
| Geminoid | 10
(14*13/29 = 6.28) | 4
(7.72) | 14 |
| Robovie | 3
(6.72) | 12
(8.28) | 15 |
| Totals | 13 | 16 | 29 |$

χ^2 CRITICAL VALUES

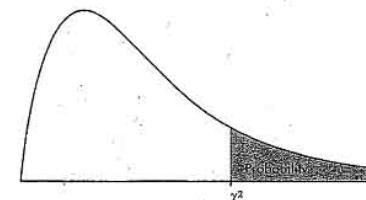


TABLE C: χ^2 CRITICAL VALUES

df	Tail probability p										
	.25	.20	.15	.10	.05	.025	.02	.01	.005	.0025	.001
1	1.32	1.64	2.07	2.71	3.84	5.02	5.41	6.63	7.88	9.14	10.83
2	2.77	3.22	3.79	4.61	5.99	7.38	7.82	9.21	10.60	11.98	13.82
3	4.11	4.64	5.32	6.25	7.81	9.35	9.84	11.34	12.84	14.32	16.27
4	5.39	5.99	6.74	7.78	9.49	11.14	11.67	13.28	14.86	16.42	18.47
5	6.63	7.29	8.12	9.24	11.07	12.83	13.39	15.09	16.75	18.39	20.51
6	7.84	8.56	9.45	10.64	12.59	14.45	15.03	16.81	18.55	20.25	22.46
7	9.04	9.80	10.75	12.02	14.07	16.01	16.62	18.48	20.28	22.04	24.32
8	10.22	11.03	12.03	13.36	15.51	17.53	18.17	20.09	21.95	23.77	26.12
9	11.39	12.24	13.29	14.68	16.92	19.02	19.68	21.67	23.59	25.46	27.88
10	12.55	13.44	14.53	15.99	18.31	20.48	21.16	23.21	25.19	27.11	29.59
11	13.70	14.63	15.77	17.28	19.68	21.92	22.62	24.72	26.76	28.73	31.26
12	14.85	15.81	16.99	18.55	21.03	23.34	24.05	26.22	28.30	30.32	32.91
13	15.98	16.98	18.20	19.81	22.36	24.74	25.47	27.69	29.82	31.88	34.53
14	17.12	18.15	19.41	21.06	23.68	26.12	26.87	29.14	31.32	33.43	36.12
15	18.25	19.31	20.60	22.31	25.00	27.49	28.26	30.58	32.80	34.95	37.70
16	19.37	20.47	21.79	23.54	26.30	28.85	29.63	32.00	34.27	36.46	39.25
17	20.49	21.61	22.98	24.77	27.59	30.19	31.00	33.41	35.72	37.95	40.79
18	21.60	22.76	24.16	25.99	28.87	31.53	32.35	34.81	37.16	39.42	42.31
19	22.72	23.90	25.33	27.20	30.14	32.85	33.69	36.19	38.58	40.88	43.82
20	23.83	25.04	26.50	28.41	31.41	34.17	35.02	37.57	40.00	42.34	45.31
21	24.93	26.17	27.66	29.62	32.67	35.48	36.34	38.93	41.40	43.78	46.80
22	26.04	27.30	28.82	30.81	33.92	36.78	37.66	40.29	42.80	45.20	48.27
23	27.14	28.43	29.98	32.01	35.17	38.08	38.97	41.64	44.18	46.62	49.73
24	28.24	29.55	31.13	33.20	36.42	39.36	40.27	42.98	45.56	48.03	51.18
25	29.34	30.63	32.28	34.38	37.65	40.65	41.57	44.31	46.93	49.44	52.62
26	30.43	31.79	33.43	35.56	38.89	41.92	42.86	45.64	48.29	50.83	54.05
27	31.53	32.91	34.57	36.74	40.11	43.19	44.14	46.96	49.64	52.22	55.48
28	32.62	34.03	35.71	37.92	41.34	44.46	45.42	48.28	50.99	53.59	56.89
29	33.71	35.14	36.85	39.09	42.56	45.72	46.69	49.59	52.34	54.97	58.30
30	34.80	36.25	37.99	40.26	43.77	46.98	47.96	50.89	53.67	56.33	59.70
40	45.62	47.27	49.24	51.81	55.76	59.34	60.44	63.69	66.77	69.70	73.40
50	56.33	58.16	60.35	63.17	67.50	71.42	72.61	76.15	79.49	82.66	86.66
60	66.98	68.97	71.34	74.40	79.08	83.30	84.58	88.38	91.95	95.34	99.61
80	88.13	90.41	93.11	96.58	101.9	106.6	108.1	112.3	116.3	120.1	124.8
100	109.1	111.7	114.7	118.5	124.3	129.6	131.1	135.8	140.2	144.3	149.4

Pearson's Chi-square in R

Between-participants comparisons

E.g., Participants interacted with two robots and measurements taken of whether they reported seeing a gaze cue that the robot exhibited

```
> setwd("C:\\\\Users\\\\Dan\\\\OneDrive\\\\Teaching\\\\HRI Spring 2016\\\\Lecture 21")  
> gaze <- read.table('RobotGaze.csv', sep=",", header=TRUE)  
> gaze
```

	Robot	Reported.Gaze.Cue
1	Robovie	Yes
2	Geminoid	Yes
3	Robovie	Yes
4	Geminoid	No
5	Robovie	Yes
6	Geminoid	No
7	Geminoid	No
8	Robovie	No

Pearson's Chi-square in R

```
> table(gaze)

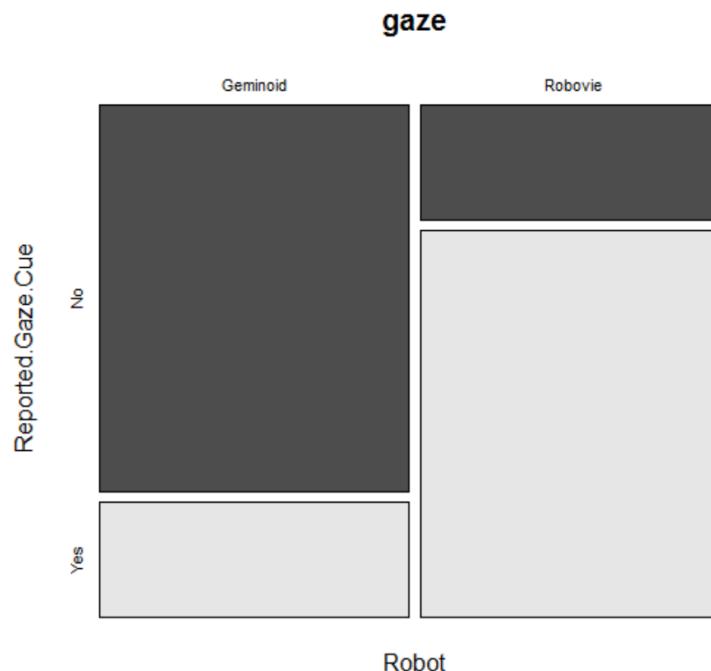
                    Reported.Gaze.Cue
Robot          No  Yes
Geminoid    10    3
Robovie      3   10

> chisq.test(table(gaze))

Pearson's Chi-squared test with Yates' continuity correction
data: table(gaze)
X-squared = 5.5385, df = 1, p-value = 0.0186
```

Pearson's Chi-square in R

```
> require(stats)  
> mosaicplot(~ Robot + Reported.Gaze.Cue, data =  
gaze, color = TRUE)
```



Chi-square in JMP

RobotGaze - JMP Pro

File Edit Tables Rows Cols DOE Analyze Graph Tools View Window Help

RobotGaze

Source

Columns (2/0)

Robot

Reported Gaze Cue

Rows

	Robot	Reported Gaze Cue
1	Robovie	Yes
2	Geminoid	Yes
3	Robovie	Yes
4	Geminoid	No
5	Robovie	Yes
6	Geminoid	No
7	Geminoid	No
8	Robovie	No
9	Robovie	Yes
10	Geminoid	No
11	Robovie	Yes
12	Geminoid	No
13	Robovie	No
14	Geminoid	Yes
15	Robovie	Yes
16	Geminoid	No
17	Robovie	Yes
18	Geminoid	No
19	Geminoid	No
20	Robovie	Yes
21	Geminoid	Yes
22	Robovie	Yes
23	Robovie	No
24	Geminoid	No
25	Robovie	Yes
26	Geminoid	No

