

Stock_Price_Forecasting_of_Apple.R

sayal

Sat Apr 20 12:11:20 2019

```
library(ggplot2)
```

```
## Warning: package 'ggplot2' was built under R version 3.5.2
```

```
library(quantmod)
```

```
## Loading required package: xts
```

```
## Loading required package: zoo
```

```
##  
## Attaching package: 'zoo'
```

```
## The following objects are masked from 'package:base':
```

```
##  
##     as.Date, as.Date.numeric
```

```
## Loading required package: TTR
```

```
## Version 0.4-0 included new data defaults. See ?getSymbols.
```

```
library(ggplot2)  
library(fpp)
```

```
## Loading required package: forecast
```

```
## Loading required package: fma
```

```
## Loading required package: expsmooth
```

```
## Loading required package: lmtest
```

```
## Loading required package: tseries
```

```
library(fpp2)
```

```
##  
## Attaching package: 'fpp2'
```

```
## The following objects are masked from 'package:fpp':  
##  
##     ausair, ausbeer, austat, austourists, debitcards, departures,  
##     elecequip, euretail, guinearice, oil, sunspotarea, usmlelec
```

```
start_date <- as.Date("2012-01-01")  
end_date <- as.Date("2018-01-01")  
start_date
```

```
## [1] "2012-01-01"
```

```
end_date
```

```
## [1] "2018-01-01"
```

```
lapply(start_date, class)
```

```
## [[1]]  
## [1] "Date"
```

```
lapply(end_date, class)
```

```
## [[1]]  
## [1] "Date"
```

```
getSymbols("AAPL", src = "yahoo", from = start_date, to = end_date)
```

```
## 'getSymbols' currently uses auto.assign=TRUE by default, but will  
## use auto.assign=FALSE in 0.5-0. You will still be able to use  
## 'loadSymbols' to automatically load data. getOption("getSymbols.env")  
## and getOption("getSymbols.auto.assign") will still be checked for  
## alternate defaults.  
##  
## This message is shown once per session and may be disabled by setting  
## options("getSymbols.warning4.0"=FALSE). See ?getSymbols for details.
```

```
##
## WARNING: There have been significant changes to Yahoo Finance data.
## Please see the Warning section of '?getSymbols.yahoo' for details.
##
## This message is shown once per session and may be disabled by setting
## options("getSymbols.yahoo.warning"=FALSE).
```

```
## [1] "AAPL"
```

```
summary(AAPL)
```

| | Index | AAPL.Open | AAPL.High | AAPL.Low |
|---------------|-------------|-------------------|----------------|----------------|
| ## Min. | :2012-01-03 | Min. : 55.42 | Min. : 57.09 | Min. : 55.01 |
| ## 1st Qu. | :2013-07-05 | 1st Qu.: 78.78 | 1st Qu.: 79.37 | 1st Qu.: 77.68 |
| ## Median | :2015-01-02 | Median : 99.25 | Median :100.33 | Median : 98.40 |
| ## Mean | :2015-01-01 | Mean :102.88 | Mean :103.74 | Mean :101.97 |
| ## 3rd Qu. | :2016-07-01 | 3rd Qu.:118.98 | 3rd Qu.:119.92 | 3rd Qu.:118.22 |
| ## Max. | :2017-12-29 | Max. :175.11 | Max. :177.20 | Max. :174.86 |
| ## AAPL.Close | | AAPL.Volume | AAPL.Adjusted | |
| ## Min. | : 55.79 | Min. : 11475900 | Min. : 39.17 | |
| ## 1st Qu. | : 78.44 | 1st Qu.: 33257300 | 1st Qu.: 58.93 | |
| ## Median | : 99.52 | Median : 53583400 | Median : 93.16 | |
| ## Mean | :102.87 | Mean : 68962505 | Mean : 91.97 | |
| ## 3rd Qu. | :119.25 | 3rd Qu.: 88569600 | 3rd Qu.:113.01 | |
| ## Max. | :176.42 | Max. :376530000 | Max. :173.07 | |

```
head(AAPL)
```

| | AAPL.Open | AAPL.High | AAPL.Low | AAPL.Close | AAPL.Volume |
|------------------|-----------|-----------|----------|------------|-------------|
| ## 2012-01-03 | 58.48571 | 58.92857 | 58.42857 | 58.74714 | 75555200 |
| ## 2012-01-04 | 58.57143 | 59.24000 | 58.46857 | 59.06286 | 65005500 |
| ## 2012-01-05 | 59.27857 | 59.79286 | 58.95286 | 59.71857 | 67817400 |
| ## 2012-01-06 | 59.96714 | 60.39286 | 59.88857 | 60.34286 | 79573200 |
| ## 2012-01-09 | 60.78571 | 61.10714 | 60.19286 | 60.24714 | 98506100 |
| ## 2012-01-10 | 60.84428 | 60.85714 | 60.21429 | 60.46286 | 64549100 |
| ## AAPL.Adjusted | | | | | |
| ## 2012-01-03 | | 39.17277 | | | |
| ## 2012-01-04 | | 39.38329 | | | |
| ## 2012-01-05 | | 39.82052 | | | |
| ## 2012-01-06 | | 40.23681 | | | |
| ## 2012-01-09 | | 40.17297 | | | |
| ## 2012-01-10 | | 40.31681 | | | |

```
names(AAPL)
```

```
## [1] "AAPL.Open"      "AAPL.High"       "AAPL.Low"        "AAPL.Close"
## [5] "AAPL.Volume"    "AAPL.Adjusted"
```

```
data <- ts(AAPL,start=c(2012,1),end=c(2018,12), frequency = 12)
data=data[,3]

#####Train and Test data#####
train_data = window(data,start=c(2012,1), end=c(2016,12))
test_data = window(data,start=c(2017,1), end=c(2018,12))
train_data
```

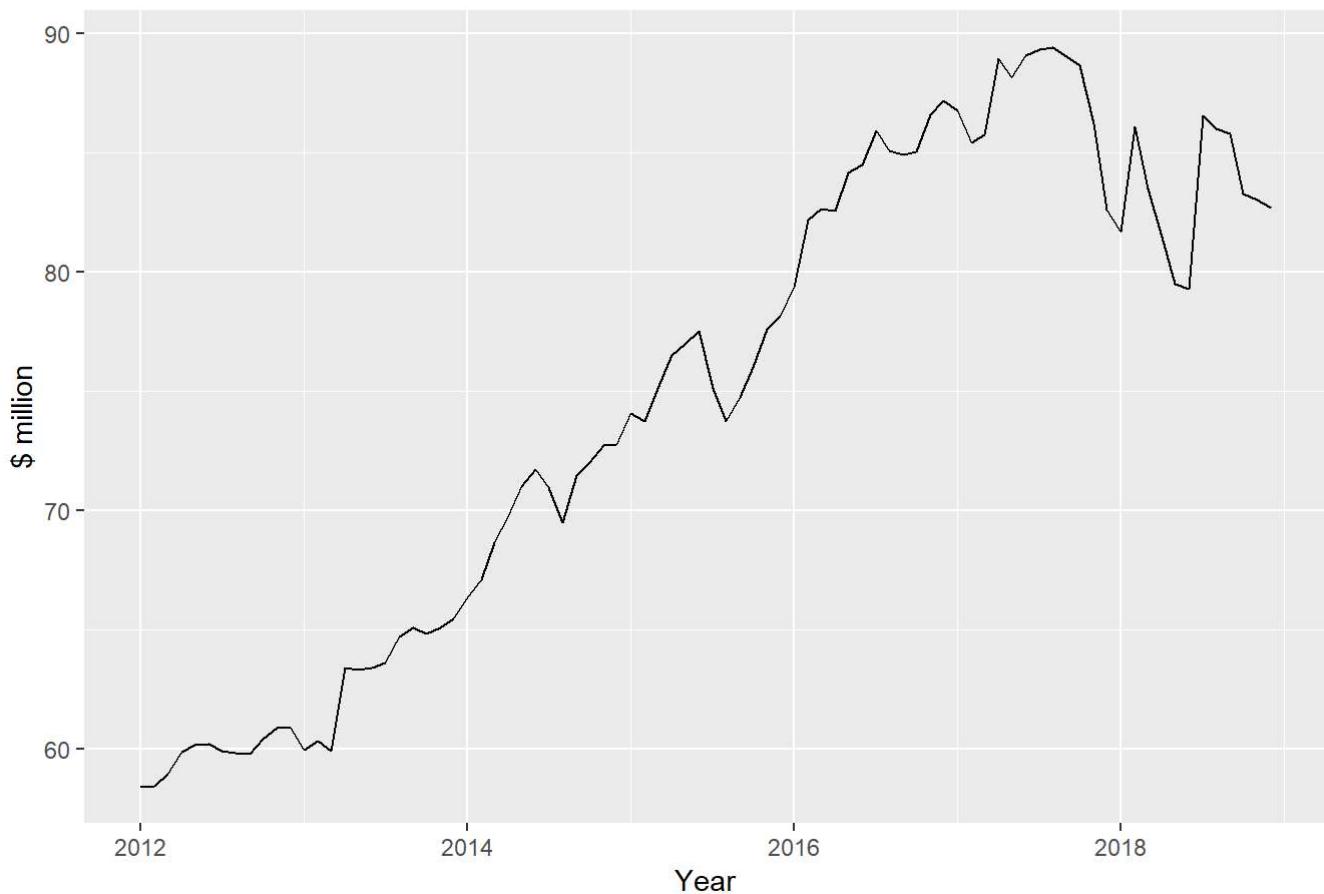
```
##           Jan      Feb      Mar      Apr      May      Jun      Jul
## 2012 58.42857 58.46857 58.95286 59.88857 60.19286 60.21429 59.90143
## 2013 59.96429 60.32857 59.93572 63.39000 63.30571 63.39571 63.62714
## 2014 66.36857 67.10000 68.65143 69.79285 71.01286 71.71429 70.98428
## 2015 74.09143 73.75429 75.12143 76.52857 76.96714 77.50285 75.14286
## 2016 79.39286 82.20000 82.65000 82.57143 84.15000 84.49715 85.91572
##           Aug      Sep      Oct      Nov      Dec
## 2012 59.82143 59.80857 60.42285 60.90000 60.93000
## 2013 64.72429 65.07858 64.85429 65.08000 65.45715
## 2014 69.51857 71.47143 72.01714 72.72429 72.78571
## 2015 73.74571 74.75714 76.01714 77.58714 78.14286
## 2016 85.07571 84.91428 85.03714 86.58000 87.18714
```

```
test_data
```

