protein_consumption.R

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```
#Protein-Consumption-Analysis

#Loading the requited dataset
protein_consumption <- read.csv("C:/Users/sayal/Downloads/Protein_Consumption.csv",row.names = 1
)
#Print the data on console
head(protein_consumption)</pre>
```

```
##
                   Red.Meat White.Meat Egg Milk Fish Cereals Starchy.Foods
## Albania
                                                             42
                                      1
                                          1
## Austria
                          9
                                     14
                                                     2
                                                                             4
                                          4
                                               20
                                                             28
## Belgium
                         14
                                      9
                                          4
                                               18
                                                     5
                                                             27
                                                                             6
## Bulgaria
                          8
                                      6
                                          2
                                                8
                                                     1
                                                             57
                                                                             1
## Czechoslovakia
                         10
                                               13
                                                     2
                                                                             5
                                     11
                                          3
                                                             34
## Denmark
                          11
                                     11
                                           4
                                               25
                                                    10
                                                             22
##
                   Pulses.Nuts.and.Oilseeds Fruits.and.Vegetables Total
## Albania
## Austria
                                            1
                                                                   4
                                                                         86
## Belgium
                                            2
                                                                   4
                                                                         89
## Bulgaria
                                            4
                                                                   4
                                                                         91
## Czechoslovakia
                                            1
                                                                         83
                                            1
## Denmark
                                                                         91
```

```
#Printing the dimension of data to console
dim(protein_consumption)
```

```
## [1] 25 10
```

```
#Principal components analysis

#Applying PCA function on the dataset
protein_pca <- prcomp(protein_consumption, scale=TRUE)
#Printing the results of pca to console
protein_pca</pre>
```

```
## Standard deviations (1, .., p=10):
   [1] 2.032257e+00 1.319067e+00 1.144237e+00 1.021544e+00 8.360847e-01
##
   [6] 6.531975e-01 5.841454e-01 4.366348e-01 3.458098e-01 6.618503e-16
##
## Rotation (n x k) = (10 x 10):
##
                                            PC2
                                PC1
                                                       PC3
                                                                   PC4
## Red.Meat
                          -0.3180769 -0.17809245 -0.38142753 -0.039766137
## White.Meat
                          -0.3140588 -0.11783853 0.36420271 0.538507972
                          -0.4202281 -0.08236350 0.02047575 0.155623651
## Egg
## Milk
                          -0.3870300 -0.23356182 -0.19997405 -0.320360929
## Fish
                          -0.1271598   0.57388821   -0.33003267   -0.304161366
## Cereals
                          0.4177240 -0.31321549 -0.02354236 0.104798477
## Starchy.Foods
                          -0.2880798 0.41038324 0.05768490 0.150709175
## Pulses.Nuts.and.Oilseeds 0.4177658 0.04145202 -0.24796403 0.008042093
## Fruits.and.Vegetables
                          0.1197680 0.34858202 -0.41210384 0.643455476
                          -0.1062294 -0.41709540 -0.58081103 0.203145847
## Total
##
                                 PC5
                                             PC6
                                                         PC7
                                                                   PC8
## Red.Meat
                          ## White.Meat
                          -0.09760147   0.309417061   0.09254681   -0.2919567
## Egg
                          0.26932734 -0.059357751 -0.63995627 -0.2652806
## Milk
                          ## Fish
                          ## Cereals
                          -0.29201244 -0.196460437 0.06971238 -0.2001491
## Starchy.Foods
                          -0.42198545 -0.680457657 -0.11769041 0.1889672
## Pulses.Nuts.and.Oilseeds 0.22507285 -0.087921207 -0.57816932 -0.0829400
## Fruits.and.Vegetables
                          0.16834367 0.222568384
                                                  0.08684392 0.3701826
## Total
                          -0.47623561 -0.007702046 -0.05178373 -0.1801923
##
                                 PC9
                                           PC10
## Red.Meat
                          -0.17150487
                                      0.20838019
## White.Meat
                          -0.46186736
                                      0.22903415
## Egg
                          0.48098579
                                      0.06827056
## Milk
                          -0.13218960 0.43456461
## Fish
                          0.01789764 0.21247753
## Cereals
                           0.30436394 0.67412235
## Starchy.Foods
                          -0.14706957 0.10134794
## Pulses.Nuts.and.Oilseeds -0.58938418 0.12362100
## Fruits.and.Vegetables
                          0.20995988 0.11723988
## Total
                          -0.04898111 -0.41440004
```

#Printing the summary of the pca to console
summary(protein_pca)