All rows 26
Selected 0
Excluded 0
Hidden 0
Labelled 0

25

RobotGaze - JMP Pro

File Edit Tables Rows Cols DOE Analyze Graph Tools View Window Help

Distribution

Fit Y by X

Matched Pairs

Tabulate

Fit Model

Modeling

Multivariate Methods

Quality and Process

Reliability and Survival

Consumer Research

Reported Gaze Cue

	Robot	Reported Gaze	Cue
12	Geminoid	No	
13	Robovie	No	
14	Geminoid	Yes	
15	Robovie	Yes	
16	Geminoid	No	
17	Robovie	Yes	
18	Geminoid	No	
19	Geminoid	No	
20	Robovie	Yes	
21	Geminoid	Yes	
22	Robovie	Yes	
23	Robovie	No	
24	Geminoid	No	
25	Robovie	Yes	
26	Geminoid	No	

Columns (1)

Robot

Reported Gaze

Rows

All rows 26

Selected 0

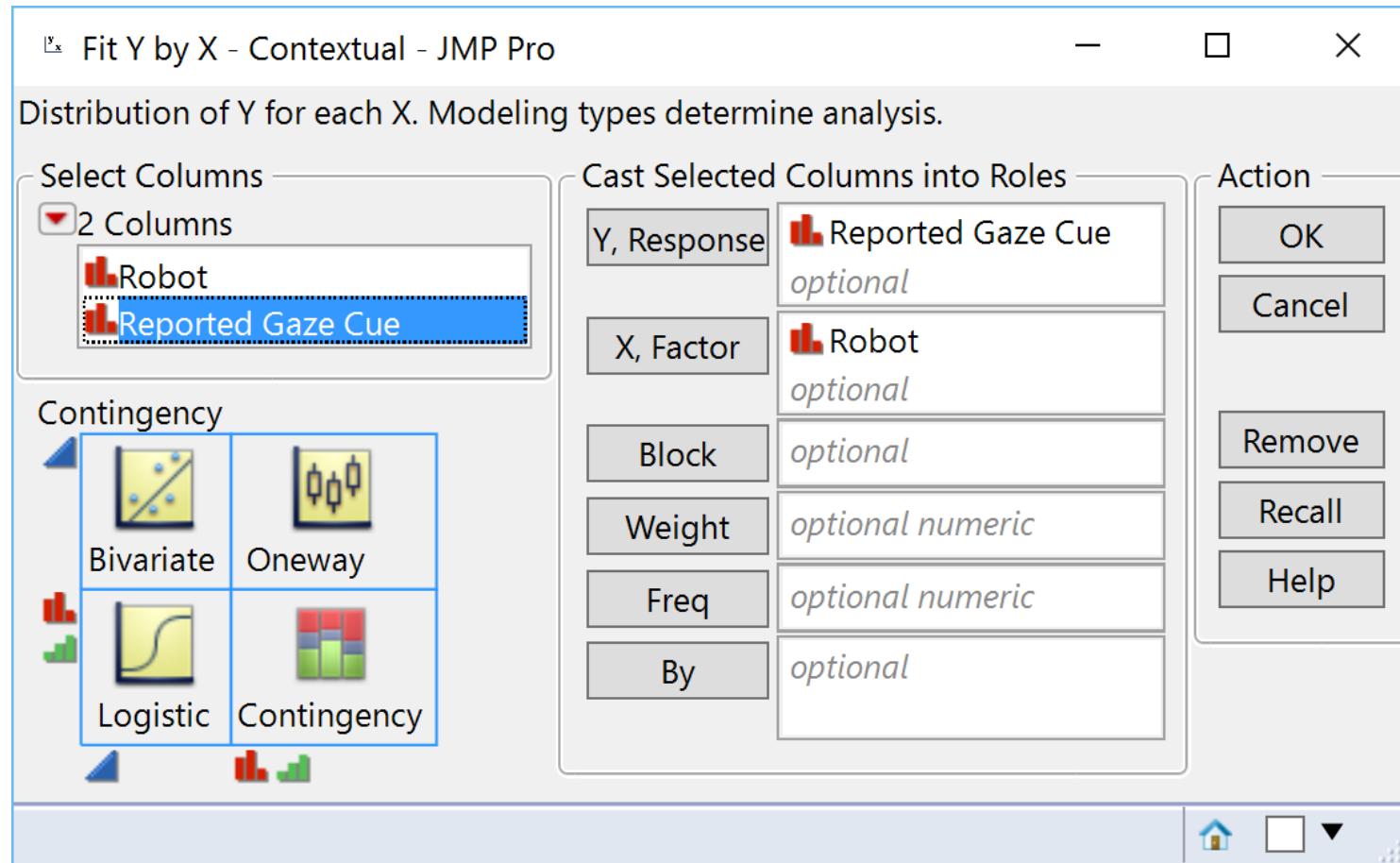
Excluded 0

Hidden 0

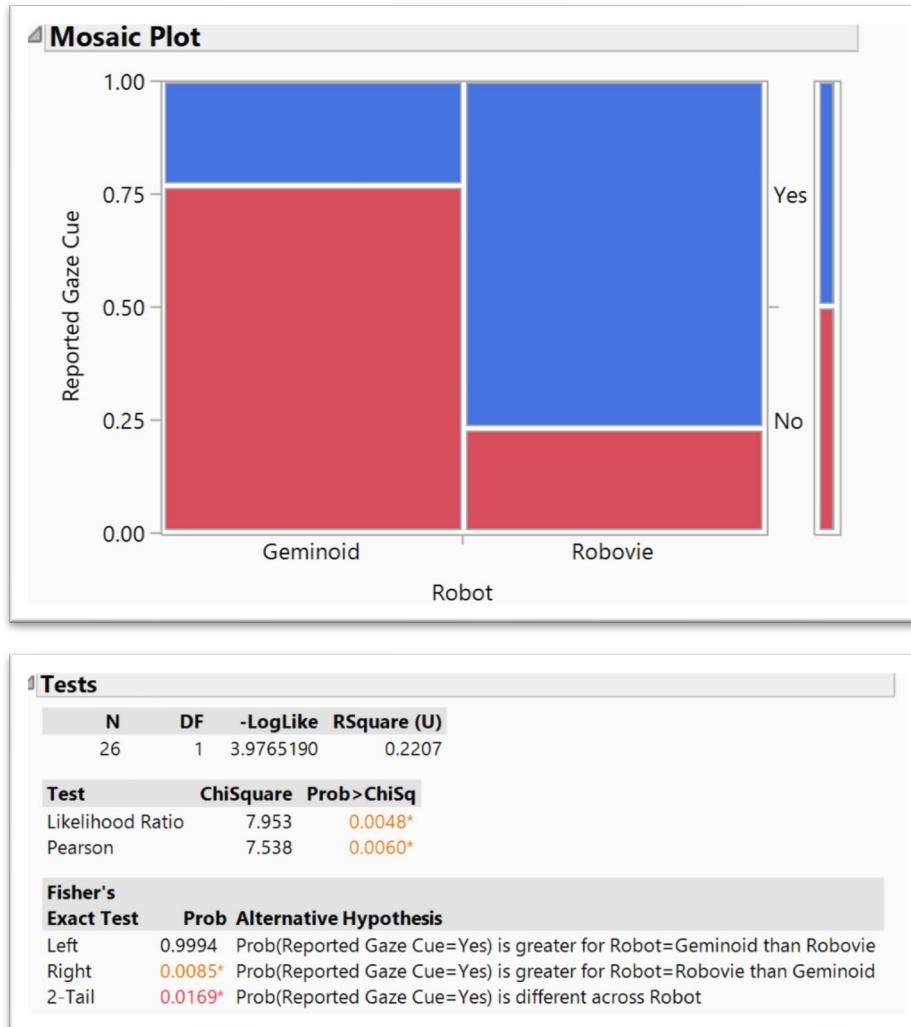
Labelled 0

26

Chi-square in JMP



Chi-square in JMP



Pearson's Chi-squared vs Fisher's Exact Test

Chi-square can be used with large samples

But with small samples or when data is very unequally distributed among table cells, sampling distribution of test statistic may be poor approximation of theoretical chi-squared distribution