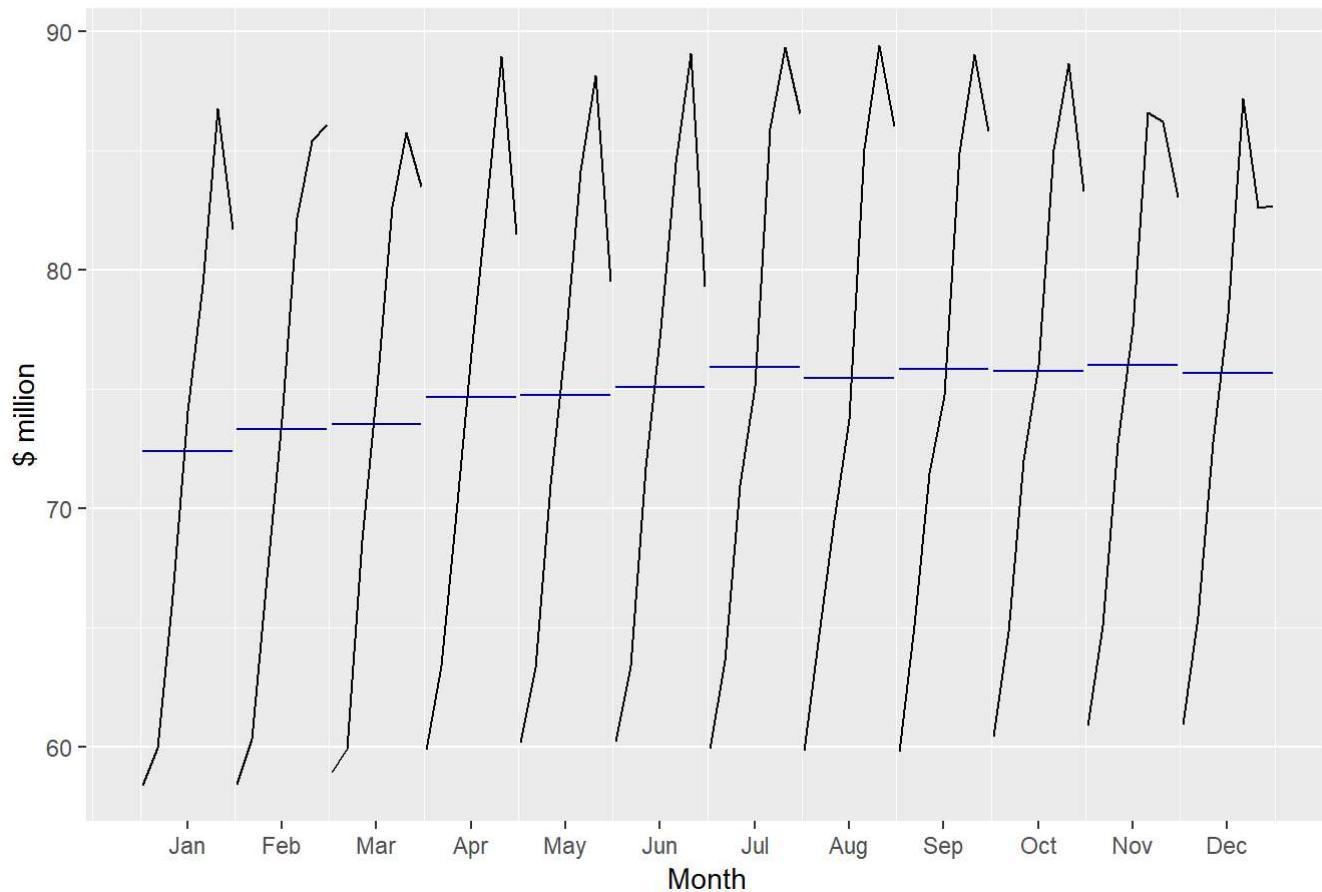
```
##           Jan      Feb      Mar      Apr      May      Jun      Jul
## 2017 86.74715 85.42000 85.76857 88.93000 88.14286 89.05714 89.32858
## 2018 81.70143 86.10143 83.50285 81.48857 79.51714 79.28571 86.57143
##           Aug      Sep      Oct      Nov      Dec
## 2017 89.42857 89.04857 88.64286 86.21571 82.60714
## 2018 86.01857 85.78571 83.28571 83.03286 82.69428
```

```
autplot(data) + ggtitle("Apple stock price") + ylab("$ million") + xlab("Year")
```

Apple stock price

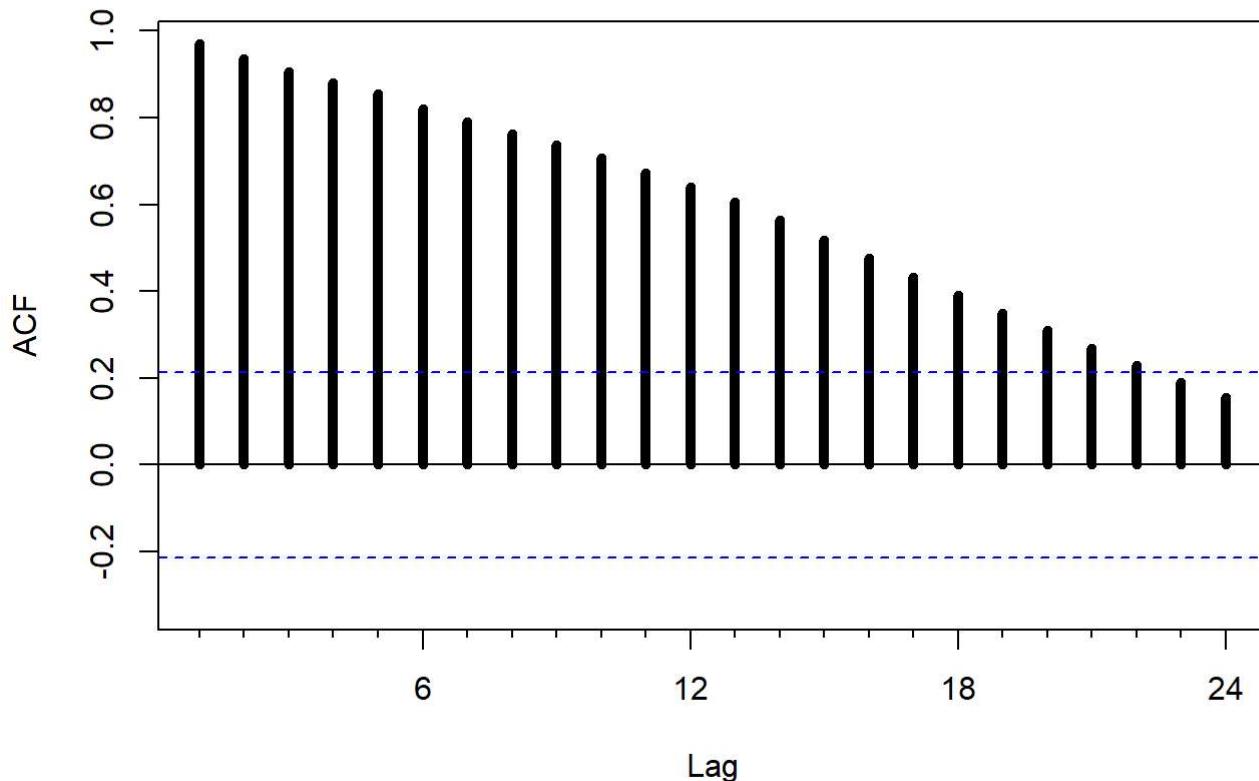


```
ggsubseriesplot(data) + ylab("$ million") + ggtitle("Seasonal subseries plot:Apple stock price")
```

Seasonal subseries plot:Apple stock price

```
Acf(data, lwd=5, main="Apple stock price")
```

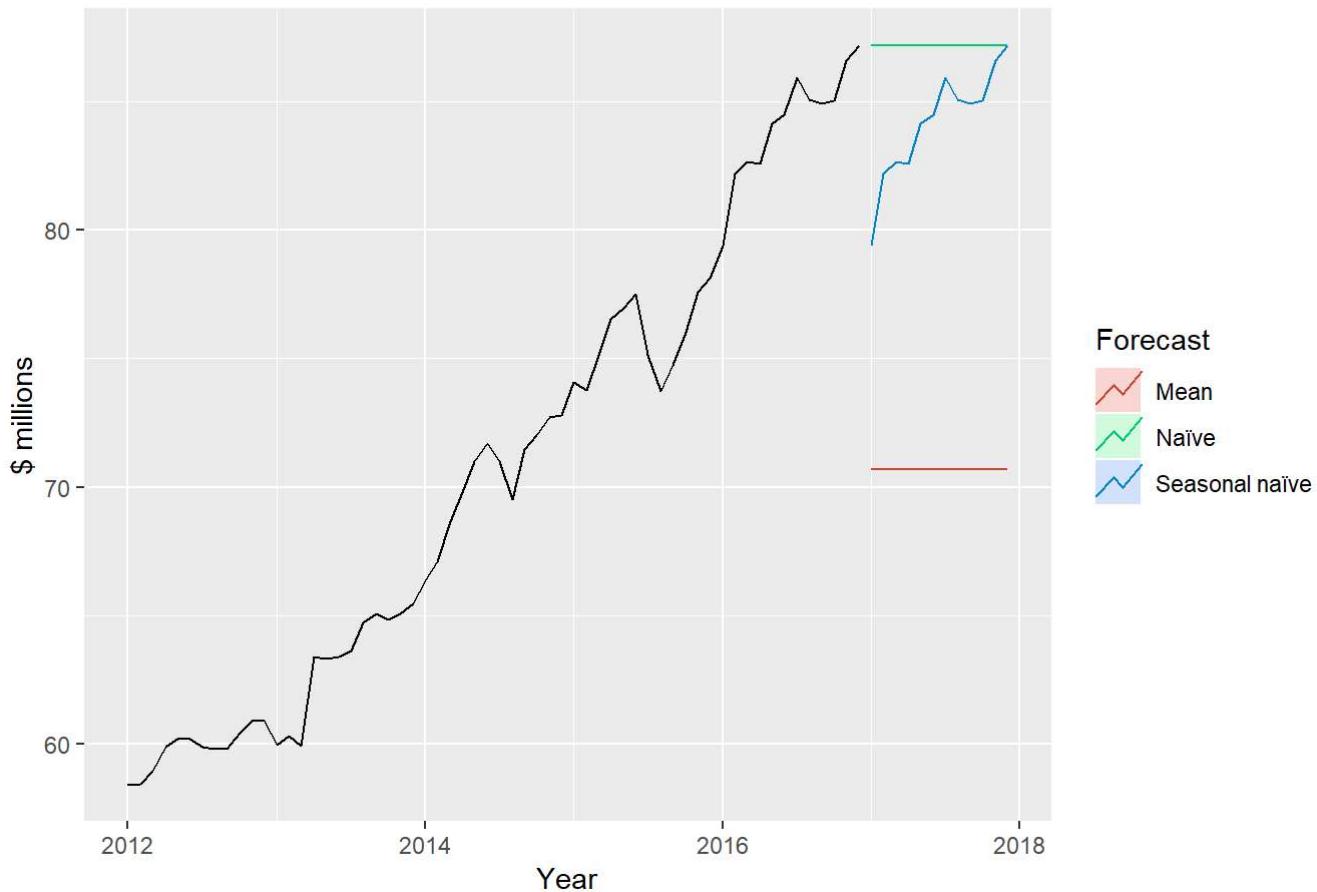
Apple stock price



```
#####
#Mean, Naive, Seasonal Naive#####
fit.mean=meanf(train_data,h=12)
fit.naive=naive(train_data,h=12)
fit.snaive=snaive(train_data,h=12)

autoplot(train_data) +
  autolayer(meanf(train_data, h=12),
            series="Mean", PI=FALSE) +
  autolayer(naive(train_data, h=12),
            series="Naïve", PI=FALSE) +
  autolayer(snaive(train_data, h=12),
            series="Seasonal naïve", PI=FALSE) +
  ggtitle("Forecasts Apple stock price") +
  xlab("Year") + ylab("$ millions") +
  guides(colour=guide_legend(title="Forecast"))
```