```
## Importance of components:
##
                             PC1
                                   PC2
                                          PC3
                                                  PC4
                                                         PC5
                                                                 PC<sub>6</sub>
                                                                          PC7
## Standard deviation
                           2.032 1.319 1.1442 1.0215 0.8361 0.65320 0.58415
## Proportion of Variance 0.413 0.174 0.1309 0.1044 0.0699 0.04267 0.03412
## Cumulative Proportion 0.413 0.587 0.7179 0.8223 0.8922 0.93485 0.96898
##
                                       PC9
                               PC8
                                                 PC10
## Standard deviation
                           0.43663 0.34581 6.619e-16
## Proportion of Variance 0.01906 0.01196 0.000e+00
## Cumulative Proportion 0.98804 1.00000 1.000e+00
```

#We get from summary the std deviation, Proportion of Variance and the cummulative variance.
#In order to find the eigen values we need to square the std deviations. Which is done as below

#Storing and Printing the eigen values on the console
eigen_protien <- protein_pca\$sdev^2
eigen_protien</pre>

[1] 4.130067e+00 1.739939e+00 1.309278e+00 1.043551e+00 6.990377e-01

[6] 4.266669e-01 3.412258e-01 1.906500e-01 1.195844e-01 4.380459e-31

#Assigning names of PC to the values of PCA
names(eigen_protien) <- paste("PC",1:10,sep="")
#Printing the sum of eigen values to console
sum(eigen_protien)</pre>

[1] 10

#Visualizing the results of PCA

#Importing the required libraries
library(factoextra)

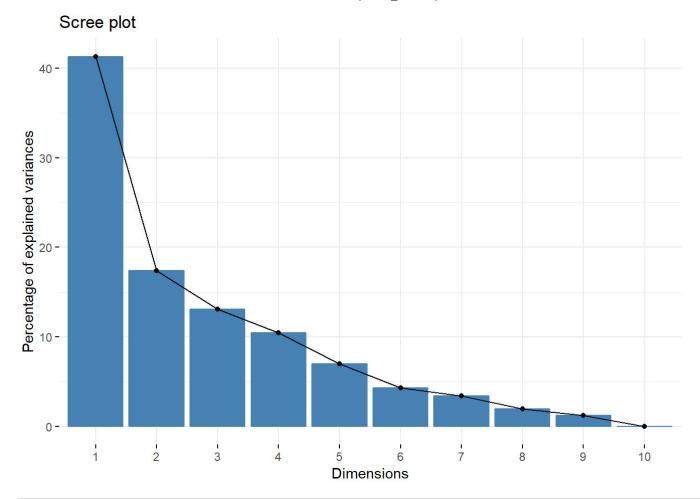
Warning: package 'factoextra' was built under R version 3.5.3

Loading required package: ggplot2

Warning: package 'ggplot2' was built under R version 3.5.2

Welcome! Related Books: `Practical Guide To Cluster Analysis in R` at https://goo.gl/13EFCZ

#Printing the Scree plot of PCA to console
fviz eig(protein pca)



#In order to retain the values of Principal Components we have 2 approaches take in account the values whose eigen values are greater than 0.7 or we can take components who account for 70-90% variablility.

#Here , in our case if we take 0.7 as threshold for eigen values we get first four components

#Printing the names of the eigenvalues who crosses 0.7 threshold value names(eigen_protien[eigen_protien>0.7])

[1] "PC1" "PC2" "PC3" "PC4"

#Printing the summary of PCA to concole
summary(protein_pca)