In other words, Chi-squared test may not be appropriate in these cases

Rule of thumb: Only use Chi-square when expected values in all cells are ≥ 5

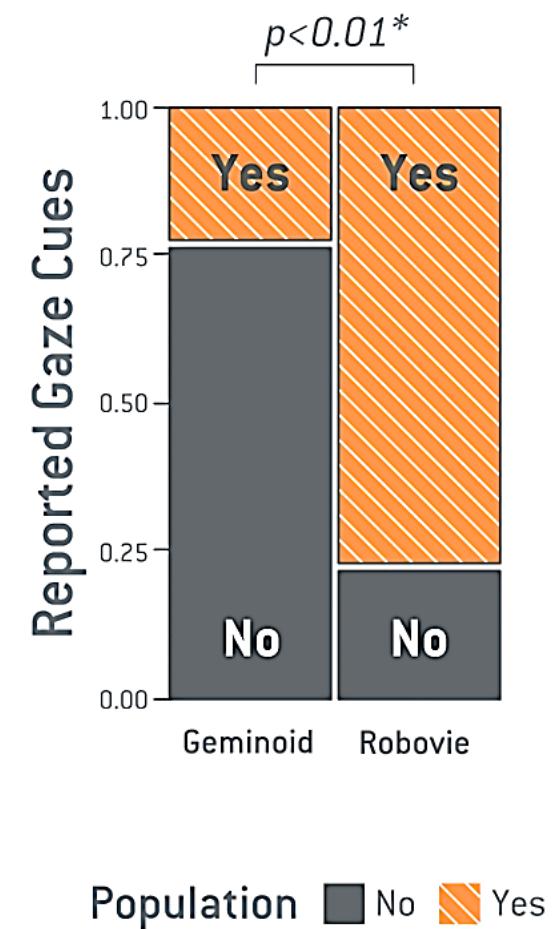
If any expected value is < 5 , use Fisher's exact test

Contingency Table			
	Reported Gaze Cue		
	No	Yes	Total
Robot	10	3	13
	38.46	11.54	50.00
	76.92	23.08	
	76.92	23.08	
Robovie	3	10	13
	11.54	38.46	50.00
	23.08	76.92	
	23.08	76.92	
Total	13	13	26
	50.00	50.00	

Tests			
N	DF	-LogLike	RSquare (U)
26	1	3.9765190	0.2207
Test			
Test	ChiSquare	Prob>ChiSq	
Likelihood Ratio	7.953	0.0048*	
Pearson	7.538	0.0060*	
Fisher's			
Exact Test	Prob	Alternative Hypothesis	
Left	0.9994	Prob(Reported Gaze Cue=Yes) is greater for Robot=Geminoid than Robovie	
Right	0.0085*	Prob(Reported Gaze Cue=Yes) is greater for Robot=Robovie than Geminoid	
2-Tail	0.0169*	Prob(Reported Gaze Cue=Yes) is different across Robot	

Reporting Results

“A contingency analysis for the manipulation check showed that significantly fewer participants reported identifying the gaze cue in Geminoid’s behavior than in Robovie’s ($\chi^2(1,26) = 7.54$, $p < .01$).”



Questions?

Correlation / Regression

Correlation

Measure of relation between two variables

Used mostly for *interval* or *ratio* scales

Range from -1 to 1

-1 is negative correlation

1 is positive correlation

0 is no correlation

Output Variable

Input Variable

	Nominal	Categorical (>2 categories)	Ordinal	Quantitative Discrete	Quantitative Non-Normal	Quantitative Normal
Nominal	χ^2 or Fisher's	χ^2	χ^2 trend or Mann-Whitney	Mann-Whitney	Mann-Whitney or log-rank (a)	Student's t-test
Categorical (>2 categories)	χ^2	χ^2	Kruskal-Wallis (b)	Kruskal-Wallis (b)	Kruskal-Wallis (b)	Analysis of variance (c)
Ordinal	χ^2 trend or Mann-Whitney	(e)	Spearman rank	Spearman rank	Spearman rank	Spearman rank or linear regression (d)
Quantitative Discrete	Logistic regression	(e)	(e)	Spearman rank	Spearman rank	Spearman rank or linear regression (d)
Quantitative Non-Normal	Logistic regression	(e)	(e)	(e)	Plot data and Pearson or Spearman rank	Plot data and Pearson or Spearman rank and linear regression
Quantitative Normal	Logistic regression	(e)	(e)	(e)	Linear regression (d)	Pearson and linear regression

IV: Continuous | DV: Continuous

Correlation: measure the relation between two variables

Pearson's r

Simple linear correlation

To what extent are two variables *proportional* or *linearly related* to each other

r value denotes the strength of the linear relationship [-1,1]

R^2 is the coefficient of determination = percent of variation in one variable that is related to the variation in the other

E.g., $r = 0.7$ means $R^2 = .49$, thus 49% of the variance is related

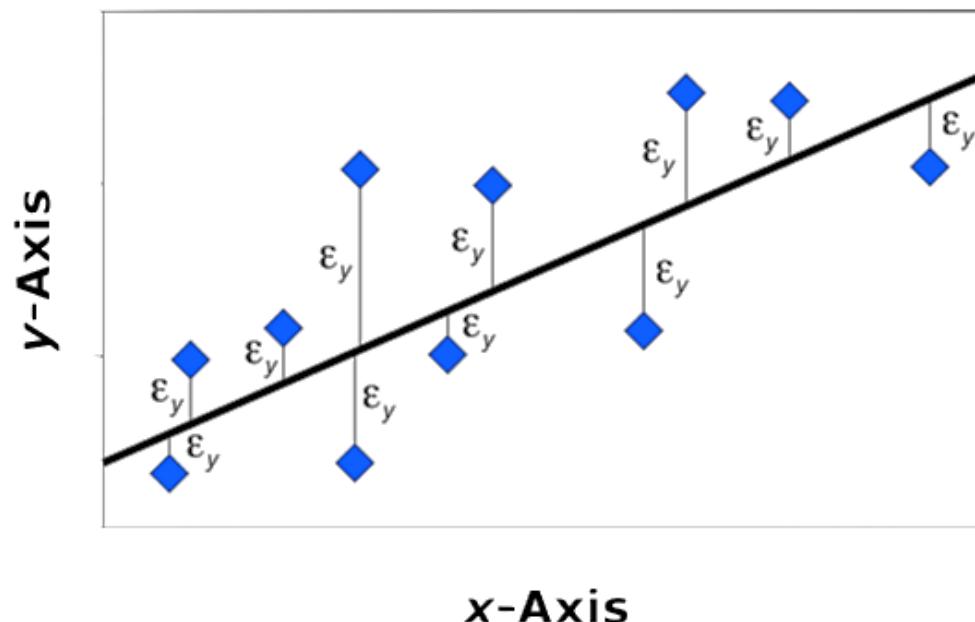
The proportion can be summarized by a simple line

The regression or *least squares* line

Determined by minimizing the sum of squared distances

Regression Line

$$Y = \beta_0 + \sum_{i=1}^n \beta_i X_i + \epsilon_i$$



Correlational Significance

The extent to which a result would not be obtained by chance

E.g., a p-value of 0.05 indicates that there is a 5% probability that the relation between the variables found in our sample is a fluke

Lower p-value indicates higher reliability of result

Sample Size

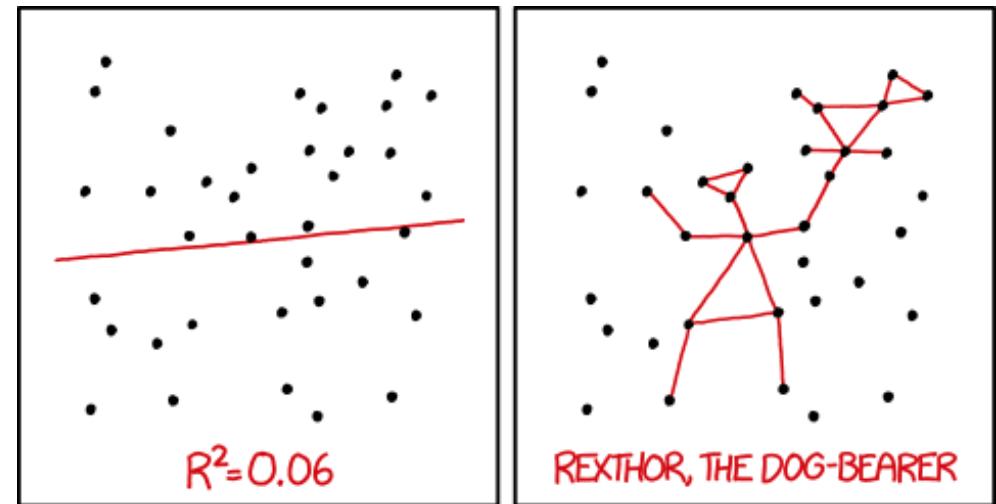
Significance level is primary source of information about the reliability of the correlation

Significance of a correlation depends on sample size

Rule of thumb

Sample size above 50 is good

Sample size above 100 is safe



I DON'T TRUST LINEAR REGRESSIONS WHEN IT'S HARDER
TO GUESS THE DIRECTION OF THE CORRELATION FROM THE
SCATTER PLOT THAN TO FIND NEW CONSTELLATIONS ON IT.