Forecasts Apple stock price

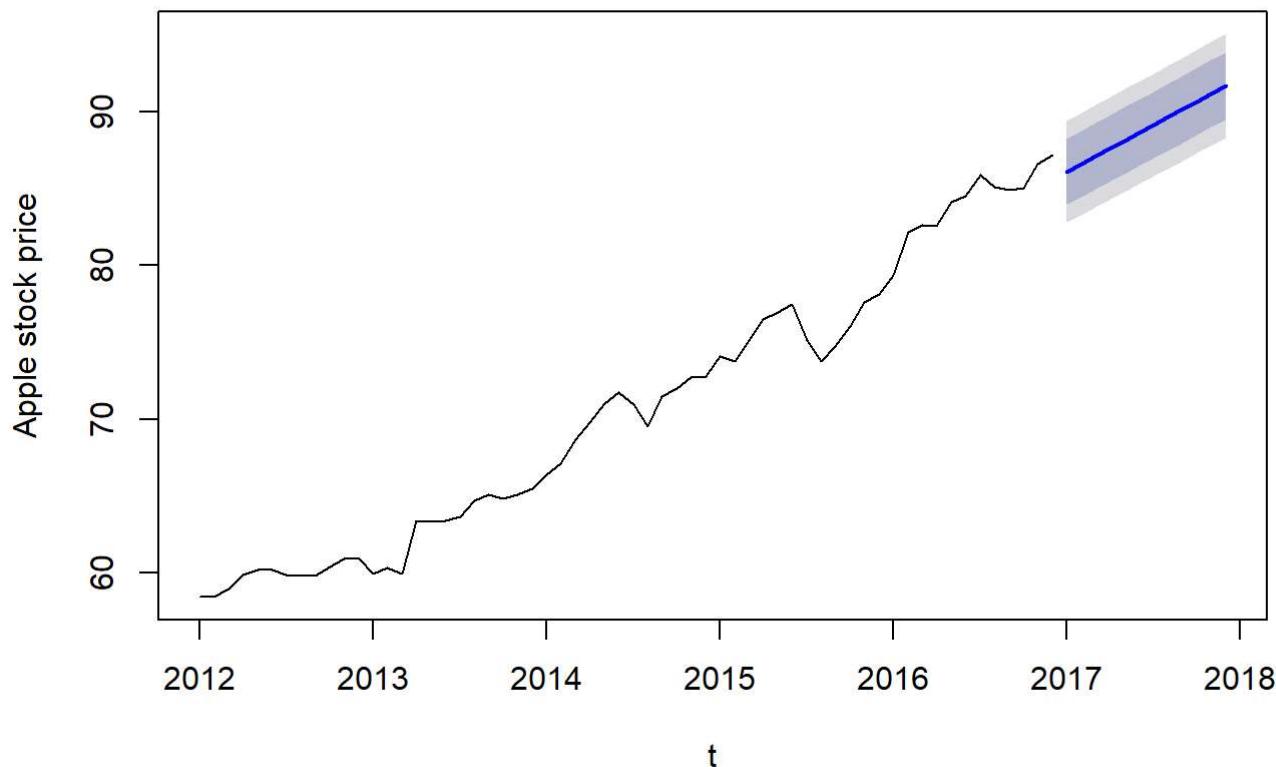


```
#####Linear Trend#####
linear_reg <- tslm(train_data ~ trend)
fit.ts1=forecast(linear_reg, h=12)
summary(fit.ts1)
```

```
##  
## Forecast method: Linear regression model  
##  
## Model Information:  
##  
## Call:  
## tslm(formula = train_data ~ trend)  
##  
## Coefficients:  
## (Intercept)      trend  
##      55.246      0.506  
##  
##  
## Error measures:  
##  
##               ME      RMSE      MAE      MPE      MAPE      MASE  
## Training set 1.184961e-16 1.572859 1.299547 -0.03258308 1.868646 0.2134477  
##  
##          ACF1  
## Training set 0.7859229  
##  
##  
## Forecasts:  
##  
##       Point Forecast    Lo 80     Hi 80     Lo 95     Hi 95  
## Jan 2017   86.11242 83.96893 88.25592 82.80253 89.42231  
## Feb 2017   86.61843 84.47148 88.76538 83.30321 89.93365  
## Mar 2017   87.12445 84.97394 89.27495 83.80373 90.44516  
## Apr 2017   87.63046 85.47629 89.78463 84.30408 90.95683  
## May 2017   88.13647 85.97853 90.29441 84.80427 91.46866  
## Jun 2017   88.64248 86.48067 90.80430 85.30431 91.98066  
## Jul 2017   89.14849 86.98270 91.31428 85.80418 92.49281  
## Aug 2017   89.65451 87.48464 91.82437 86.30389 93.00512  
## Sep 2017   90.16052 87.98647 92.33457 86.80345 93.51759  
## Oct 2017   90.66653 88.48820 92.84486 87.30285 94.03021  
## Nov 2017   91.17254 88.98983 93.35526 87.80209 94.54300  
## Dec 2017   91.67856 89.49135 93.86576 88.30118 95.05593
```

```
plot(fit.ts1, ylab="Apple stock price",  
     xlab="t")
```