```
## Importance of components:
                                                 PC4
##
                            PC1
                                  PC2
                                         PC3
                                                        PC5
                                                                PC6
                                                                        PC7
## Standard deviation
                          2.032 1.319 1.1442 1.0215 0.8361 0.65320 0.58415
## Proportion of Variance 0.413 0.174 0.1309 0.1044 0.0699 0.04267 0.03412
## Cumulative Proportion 0.413 0.587 0.7179 0.8223 0.8922 0.93485 0.96898
##
                              PC8
                                      PC9
                                                PC10
## Standard deviation
                          0.43663 0.34581 6.619e-16
## Proportion of Variance 0.01906 0.01196 0.000e+00
## Cumulative Proportion 0.98804 1.00000 1.000e+00
```

```
#If we look at the summary we know that first four principal components accounts for roughly 82% of the total variance. Thus, we can consider our first four components as our Principal components.

#Now we predict the value of these components using predict function

# Constructing the new dataframe with 4 Principal components and output variable new_protien <- predict(protein_pca)[,1:4]

#Changing the row names of the row.names(new_protien) <- row.names(protein_consumption)

#Printing the head of the data head(new_protien)
```

```
##
                        PC1
                                   PC2
                                              PC3
                                                         PC4
## Albania
                  3.5978397 -0.6406110 1.1118946 -1.9111924
## Austria
                 -1.3862854 -0.7099190 1.1613381 0.9310749
## Belgium
                 -1.6608482 0.1078173 -0.4231894 0.2468077
## Bulgaria
                  2.9881523 -1.8436131 -0.0730564 0.3061617
## Czechoslovakia -0.3686147 -0.1014183 1.2155042 0.7220209
## Denmark
                 -2.4923551 0.1847475 -0.2075253 -0.9390683
```

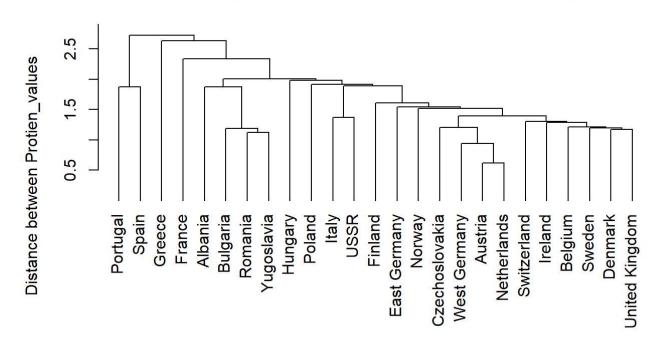
```
#Cluster Analysis (Using Principal Component Analysis):
#Agglomerative Clustering Using Single, Complete and average Linkage