Calculating Correlations in R

Create correlation matrices

```
cor(q, use="complete.obs", method="pearson")
```

Decide how to deal with missing data

- Assume that data is complete (all.obs)

- Use complete data (complete.obs)

- Use all complete pairs (pairwise.complete.obs)

Choose a method

- Pearson**, Spearman, Kendall

```

> setwd("C:\\\\Users\\\\Dan\\\\OneDrive\\\\Teaching\\\\HRI Spring 2016\\\\Lecture 19")
> qdata <- read.csv("FactorAnalysis_Data.csv")
> q <- qdata[,3:21]
> cor(q, use="complete.obs", method="pearson")

          Looks_humanlike Behaves_humanlike Attractive       Cute    Cheerful   Friendly Optimistic      Warm
Looks_humanlike 1.0000000000
Behaves_humanlike 0.4460335600
Attractive        0.1579833720
Cute              0.127183004
Cheerful          0.269591275
Friendly          0.215295243
Optimistic         -0.184166063
Warm              0.031285597
Happy             0.217179525
Knowledgeable     0.362102228
Responsible       0.003858589
Intelligent       0.429512593
Sensible          0.441047628
Loyal              0.074197414
Honest             -0.089310583
Cooperative        -0.114363909
Attentive          0.264076764
You_like_the_robot 0.180465620
Robot_likes_you   0.077527181

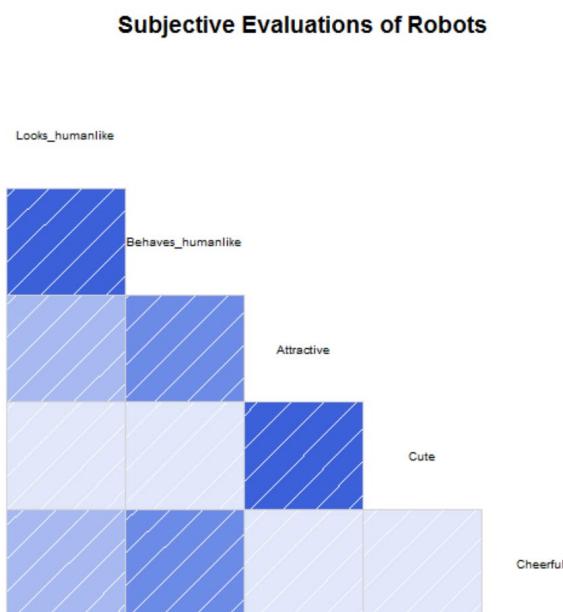
          Happy Knowledgeable Responsible Intelligent Sensible Loyal Honest Cooperative
Looks_humanlike 0.21717952 0.36210223 0.003858589 0.4295125934 0.44104763 0.07419741 -0.08931058 -0.114363909
Behaves_humanlike 0.02898437 0.20109834 -0.070803702 0.2984633429 0.26769554 -0.09136711 -0.10009483 -0.111193875
Attractive        -0.06506949 0.16462753 0.309710117 0.1230696411 0.28256988 0.39709652 0.25984151 0.307339316
Cute              0.08429582 -0.14615269 0.140435406 0.0006549498 0.16006712 0.07431983 -0.11163127 -0.028548528
Cheerful          0.32716571 0.27862653 -0.140085903 0.2406394570 0.11096477 0.02460031 -0.08313890 -0.029136680
Friendly          0.64424695 0.39205549 0.216384813 0.3057089466 0.11333561 0.19154632 0.13453646 0.099197354
Optimistic         0.28240538 0.29599271 0.336523795 -0.0186161459 0.24578385 0.15325031 0.26065396 0.398610449
Warm              0.55431834 0.32010781 0.423487672 0.3954291700 0.40563392 -0.10876876 0.11674230 -0.056805183
Happy             1.00000000 0.32385994 0.441806745 0.3670399283 0.23100943 0.20574245 0.20676318 -0.111322334
Knowledgeable     0.32385994 1.00000000 0.167220231 0.6692242683 0.46754583 0.26815566 0.21494520 0.173053650
Responsible       0.44180674 0.16722023 1.000000000 0.1821125508 0.15365926 0.42462989 0.38018745 0.089139224
Intelligent       0.36703993 0.66922427 0.182112551 1.0000000000 0.57014444 0.12166221 0.11957908 -0.202122744

```

Visualizing Correlations

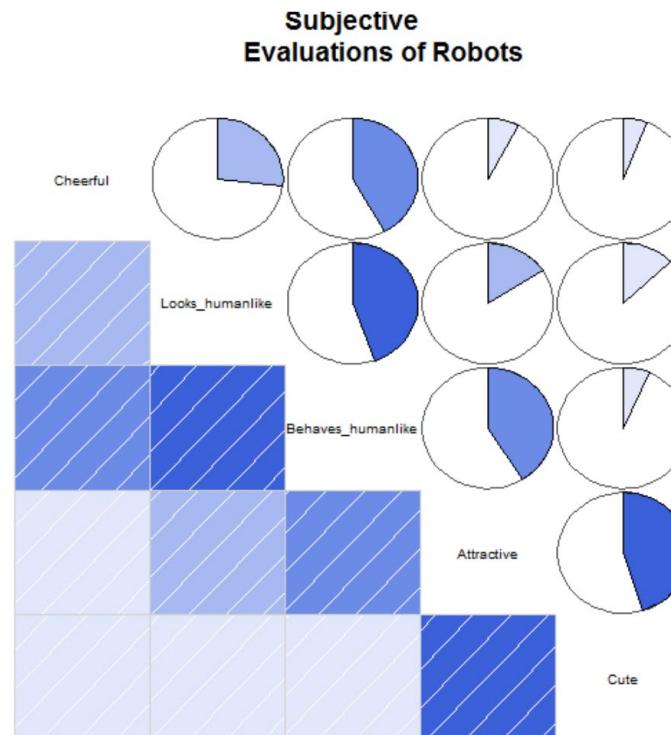
Create correlation matrices

```
> library(corrgram)
> corrgram(q[,1:5], order=NULL, lower.panel=panel.shade,
upper.panel=NULL, text.panel=panel.txt, main="Subjective
Evaluations of Robots")
```



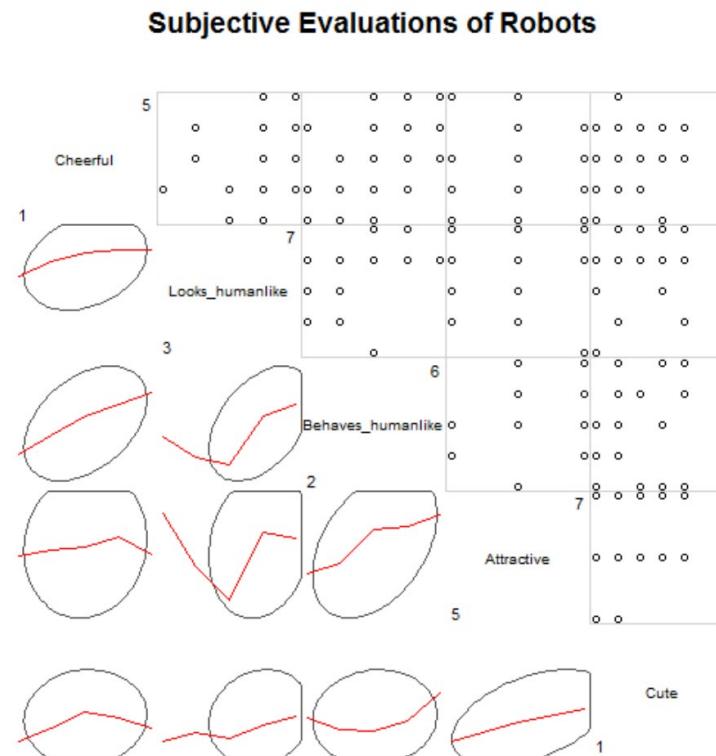
Visualizing Correlations

```
> corrgram(q[,1:5], order=TRUE, lower.panel=panel.shade,  
upper.panel=panel.pie, text.panel=panel.txt, main="Subjective  
Evaluations of Robots")
```



