## **Spring 2025**Due date: April 4, 2025

## Problem 1:

The softmax temperature is a parameter used to adjust how a language model selects words during text generation. It changes the probability distribution of possible next words, allowing us to tune the balance between randomness and predictability in the output. Given a vector of logits  $z_i$  for each possible token, the temperature scaled softmax is defined as:

$$P(w_i) = \frac{e^{z_i/T}}{\sum_j e^{z_j/T}}$$

where T is the temperature,  $z_i$  is the pre-softmax score for token i, and  $P(w_i)$  is the resulting probability for token i.

When the temperature is close to 0.7 or below, the model becomes more confident and focused. It strongly favors high-probability words, resulting in precise, factual, and consistent outputs. This setting is well-suited for tasks where accuracy and coherence are important, such as summarization, and QA.

In contrast, a higher temperature which can be selected as 1.2 or more makes the output distribution flatter, giving more weight to less likely words. This leads to more creative, varied, and sometimes unexpected text, which is ideal for poetry, storytelling, or brainstorming tasks. However, very high temperatures can also introduce nonsense or off-topic responses.

