#1.Single Linkage

#Calculating distance Matrix for the PRincipal components
dist.protien <- dist(new_protien,method='euclidean')
#Calculating Agglomerative Clustering using single linkage
clustprotien.nn <- hclust(dist.protien, method = "single")
#Plotting the Agglomeratuve Clustering
plot(clustprotien.nn,hang=-1,xlab="Object",ylab="Distance between Protien values",main="Dendrogr")</pre>
```

am of Countries using Single Linkage")

Dendrogram of Countries using Single Linkage

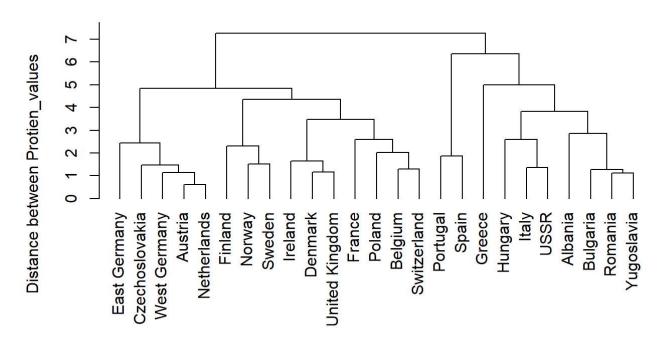


Object hclust (*, "single")

#2.Complete Linkage

#Calculating Agglomerative Clustering using single linkage
clustprotien.nn <- hclust(dist.protien, method = "complete")
#Plotting the Agglomeratuve Clustering
plot(clustprotien.nn,hang=-1,xlab="Object",ylab="Distance between Protien_values",main="Dendrogr
am of Countries using Complete Linkage")</pre>

Dendrogram of Countries using Complete Linkage



Object hclust (*, "complete")

#3. Average Linkage

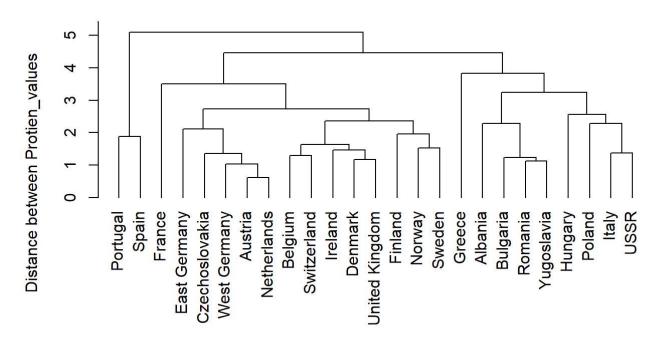
#Calculating Agglomerative Clustering using Average linkage i.e calculating the average distance

clustprotien.nn <- hclust(dist.protien, method = "average")</pre>

#Plotting the Agglomeratuve Clustering

plot(clustprotien.nn,hang=-1,xlab="Object",ylab="Distance between Protien_values",main="Dendrogr am of Countries using Average Linkage")

Dendrogram of Countries using Average Linkage



Object hclust (*, "average")

#We get the dendograms for single linkage, complete linkage and average linkage as above. We can Thus group the protien consumption by countries as shown above. If the data is large it is not a dvised to use agglomerative clustering instead we use k-means clustering.

#Q3.Identify the important factors underlying the observed variables and examine the relationships between the countries with respect to these factors

#Ans: In order to solve this we need to use the original data

#Printing the head of data to console
head(protein_consumption)

```
##
                   Red.Meat White.Meat Egg Milk Fish Cereals Starchy.Foods
                                                     0
## Albania
                         10
                                      1
                                          1
                                               9
                                                            42
## Austria
                          9
                                     14
                                          4
                                              20
                                                     2
                                                            28
                                                                            4
                                                     5
## Belgium
                         14
                                      9
                                          4
                                              18
                                                            27
                                                                            6
## Bulgaria
                          8
                                      6
                                          2
                                               8
                                                     1
                                                            57
                                                                            1
## Czechoslovakia
                                          3
                                              13
                                                     2
                                                            34
                         10
                                     11
                                                                            5
## Denmark
                         11
                                     11
                                          4
                                              25
                                                    10
                                                            22
##
                   Pulses.Nuts.and.Oilseeds Fruits.and.Vegetables Total
## Albania
                                           6
                                                                        72
## Austria
                                                                   4
                                           1
                                                                        86
                                           2
## Belgium
                                                                   4
                                                                        89
## Bulgaria
                                           4
                                                                   4
                                                                        91
## Czechoslovakia
                                           1
                                                                   4
                                                                        83
## Denmark
                                           1
                                                                   2
                                                                        91
```

```
#Loading the required library
library(psych)

## Warning: package 'psych' was built under R version 3.5.3

##
## Attaching package: 'psych'
```

```
## The following objects are masked from 'package:ggplot2':
##
## %+%, alpha
```

```
#Applying Factor Analysis on the data with 4 factors
fit.pc <- principal(protein_consumption,nfactors = 4, rotate = "varimax")</pre>
```

```
## Warning in cor.smooth(r): Matrix was not positive definite, smoothing was
## done
```

 $\mbox{\tt \#\#}$ In factor.stats, I could not find the RMSEA upper bound . Sorry about that

```
## Warning in principal(protein_consumption, nfactors = 4, rotate =
## "varimax"): The matrix is not positive semi-definite, scores found from
## Structure loadings
```