Visualizing Correlations

```
> corrgram(q[,1:5], order=TRUE, lower.panel=panel.ellipse,  
upper.panel=panel pts, text.panel=panel.txt,  
diag.panel=panel.minmax, main="Subjective Evaluations of Robots")
```



Correlational Significance Test

```
> library(Hmisc)  
> rcorr(as.matrix(q), type="pearson")
```

r	Looks_humanlike	Behaves_humanlike	Attractive	Cute	Cheerful
Looks_humanlike	1.00	0.45	0.16	0.13	0.27
Behaves_humanlike	0.45	1.00	0.41	0.06	0.42
Attractive	0.16	0.41	1.00	0.45	0.08
Cute	0.13	0.06	0.45	1.00	0.06
Cheerful	0.27	0.42	0.08	0.06	1.00

p	Looks_humanlike	Behaves_humanlike	Attractive	Cute	Cheerful
Looks_humanlike	0.0153		0.4131	0.5109	0.1573
Behaves_humanlike	0.0153		0.0264	0.7394	0.0233
Attractive	0.4131	0.0264		0.0136	0.6904
Cute	0.5109	0.7394	0.0136		0.7603
Cheerful	0.1573	0.0233	0.6904	0.7603	

Significant — based on .05 confidence level

Correlations in JMP

FactorAnalysis_Data - JMP Pro

File Edit Tables Rows Cols DOE Analyze Graph Tools View Window Help

FactorAnalysis_Data
Source

Columns (21/5)
Participant ID
Condition
Looks_humanlike
Behaves_humanlike
Attractive
Cute
Cheerful
Friendly
Optimistic
Warm
Happy
Knowledgeable
Responsible
Intelligent
Sensible
Loyal
Honest
Cooperative
Attentive
You_like_the_robot
Robot_likes_you

Rows
All rows 29
Selected 0
Excluded 0
Hidden 0
Labelled 0

	Participant ID	Condition	Looks_humanlike	Behaves_humanlike	Attractive	Cute	Cheerful	Friendly	Optimistic	Warm	Happy	Knowledgeable	Responsible	Intelligent	Sensible	L
1	p01	Control	6	4	7	1	1	2	3	2	2	4	6	6	6	6
2	p02	Control	6	5	7	3	4	6	5	6	7	7	7	7	7	7
3	p03	Control	5	3	5	1	1	5	4	4	4	5	5	5	5	2
4	p04	Control	7	4	7	4	4	6	4	5	4	6	6	6	5	5
5	p05	Cue	7	5	6	3	3	4	4	3	5	6	4	6	5	5
6	p06	Cue	6	5	6	2	4	5	3	3	4	5	5	5	6	5
7	p07	Cue	7	5	7	2	4	5	4	3	4	5	5	5	4	4
8	p08	Cue	6	2	6	3	2	5	5	5	5	7	7	7	7	7
9	p09	Cue	6	4	7	4	3	5	5	5	5	5	6	6	6	6
10	p10	Control	6	6	6	2	5	3	4	4	4	6	5	6	5	5
11	p11	Control	6	4	6	2	2	3	6	3	4	5	6	5	6	6
12	p12	Cue	6	4	7	2	2	2	4	2	2	6	3	6	5	5
13	p13	Cue	5	3	5	1	2	3	4	3	2	3	3	3	3	5
14	p14	Control	6	4	6	2	3	5	4	4	5	6	4	7	6	6
15	p15	Control	6	6	7	5	4	3	3	5	2	4	5	5	6	6
16	p16	Cue	6	5	6	2	5	5	5	5	6	5	6	6	4	4
17	p17	Cue	6	3	7	7	2	3	3	3	2	5	5	6	5	5
18	p18	Control	7	5	6	3	2	3	2	3	4	3	5	6	4	4
19	p19	Control	6	3	5	1	3	3	5	3	2	5	3	5	5	5
20	p20	Cue	7	5	7	5	3	4	4	2	3	5	4	4	5	5
21	p21	Control	6	6	7	4	3	3	4	4	3	5	5	7	5	5
22	p22	Cue	3	4	7	1	2	3	5	3	1	5	6	4	2	2
23	p23	Control	6	2	6	1	4	5	2	3	4	6	6	6	6	4
24	p24	Cue	5	2	6	4	1	2	4	2	4	2	7	2	2	2
25	p25	Control	7	5	7	2	4	5	3	5	3	5	5	6	6	6
26	p26	Cue	7	4	5	2	2	3	5	3	4	6	7	7	6	6
27	p27	Control	4	2	6	5	4	6	4	5	5	3	5	5	4	4
28	p28	Cue	7	4	5	2	5	5	2	2	3	5	3	6	3	3
29	p29	Cue	4	3	5	2	3	2	3	2	3	4	3	4	4	4

Correlations in JMP

Screenshot of the JMP software interface showing a correlation matrix for FactorAnalysis_Data.

The Analyze menu is selected, and the Multivariate Methods option is highlighted.

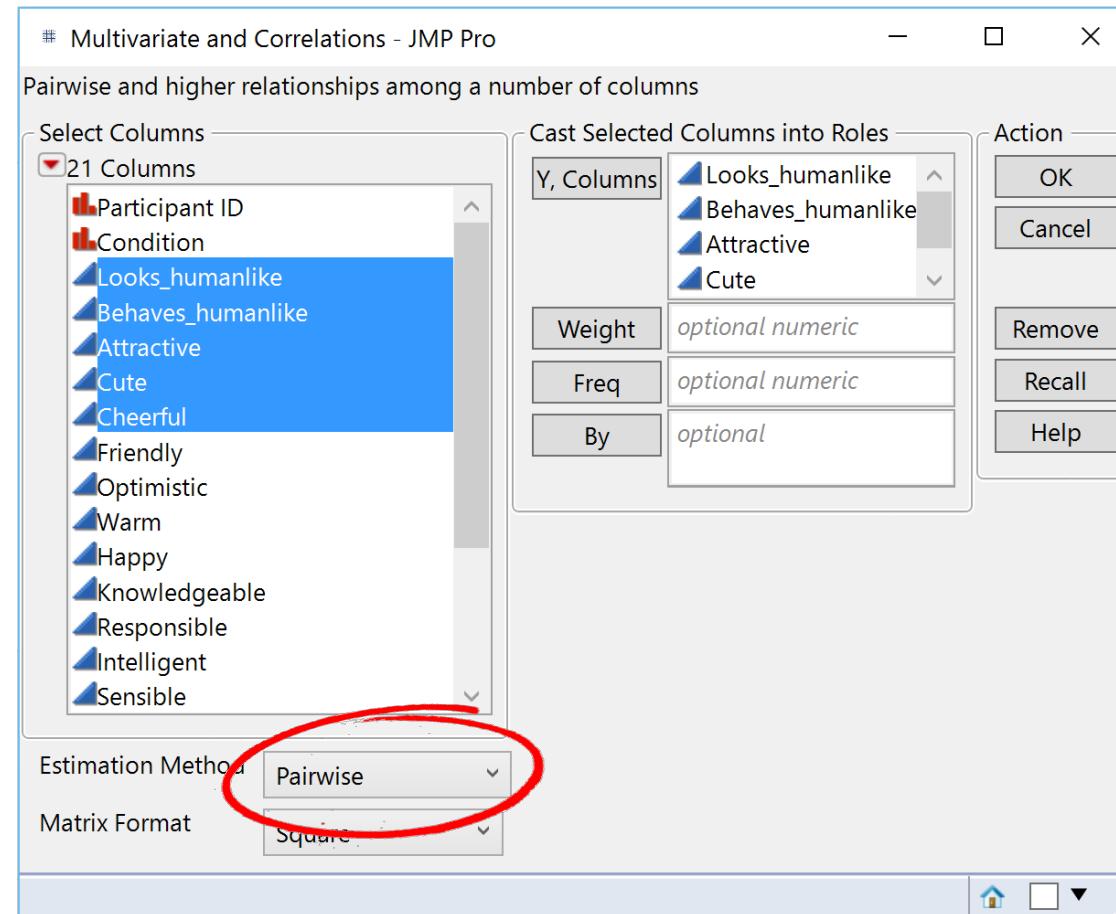
The data table contains 29 rows (labeled p12 through p29) and 17 columns, including:

- Participant ID (Column 1)
- Condition (Column 2)
- Looks_humanlike (Column 3)
- Behaves_humanlike (Column 4)
- Attractive (Column 5)
- Cute (Column 6)
- Cheerful (Column 7)
- Friendly (Column 8)
- Optimistic (Column 9)
- Warm (Column 10)
- Happy (Column 11)
- Knowledgeable (Column 12)
- Responsible (Column 13)
- Intelligent (Column 14)
- Sensible (Column 15)
- Loyal (Column 16)
- Honest (Column 17)
- Cooperative (Column 18)
- Attentive (Column 19)
- You_like_the_robot (Column 20)
- Robot_likes_you (Column 21)

The table shows correlations between these variables across the 29 participants. The "Looks_humanlike" and "Behaves_humanlike" columns show high positive correlations with most other variables, particularly "Cute", "Cheerful", and "Friendly".

Participant ID	Condition	Looks_humanlike	Behaves_humanlike	Attractive	Cute	Cheerful	Friendly	Optimistic	Warm	Happy	Knowledgeable	Responsible	Intelligent	Sensible	Loyal	Honest	Cooperative	Attentive	You_like_the_robot	Robot_likes_you
p12	Control	6	4	7	1	1	2	3	2	2	4	6	6	6	6	6	6	6	6	6
p13	Cue	5	6	2	4	5	3	3	4	4	5	5	5	5	5	5	5	5	5	5
p14	Control	6	4	6	2	3	5	4	3	4	5	5	5	5	5	5	5	5	5	4
p15	Control	6	6	7	5	4	3	3	5	5	5	5	5	5	5	7	7	7	7	7
p16	Cue	6	5	6	2	5	5	5	5	5	4	4	4	6	6	6	6	6	6	5
p17	Cue	6	3	7	7	2	3	3	3	3	2	3	4	3	5	5	5	5	6	4
p18	Control	7	5	6	3	2	3	2	3	3	2	3	4	3	3	5	5	5	6	4
p19	Control	6	3	5	1	3	3	3	5	3	2	3	2	5	3	5	5	3	5	5
p20	Cue	7	5	7	5	3	4	4	2	3	4	2	3	5	4	4	4	4	5	5
p21	Control	6	6	7	4	3	3	4	4	4	3	5	5	5	5	5	7	5	7	5
p22	Cue	3	4	7	1	2	3	5	3	1	5	3	1	5	6	6	4	2	6	4
p23	Control	6	2	6	1	4	5	2	3	4	6	4	5	6	6	6	6	6	4	4
p24	Cue	5	2	6	4	1	2	4	2	4	2	4	2	2	7	2	2	2	2	2
p25	Control	7	5	7	2	4	5	3	5	3	5	3	5	5	5	5	6	6	6	6
p26	Cue	7	4	5	2	2	3	5	3	4	6	4	5	4	6	7	7	7	6	6
p27	Control	4	2	6	5	4	6	4	5	5	5	4	5	5	3	5	5	5	4	4
p28	Cue	7	4	5	2	5	5	2	2	3	2	3	5	3	3	6	3	6	3	3
p29	Cue	4	3	5	2	3	2	3	2	3	2	3	2	4	3	4	3	4	4	4

Correlations in JMP



Correlations in JMP

FactorAnalysis_Data - JMP Pro

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FactorAnalysis_Data Source

Participant ID Condition Looks_humanlike

1 p01 ✓ Correlations Multivariate
2 p02 Correlation Probability
3 p03 CI of Correlation
4 p04 Inverse Correlations
5 p05 Partial Correlations
6 p06 Covariance Matrix
7 p07 ✓ Pairwise Correlations
8 p08
9 p09
10 p10 Hotelling's T² Test
11 p11 Simple Statistics
12 p12 Nonparametric Correlations
13 p13 Set α Level
14 p14
15 p15 Scatterplot Matrix
16 p16 Color Maps
17 p17 Parallel Coord Plot
18 p18 Ellipsoid 3D Plot
19 p19 Principal Components
20 p20 Outlier Analysis
21 p21 Item Reliability
22 p22 Impute Missing Data
23 p23 Save Imputed Formula
24 p24 Script
25 p25
26 p26
27 p27
28 p28 Cue
29 p29 Cue

All rows 29
Selected 0
Excluded 0
Hidden 0
Labelled 0

FactorAnalysis_Data - Multivariate - JMP Pro

File Edit Tables Rows Cols DOE Analyze Graph Tools View Window Help

Multivariate Correlations

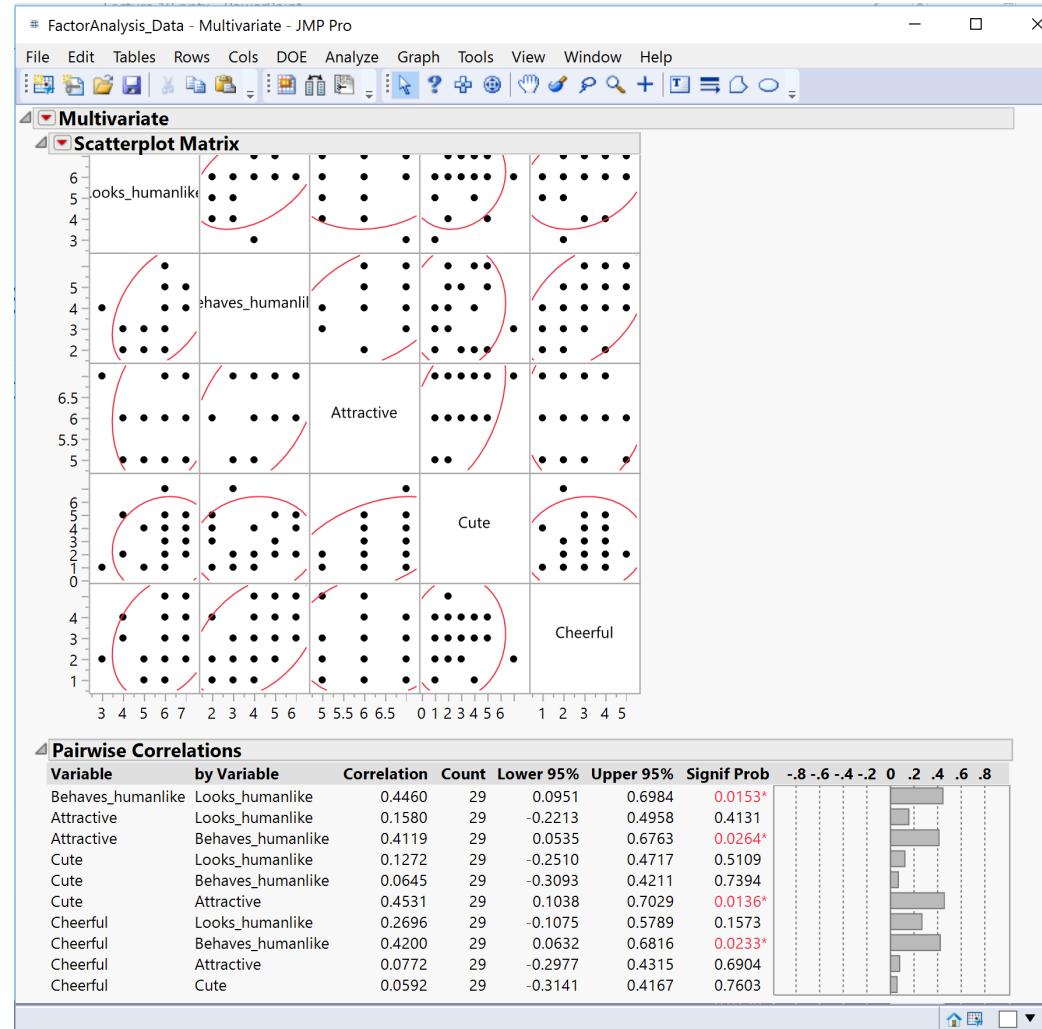
	Looks_humanlike	Behaves_humanlike	Attractive	Cute	Cheerful
Looks_humanlike	1.0000	0.4460	0.1580	0.1272	0.2696
Behaves_humanlike	0.4460	1.0000	0.4119	0.0645	0.4200
Attractive	0.1580	0.4119	1.0000	0.4531	0.0772
Cute	0.1272	0.0645	0.4531	1.0000	0.0592
Cheerful	0.2696	0.4200	0.0772	0.0592	1.0000