Forecasts from Linear regression model



```
#####Season + Trend#####
linear_season <- tslm(train_data ~ trend + season)
fit.ts1m2=forecast(linear_season, h=12)
summary(fit.ts1m2)
```

```

##  

## Forecast method: Linear regression model  

##  

## Model Information:  

##  

## Call:  

## tslm(formula = train_data ~ trend + season)  

##  

## Coefficients:  

## (Intercept)      trend      season2      season3      season4  

##      54.8939     0.5102     0.2109     0.3927     1.2545  

##    season5      season6      season7      season8      season9  

##      1.4357     1.2647     0.4039    -0.6435    -0.5248  

##   season10     season11     season12  

##     -0.5713    -0.1769    -0.3609  

##  

##  

## Error measures:  

##               ME      RMSE      MAE      MPE      MAPE      MASE  

## Training set -1.184455e-16 1.401696 1.133838 -0.02238192 1.65084 0.1862304  

##           ACF1  

## Training set 0.7761691  

##  

## Forecasts:  

##          Point Forecast    Lo 80    Hi 80    Lo 95    Hi 95  

## Jan 2017 86.01664 83.69219 88.34110 82.41909 89.61420  

## Feb 2017 86.73778 84.41333 89.06224 83.14023 90.33534  

## Mar 2017 87.42979 85.10533 89.75424 83.83223 91.02734  

## Apr 2017 88.80178 86.47733 91.12624 85.20423 92.39934  

## May 2017 89.49321 87.16876 91.81767 85.89566 93.09077  

## Jun 2017 89.83236 87.50791 92.15681 86.23480 93.42991  

## Jul 2017 89.48179 87.15733 91.80624 85.88423 93.07934  

## Aug 2017 88.94464 86.62019 91.26910 85.34709 92.54220  

## Sep 2017 89.57350 87.24905 91.89795 85.97594 93.17106  

## Oct 2017 90.03721 87.71276 92.36167 86.43966 93.63477  

## Nov 2017 90.94179 88.61734 93.26624 87.34423 94.53934  

## Dec 2017 91.26807 88.94362 93.59252 87.67051 94.86563

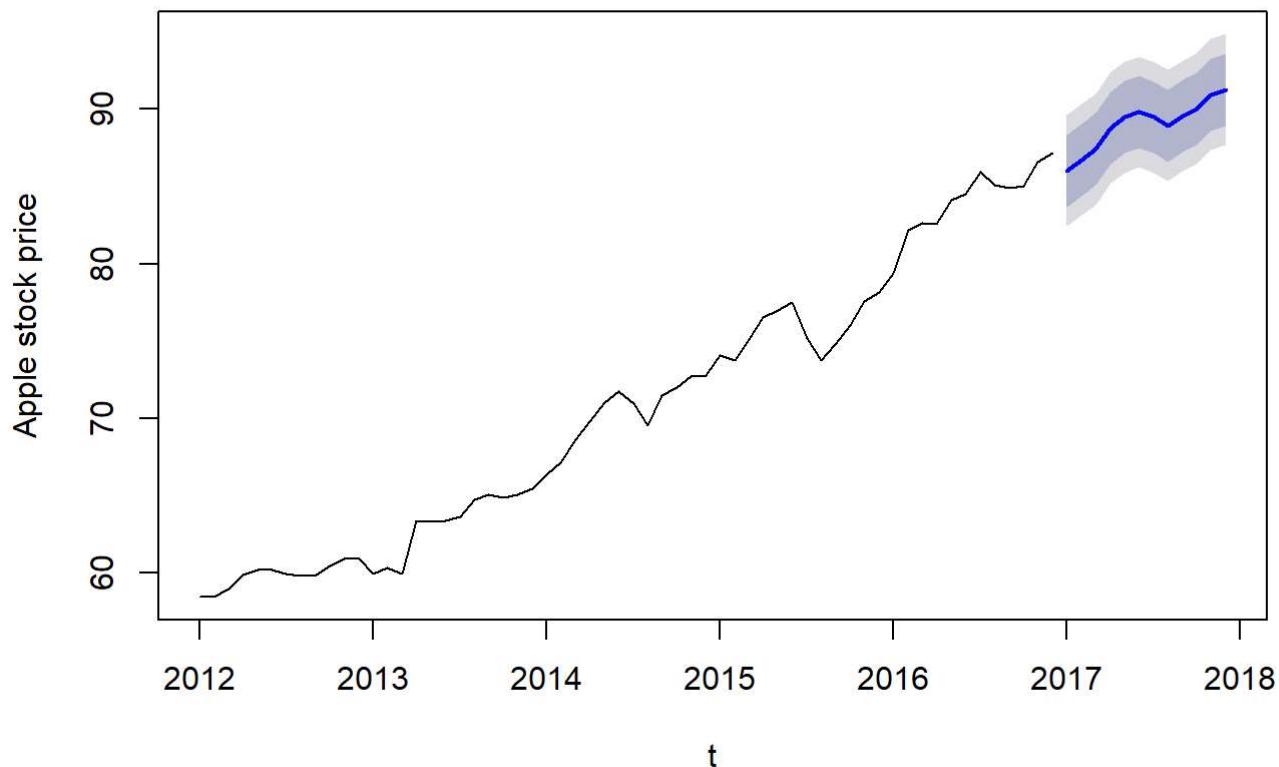
```

```

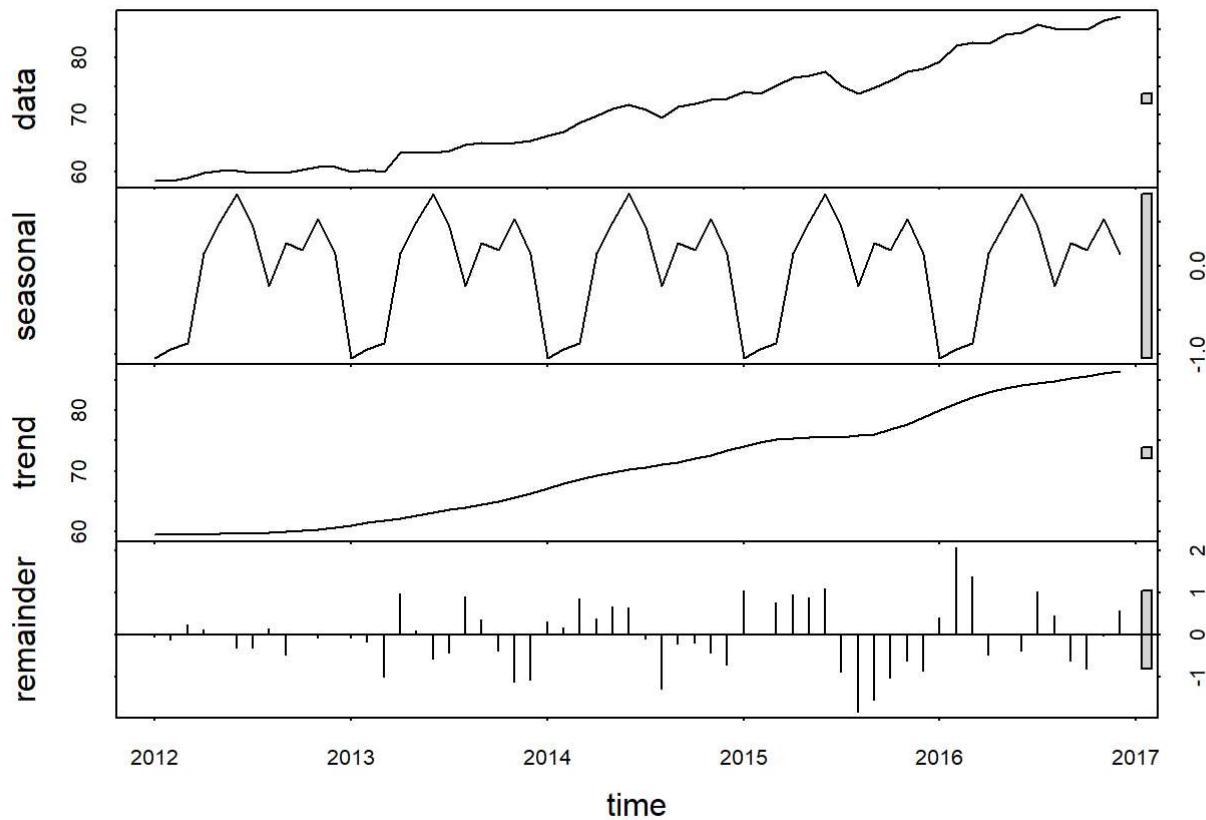
plot(fit.tsLM2, ylab="Apple stock price",
      xlab="t")

```

Forecasts from Linear regression model



```
#####STL decomposition#####
stl_decomp <- stl(train_data, t.window=12, s.window="periodic")
plot(stl_decomp)
```



```
fit.stl <- forecast(stl_decomp,h=12)
summary(fit.stl)
```

```

##  

## Forecast method: STL + ETS(M,A,N)  

##  

## Model Information:  

## ETS(M,A,N)  

##  

## Call:  

## ets(y = x, model = etsmodel, allow.multiplicative.trend = allow.multiplicative.trend)  

##  

## Smoothing parameters:  

##   alpha = 0.9924  

##   beta  = 1e-04  

##  

## Initial states:  

##   l = 59.244  

##   b = 0.4363  

##  

## sigma: 0.0131  

##  

##      AIC     AICC      BIC  

## 241.7742 242.8853 252.2459  

##  

## Error measures:  

##  

##               ME      RMSE      MAE      MPE      MAPE      MASE  

## Training set 0.02738604 0.9168425 0.697892 0.007787811 0.9767164 0.1146272  

##  

##          ACF1  

## Training set 0.08221281  

##  

## Forecasts:  

##  

##       Point Forecast    Lo 80    Hi 80    Lo 95    Hi 95  

## Jan 2017 86.43741 84.96352 87.91131 84.18328 88.69154  

## Feb 2017 86.97168 84.88977 89.05360 83.78766 90.15570  

## Mar 2017 87.47681 84.92364 90.02999 83.57207 91.38156  

## Apr 2017 88.94046 85.98657 91.89436 84.42288 93.45805  

## May 2017 89.72354 86.41375 93.03334 84.66164 94.78544  

## Jun 2017 90.48050 86.84639 94.11460 84.92261 96.03838  

## Jul 2017 90.54774 86.61309 94.48238 84.53021 96.56526  

## Aug 2017 90.30809 86.09157 94.52462 83.85948 96.75671  

## Sep 2017 91.23445 86.75118 95.71772 84.37789 98.09102  

## Oct 2017 91.58504 86.84759 96.32249 84.33974 98.83034  

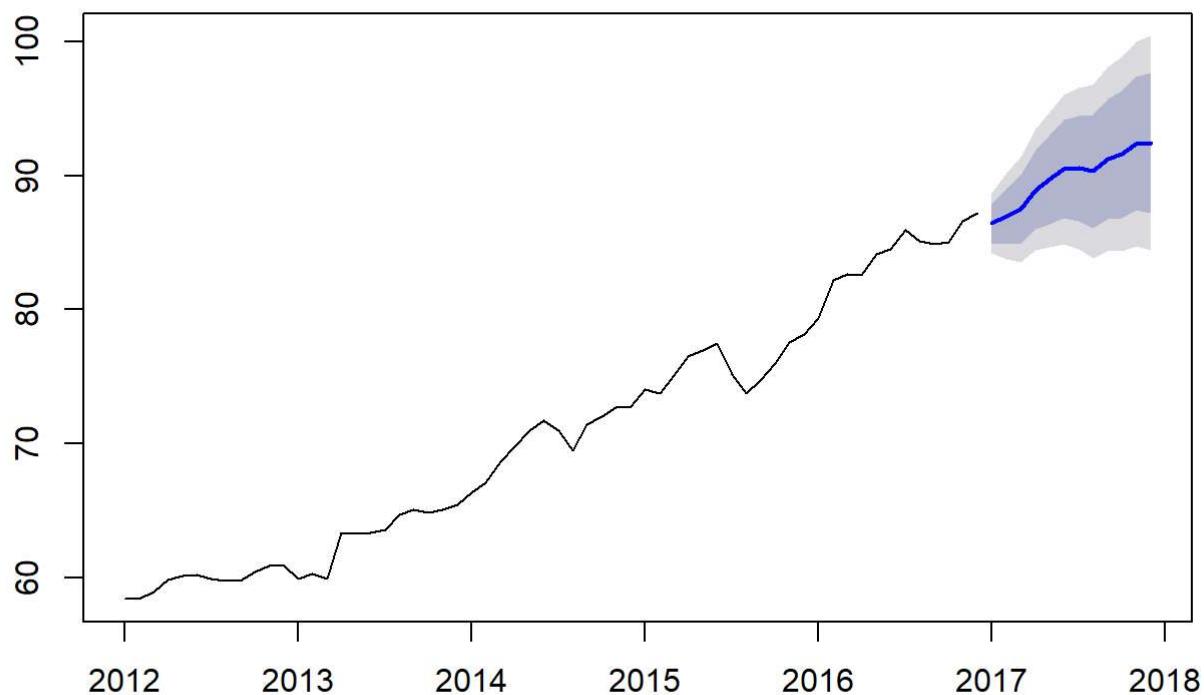
## Nov 2017 92.37649 87.39549 97.35749 84.75871 99.99428  

## Dec 2017 92.41983 87.20440 97.63526 84.44352 100.39614