```
#Printing the results of Factor Analysis
fit.pc
```

```
## Principal Components Analysis
## Call: principal(r = protein consumption, nfactors = 4, rotate = "varimax")
## Standardized loadings (pattern matrix) based upon correlation matrix
                              RC1
                                    RC2
                                         RC3
                                                RC4
                                                      h2
## Red.Meat
                             0.26 0.21 0.74 -0.11 0.67 0.335 1.5
## White.Meat
                            0.94 -0.16 0.05 0.03 0.91 0.092 1.1
## Egg
                            0.72 0.21 0.43 -0.15 0.77 0.233 1.9
## Milk
                            0.32 0.26 0.68 -0.49 0.87 0.127 2.6
                            -0.15 0.92 0.03 0.11 0.88 0.121 1.1
## Fish
                            -0.58 -0.71 -0.17 0.18 0.90 0.096 2.2
## Cereals
                            0.53   0.60   -0.05   0.13   0.66   0.336   2.1
## Starchy.Foods
## Pulses.Nuts.and.Oilseeds -0.75 -0.24 -0.21 0.37 0.80 0.196 1.9
## Fruits.and.Vegetables
                           -0.07 0.15 0.01 0.95 0.93 0.075 1.1
## Total
                            -0.03 -0.25 0.86 0.18 0.83 0.166 1.3
##
##
                         RC1 RC2 RC3 RC4
## SS loadings
                         2.77 2.04 2.00 1.41
## Proportion Var
                         0.28 0.20 0.20 0.14
## Cumulative Var
                         0.28 0.48 0.68 0.82
## Proportion Explained 0.34 0.25 0.24 0.17
## Cumulative Proportion 0.34 0.59 0.83 1.00
##
## Mean item complexity = 1.7
## Test of the hypothesis that 4 components are sufficient.
##
## The root mean square of the residuals (RMSR) is 0.07
   with the empirical chi square 10.96 with prob < 0.45
##
## Fit based upon off diagonal values = 0.97
```

```
#rounding the values to 3 decimal places
round(fit.pc$values, 3)
```

```
## [1] 4.130 1.740 1.309 1.044 0.699 0.427 0.341 0.191 0.120 0.000
```

```
#Printing the loading data to console for the fit.pc$loadings
```

```
##
## Loadings:
##
                           RC1
                                  RC2
                                         RC3
                                                RC4
## Red.Meat
                            0.259 0.213 0.735 -0.111
## White.Meat
                            0.937 -0.161
                            0.720 0.208 0.426 -0.154
## Egg
## Milk
                            0.316 0.261 0.684 -0.488
## Fish
                           -0.148 0.918
                                                 0.113
## Cereals
                           -0.579 -0.714 -0.167 0.176
## Starchy.Foods
                            0.531 0.602
                                                 0.131
## Pulses.Nuts.and.Oilseeds -0.752 -0.240 -0.205 0.373
## Fruits.and.Vegetables
                                                 0.947
                                   0.153
## Total
                                  -0.246 0.860 0.183
##
##
                   RC1
                         RC2
                               RC3
                                     RC4
## SS loadings
                 2.773 2.040 2.005 1.405
## Proportion Var 0.277 0.204 0.200 0.141
## Cumulative Var 0.277 0.481 0.682 0.822
```

#Now we look at the cummunality
fit.pc\$communality

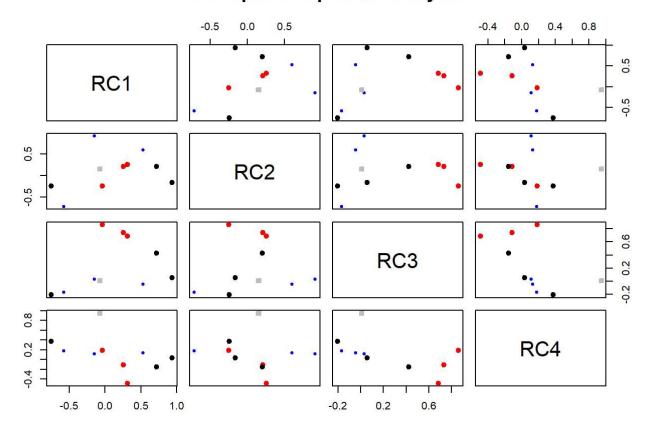
##	Red.Meat	White.Meat	Egg	
##	0.6651696	0.9078091	0.7669612	
##	Milk	Fish	Cereals	
##	0.8730259	0.8789782	0.9035506	
##	Starchy.Foods Pul	lses.Nuts.and.Oilseeds	Fruits.and.Vegetables	
##	0.6638440	0.8043733	0.9250830	
##	Total			
##	0.8340405			

#Printing the scores
fit.pc\$scores

