

DEMAND FORECASTING

Even number of Year $x = \text{Year} - \text{Mean of 2 middle years} / \frac{1}{2} \text{ Interval}$

Origin $= (2012 + 2013) / 2 = 2012.5$

$X = \text{Year} - 2012.5 / \frac{1}{2} \text{ Interval}$

For year 2009 It is $2009 - 2012.5 / 0.5 = (-7)$

| Year | y | x | xy | X ² | |
|------|----------------|--------------|-----------------|------------------|--|
| 2009 | 80 | -7 | -560 | 49 | |
| 2010 | 90 | -5 | -450 | 25 | |
| 2011 | 92 | -3 | -276 | 9 | |
| 2012 | 83 | -1 | -83 | 1 | |
| 2013 | 94 | 1 | 94 | 1 | |
| 2014 | 99 | 3 | 297 | 9 | |
| 2015 | 92 | 5 | 460 | 25 | |
| 2016 | 104 | 7 | 728 | 49 | |
| | $\sum y = 734$ | $\sum x = 0$ | $\sum xy = 210$ | $\sum x^2 = 168$ | |

$$\sum y = a + b \sum x \quad \Rightarrow 734 = 8a \text{ so } a = 91.75$$

$$\sum xy = a \sum x + b \sum x^2 \quad \Rightarrow 210 = 168b \text{ so } b = 1.25$$

$$Y = a + bx = 91.75 + 1.25x$$

Estimate for 2017

$$2017 - 2012.5 / 0.5 = (9)$$

$$Y = 91.75 + 1.25x = 91.75 + 1.25 \cdot 9 = 103$$

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Odd number of Year

| Year | y | x | xy | X ² | |
|------|----------------|--------------|----------------|-----------------|--|
| 2010 | 125 | -3 | -376 | 9 | |
| 2011 | 128 | -2 | -256 | 4 | |
| 2012 | 133 | -1 | -133 | 1 | |
| 2013 | 135 | 0 | 0 | 0 | |
| 2014 | 140 | 1 | 140 | 1 | |
| 2015 | 141 | 2 | 282 | 4 | |
| 2016 | 143 | 3 | 429 | 9 | |
| | $\sum y = 945$ | $\sum x = 0$ | $\sum xy = 87$ | $\sum x^2 = 28$ | |

$x = (\text{Year} - \text{origin}) / \text{Interval}$

For 2010

$$X = 2010 - 2013 / 1 = (-3)$$

$$\sum y = a + b \sum x \quad \Rightarrow 945 = 7a \text{ so } a = 135$$

$$\sum xy = a \sum x + b \sum x^2 \quad \Rightarrow 87 = 28b \text{ so } b = 3.107$$

$$Y = a + bx = 135 + 3.107x$$

Estimate for year 2017

$$X = 2017 - 2013 / 1 = 4$$

$$Y = a + bx = 135 + 3.107 * 4 = 147.428$$

Direct Method

Calculate the regression equations Y on X from the data given below,

| | | | | | | |
|--------|----|----|----|----|----|----|
| Price | 10 | 12 | 13 | 12 | 16 | 15 |
| Demand | 40 | 38 | 43 | 45 | 37 | 43 |

| Price(X) | Demand(Y) | ΣXY | ΣX^2 |
|---------------|----------------|-------------------|--------------------|
| 10 | 40 | 400 | 100 |
| 12 | 38 | 456 | 144 |
| 13 | 43 | 559 | 169 |
| 12 | 45 | 540 | 144 |
| 16 | 37 | 592 | 256 |
| 15 | 43 | 645 | 225 |
| $\Sigma X=78$ | $\Sigma Y=246$ | $\Sigma XY= 3192$ | $\Sigma X^2= 1038$ |

$$\Sigma y = N a + b \Sigma x \quad \Rightarrow 246 = 6a + 78b \dots\dots\dots (i)$$

$$\Sigma xy = a \Sigma x + b \Sigma x^2 \quad \Rightarrow 3192 = 78a + 1038b \dots\dots\dots (ii)$$

Solving (i) & (ii)

$$a = 44.25$$

$$b = (-0.25)$$

$$Y = a + bx \Rightarrow Y = 44.25 - 0.25X$$