```

```
plot(fit.stl)
```

Forecasts from STL + ETS(M,A,N)



```
#####
#ETS#####
library(forecast)
ets_forecast<-ets(train_data)
fit.ets_forecast <- forecast(ets_forecast)

#####
#SES#####
fit.ses <- ses(train_data, h = 12)
fit.ses <- forecast(fit.ses)
summary(fit.ses)
```

```

##  

## Forecast method: Simple exponential smoothing  

##  

## Model Information:  

## Simple exponential smoothing  

##  

## Call:  

##   ses(y = train_data, h = 12)  

##  

##   Smoothing parameters:  

##     alpha = 0.9999  

##  

##   Initial states:  

##     l = 58.4301  

##  

##     sigma: 1.0819  

##  

##     AIC      AICc      BIC  

## 259.0724 259.5010 265.3555  

##  

## Error measures:  

##               ME      RMSE      MAE      MPE      MAPE      MASE  

## Training set 0.4793308 1.063712 0.79413 0.6560745 1.10028 0.1304341  

##                      ACF1  

## Training set 0.07868901  

##  

## Forecasts:  

##           Point Forecast    Lo 80     Hi 80     Lo 95     Hi 95  

## Jan 2017    87.18708 85.80057 88.57359 85.06660 89.30756  

## Feb 2017    87.18708 85.22636 89.14780 84.18842 90.18574  

## Mar 2017    87.18708 84.78574 89.58842 83.51455 90.85961  

## Apr 2017    87.18708 84.41428 89.95988 82.94644 91.42772  

## May 2017    87.18708 84.08701 90.28715 82.44593 91.92823  

## Jun 2017    87.18708 83.79113 90.58303 81.99342 92.38074  

## Jul 2017    87.18708 83.51904 90.85512 81.57730 92.79686  

## Aug 2017    87.18708 83.26579 91.10837 81.18999 93.18417  

## Sep 2017    87.18708 83.02793 91.34623 80.82621 93.54795  

## Oct 2017    87.18708 82.80296 91.57120 80.48214 93.89202  

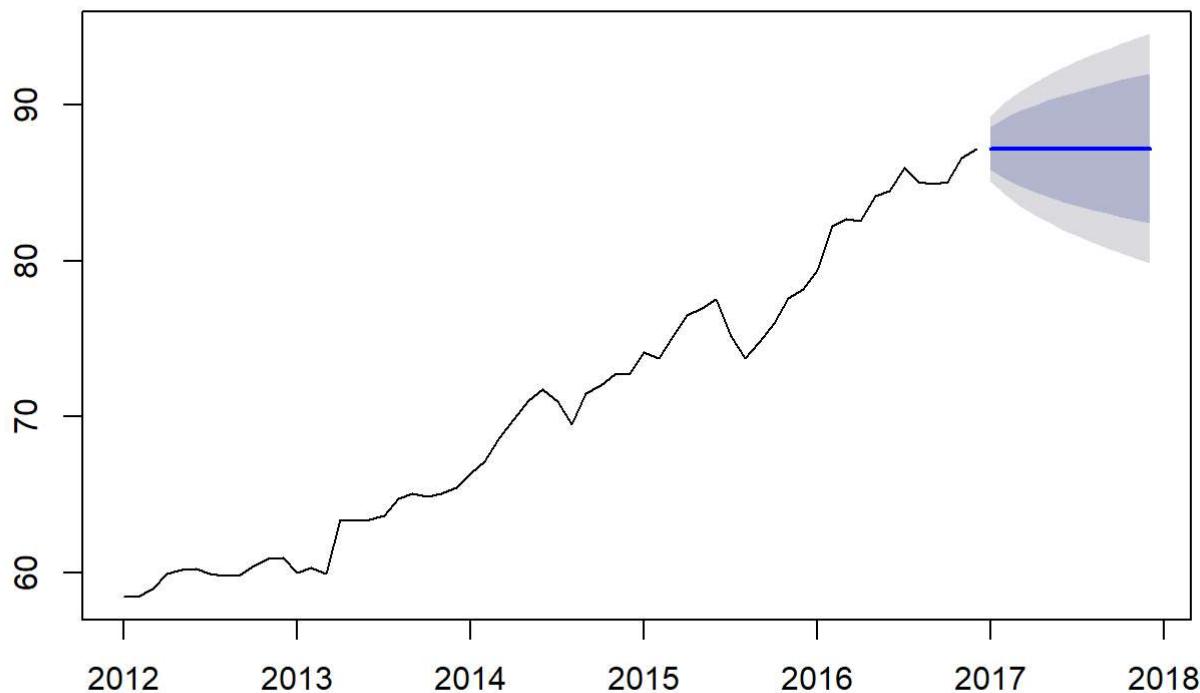
## Nov 2017    87.18708 82.58898 91.78518 80.15489 94.21927  

## Dec 2017    87.18708 82.38452 91.98964 79.84220 94.53196

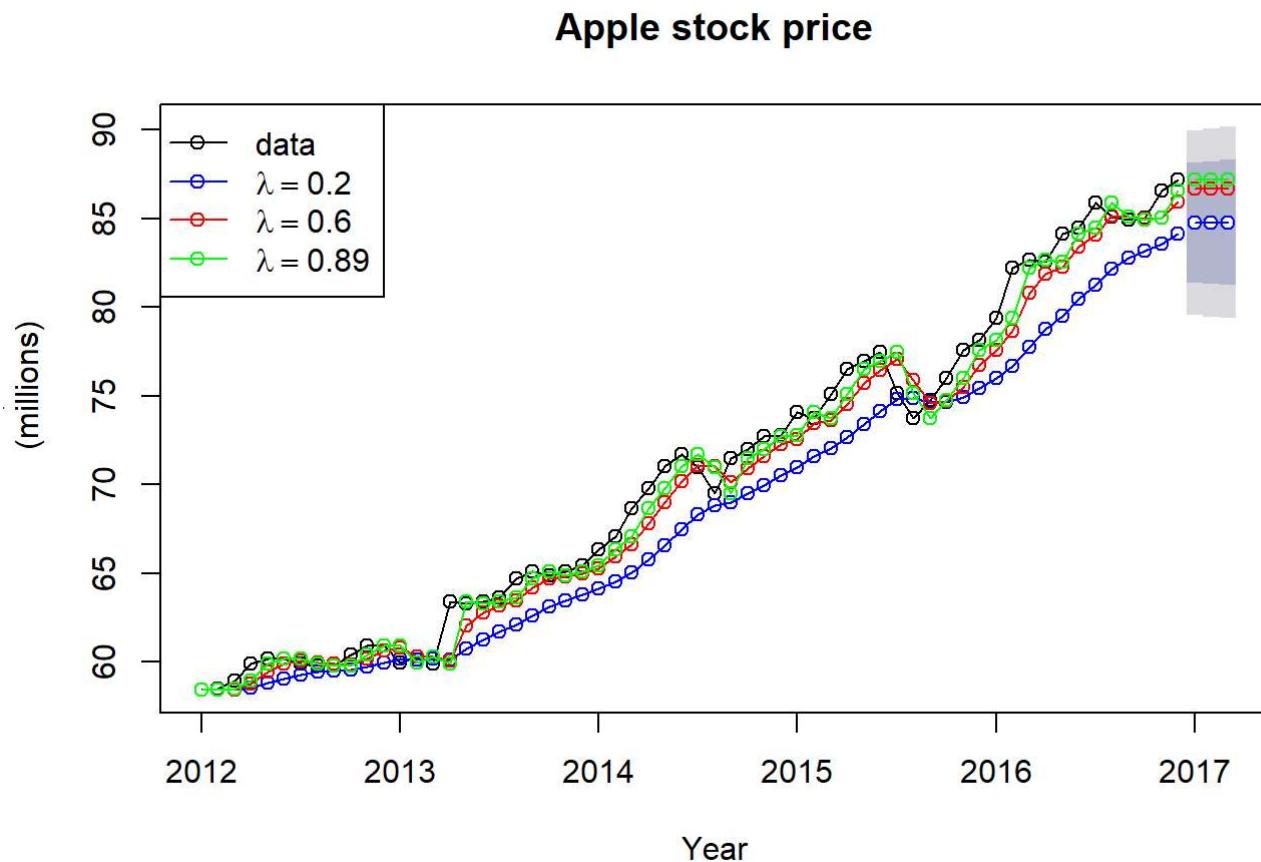
```

```
plot(fit.ses)
```