```
RC1
##
                                    RC2
                                               RC3
                                                           RC4
## Albania
                 -5.7605734 -3.36700491 -3.8633784 -0.39909495
## Austria
                  3.1694665 -0.25158518 0.7561406 -0.89662602
## Belgium
                  2.3868189 1.56149347 1.8337942 -0.46124833
## Bulgaria
                 -4.3208782 -4.55896299 -1.5315590 1.04713255
## Czechoslovakia 1.5578630 -0.41964941 -0.6288392 -0.24291402
## Denmark
                  3.1399401 2.71500531 2.3853571 -1.94188415
                  3.2301617 1.84901437 -1.5130562 -0.21860020
## East Germany
## Finland
                  1.3146712 1.65752382 2.4667399 -3.00560097
## France
                  1.8007806 1.36671635 3.8271586 1.14045289
## Greece
                 -4.5810717 -1.61817397 1.0655364 2.56985982
## Hungary
                 -0.7455549 -2.64356726 -2.4704373 0.82593410
## Ireland
                  3.9476155 1.21073039 3.3976235 -1.69957990
## Italy
                 -2.3770340 -1.36214582 -0.9545821 1.57348514
## Netherlands
                  3.2792689 0.45581557 1.2593824 -1.01402637
## Norway
                  0.3278365 2.77552853 0.1615539 -1.17661290
## Poland
                  0.9782808 -0.08782629 0.4161197 1.51507925
## Portugal
                 -3.5783940 3.05623951 -4.2281851 3.53676835
## Romania
                 -3.6436378 -3.44529927 -2.2388510 0.53509931
## Spain
                 -2.4289034 1.46500473 -2.9477324 2.46464265
## Sweden
                  2.2286387 2.34569499 1.0237541 -2.35625096
## Switzerland
                  1.3670756 -0.21504380 1.7800778 -0.57852957
## United Kingdom 2.1943713 1.57880111 2.9414916 -1.42721666
## USSR
                 -1.4884026 -0.92805896 -0.1658179 -0.01163555
## West Germany
                  3.4360982 1.19111164 0.3305165 -0.91145006
## Yugoslavia
                 -5.4344376 -4.33136193 -3.1028077 1.13281655
```

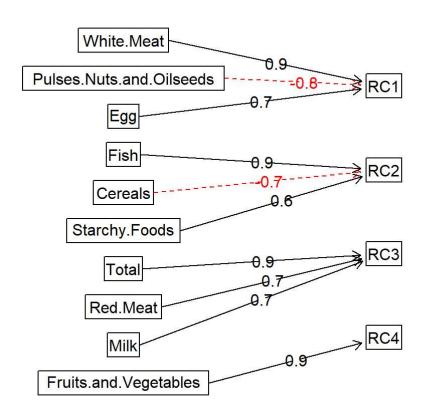
See Correlations within Factors
fa.plot(fit.pc)

Principal Component Analysis



#Visualize the relationship
fa.diagram(fit.pc)

Components Analysis



```
#Visualizing the data
vss(protein_consumption)
```

```
## Warning in sqrt(e$values): NaNs produced
```

```
## Warning in cor.smooth(R): Matrix was not positive definite, smoothing was
## done

## Warning in cor.smooth(R): Matrix was not positive definite, smoothing was
## done

## Warning in cor.smooth(R): Matrix was not positive definite, smoothing was
## done
```

```
## Warning in cor.smooth(r): Matrix was not positive definite, smoothing was
## done
```

```
## Warning in fa.stats(r = r, f = f, phi = phi, n.obs = n.obs, np.obs
## = np.obs, : The estimated weights for the factor scores are probably
## incorrect. Try a different factor extraction method.
```