Scatterplot Matrix

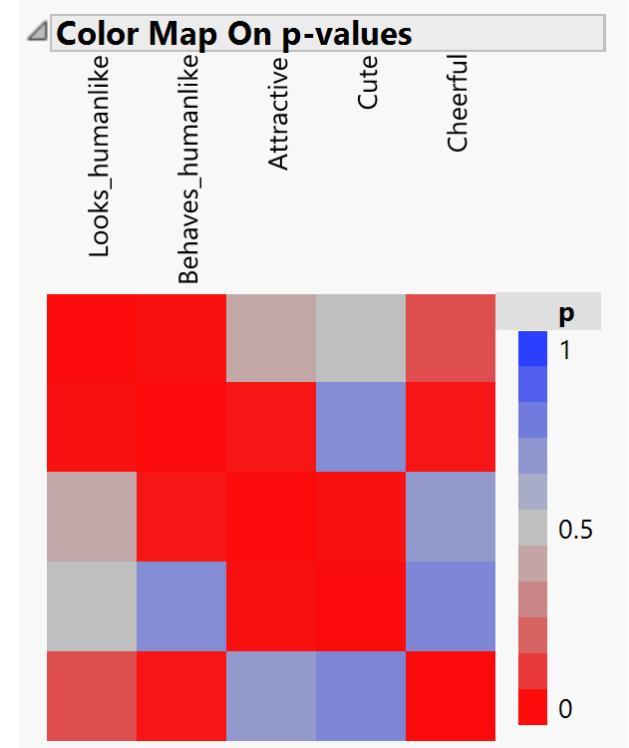
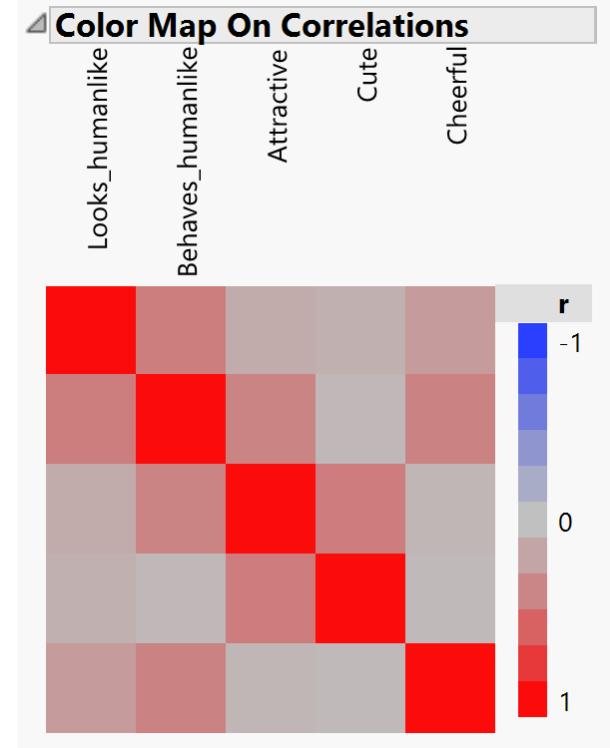
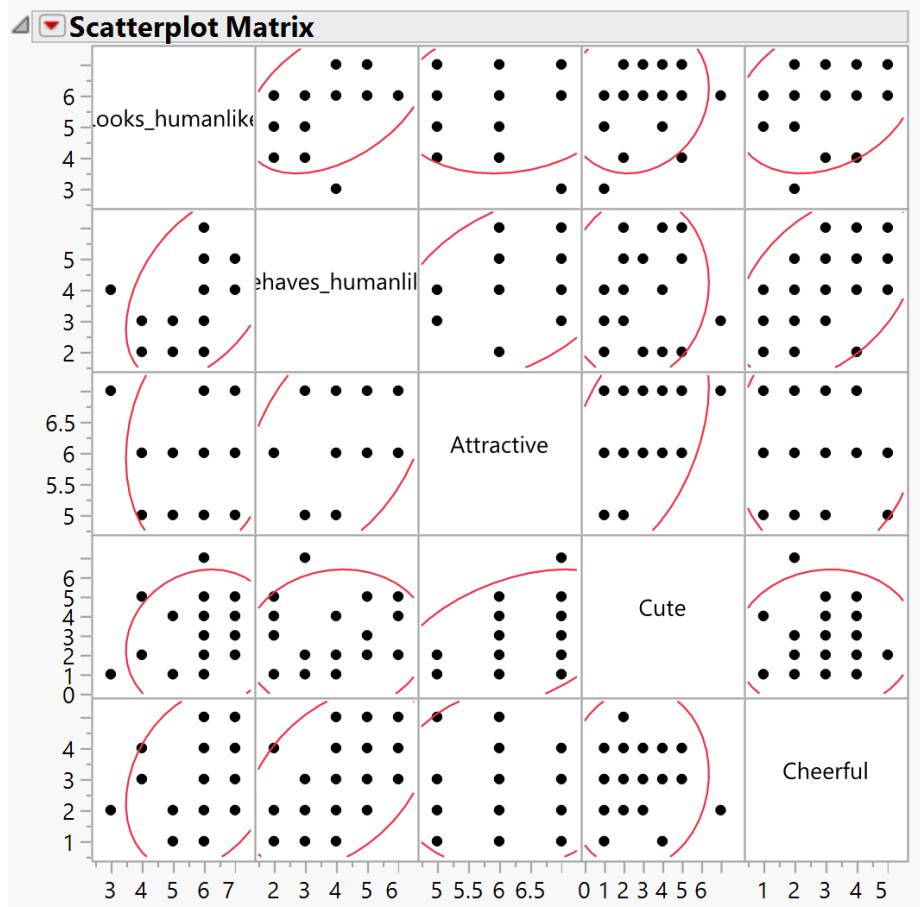
Pairwise Correlations

Variable	by Variable	Correlation	Count	Lower 95%	Upper 95%	Signif Prob
Behaves_humanlike	Looks_humanlike	0.4460	29	0.0951	0.6984	0.0153*

Correlations in JMP



Visualization



Regression in JMP

			ID	Condition	Looks_humanlike	Behaves_huma...	Attractive	Cute	Cheerfu
			2	p02	Control	6	4	7	1
			3	p03	Control	5	3	5	1
			4	p04	Control	7	4	7	4
			5	p05	Cue	7	5	6	3
			6	p06	Cue	6	5	6	2
			7	p07	Cue	7	5	7	2
			8	p08	Cue	6	2	6	3
			9	p09	Cue	6	4	7	4
			10	p10	Control	6	6	6	2
			11	p11	Control	6	4	6	2
			12	p12	Cue	6	4	7	2
			13	p13	Cue	5	3	5	1
			14	p14	Control	6	4	6	2
			15	p15	Control	6	6	7	5
			16	p16	Cue	6	5	6	2
			17	p17	Cue	6	3	7	7
			18	p18	Control	7	5	6	3
			19	p19	Control	6	3	5	1
	All rows	29	20	p20	Cue	7	5	7	5
	Selected	0	21	p21	Control	6	6	7	4
	Excluded	0	22	p22	Cue	3	4	7	1
	Hidden	0	23	p23	Control	6	2	6	1
	Labelled	0	24	p24	Cue	5	2	6	4
			25	p25	Control	7	7	7	2

Distribution of Y for each X. Modeling types
determine analysis.