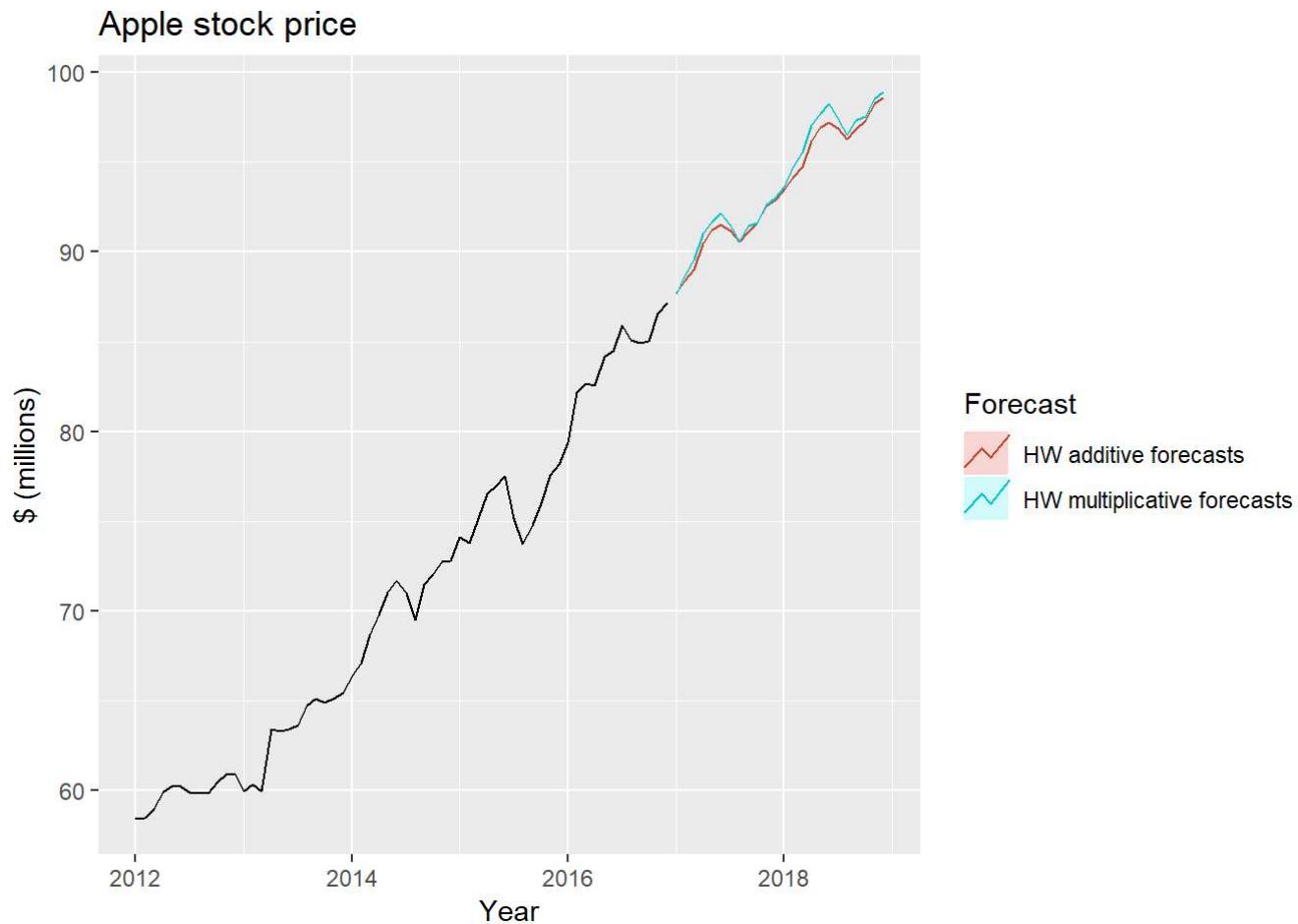
Forecasts from Simple exponential smoothing



```
fit1 <-ses(train_data, alpha=0.2, initial="simple", h=3)
fit2 <-ses(train_data, alpha=0.6, initial="simple", h=3)
fit3 <-ses(train_data, h=3)
plot(fit1,main="Apple stock price", ylab="$
(millions)", xlab="Year", fcol="white", type="o")
lines(fitted(fit1), col="blue", type="o")
lines(fitted(fit2), col="red", type="o")
lines(fitted(fit3), col="green", type="o")
lines(fit1$mean, col="blue", type="o")
lines(fit2$mean, col="red", type="o")
lines(fit3$mean, col="green", type="o")
legend("topleft",lty=1, col=c(1,"blue","red","green"),
c("data", expression(lambda == 0.2), expression(lambda == 0.6),
expression(lambda == 0.89)),pch=1)
```



```
#####
# HW Additive and Multiplicative #####
fit1_add <- hw(train_data, seasonal="additive")
fit1_add <- forecast(fit1_add)
fit2_multi <- hw(train_data, seasonal="multiplicative")
fit2_multi <- forecast(fit2_multi)
autoplot(train_data) +
  autolayer(fit1_add, series="HW additive forecasts", PI=FALSE) +
  autolayer(fit2_multi, series="HW multiplicative forecasts", PI=FALSE) +
  xlab("Year") +
  ylab("$ (millions)") +
  ggtitle("Apple stock price") +
  guides(colour=guide_legend(title="Forecast"))
```



```
##### Holt's Linear trend#####
fit.hlinear <- holt(train_data, h=3)
fit.hlinear <- forecast(fit.hlinear)
summary(fit.hlinear)
```

```

##  

## Forecast method: Holt's method  

##  

## Model Information:  

## Holt's method  

##  

## Call:  

##   holt(y = train_data, h = 3)  

##  

##   Smoothing parameters:  

##     alpha = 0.9999  

##     beta  = 1e-04  

##  

##   Initial states:  

##     l = 57.9212  

##     b = 0.4885  

##  

##   sigma:  0.9808  

##  

##      AIC      AICC      BIC  

## 249.1990 250.3101 259.6707  

##  

## Error measures:  

##      ME      RMSE      MAE      MPE      MAPE  

## Training set -0.0004784057 0.947577 0.6877916 -0.03113668 0.9677082  

##           MASE      ACF1  

## Training set 0.1129682 0.07482566  

##  

## Forecasts:  

##      Point Forecast    Lo 80     Hi 80     Lo 95     Hi 95  

## Jan 2017      87.67558 86.41859 88.93258 85.75318 89.59799  

## Feb 2017      88.16404 86.38639 89.94169 85.44535 90.88272  

## Mar 2017      88.65249 86.47525 90.82974 85.32269 91.98230

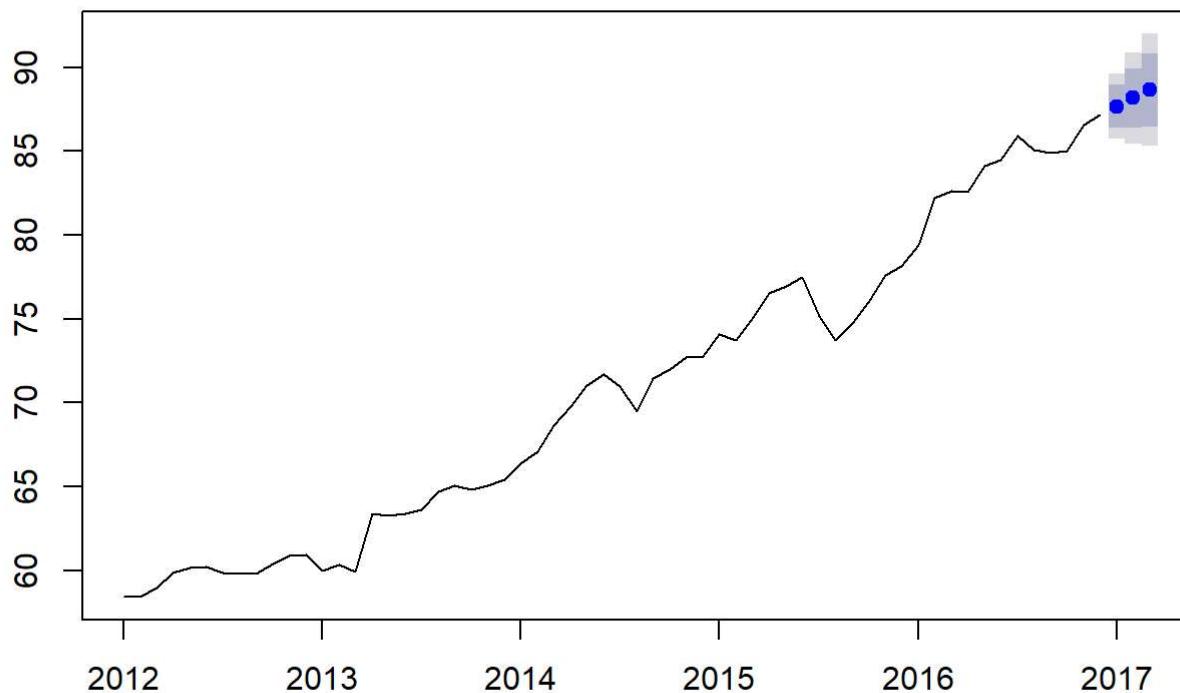
```

```

plot(fit.hlinear, main = "Holt's Linear Trend")
lines(train_data)

```

Holt's Linear Trend



```
#####Check stationarity#####
ndiffs(train_data)
```

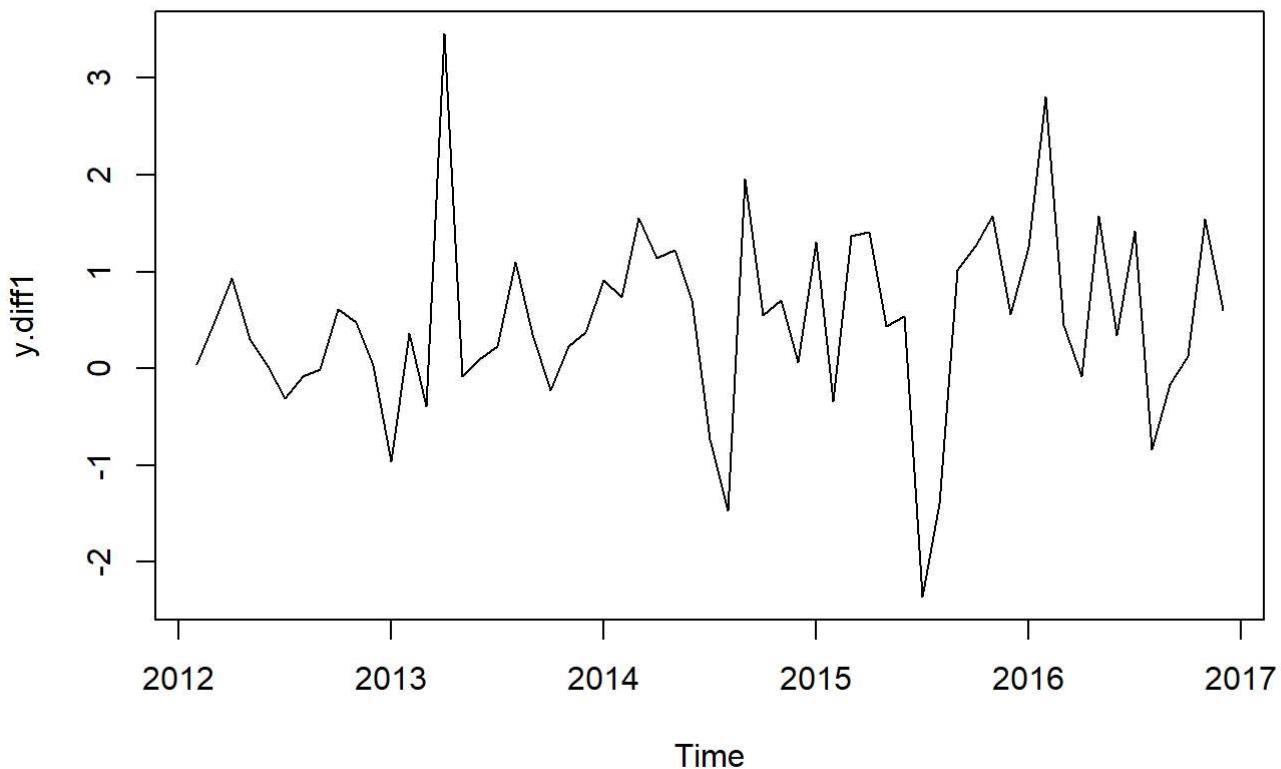
```
## [1] 1
```

```
y.diff1 = diff(train_data, differences = 1)
adf.test(y.diff1, alternative = "stationary")
```