```
## Warning in cor.smooth(R): Matrix was not positive definite, smoothing was
## done
## Warning in cor.smooth(R): Matrix was not positive definite, smoothing was
## Warning in cor.smooth(R): Matrix was not positive definite, smoothing was
## Warning in cor.smooth(r): Matrix was not positive definite, smoothing was
## done
## Warning in fa.stats(r = r, f = f, phi = phi, n.obs = n.obs, np.obs
## = np.obs, : The estimated weights for the factor scores are probably
## incorrect. Try a different factor extraction method.
## Warning in fac(r = r, nfactors = nfactors, n.obs = n.obs, rotate =
## rotate, : An ultra-Heywood case was detected. Examine the results carefully
## Warning in cor.smooth(R): Matrix was not positive definite, smoothing was
## done
## Warning in cor.smooth(R): Matrix was not positive definite, smoothing was
## done
## Warning in cor.smooth(R): Matrix was not positive definite, smoothing was
## done
## Warning in cor.smooth(r): Matrix was not positive definite, smoothing was
## done
## Warning in fa.stats(r = r, f = f, phi = phi, n.obs = n.obs, np.obs
## = np.obs, : The estimated weights for the factor scores are probably
## incorrect. Try a different factor extraction method.
## Warning in cor.smooth(R): Matrix was not positive definite, smoothing was
## done
## Warning in cor.smooth(R): Matrix was not positive definite, smoothing was
## done
## Warning in cor.smooth(R): Matrix was not positive definite, smoothing was
## done
## Warning in cor.smooth(r): Matrix was not positive definite, smoothing was
## done
```

```
## In factor.stats, I could not find the RMSEA upper bound . Sorry about that
```

```
## Warning in fa.stats(r = r, f = f, phi = phi, n.obs = n.obs, np.obs
## = np.obs, : The estimated weights for the factor scores are probably
## incorrect. Try a different factor extraction method.
```

```
## Warning in fac(r = r, nfactors = nfactors, n.obs = n.obs, rotate =
## rotate, : An ultra-Heywood case was detected. Examine the results carefully
```

```
## Warning in cor.smooth(R): Matrix was not positive definite, smoothing was
## done

## Warning in cor.smooth(R): Matrix was not positive definite, smoothing was
## done

## Warning in cor.smooth(R): Matrix was not positive definite, smoothing was
## done
```

```
## Warning in cor.smooth(r): Matrix was not positive definite, smoothing was
## done
```

```
## In factor.stats, I could not find the RMSEA upper bound . Sorry about that
```

```
## Warning in fa.stats(r = r, f = f, phi = phi, n.obs = n.obs, np.obs
## = np.obs, : The estimated weights for the factor scores are probably
## incorrect. Try a different factor extraction method.
```

```
## Warning in fac(r = r, nfactors = nfactors, n.obs = n.obs, rotate =
## rotate, : An ultra-Heywood case was detected. Examine the results carefully
```

```
## Warning in cor.smooth(R): Matrix was not positive definite, smoothing was
## done

## Warning in cor.smooth(R): Matrix was not positive definite, smoothing was
## done

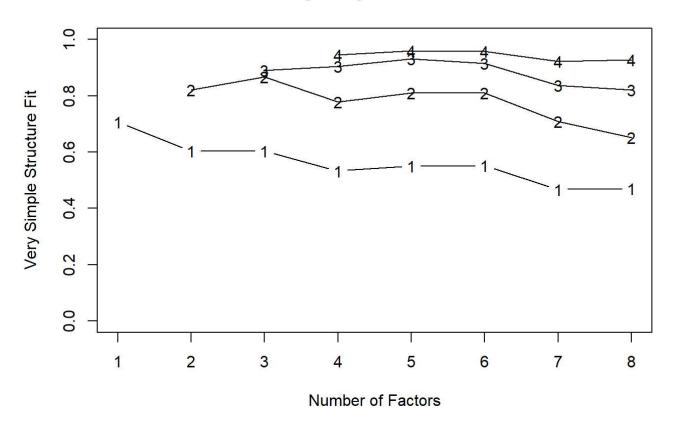
## Warning in cor.smooth(R): Matrix was not positive definite, smoothing was
## done
```

```
## Warning in cor.smooth(r): Matrix was not positive definite, smoothing was
## done
```