Select Columns

21 Columns

Participant ID

Condition

Looks_humanlike

Behaves_humanlike

Attractive

Cute

Cheerful

Friendly

Optimistic

Warm

Happy

Knowledgeable

Responsible

Intelligent

Sensible

Loyal

Honest

Cooperative

Attentive

You_like_the_robot

Robot_likes_you

Cast Selected Columns into Roles

Y, Response

Looks_humanlike
optional

X, Factor

Behaves_humanlike
optional

Block

optional

Weight

optional numeric

Freq

optional numeric

By

optional

Action

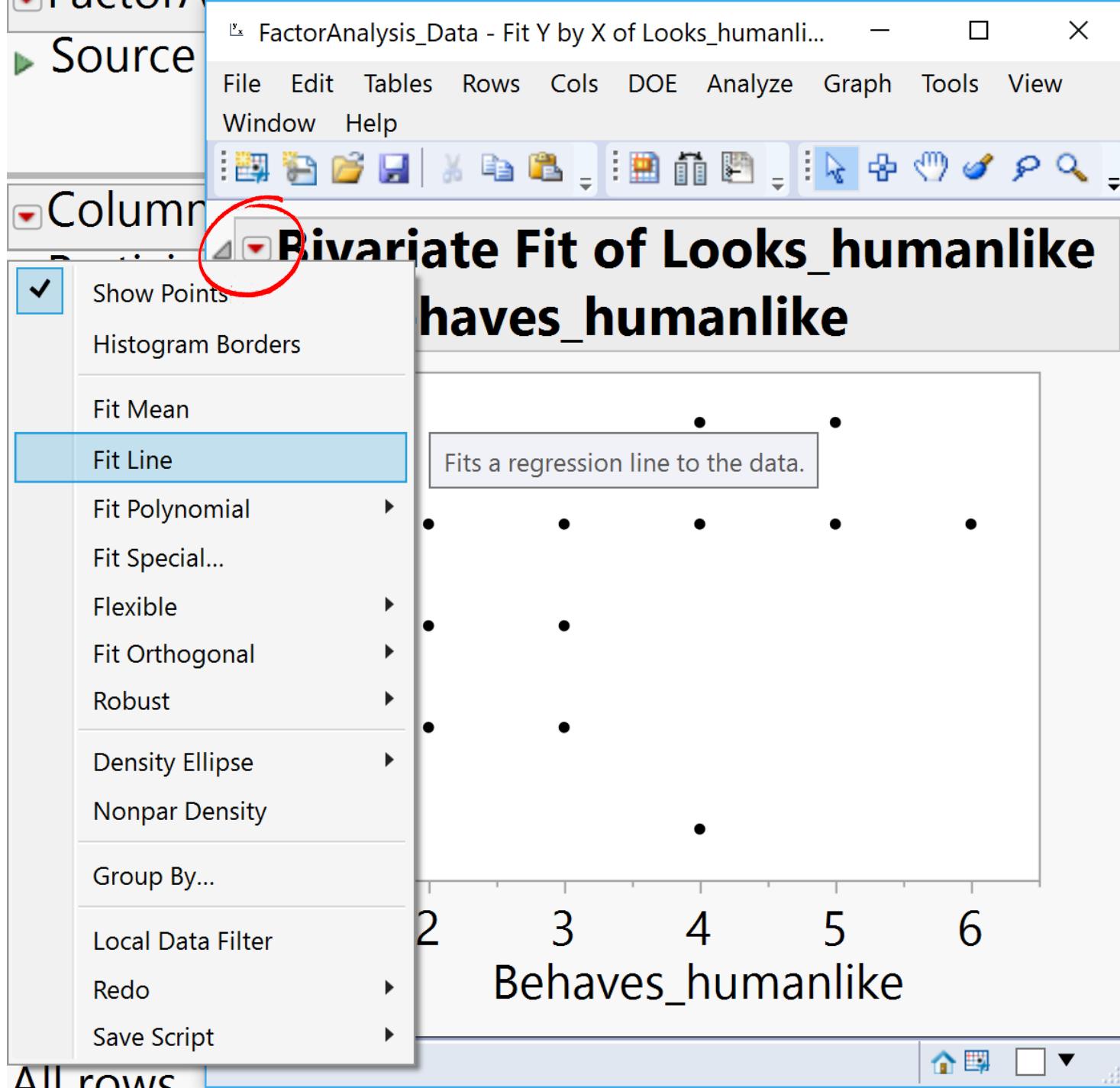
OK

Cancel

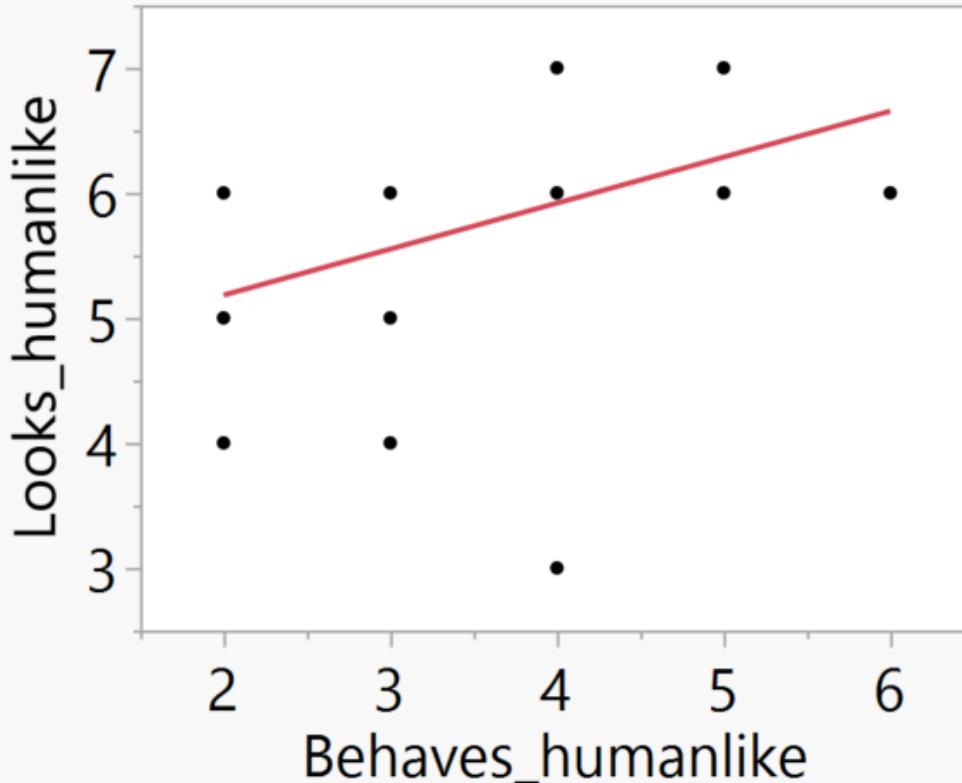
Remove

Recall

Help



Bivariate Fit of Looks_humanlike By Behaves_humanlike



Linear Fit

Linear Fit

Looks_humanlike = 4.4469697 +
0.3678451*Behaves humanlike

Summary of Fit

RSquare	0.198946
RSquare Adj	0.169277
Root Mean Square Error	0.909192
Mean of Response	5.931034
Observations (or Sum Wgts)	29

Lack Of Fit

Analysis of Variance

Source	DF	Sum of Squares		F Ratio
		Mean Square	F Ratio	
Model	1	5.543045	5.54305	6.7056
Error	27	22.319024	0.82663	Prob > F 0.0153*
C. Total	28	27.862069		

Parameter Estimates

Term	Estimate	Std Error	t Ratio	Prob> t
Intercept	4.4469697	0.597456	7.44	<.0001*
Behaves_humanlike	0.3678451	0.142052	2.59	0.0153*

Reporting

Correlations

$$DF = N - 2$$

If reporting on strength and direction of linear relationship report r

Results of the Pearson correlation indicated that there was a significant linear relationship between [var1] and [var2], $r(df) = .[value]$, $p = .[value]$

Report R^2 if discussing proportion of explained variance

[Var1] accounted for [value]% of the variation in [var2]

Or just include as $r(df) = .[value]$, $p = .[value]$, with $R^2 = [value]$

Regression

We will come back to if we have time

predictor and response variables to obtain linearity. For students in the no review condition, EEG-monitored attention levels accounted for 25.19% of the variance in student recall abilities and served as a marginal predictor of recall scores, $\beta = .187$, $t(10) = 2.17$, $p = .055$, providing partial support for our premise.

Questions?



University of Colorado
Boulder

THANKS!

Professor **Dan Szafir**

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University of Colorado Boulder*