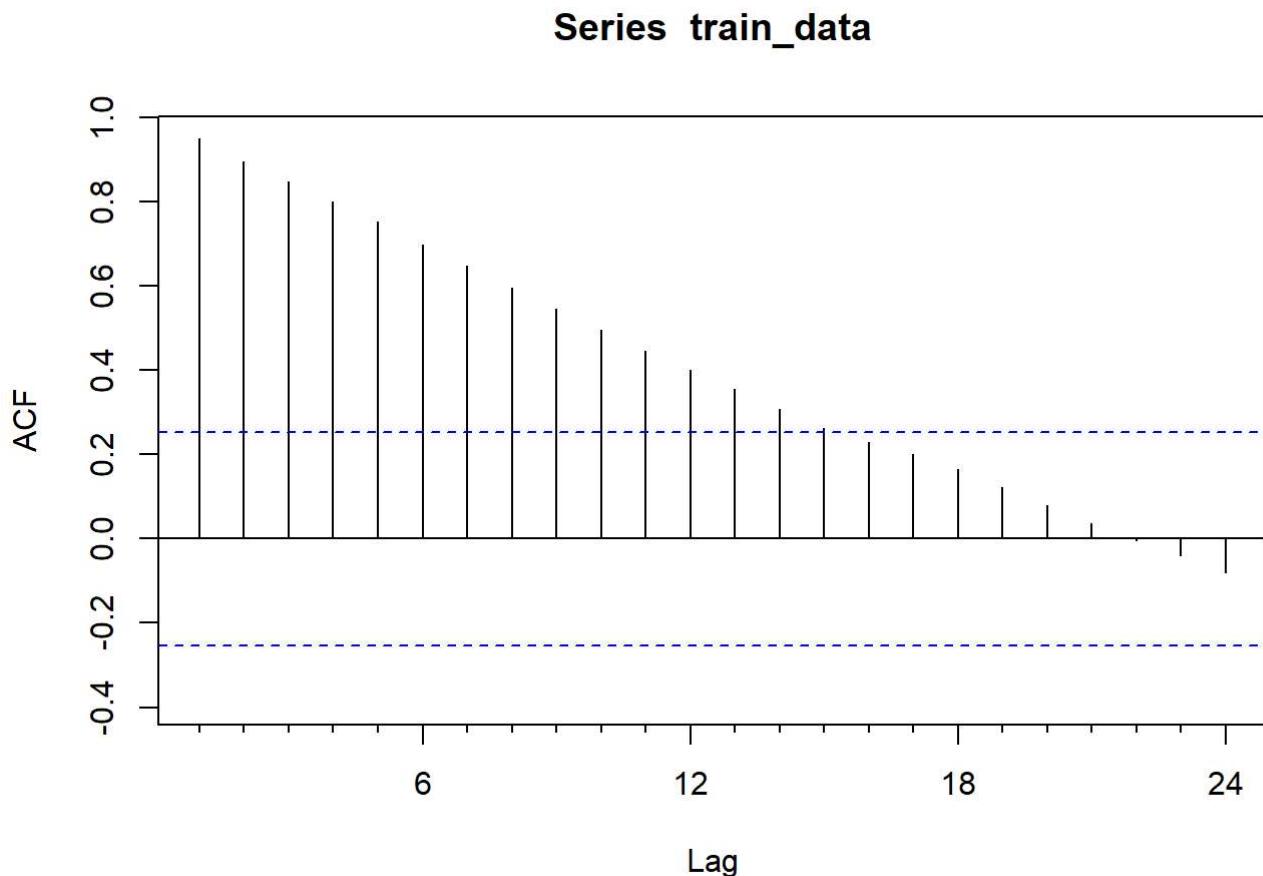
```
## Warning in adf.test(y.diff1, alternative = "stationary"): p-value smaller
## than printed p-value
```

```
##
## Augmented Dickey-Fuller Test
##
## data: y.diff1
## Dickey-Fuller = -4.3407, Lag order = 3, p-value = 0.01
## alternative hypothesis: stationary
```

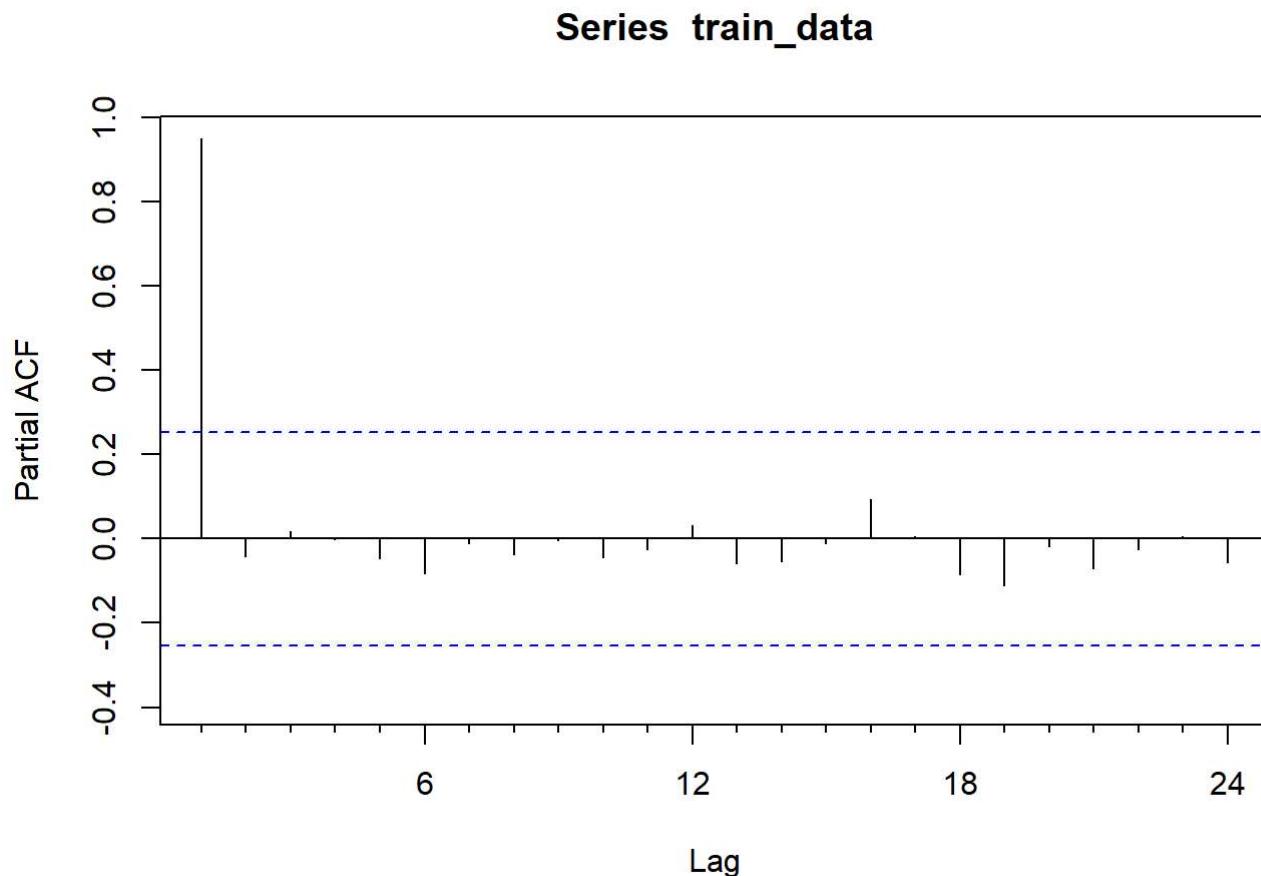
```
plot(y.diff1)
```



```
Acf(train_data)
```



```
Pacf(train_data)
```

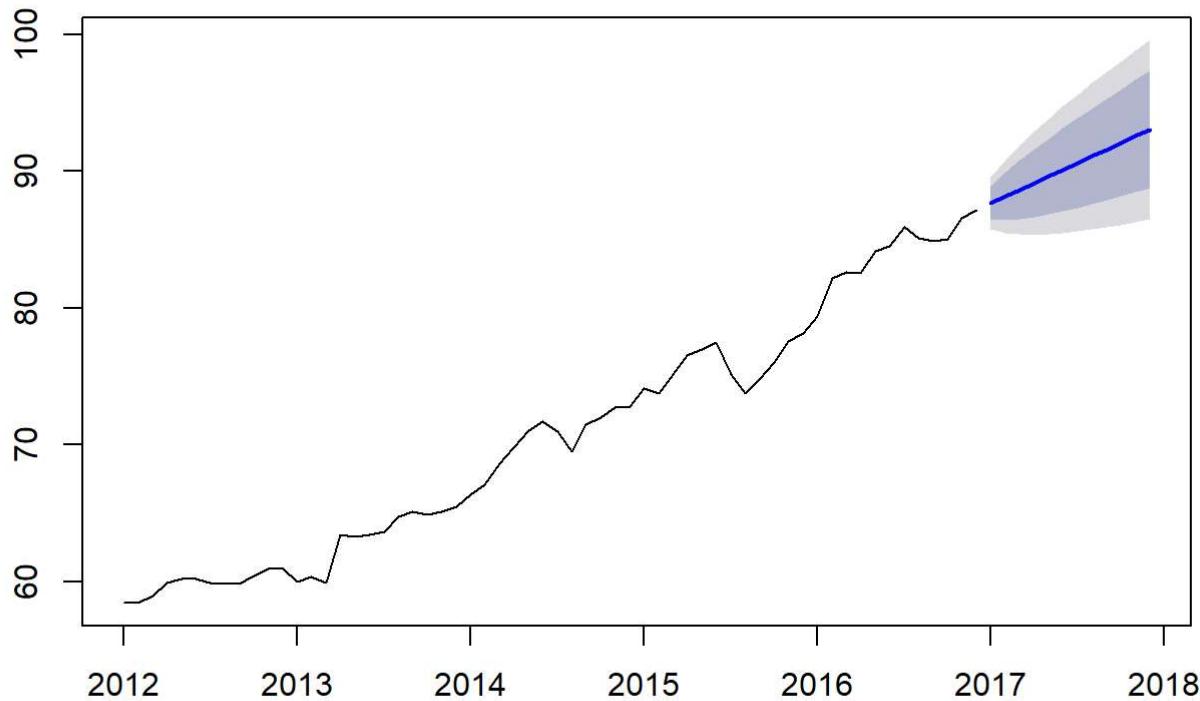


```
#####Auto ARIMA#####
y.arima <- auto.arima(train_data)
fit.arima <- forecast(y.arima, h=12)
summary(fit.arima)
```

```
##  
## Forecast method: ARIMA(0,1,0) with drift  
##  
## Model Information:  
## Series: train_data  
## ARIMA(0,1,0) with drift  
##  
## Coefficients:  
##      drift  
##      0.4874  
## s.e.  0.1244  
##  
## sigma^2 estimated as 0.9288:  log likelihood=-81.03  
## AIC=166.07  AICc=166.28  BIC=170.22  
##  
## Error measures:  
##               ME      RMSE      MAE      MPE      MAPE  
## Training set 0.0009656851 0.9475482 0.6883235 -0.02889026 0.9686066  
##                  MASE      ACF1  
## Training set 0.1130556 0.07441283  
##  
## Forecasts:  
##      Point Forecast    Lo 80     Hi 80     Lo 95     Hi 95  
## Jan 2017      87.67457 86.43948 88.90967 85.78567 89.56348  
## Feb 2017      88.16201 86.41533 89.90869 85.49069 90.83333  
## Mar 2017      88.64944 86.51020 90.78868 85.37775 91.92113  
## Apr 2017      89.13687 86.66669 91.60706 85.35906 92.91469  
## May 2017      89.62431 86.86256 92.38606 85.40058 93.84804  
## Jun 2017      90.11174 87.08640 93.13708 85.48488 94.73860  
## Jul 2017      90.59917 87.33143 93.86692 85.60159 95.59676  
## Aug 2017      91.08661 87.59324 94.57997 85.74397 96.42925  
## Sep 2017      91.57404 87.86877 95.27932 85.90731 97.24077  
## Oct 2017      92.06148 88.15577 95.96718 86.08822 98.03473  
## Nov 2017      92.54891 88.45257 96.64524 86.28411 98.81371  
## Dec 2017      93.03634 88.75786 97.31482 86.49297 99.57971
```

```
plot(fit.arima)
```