```
## Warning in fa.stats(r = r, f = f, phi = phi, n.obs = n.obs, np.obs
## = np.obs, : The estimated weights for the factor scores are probably
## incorrect. Try a different factor extraction method.
```

```
## Warning in fac(r = r, nfactors = nfactors, n.obs = n.obs, rotate =
## rotate, : An ultra-Heywood case was detected. Examine the results carefully
## Warning in cor.smooth(R): Matrix was not positive definite, smoothing was
## done
## Warning in cor.smooth(R): Matrix was not positive definite, smoothing was
## done
## Warning in cor.smooth(R): Matrix was not positive definite, smoothing was
## done
## Warning in cor.smooth(r): Matrix was not positive definite, smoothing was
## done
## Warning in fa.stats(r = r, f = f, phi = phi, n.obs = n.obs, np.obs
## = np.obs, : The estimated weights for the factor scores are probably
## incorrect. Try a different factor extraction method.
## Warning in fac(r = r, nfactors = nfactors, n.obs = n.obs, rotate =
## rotate, : An ultra-Heywood case was detected. Examine the results carefully
## Warning in cor.smooth(R): Matrix was not positive definite, smoothing was
## done
## Warning in cor.smooth(R): Matrix was not positive definite, smoothing was
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## done
## Warning in cor.smooth(r): Matrix was not positive definite, smoothing was
## done
## Warning in fa.stats(r = r, f = f, phi = phi, n.obs = n.obs, np.obs
## = np.obs, : The estimated weights for the factor scores are probably
## incorrect. Try a different factor extraction method.
## Warning in fac(r = r, nfactors = nfactors, n.obs = n.obs, rotate =
## rotate, : An ultra-Heywood case was detected. Examine the results carefully
```

Very Simple Structure



```
##
## Very Simple Structure
## Call: vss(x = protein_consumption)
## VSS complexity 1 achieves a maximimum of 0.71 with 1 factors
## VSS complexity 2 achieves a maximimum of 0.87 with 3 factors
##
## The Velicer MAP achieves a minimum of 0.09 with 1 factors
## BIC achieves a minimum of NA with 5 factors
## Sample Size adjusted BIC achieves a minimum of NA with 5 factors
##
## Statistics by number of factors
     vss1 vss2
                 map dof chisq
                                  prob sqresid fit RMSEA BIC SABIC complex
## 1 0.71 0.00 0.087
                      35
                           453 3.6e-74
                                         6.941 0.71 0.80 341
                                                                449
                                                                        1.0
## 2 0.60 0.82 0.106 26
                           419 2.0e-72
                                         4.245 0.82 0.91 335
                                                                416
                                                                        1.3
## 3 0.60 0.87 0.145 18
                           390 1.0e-71
                                        2.603 0.89
                                                    1.08 332
                                                                388
                                                                        1.6
## 4 0.53 0.78 0.173 11
                           356 1.2e-69
                                                                        1.7
                                         1.284 0.95 1.36 321
                                                                355
## 5 0.55 0.81 0.209
                           323 1.4e-67
                                         0.699 0.97 1.97 307
                                                                        1.8
                                                                322
## 6 0.55 0.81 0.314
                           305
                                         0.411 0.98
                                                                        1.9
                       0
                                    NA
                                                       NA
                                                           NA
                                                                 NA
## 7 0.47 0.71 0.477
                           278
                                         0.286 0.99
                                    NA
                                                       NA
                                                           NΑ
                                                                 NA
                                                                        2.3
## 8 0.47 0.65 1.000
                           250
                                    NA
                                         0.078 1.00
                                                       NA
                                                           NA
                                                                 NA
                                                                        2.3
      eChisq
               SRMR eCRMS eBIC
## 1 56.2527 0.1581 0.179
                           -56
## 2 27.4318 0.1104 0.145
                           -56
## 3 12.8827 0.0757 0.120
                           -45
## 4 4.6981 0.0457 0.092
                           -31
## 5
      0.9578 0.0206 0.062
                           -15
      0.3915 0.0132
## 6
                            NA
## 7
      0.0359 0.0040
                       NA
                            NA
      0.0026 0.0011
                       NA
                            NA
```