Forecasts from ARIMA(0,1,0) with drift



```
#####
#Comparison#####
a.mean=accuracy(fit.mean,test_data)
a.naive=accuracy(fit.naive,test_data)
a.snaive=accuracy(fit.snaive,test_data)
a.linear=accuracy(fit.tsLM1,test_data)
a.linear_season=accuracy(fit.tsLM2,test_data)
a.ets=accuracy(fit.ets_forecast,test_data)
a.ses=accuracy(fit.ses,test_data)
a.stl=accuracy(fit.stl,test_data)
a.holt=accuracy(fit.hlinear,test_data)
a.multi=accuracy(fit1_add,test_data)
a.add=accuracy(fit2_multi,test_data)
a.arima=accuracy(fit.arima,test_data)

a.table<-rbind(a.mean, a.naive, a.snaive, a.linear, a.linear_season, a.ets, a.ses, a.stl, a.holt, a.add, a.multi, a.arima)
a.table
```

```

##               ME      RMSE      MAE      MPE      MAPE
## Training set 4.503053e-15 8.9032051 7.7063175 -1.574440099 11.0144268
## Test set     1.676571e+01 16.8872841 16.7657148 19.128589860 19.1285899
## Training set 4.874334e-01 1.0726601 0.8075307 0.667174022 1.1188413
## Test set     2.576216e-01 2.0390045 1.7871442 0.239925930 2.0567580
## Training set 6.088363e+00 6.5115185 6.0883632 8.140173840 8.1401738
## Test set     3.263810e+00 4.4078055 4.0878580 3.676284667 4.6707592
## Training set 1.184961e-16 1.5728594 1.2995469 -0.032583082 1.8686463
## Test set     -1.450725e+00 3.1333447 1.8732924 -1.719282838 2.1971936
## Training set -1.184455e-16 1.4016964 1.1338384 -0.022381915 1.6508397
## Test set     -1.601785e+00 2.9902011 1.8255601 -1.887899865 2.1424698
## Training set 3.771897e-03 0.9523994 0.6980538 -0.024680434 0.9840451
## Test set     -7.960162e+00 9.8077564 7.9601624 -9.551741436 9.5517414
## Training set 4.793308e-01 1.0637119 0.7941300 0.656074513 1.1002801
## Test set     2.576823e-01 2.0390122 1.7871544 0.239995419 2.0567682
## Training set 2.738604e-02 0.9168425 0.6978920 0.007787811 0.9767164
## Test set     -2.430410e+00 3.6501703 2.4820320 -2.833431113 2.8929399
## Training set -4.784057e-04 0.9475770 0.6877916 -0.031136676 0.9677082
## Test set     -2.185467e+00 2.3599983 2.1854675 -2.548379708 2.5483797
## Training set 2.287631e-02 1.0435227 0.8090299 0.031483026 1.1445557
## Test set     -8.603157e+00 10.3822584 8.6031574 -10.315422546 10.3154225
## Training set 1.305267e-02 0.8090733 0.6158147 -0.014935041 0.8737645
## Test set     -8.205216e+00 9.9776680 8.2052156 -9.843121038 9.8431210
## Training set 9.656851e-04 0.9475482 0.6883235 -0.028890263 0.9686066
## Test set     -2.910696e+00 3.9930551 2.9106956 -3.389624529 3.3896245
##               MASE      ACF1 Theil's U
## Training set 1.2657454 0.94843626      NA
## Test set     2.7537311 0.42429116 9.689557
## Training set 0.1326351 0.07489653      NA
## Test set     0.2935344 0.42429116 1.224775
## Training set 1.0000000 0.79681952      NA
## Test set     0.6714215 0.29812931 2.318251
## Training set 0.2134477 0.78592295      NA
## Test set     0.3076841 0.44862792 1.892951
## Training set 0.1862304 0.77616906      NA
## Test set     0.2998442 0.38271319 1.805318
## Training set 0.1146538 0.11073137      NA
## Test set     1.3074388 0.83806826 4.204542
## Training set 0.1304341 0.07868901      NA
## Test set     0.2935361 0.42429116 1.224779
## Training set 0.1146272 0.08221281      NA
## Test set     0.4076682 0.45506900 2.200972
## Training set 0.1129682 0.07482566      NA
## Test set     0.3589581 -0.13109590 2.921910
## Training set 0.1328814 0.49839658      NA
## Test set     1.4130493 0.82611868 4.460046
## Training set 0.1011462 0.01198980      NA
## Test set     1.3476883 0.82765257 4.285148
## Training set 0.1130556 0.07441283      NA
## Test set     0.4780752 0.44378624 2.404093

```

```
row.names(a.table)<-c('Mean training', 'Mean test', 'Naive training', 'Naive test', 'S. Naive tra  
ining', 'S. Naive test' , 'Linear training', 'Linear test', 'season-trend training', 'season-trend  
test', 'ets training', 'ets test', "ses training", "ses test", 'STL training', 'STL test', "Holt's  
Linear training", "Holt's Linear test", 'Add training', 'Add test', 'Multi training', 'Multi tes  
t', 'ARIMA training', 'ARIMA test')
```

```
#####Tabular format#####
a.table<-as.data.frame(a.table)
a.table
```

| | ME | RMSE | MAE | MPE |
|---------------------------|---------------|------------|-------------|---------------|
| ## Mean training | 4.503053e-15 | 8.9032051 | 7.7063175 | -1.574440099 |
| ## Mean test | 1.676571e+01 | 16.8872841 | 16.7657148 | 19.128589860 |
| ## Naive training | 4.874334e-01 | 1.0726601 | 0.8075307 | 0.667174022 |
| ## Naive test | 2.576216e-01 | 2.0390045 | 1.7871442 | 0.239925930 |
| ## S. Naive training | 6.088363e+00 | 6.5115185 | 6.0883632 | 8.140173840 |
| ## S. Naive test | 3.263810e+00 | 4.4078055 | 4.0878580 | 3.676284667 |
| ## Linear training | 1.184961e-16 | 1.5728594 | 1.2995469 | -0.032583082 |
| ## Linear test | -1.450725e+00 | 3.1333447 | 1.8732924 | -1.719282838 |
| ## season-trend training | -1.184455e-16 | 1.4016964 | 1.1338384 | -0.022381915 |
| ## season-trend test | -1.601785e+00 | 2.9902011 | 1.8255601 | -1.887899865 |
| ## ets training | 3.771897e-03 | 0.9523994 | 0.6980538 | -0.024680434 |
| ## ets test | -7.960162e+00 | 9.8077564 | 7.9601624 | -9.551741436 |
| ## ses training | 4.793308e-01 | 1.0637119 | 0.7941300 | 0.656074513 |
| ## ses test | 2.576823e-01 | 2.0390122 | 1.7871544 | 0.239995419 |
| ## STL training | 2.738604e-02 | 0.9168425 | 0.6978920 | 0.007787811 |
| ## STL test | -2.430410e+00 | 3.6501703 | 2.4820320 | -2.833431113 |
| ## Holt's Linear training | -4.784057e-04 | 0.9475770 | 0.6877916 | -0.031136676 |
| ## Holt's Linear test | -2.185467e+00 | 2.3599983 | 2.1854675 | -2.548379708 |
| ## Add training | 2.287631e-02 | 1.0435227 | 0.8090299 | 0.031483026 |
| ## Add test | -8.603157e+00 | 10.3822584 | 8.6031574 | -10.315422546 |
| ## Multi training | 1.305267e-02 | 0.8090733 | 0.6158147 | -0.014935041 |
| ## Multi test | -8.205216e+00 | 9.9776680 | 8.2052156 | -9.843121038 |
| ## ARIMA training | 9.656851e-04 | 0.9475482 | 0.6883235 | -0.028890263 |
| ## ARIMA test | -2.910696e+00 | 3.9930551 | 2.9106956 | -3.389624529 |
| | MAPE | MASE | ACF1 | Theil's U |
| ## Mean training | 11.0144268 | 1.2657454 | 0.94843626 | NA |
| ## Mean test | 19.1285899 | 2.7537311 | 0.42429116 | 9.689557 |
| ## Naive training | 1.1188413 | 0.1326351 | 0.07489653 | NA |
| ## Naive test | 2.0567580 | 0.2935344 | 0.42429116 | 1.224775 |
| ## S. Naive training | 8.1401738 | 1.0000000 | 0.79681952 | NA |
| ## S. Naive test | 4.6707592 | 0.6714215 | 0.29812931 | 2.318251 |
| ## Linear training | 1.8686463 | 0.2134477 | 0.78592295 | NA |
| ## Linear test | 2.1971936 | 0.3076841 | 0.44862792 | 1.892951 |
| ## season-trend training | 1.6508397 | 0.1862304 | 0.77616906 | NA |
| ## season-trend test | 2.1424698 | 0.2998442 | 0.38271319 | 1.805318 |
| ## ets training | 0.9840451 | 0.1146538 | 0.11073137 | NA |
| ## ets test | 9.5517414 | 1.3074388 | 0.83806826 | 4.204542 |
| ## ses training | 1.1002801 | 0.1304341 | 0.07868901 | NA |
| ## ses test | 2.0567682 | 0.2935361 | 0.42429116 | 1.224779 |
| ## STL training | 0.9767164 | 0.1146272 | 0.08221281 | NA |
| ## STL test | 2.8929399 | 0.4076682 | 0.45506900 | 2.200972 |
| ## Holt's Linear training | 0.9677082 | 0.1129682 | 0.07482566 | NA |
| ## Holt's Linear test | 2.5483797 | 0.3589581 | -0.13109590 | 2.921910 |
| ## Add training | 1.1445557 | 0.1328814 | 0.49839658 | NA |
| ## Add test | 10.3154225 | 1.4130493 | 0.82611868 | 4.460046 |
| ## Multi training | 0.8737645 | 0.1011462 | 0.01198980 | NA |
| ## Multi test | 9.8431210 | 1.3476883 | 0.82765257 | 4.285148 |
| ## ARIMA training | 0.9686066 | 0.1130556 | 0.07441283 | NA |
| ## ARIMA test | 3.3896245 | 0.4780752 | 0.44378624 | 2.404093 |